



# Raster Analysis

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Today's programme:

9.00-9.45 AM: Lecture on Raster Analysis, part 1

9.55-10.20 AM: Lecture on Raster Analysis, part 2

10.25-11.00 AM: Lecture on Cost Distance analysis

11.00-12.00 AM: Exercise

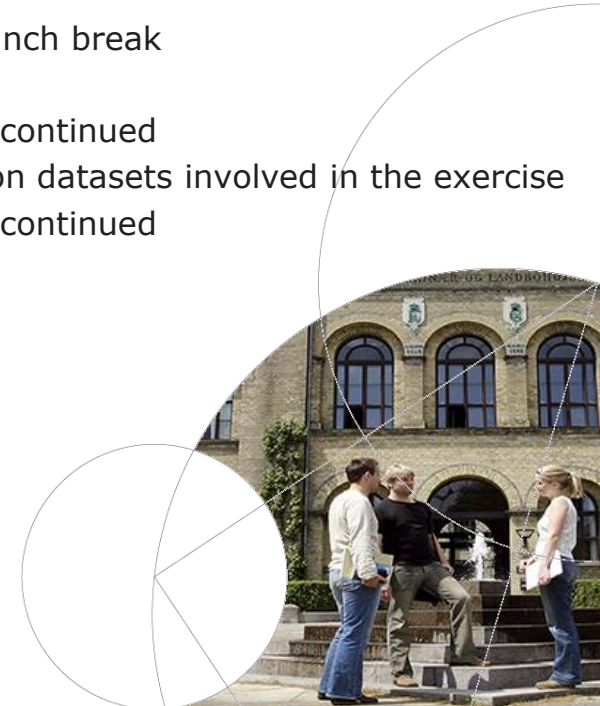
12.00 AM – 1.00 PM: Lunch break

1.00-2.00 PM: Exercise continued

