Answers to Problem Set 1 Group name: Ferienspass

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1 Question 1

1.1

A market equilibrium occurs when markets clear. This implies no excess demand (D) or supply (S) of Goods. Thus, $q_D = q_S$. This only occurs when $p_D = p_S$ (the market clearing price prevails).

$$p_D = p_S$$

using

$$p_D = a - b * q_D$$
 and $p_S = c + d * q_S$

we get

$$a - b * q_D = c + d * q_S$$

$$0 = c + d * q_S - (a - b * q_D)$$

$$0 = c - a + d * q_S + b * q_D$$

$$0 = b * q_D + d * q_S - (a - c)$$

Since $q_D = q_S$ holds, this can be simplified even further

$$0 = (b+d) * q - (a-c)$$
 (1)

1.2

Analytical computation of the equilibrium allocation. Alternative approach of previous question used. First, set quantities equal, $q_D = q_S$ and calculate the resulting equilibrium price p^* . By inserting the equilibrium price into both quantity functions, we get the equilibrium quantity and can show that $q_D = q_S$ in fact holds.

$$q_D = q_S$$

$$\frac{a-p}{b} = \frac{c-p}{d}$$

$$d(a-p) = b(p-c)$$

$$da + bc = p(d+b)$$

$$\frac{da+bc}{d+b} = p^*$$

Now, insert into the quantity functions:

$$q_D = \frac{a - p^*}{b} \qquad q_S = \frac{c - p^*}{d}$$

$$q_D = \frac{a - \frac{da + bc}{d + b}}{b} \qquad q_S = \frac{c - \frac{da + bc}{d + b}}{d}$$

$$q_D = \frac{a - c}{d + b} = q \qquad q_S = \frac{a - c}{d + b} = q$$

which can also be computed by rearranging (1):

$$0 = (b+d) * q - (a-c)$$
$$(a-c) = (b+d) * q$$
$$\frac{a-c}{b+d} = q$$

1.3

The LU decomposition. The application of this procedure can be found in the MATLAB file PS1Q1.m.

1. Rearrange the equations given in the problem set so that, when solving for x, we solve for x = [p, q]'.

$$a = p + bq$$

$$c = p - dq$$

Which gives the system

$$\begin{pmatrix} 1 & b \\ 1 & -d \end{pmatrix} \begin{pmatrix} p \\ q \end{pmatrix} = \begin{pmatrix} a \\ c \end{pmatrix}$$

2. Decompose the matrix A into the two factors L and U:

$$A = L * U = \begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} 1 & b \\ 0 & -b - d \end{pmatrix}$$

Which then gives the following system of equations:

$$\begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} 1 & b \\ 0 & -b - d \end{pmatrix} \begin{pmatrix} p \\ q \end{pmatrix} = \begin{pmatrix} a \\ c \end{pmatrix}$$

- 3. Solve this system of equations.
 - (a) First solve Ly = b by forward induction.

$$\begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} a \\ c \end{pmatrix}$$

$$y_1 = a$$

$$y_1 + y_2 = c$$

which gives

$$y_1 = a$$

$$y_2 = c - a$$

(b) Then solve Ux = y by backward induction.

$$\begin{pmatrix} 1 & b \\ 0 & -(b+d) \end{pmatrix} \begin{pmatrix} p \\ q \end{pmatrix} = \begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} a \\ c-a \end{pmatrix}$$

