

Options

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Lecture notes for Econ 235

- An *option* on a futures contract gives its owner the right but not the obligation to enter a position on a futures contract at a predetermined price.
- Options are derivatives because their value depends on the value of another asset, a futures contract in this case.
- Options on futures contracts specify whether they are attached to a long or a short futures contract.

- The seller of an option is also called the writer.
- A *call* option specifies that the seller must deliver a *long* futures position to the option buyer.
- A *put* option specifies that the seller must deliver a *short* futures position to the option buyer.
- The seller of an option must provide the futures contract only if the buyer decides to exercise the option.
- The seller is obligated to comply.

- The owner of an *American option* can exercise the option within a certain period of time.
- The owner of an *European option* can exercise the option only at its expiration.
- We will focus on American options.

- The *strike price* or the *exercise price* is the price of the futures contract when exercising the option.
- The *premium* is the price of the option itself.

Examples of options prices - CME website

- See CME website [here](#) for prices of options on corn contracts.
- See CME website [here](#) for prices of options on soybeans contracts.

Difference between futures contracts and options on futures

Table : Difference between futures contracts and options on futures

Positions	Trader's right	Trader's obligation	Margin required?
Futures contract buyer (long)		Accept commodity or financial asset at contract price or cash settle	Yes
Futures contract seller (short)		Deliver commodity or financial asset at contract price or cash settle	Yes
Put option buyer	Sell futures contract at strike price		No
Put option seller		Buy futures contract at strike price	Yes
Call option buyer	Buy futures contract at strike price		No
Call option seller		Sell futures contract at strike price	Yes

Source: Carter (2003)

What determines the value of an option?

- The price of options is determined by the intersection of the demand and the supply.
- The demand and supply for options are motivated by willingness to avoid price uncertainty through hedging or willingness to speculate.

Futures price and options premium

Table : Futures price and options premium

	Underlying futures price	
	Declines	Increases
Call option premium	Declines	Increases
Put option premium	Increases	Declines

Why traders are willing to pay for an option?

- The premium for an option has two components; the *intrinsic value* and the *time value*:

$$\text{Premium} = \text{Intrinsic Value} + \text{Time Value.}$$

- The intrinsic value is the difference between the strike price and the current futures contract price.
- The time value is the amount that buyers are willing to pay because they expect that the price of futures will change favorably.

- The intrinsic value is the amount by which an option is *in the money*.

Table : In and out of the money

	Call option	Put option
In the money (has intrinsic value)	Futures $>$ strike	Futures $<$ strike
At the money	Futures $=$ strike	Futures $=$ strike
Out of the money (no intrinsic value)	Futures $<$ strike	Futures $>$ strike

Example of intrinsic value: call option

	Strike price	Futures price	Intrinsic value
Option 1	\$4.00	\$4.25	\$0.25
		\$4.75	\$0.75
Option 2	\$4.50	\$4.25	\$0.00
		\$4.75	\$0.25
Option 3	\$5.00	\$4.25	\$0.00
		\$4.75	\$0.00

Example of intrinsic value: put option

	Strike price	Futures price	Intrinsic value
Option 1	\$4.00	\$4.25	\$0.00
		\$4.75	\$0.00
Option 2	\$4.50	\$4.25	\$0.25
		\$4.75	\$0.00
Option 3	\$5.00	\$4.25	\$0.75
		\$4.75	\$0.25