2.00-2.35 PM: Lecture on datasets involved in the exercise

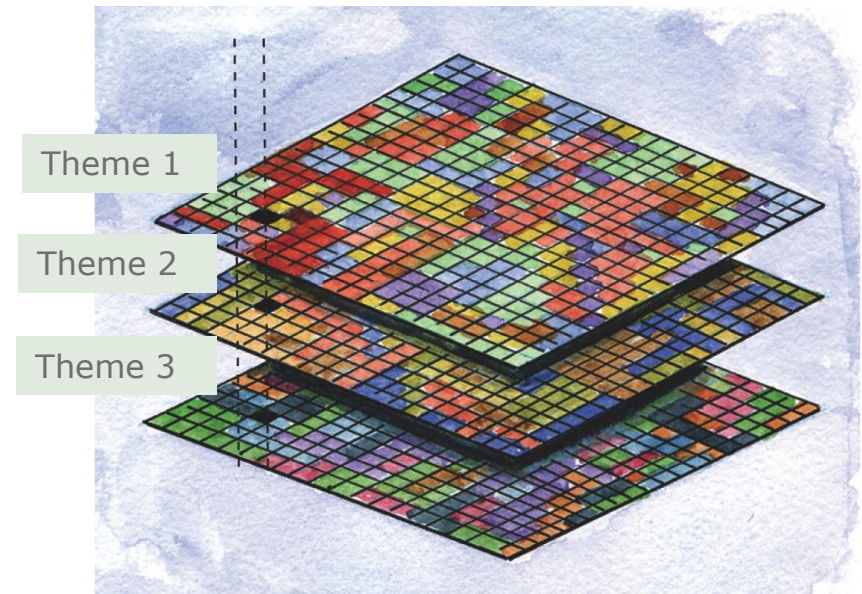
2.35-3.45 PM: Exercise continued

3.45-4.00 PM: Wrap up

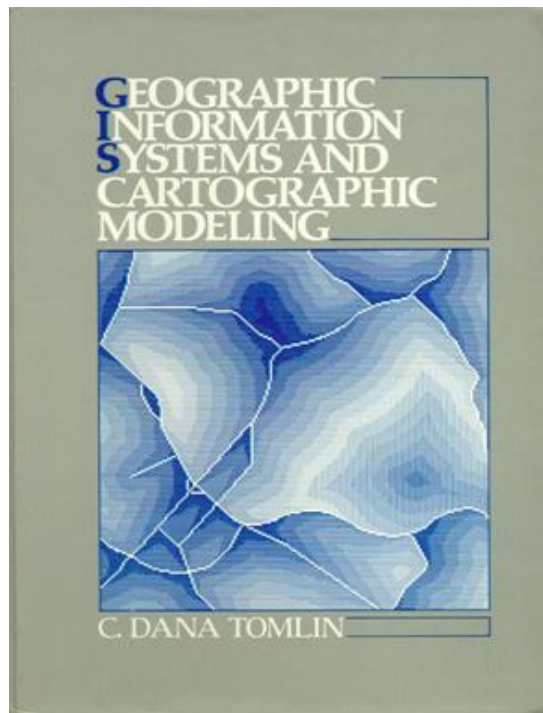


## Agenda

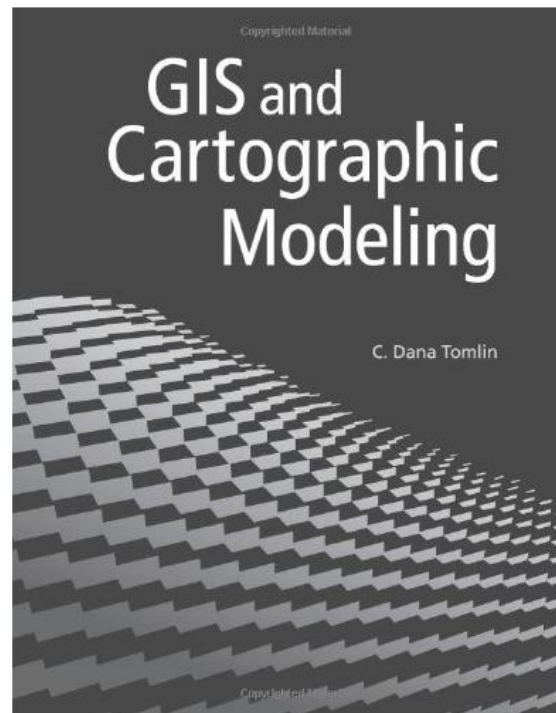
- Introduction to the raster based GIS-datamodel
- When to use it?
- How to use it?
- Map Algebra and cartographic modelling
- Analysis examples



