CSR 102 4-27-24

Supplemental Lecture

Recall:

$$\frac{1}{1}(n) = \begin{cases} 2 - (\lfloor \frac{2}{3} \rfloor) + N & N \geq 3 \end{cases}$$

$$\frac{1}{|n|} = \sum_{i=0}^{K-1} 2^{i} \cdot \left[\frac{N}{3^{i}} \right] + 2^{K} \quad \text{where } K = \left[\log_{3}(n) \right]$$

$$\leq \sum_{i=0}^{K-1} 2^{i} \left(\frac{N}{3^{i}} \right) + 2^{\log_{3}(n)}$$

$$= N \cdot \sum_{i=0}^{K-1} \left(\frac{2}{3} \right)^{i} + N \cdot \log_{3}(2)$$

$$\leq N \cdot \sum_{i=0}^{\infty} \left(\frac{2}{3} \right)^{i} + N \cdot \log_{3}(2)$$

$$\leq N \cdot \sum_{i=0}^{\infty} (\frac{1}{3}) + N$$

$$= N \cdot \left(\frac{1}{1 - \frac{3}{2}}\right) + N \log_3(2)$$

$$= (n) = O(n)$$

Also by the recorrence

$$= \bigcirc (n) = \bigcirc (n)$$

$$\frac{1}{(n)} = \begin{cases} 5 \\ \frac{1}{(n-2)} + n \end{cases} \quad 0 \le n < 2$$

$$T(n) = n + T(n-2)$$

$$= n + (n-2) + T(n-2\cdot2)$$

$$= n + (n-2) + (n-2\cdot2) + T(n-2\cdot3)$$

$$\vdots$$

$$\vdots$$

$$= \sum_{i=0}^{K-1} (n-2i) + T(n-2K)$$

recorsion terminates when

$$0 \le N - 2K < 2$$

$$2K \le N < 2K + 2$$

$$K \le \frac{N}{2} < K + 1$$

$$C = \lfloor \frac{N}{2} \rfloor$$

$$r = \frac{K-1}{1-2} = \frac{K-1}{1-2} = \frac{K-1}{1-2} = \frac{K-1}{1-2}$$

with K= L=] we have

$$\frac{1}{n} = \begin{cases} 0 & n = 1 \\ \frac{1}{n} = \frac{1}{n} \end{cases}$$

$$T(n) = 1 + T(\lfloor \frac{n}{2} \rfloor)$$

$$= 1 + 1 + T(\lfloor \frac{n}{2} \rfloor)$$

$$= 1 + 1 + T(\lfloor \frac{n}{2} \rfloor)$$

$$= 1 + 1 + T(\lfloor \frac{n}{2} \rfloor)$$

recursion terminates when

Thus

Exe-cise cheek-that T(n)=[19n] really solver the recomence

Exectse

use same Lechnique to Show

$$S(n) = \begin{cases} 0 & n=1 \\ S(LAJ) + 1 & n \geq 2 \end{cases}$$

has solution [S(n) = Flg(n)]

$$S(n) = O(\log n)$$

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$$\frac{1}{\Gamma(n)} = \begin{cases} c & 1 \leq n < 10 \\ \frac{1}{\Gamma(\lfloor \frac{n}{2} \rfloor)} + d & n \geq n_0 \end{cases}$$

$$T(n) = d + T(\lfloor \frac{N}{2} \rfloor)$$

$$= d + d + T(\lfloor \frac{N}{2} \rfloor)$$

$$= 2d + T(\lfloor \frac{N}{2} \rfloor)$$

$$= 2d + T(\lfloor \frac{N}{2} \rfloor)$$

$$\vdots$$

$$= Kd + T(\lfloor \frac{N}{2} \rfloor)$$

To terminate recorssion, we seek the first (i.e. smallest) & such that

K-1=[19(40)]

$$\kappa = \lfloor \lg \left(\frac{1}{n_0} \right) \rfloor + 1$$

Thus

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