$$-(b+d)q = y_2 = c - a$$

$$p + bq = a$$

which gives

$$q = \frac{a - c}{b + d}$$

$$p = \frac{ad+bc}{b+d}$$

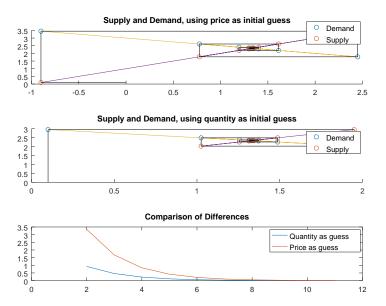
1.4

```
% Subquestion 4 - LU-Decomposition
clear;
clc;
close all;
a=3;
b = 0.5;
c=1;
d=c;
A = [1, b; 1 - d];
y = [a; c];
[L,U]=lu(A);
t=L \setminus y;
x=U \setminus t;
disp(['LU Result: The market clearing price', num2str(x(1,1)), 'clears the man
LU Result: The market clearing price 2.3333 clears the market at the quantity
1.3333!
1.5
% Subquestion 5 - Gauss-Seidel fixed-point iteration
clear;
a = 3;
b = 0.5;
c=1;
d=c;
%initial guess of quantity
%Set up difference criterion to a value higher than in the while loop
q_difference=100;
%Set up empty vectors for storage of historical values
q_difference_hist=nan(100,1);
q_Dp_hist=nan(100,1);
q_Dq_{hist}=nan(100,1);
```

```
q_Sq_hist=nan(100,1);
q_Sp_hist=nan(100,1);
q_Time=nan(100,1);
%Iteration index
i = 1;
%Begin iteration
while q_difference > 0.01
    q_Dp=a-b*q;
                        %Demand-price from initial quantity
    q_Dp_hist(i,1) = q_Dp;
    q_Dq_hist(i,1)=q;
                          %Supply-quantity from Demand-price
    q_Sq = (q_Dp - c)/d;
    q_Sq_hist(i,1) = q_Sq;
                           %Supply-price for difference
    q_Sp=c+d*q_Sq;
    q_Sp_hist(i,1)=q_Sp;
    if i > 1
    q_difference=abs(q_Sp_hist(i,1)-q_Dp_hist(i-1,1));
    q_difference_hist(i,1) = q_difference;
    end
    q=q_-Sq;
                        %Quantity for next guess set
    q_{-}Time(i,1)=i;
    i = i + 1;
end
disp (['Gauss-Seidel Iteration Result (using quantity as initial guess): The mark
Gauss-Seidel Iteration Result (using quantity as initial guess): The market clear-
ing price 2.3357 clears the market at the quantity 1.3357 after 9 iterations!
%Alternatively: Using the price as a first guess
%Initial Guess
p = 0.1;
%Set up difference criterion to a value higher than in the while loop
difference=100;
%Set up empty vectors for storage of historical values
difference_hist=nan(100,1);
Dp_hist=nan(100,1);
Dq_hist=nan(100,1);
```

```
Sq_hist=nan(100,1);
Sp_hist=nan(100,1);
Time=nan (100, 1);
%Iteration index
i = 1;
while difference > 0.01
                     %Supply-quantity from price
    Sq=(p-c)/d;
    Sq_hist(i,1)=Sq;
    Sp=p;
                 %Supply-price for difference
    Sp_hist(i,1)=Sp;
                       %Demand-price from initial quantity
    Dp=a-b*Sq;
    Dp_hist(i,1)=Dp;
    Dq_hist(i,1)=Sq;
    difference=abs(Sq_hist(i-1,1)-Dq_hist(i,1));
    difference_hist(i,1)=difference;
    end
    p=Dp;
                      %Quantity for next guess set
    Time (i, 1) = i;
    i=i+1;
end
disp (['Gauss-Seidel Iteration Result (using price as initial guess): The market
Gauss-Seidel Iteration Result (using price as initial guess): The market clearing
price 2.3312 clears the market at the quantity 1.3312 after 11 iterations!
figure
subplot (3,1,1);
scatter (Dq_hist , Dp_hist )
hold on
scatter (Sq_hist, Sp_hist)
plot(Dq_hist, Dp_hist, Sq_hist, Sp_hist)
line ([Sq_hist(1,1) \ 0], [Sp_hist(1,1) \ Sp_hist(1,1)])
%TO SHOW HOW THE ALGORITHM WORKS!
for j = 1:(i-1)
line([Dq\_hist(j,1) \ Sq\_hist(j+1,1)], [Dp\_hist(j,1) \ Dp\_hist(j,1)])
```

```
end
for i = 1:(i-1)
line ([Sq\_hist(j,1) Sq\_hist(j,1)], [Dp\_hist(j,1) Sp\_hist(j,1)])
title ('Supply and Demand, using price as initial guess')
legend('Demand', 'Supply')
hold off
subplot(3,1,2);
scatter (q_Dq_hist, q_Dp_hist)
hold on
scatter (q_Sq_hist, q_Sp_hist)
plot(q_Dq_hist,q_Dp_hist,q_Sq_hist,q_Sp_hist)
line ([q_Dq_hist(1,1) \ q_Dq_hist(1,1)], [q_Dp_hist(1,1) \ 0])
%TO SHOW HOW THE ALGORITHM WORKS!
for j = 1:(i-1)
line([q_Dq_hist(j,1) \quad q_Sq_hist(j,1)], \quad [q_Dp_hist(j,1) \quad q_Dp_hist(j,1)])
end
for j = 1:(i-1)
line([q_Sq_hist(j,1) \quad q_Sq_hist(j,1)], \quad [q_Dp_hist(j,1) \quad q_Sp_hist(j+1,1)])
end
title ('Supply and Demand, using quantity as initial guess')
legend('Demand', 'Supply')
hold off
%To show convergence
%figure
%plot (q_Time, q_difference_hist)
%title ('Difference, using quantity as initial guess')
subplot(3,1,3);
plot(q_Time, q_difference_hist, Time, difference_hist)
title ('Comparison of Differences')
legend ('Quantity as guess', 'Price as guess')
%Non convergent case
a=3;
b = 0.5;
c=b:
d=c;
```