Call option payoff line

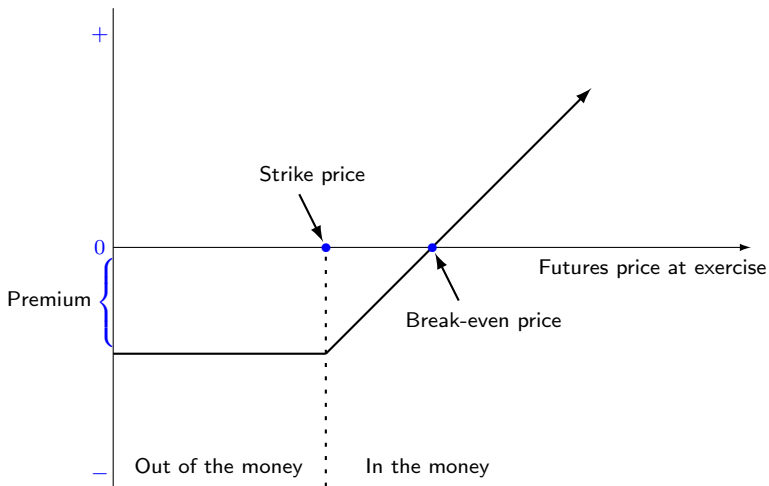


Figure : Call option payoff line

Put option payoff line

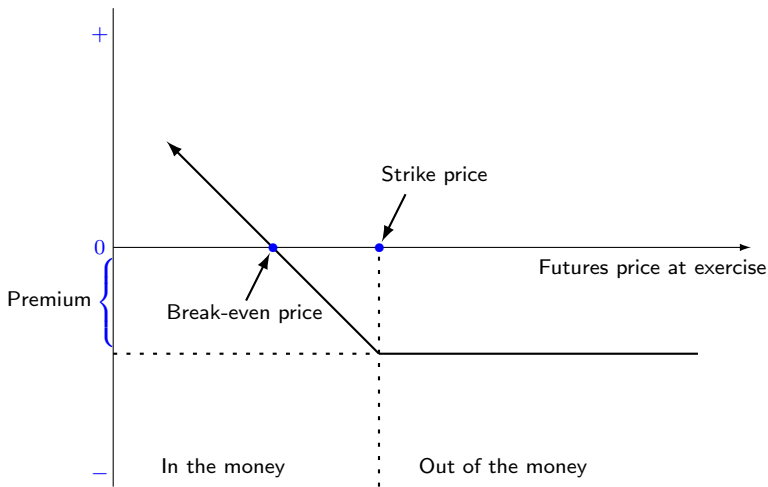


Figure : Put option payoff line

- The time value represents the expectations regarding the price of a futures contract to exceed the strike price for a call option or to fall below the strike price of a put option.
- We know the price of an option (premium) and can calculate the intrinsic value.
- The time value is:

$$\text{Time Value} = \text{Premium} - \text{Intrinsic Value.}$$

Time value of an option

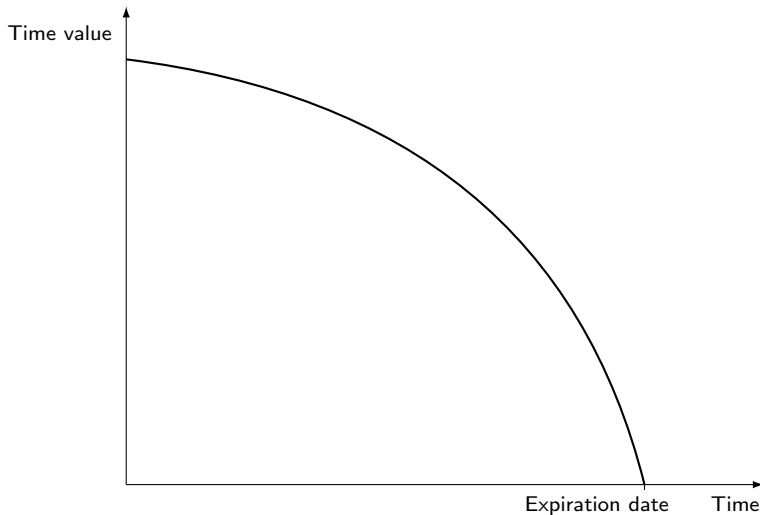


Figure : Decaying value of an option

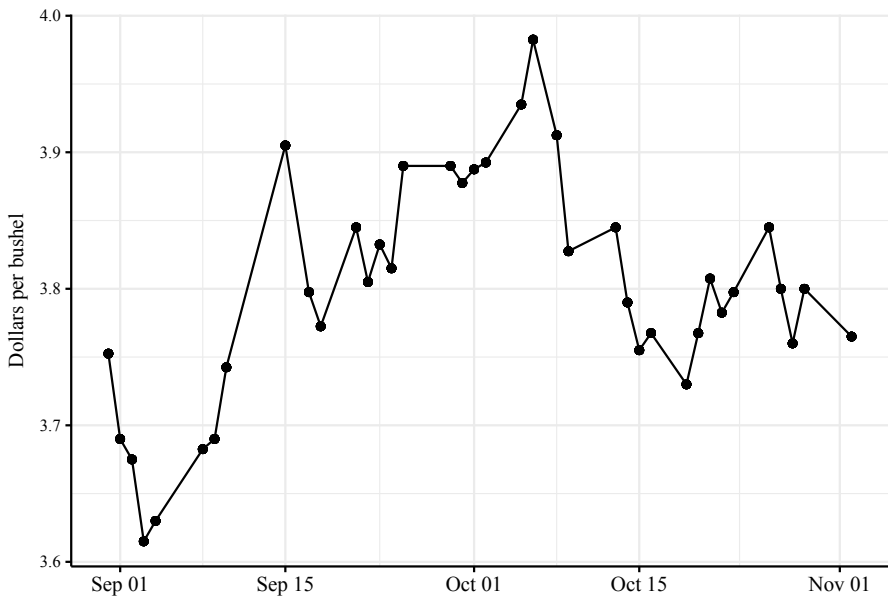
Time value of options

- Time adds value to an option.
- The more time before the expiration of an option, the greater is the probability that the option falls in the money and the greater the probability that the option is in the money by much.
- The more volatile is the price of the underlying futures contract, the greater is the time value of an option.
- An option is a decaying asset because its time value declines as it approaches its expiration.
- At expiration, the time value of an option is zero.

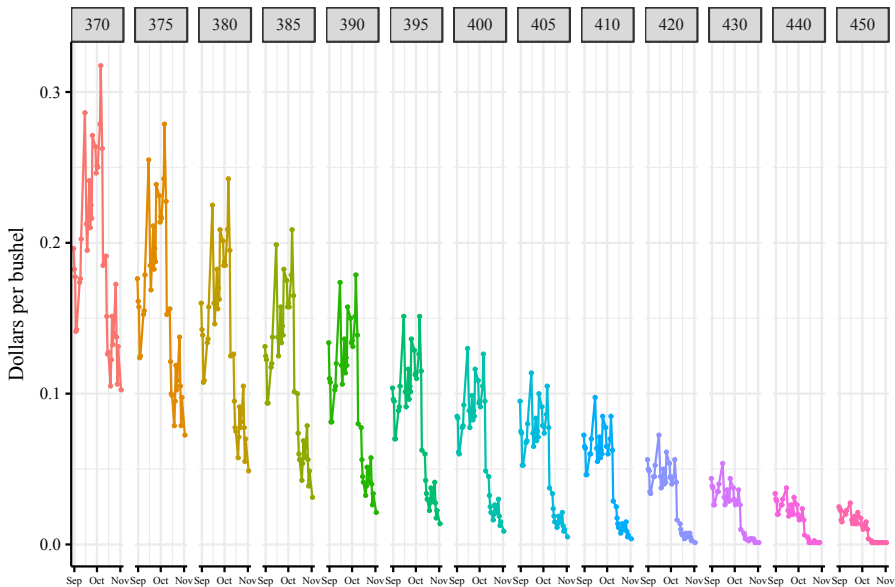
In practice, how does the price of an option change?

- The following figures are for options on the December futures contract for corn.
- The option expired on November 20, 2015.
- The graphs are for options with different strike prices.