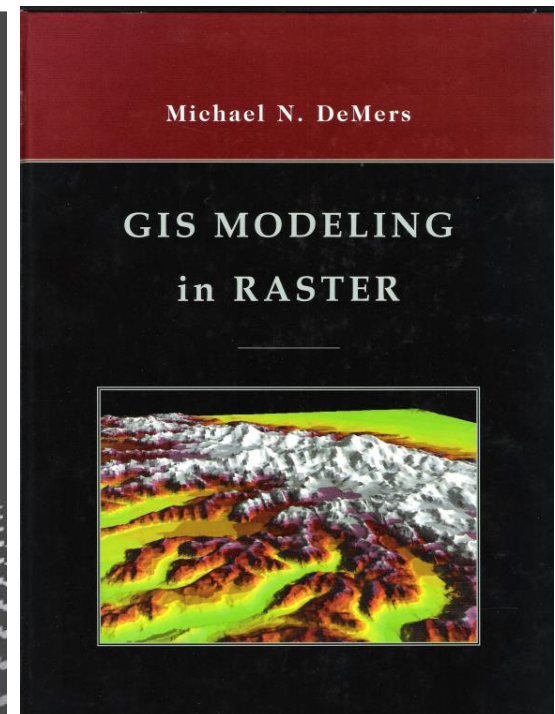
## Literature



1990

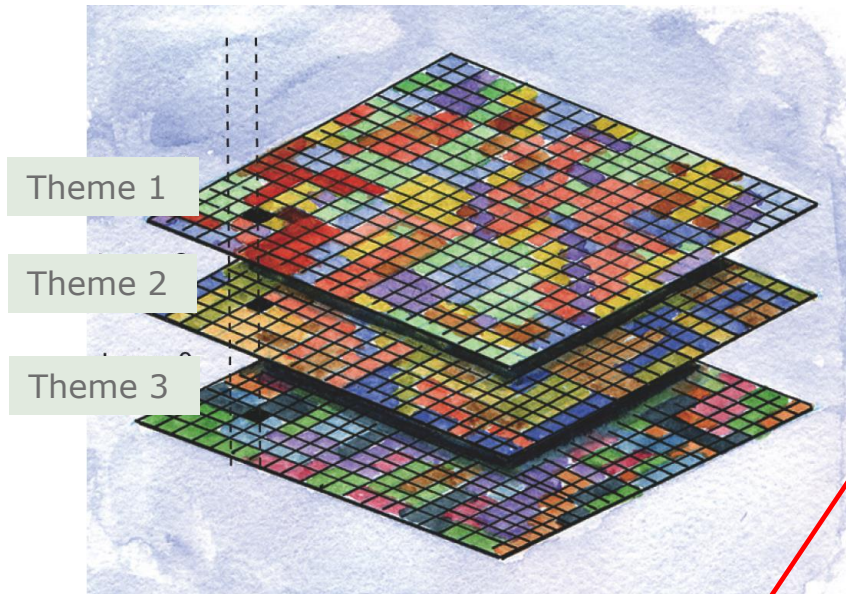


2013



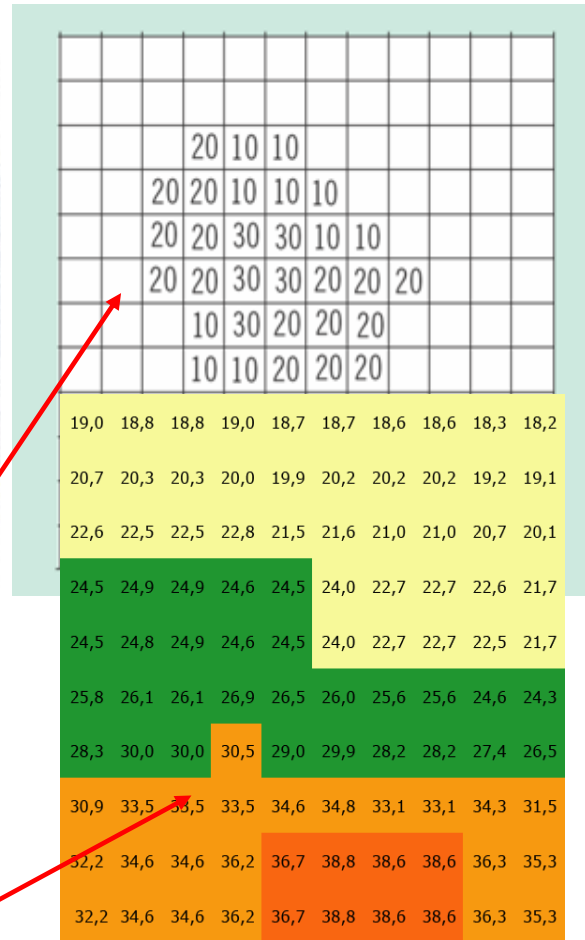
2002

## Raster data – qualitative vs. quantitative data sets

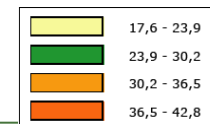


**Qualitative** (discontinuous)  
data set: integers to represent  
a class relationship – like land  
use

**Quantitative** (continuous)  
data set: values according to a  
linear, calibrated scale – like  
terrain elevations relative to a  
vertical datum