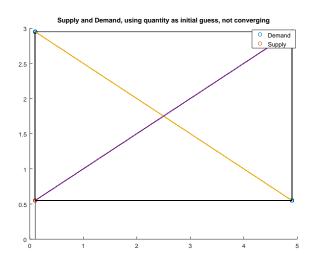


%initial guess of quantity q=0.1;

%Set up difference criterion to a value higher than in the while loop $nq_difference=100;$

%Set up empty vectors for storage of historical values

```
nq_difference_hist=nan(100,1);
nq_Dp_hist=nan(100,1);
nq_Dq_hist=nan(100,1);
nq_Sq_hist=nan(100,1);
nq_Sp_hist=nan(100,1);
nq_Time=nan(100,1);
%Iteration index
%Begin iteration
for i = 1:100
    nq_Dp=a-b*q;
                         %Demand-price from initial quantity
    nq_Dp_hist(i,1) = nq_Dp;
    nq_Dq_hist(i,1)=q;
    nq_Sq = (nq_Dp - c)/d;
                             %Supply-quantity from Demand-price
    nq_Sq_hist(i,1) = nq_Sq;
                              %Supply-price for difference
    nq_Sp=c+d*nq_Sq;
    nq_Sp_hist(i,1) = nq_Sp;
    if i > 1
    nq_difference=abs(nq_Sp_hist(i,1)-nq_Dp_hist(i-1,1));
    nq_difference_hist(i,1)=nq_difference;
    end
                         %Quantity for next guess set
    q=nq_Sq;
    nq_Time(i,1)=i;
end
figure
scatter (nq_Dq_hist, nq_Dp_hist)
hold on
scatter (nq_Sq_hist, nq_Sp_hist)
plot(nq_Dq_hist, nq_Dp_hist, nq_Sq_hist, nq_Sp_hist)
line (\lceil nq_Dq_hist(1,1) \quad nq_Dq_hist(1,1) \rceil, \quad \lceil nq_Dp_hist(1,1) \quad 0 \rceil)
%TO SHOW HOW THE ALGORITHM WORKS!
for j = 1:(i-1)
line([nq\_Dq\_hist(j,1) nq\_Sq\_hist(j,1)], [nq\_Dp\_hist(j,1) nq\_Dp\_hist(j,1)])
for j = 1:(i-1)
line ([nq\_Sq\_hist(j,1) \quad nq\_Sq\_hist(j,1)], \quad [nq\_Dp\_hist(j,1) \quad nq\_Sp\_hist(j+1,1)])
title ('Supply and Demand, using quantity as initial guess, not converging')
legend('Demand', 'Supply')
hold off
```

