## IR fixed point theory

Low energy fixed point Hamiltonian for  $J_0 > 0$ 

$$H^*(\omega) = \sum_{|\Lambda| < \Lambda^*} \hbar v_F \Lambda \hat{n}_{\Lambda,\hat{s},\sigma} + \frac{J^*(\omega)}{2} \sum_{\Lambda,\Lambda' < \Lambda^*,\hat{s}\hat{s}'} \mathbf{S} \cdot c^{\dagger}_{\mathbf{k}_{\Lambda\hat{s}},\alpha} \boldsymbol{\sigma}_{\alpha\beta} c^{\dagger}_{\mathbf{k}_{\Lambda'\hat{s}'},\alpha}$$

Hamiltonian containing only zero mode  $J_0 > 0$ 

$$H_0^*(\omega) = \frac{\hbar v_F}{N(\Lambda^*)} \sum_{|\Lambda| \leq \Lambda^*, \hat{n}} \Lambda \sum_{\Lambda, \hat{n}} \hat{n}_{\mathbf{k}_{\Lambda}\hat{s}\sigma} + \frac{J^*(\omega)}{2} \sum_{\Lambda, \Lambda' \leq \Lambda^*, \hat{n}\hat{s}'} \mathbf{S} \cdot c^{\dagger}_{\mathbf{k}_{\Lambda}\hat{s}, \alpha} \boldsymbol{\sigma}_{\alpha\beta} c^{\dagger}_{\mathbf{k}_{\Lambda'}\hat{s}', \alpha}$$

- Zero mode accounts for the low enery physics near FS, and is responsible for the singlet ground state.
- $\bullet$  The other non-zero mode are sources of excitation around the ground state.