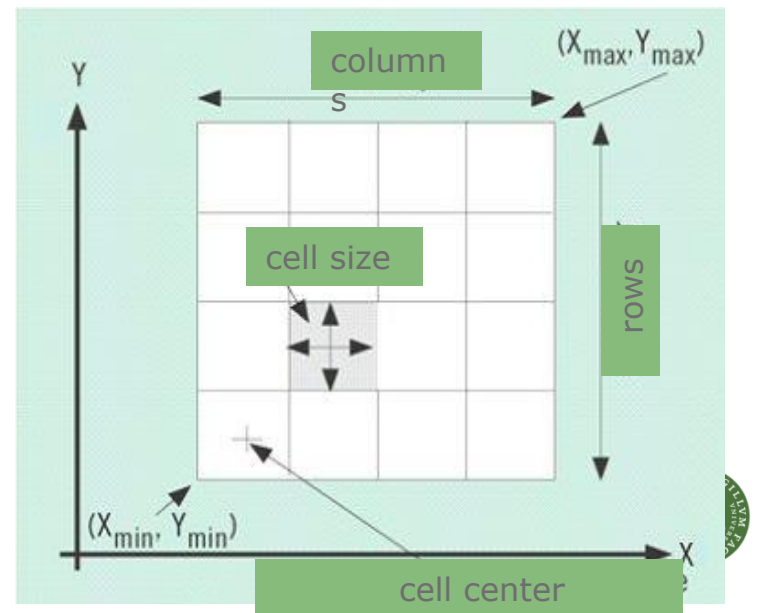
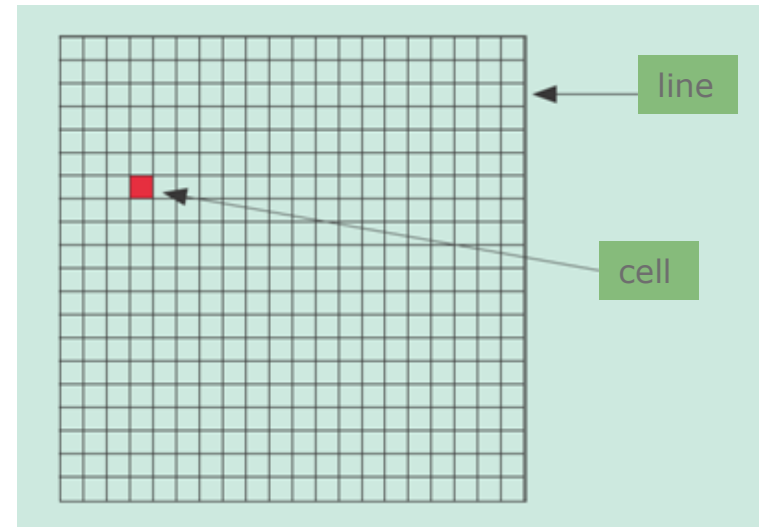
10 = agriculture  
20 = forest  
30 = urban



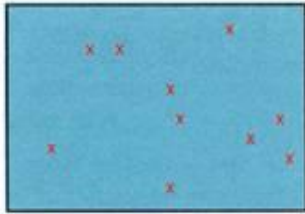


## Raster - definitions

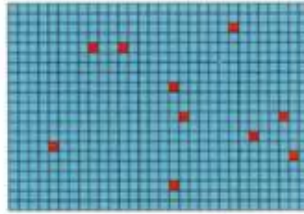
- A cell is referenced by a row/column-position
- All cells in a raster have the same geometric shape and size (spatial resolution)
- If the number of rows and columns, the size of one cell and its orientation are known, the world coordinates to all other cells can be derived
- The topology is implicit – the neighbours are easily identified