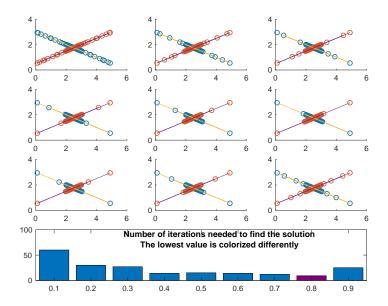


1.6

```
%% Subquestion 6 - Using a dampening factor lambda=linspace (0.1,0.9,9); iteration_count=nan(9,1); a=3; b=0.5; c=b; d=c;
```

```
%Set up empty vectors for storage of historical values
d_difference_hist=nan(100,1);
d_Dp_hist=nan(100,1);
d_Dq_hist=nan(100,1);
d_Sq_hist=nan(100,1);
d_Sp_hist=nan(100,1);
d_{\text{-}}\text{Time}=\text{nan}(100,1);
figure
for j=1:9
%initial guess of quantity
q = 0.1;
%Set up difference criterion to a value higher than in the while loop
d_difference=100;
i = 1;
while d_difference > 0.01
    d_Dp=a-b*q;
                        %Demand-price from initial quantity
    d_Dp_hist(i,1)=d_Dp;
    d_Dq_hist(i,1)=q;
                          %Supply-quantity from Demand-price
    d_Sq=(d_Dp-c)/d;
    d_Sq_hist(i,1) = d_Sq;
                           %Supply-price for difference
    d_Sp=c+d*d_Sq;
    d_Sp_hist(i,1) = d_Sp;
    if i>1
    d_difference=abs(d_Sp_hist(i,1)-d_Dp_hist(i-1,1));
    d_difference_hist(i,1) = d_difference;
    q = lambda(1, j) * d_Sq_hist(i, 1) + (1 - lambda(1, j)) * d_Sq_hist(i-1, 1);
    else
    q=d_{-}Sq;
    %Quantity for next guess set
    d_{-}Time(i,1)=i;
    i=i+1;
end
iteration\_count(j,1)=i;
subplot(4,3,j)
scatter (d_Dq_hist, d_Dp_hist)
```

```
hold on
scatter (d_Sq_hist, d_Sp_hist)
plot(d_Dq_hist,d_Dp_hist,d_Sq_hist,d_Sp_hist)
hold off
end
[\,M,\,I\,\,] \ = \ \min\left(\,\mathrm{iteration\_count}\,\,\right);
Size_I=size(I);
c = categorical({'0.1', '0.2', '0.3', '0.4', '0.5', '0.6', '0.7', '0.8', '0.9'});
%bar(c, iteration_count)
subplot(4,3,[10 \ 11 \ 12]);
for i=1:Size_I(1,2) %allows for multiple minima
b = bar(c, iteration_count);
title ({'Number of iterations needed to find the solution'; 'The lowest value is c
set (get (gca, 'title '), 'Position', [5.5 60 1])
b.FaceColor = 'flat';
b.CData(I(1,i),:) = [.5 \ 0 \ .5];
```

