Hamiltonian RG flow equation

Definition of electron-hole transition operator

$$\eta_{j,l} = Tr(c_{j,l}^{\dagger} H_{j,l}) c_{j,l} \frac{1}{\hat{\omega}_{j,l} - Tr_{j,l}(H_{j,l}^{D} \hat{\eta}_{j,l}) \hat{n}_{j,l}}$$

off-diagonal scattering operation between e-h configuration

diag. part
$$\hat{\omega}_{j,l} = H_{j,l}^D + H_{j,l}^X - H_{j,l-1}^X \quad \text{renormalized} \\ \text{of H} \quad H_{j,l}^X = \sum_{\alpha} \Gamma_{\alpha}^2 c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}'\sigma'} + \sum_{\beta} \Gamma_{\beta}^2 c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}'\sigma'}^\dagger c_{\mathbf{k}'\sigma'}^\dagger c_{\mathbf{k}'_1\sigma'_1} c_{\mathbf{k}_1\sigma_1} + \dots$$

 lpha Number off-diagonal Hamiltonian composed of 1-p scattering vertex and higher order terms.