## Vector vs. raster?



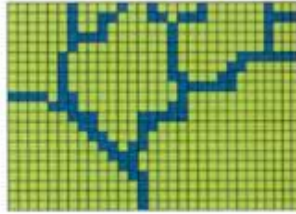
*Point features*



*Raster point features*



*Polyline features*



*Raster line features*



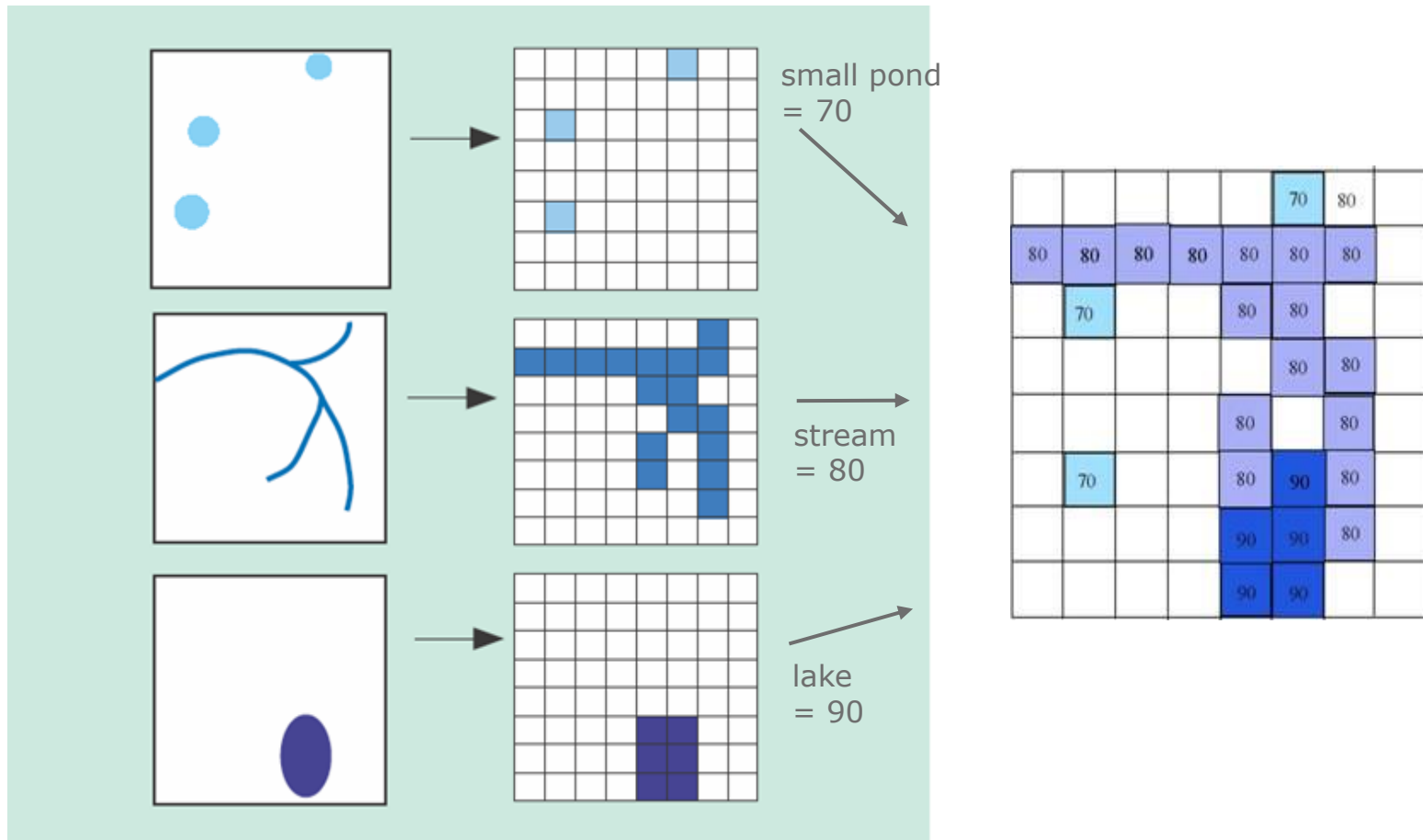