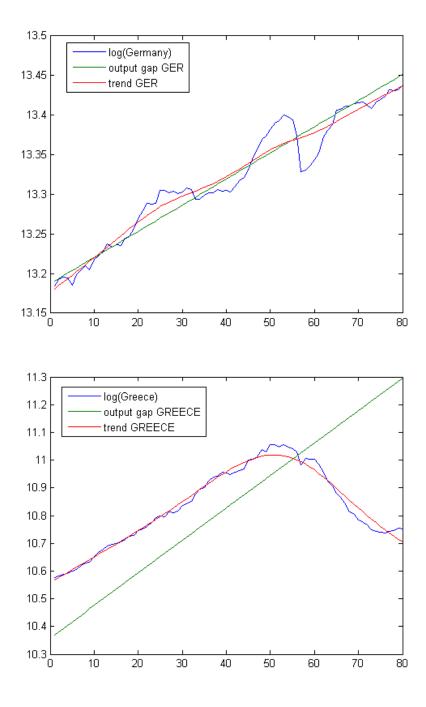


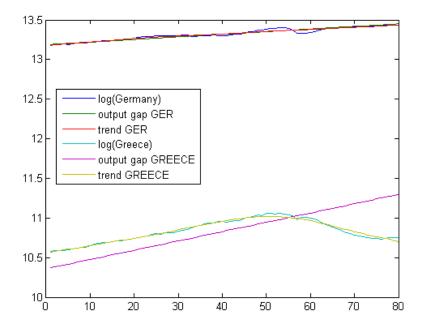
2 Question 2

2.1

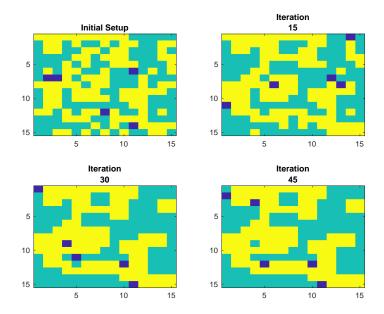
```
M Part 1 - loading and computing the logarithms
clear all;
clc:
A=xlsread('/Users/sebastiankuhnl/Desktop/GSEFM/Year 1/Semester 1.2/Mathematical
Germany=A(1,:);
Greece=A(2,:);
{\tt LogGermany=log\,(\,Germany\,)\,;}
LogGreece=log(Greece);
2.2
%% Part 2 - Applying HP filter
%This version requires machine learning and statistics toolbox
smoothing = 1600; %unecessary since it is the default value of the function but
TrendGermany = hpfilter (LogGermany, smoothing);
TrendGreece = hpfilter (LogGreece, smoothing);
2.3
% Part 3 - Applying OLS
%Creating time variable
Time = zeros(size(Greece));
Size = size (Greece);
for i=1: Size(1,2)
    Time(1,i)=i;
end
%OLS
Var_GRE=var (LogGreece);
Var_GER=var (LogGermany);
Cov_GRE=cov (Time, LogGreece);
Cov_GER=cov (Time, LogGermany);
b_1_GER=Var_GER/Cov_GER(1,2);
b_1_GRE=Var_GRE/Cov_GRE(1,2);
Mean_Time=mean(Time);
Mean_GER=mean (LogGermany);
Mean_GRE=mean(LogGreece);
b_0_GER=Mean_GER-Mean_Time*b_1_GER;
```

```
b_0_GRE=Mean_GRE-Mean_Time*b_1_GRE;
Yhat_GER=b_0_GER+Time*b_1_GER;
Yhat\_GRE=b\_0\_GRE+Time*b\_1\_GRE;
2.4
%% Part 4 - Output Gap
Y_GER_trend_HP=exp(TrendGermany);
Y_GER_trend_OLS=exp(Yhat_GER);
Y_GRE_trend_HP=exp(TrendGreece);
Y_GRE_trend_OLS=exp(Yhat_GRE);
Y_Gap_GER_HP=Germany-transpose(Y_GER_trend_HP);
Y_Gap_GER_OLS=Germany-Y_GER_trend_OLS;
Y_Gap_GRE_HP=Greece-transpose(Y_GRE_trend_HP);
Y_Gap_GRE_OLS=Greece-Y_GRE_trend_OLS;
2.5
%% Part 5 - Plot
figure
plot (Time, LogGermany, Time, Yhat_GER, Time, TrendGermany);
legend('log(Germany)', 'output gap GER', 'trend GER');
figure
plot (Time, LogGreece, Time, Yhat_GRE, Time, TrendGreece);
legend('log(Greece)', 'output gap GREECE', 'trend GREECE');
```





