$$|\Psi\rangle_{\mathrm{GS}} \left\{ egin{array}{c} & lpha \ \hat{n}_{1\uparrow} \hat{n}_{1\downarrow} \ 0 & 1 \end{array}
ight.$$