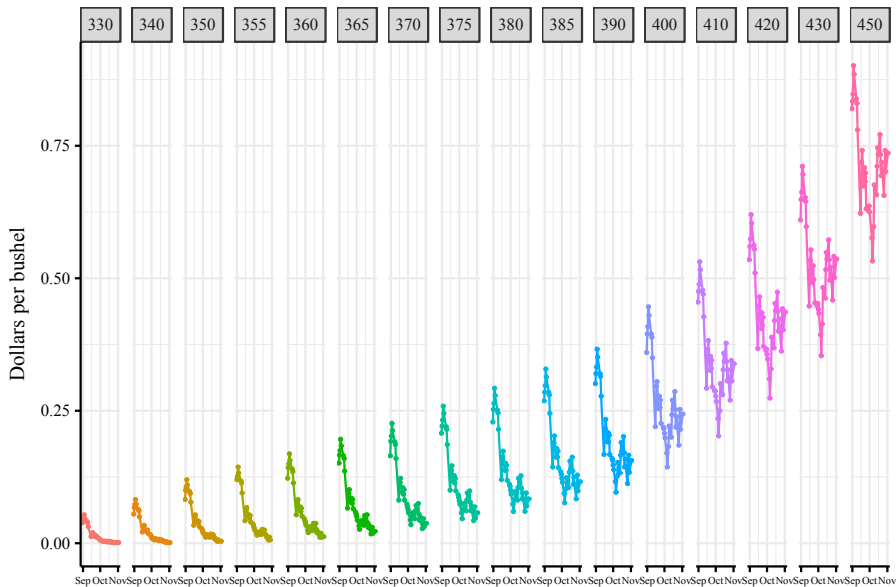
Price of corn



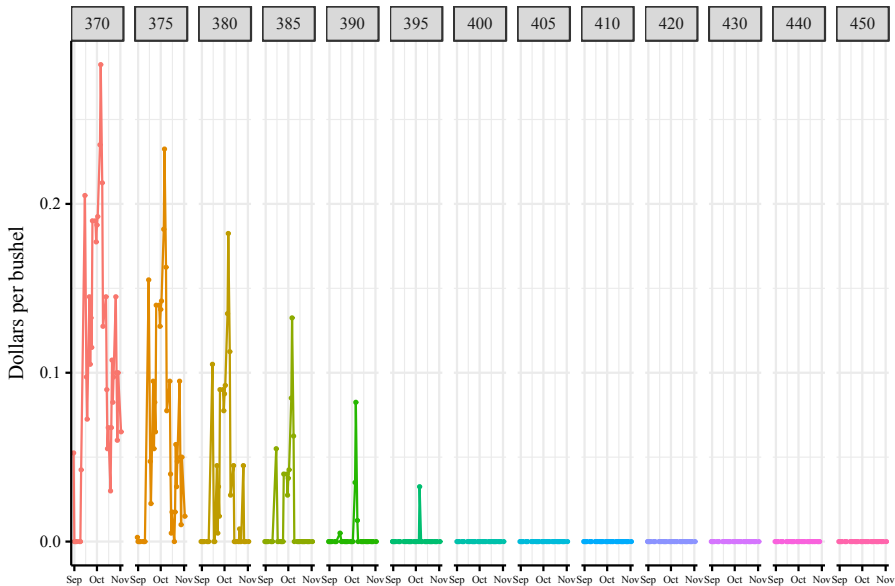
Call option premium



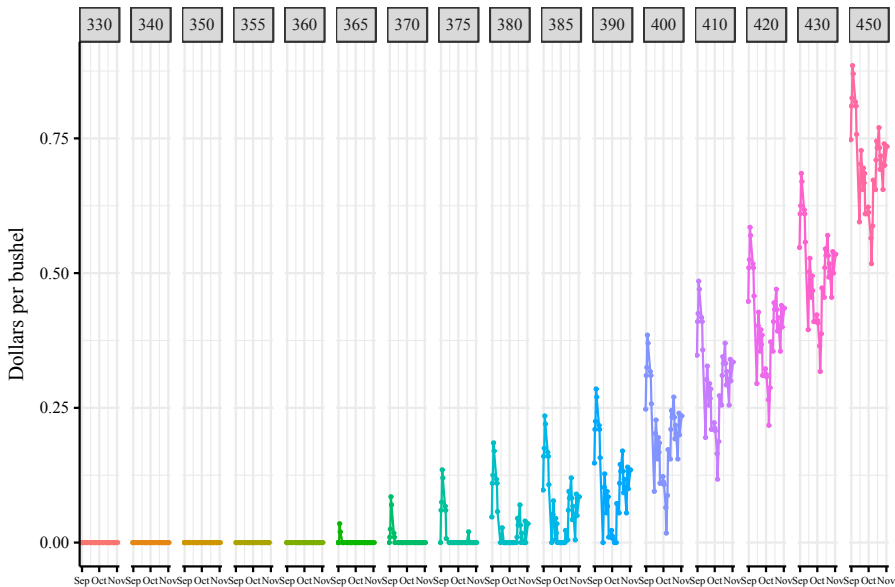
Put option premium



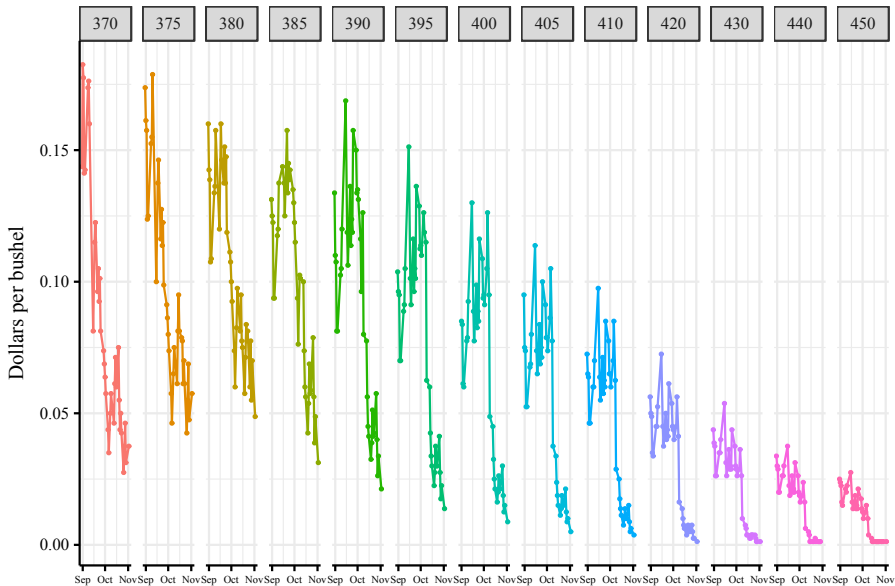
Call option intrinsic value



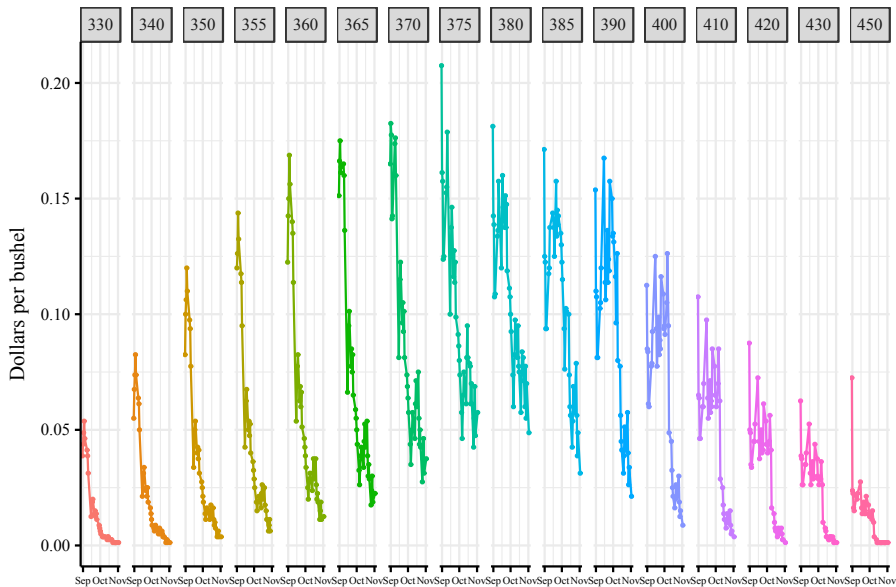
Put option intrinsic value



Call option time value



Put option time value



- Some of these options are not traded very frequently.
- This means that the time values calculated in the previous do not always reflect the value of time alone.
- The corn price used for the calculations is the closing price. The last transaction for some options might have occurred quite some time before at a different corn price.
- This means that the time values, in the two previous graphs, are calculated with less precision.
- You expect the time value to decline over time.

Price limits for options: call

- The maximum value of a call option is the price of the futures:
 - Even if the strike price is zero, no buyer would pay more than the price of the futures.
- The minimum price of a call option is the intrinsic value, if any:
 - If the time value equals zero, than a buyer would not pay more than the intrinsic value.

Price limits for options: put

- The maximum value of a put option is the strike price:
 - The maximum value of a put option is when the price of the futures contract equals zero.
- The minimum price of a put option is the intrinsic value, if any:
 - If the time value equals zero, than a buyer would not pay more than the intrinsic value.