3 Question 3



 $\%\!\%$ Set up the grid

```
clear;
clc;
Board=zeros (15,15);
Iteration_Count = 0;
%110 White (1 indicates white)
i = 1;
while i<111
Col = randi(size(Board, 2));
Row = randi(size(Board, 1));
if Board(Col,Row)==0
    Board (Col, Row)=1;
    i=i+1;
else
end
end
%110 Black (2 indicates black)
j = 1;
while \ j < 111
Col = randi(size(Board, 2));
Row = randi(size(Board, 1));
if Board (Col, Row)==0
    Board (Col, Row) = 2;
    j=j+1;
else
end
end
%Plot situation after zero iterations
figure
subplot(2,2,1)
Plot_0=imagesc (Board);
title('Initial Setup')
for ij = 1:45
%% Spot unoccupied houses
Non_Occupied=zeros (5,2);
Non_Index=1;
for \quad i = 1:15
```

```
\quad \text{for} \quad j = 1:15
         if Board(i, j) == 0
             Non_Occupied (Non_Index,1)=i;
             Non_Occupied(Non_Index, 2) = j;
             if Non\_Index < 5
             Non_Index=Non_Index+1;
             end
         else
         end
    end
end
% Evaluate position
Movers_Location=zeros(15,15);
Movers\_Count = 0;
for i = 1:15
    for j = 1:15
        Self=Board(i,j);
        if Self ~= 0 %Check if the considered house is actually occupied
       %If possible, get neighbor values, alternatively, set equal to zero
            if i==1
            Upper_N=0;
            else
            Upper_N=Board(i-1,j);
            end
            if i==15
            Lower_N=0;
            else
            Lower_N=Board(i+1,j);
            end
            if j==1
            Left_N=0;
            else
            Left_N=Board(i,j-1);
            end
            if j==15
            Right_N = 0;
```

```
else
            Right_N = Board(i, j+1);
            %Compare to neighbors
            Neigh=zeros(4,1);
            Neigh(1,1) = double((Self = Upper_N));
            Neigh(2,1) = double((Self = Lower_N));
            Neigh (3,1) = double ((Self = Left_N));
            Neigh(4,1) = double((Self == Right_N));
            %at least 35% must be equal to not move
            Neigh_Eval=sum(Neigh)/4;
           if Neigh_Eval < 0.35
               Movers_Location(i,j)=1; %everyone with a one wants to move
               Movers_Count=Movers_Count+1;
           end
       \quad \text{end} \quad
    end
end
M Only five households are allowed to move each period (since only five houses
Allowed_Movers=zeros (5,1);
Allowed_Movers_Pos=zeros (5,2);
Want_to_Move=zeros (Movers_Count, 2);
k=1;
for i = 1:15
    for j = 1:15
        if Movers\_Location(i, j) == 1
            %Store to movers
            Want_{to}Move(k,1)=i;
            Want_{to}Move(k,2) = j;
            k=k+1;
       end
    end
end
%Pick five movers
```

```
m=1;
 if Movers_Count>=5
              Movers_Counter=6;
 else
              Movers_Counter=Movers_Count+1;
 end
 while m<Movers_Counter
             New_Mover=randi(Movers_Count);
              if ismember (New_Mover, Allowed_Movers)==0
                           Allowed_Movers (m, 1) = New_Mover;
                          m=m+1;
             end
 end
 for i=1:Movers\_Counter-1
              Allowed_Movers_Pos(i,1)=Want_to_Move(Allowed_Movers(i,1),1);
              Allowed_Movers_Pos(i,2)=Want_to_Move(Allowed_Movers(i,1),2);
 end
What the five households move to a random unoccupied house
Moves\_To = zeros(5,2);
 Unoccupied_NowOccupied=zeros (5,1);
 i = 1;
 while i<Movers_Counter
             Row=randi (Movers_Counter -1);
              if ismember (Row, Unoccupied_NowOccupied)==0
             Unoccupied_NowOccupied(i,1)=Row;
             Moves_To(i,1) = Non_Occupied(Row, 1);
             Moves_To(i,2) = Non_Occupied(Row, 2);
              i=i+1;
             end
end
%Set new location of selected movers to zero, set unoccupied houses to new
%values
 for i=1:Movers\_Counter-1
             Board (Non_Occupied (i,1), Non_Occupied (i,2)) = Board (Allowed_Movers_Pos (i,1), Allowed_Movers_Pos (i,1), Allowed_Movers
             Board \, (\, Allowed\_Movers\_Pos \, (\, i \,\, ,1\, ) \,\, , \, Allowed\_Movers\_Pos \, (\, i \,\, ,2\, ) \, ) = 0;
```

```
end
Iteration_Count=Iteration_Count+1;
Title= ['Iteration' num2cell(Iteration_Count)];
if ij == 15
    subplot(2,2,2)
    Plot_1=imagesc (Board);
    title (Title)
elseif ij == 30
    subplot(2,2,3)
    Plot_2=imagesc(Board);
    title (Title)
elseif ij = 45
    subplot(2,2,4)
    Plot_3=imagesc (Board);
    title (Title)
end
```