Maximum and minimum price for options

Table : Maximum and minimum price for options

	Call option	Put option
Max. price	Futures price	Strike price
Min. price	$\text{Max}[0, (\text{futures price} - \text{strike price})]$	$\text{Max}[0, (\text{strike price} - \text{futures price})]$

Speculation using options

- Speculation is an attempt to profit from movements in the price of assets.
- Speculation using futures is relatively straightforward:
 - The seller of a futures contract, short position, gains if the price declines.
 - The buyer of a futures contract, long position, gains if the price increases.
- For options, gains are directly related to the price of the underlying futures contract.

- A *bear market* is when the price of a commodity declines.
 - If you are attacked by a bear, it will strike you DOWN with its claws.
 - A speculator who takes a bearish position expects the price of a commodity to decline.
- A *bull market* is when the price of a commodity increases.
 - If you are attacked by a bull, it will strike you UP with its horns.
 - A speculator who takes a bullish position expects the price of a commodity to increase.

Wall Street bull



Position and price expectations

Table : Position and price expectations

	Call option	Put option
Buyer	Bullish	Bearish
Seller	Neutral to bearish	Neutral to bullish

Why are sellers of options neutral?

- The seller of an option immediately receives the premium.
- Thus, a seller makes an immediate gain from selling the option.
- Future losses depend on the movement of the underlying contract.
- Given that losses are possible, and that underlying the option there is a futures contract, the seller of an option must have a margin account.
- The option may never be exercised.

Payoffs from call option

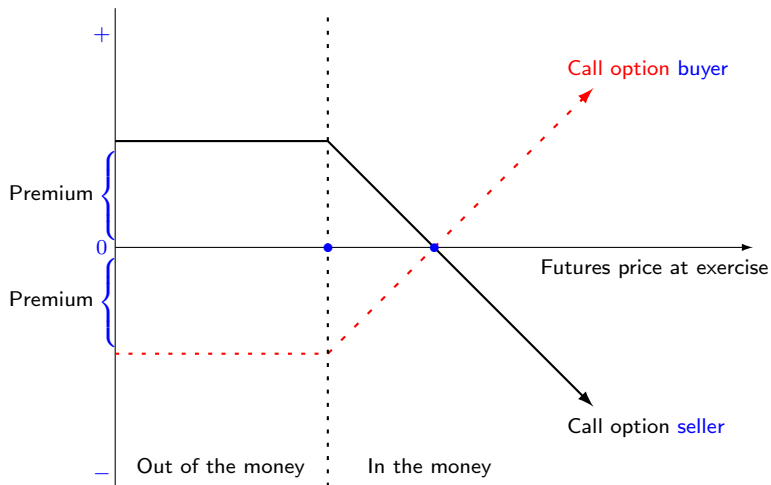


Figure : Call option payoff line

Payoffs from put option

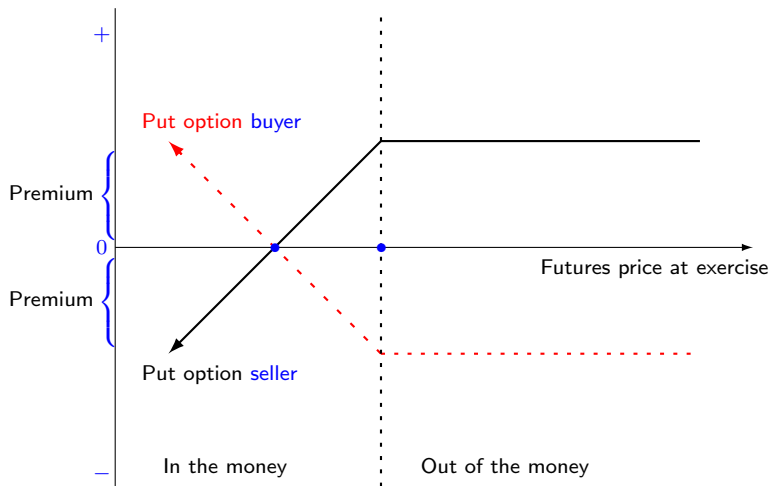


Figure : Payoffs from put option

Carter, C.A. 2003. *Futures and Options Markets: An Introduction*.
Waveland Press, Inc.