A Alternative Moving Understanding P3

```
clear;
%create the hood
Hood=zeros(15,15);
%now generate your people
n=110; %Blacks
m=110; %whites
      %unoccupied
p = 5;
%move your people into the hood
%1: Black
%2: White
%3: unoccupied
plots = 0;
for \quad i = 1:15
  for j = 1:15
     sum=n+m+p;
      x=rand;
      if x < n/sum
          Hood(i,j)=1;
          n=n-1;
     else
        if x < (n+m)/sum
```

end

```
Hood(i,j)=2;
             m=m-1;
        else
             Hood(i, j)=3;
             p=p-1;
        \quad \text{end} \quad
      end
  end
%now this is the hood (black is blue, white is green, unoccupied is red
plots = plots + 1;
figure
subplot (2,2, plots)
imagesc (Hood)
title ({'Initial Setup, blue is black, '; ' green is white, red is unoccupied'})
colorbar
iterations = 0;
%start iteration
for iterations =1:45
%detect mover
Neighbors=zeros (15,15);
Same=zeros (15,15);
movers=0;
Mover = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix};
Free = \begin{bmatrix} 0 & 0 \end{bmatrix};
%check same skin middle
for i = 1:15
   for j = 1:15
        Skin=Hood(i,j);
        if Skin==3
             Free=[Free; i j];
        else
       for z=1:3
       for w=1:3
            if (i+z-2>=1) && (i+z-2<=15)
             if (j+w-2>=1) && (j+w-2<=15)
                if Hood (i+z-2, j+w-2)^{\sim} = 3
                     Neighbors(i,j)=Neighbors(i,j)+1; %number neighbors (including of
             if isequal(Hood(i+z-2,j+w-2),Skin)
              if (z^{=2}) \mid | (w^{=2}) \% dont count yourself
                Same(i,j)=Same(i,j)+1; %number same skin
              end
             end
             end
            end
```

```
end
       end
       Neighbors (i, j)=Neighbors (i, j)-1; %deduct oneself
        if Same(i,j)/Neighbors(i,j) <= 0.35
            movers=movers+1;
            Mover=[Mover; i j Skin];
            Free=[Free; i j];
       end
       end
   end
end
Mover=Mover (2:end,:);
Free=Free(2:end,:);
%move into new house
sz = size(Mover);
for k=1:sz(1,1) %in this loop there is an error if movers<3
     newpos=unidrnd(length(Free),1,1);
     \operatorname{Hood}(\operatorname{Free}(\operatorname{newpos},1),\operatorname{Free}(\operatorname{newpos},2)) = \operatorname{Mover}(k,3);
     Free (newpos,:) = [];
end
Mover = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix};
%make free houses unoccupied
for l=1:length (Free)
     Hood(Free(1,1), Free(1,2)) = 3;
end
if (iterations == 30) || (iterations == 15)
plots = plots + 1;
subplot (2,2, plots)
imagesc (Hood)
title(['After ' num2str(iterations) ' iterations'])
colorbar
end
end
%end of iteration
plots = plots + 1;
subplot (2,2, plots)
imagesc (Hood)
title ('After 45 iterations')
colorbar
```