*Polygon features*



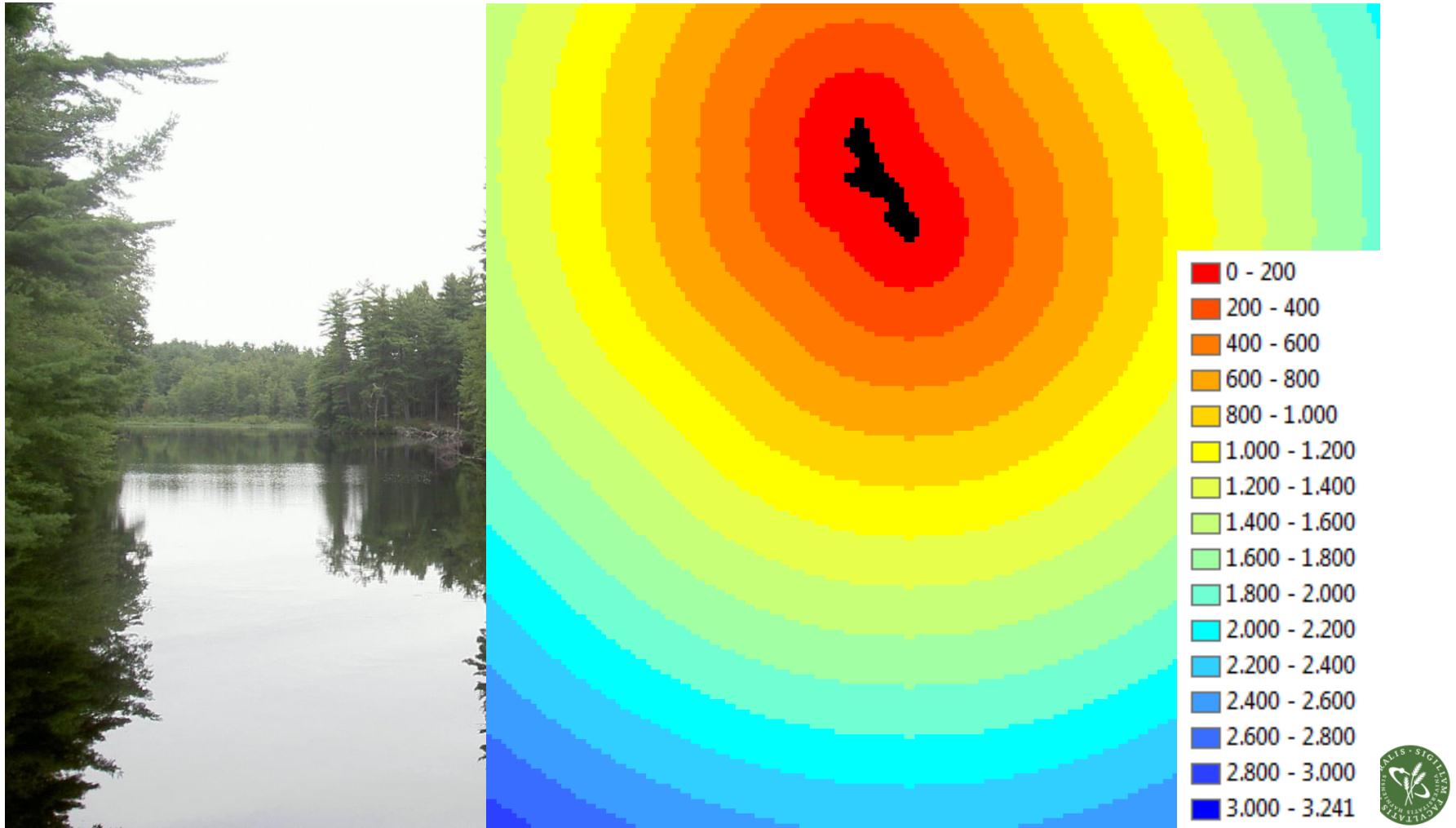
*Raster polygon features*

- Efficient storage
- Easy programming
- Fast computations

## Simple combinations of rasters (cover)

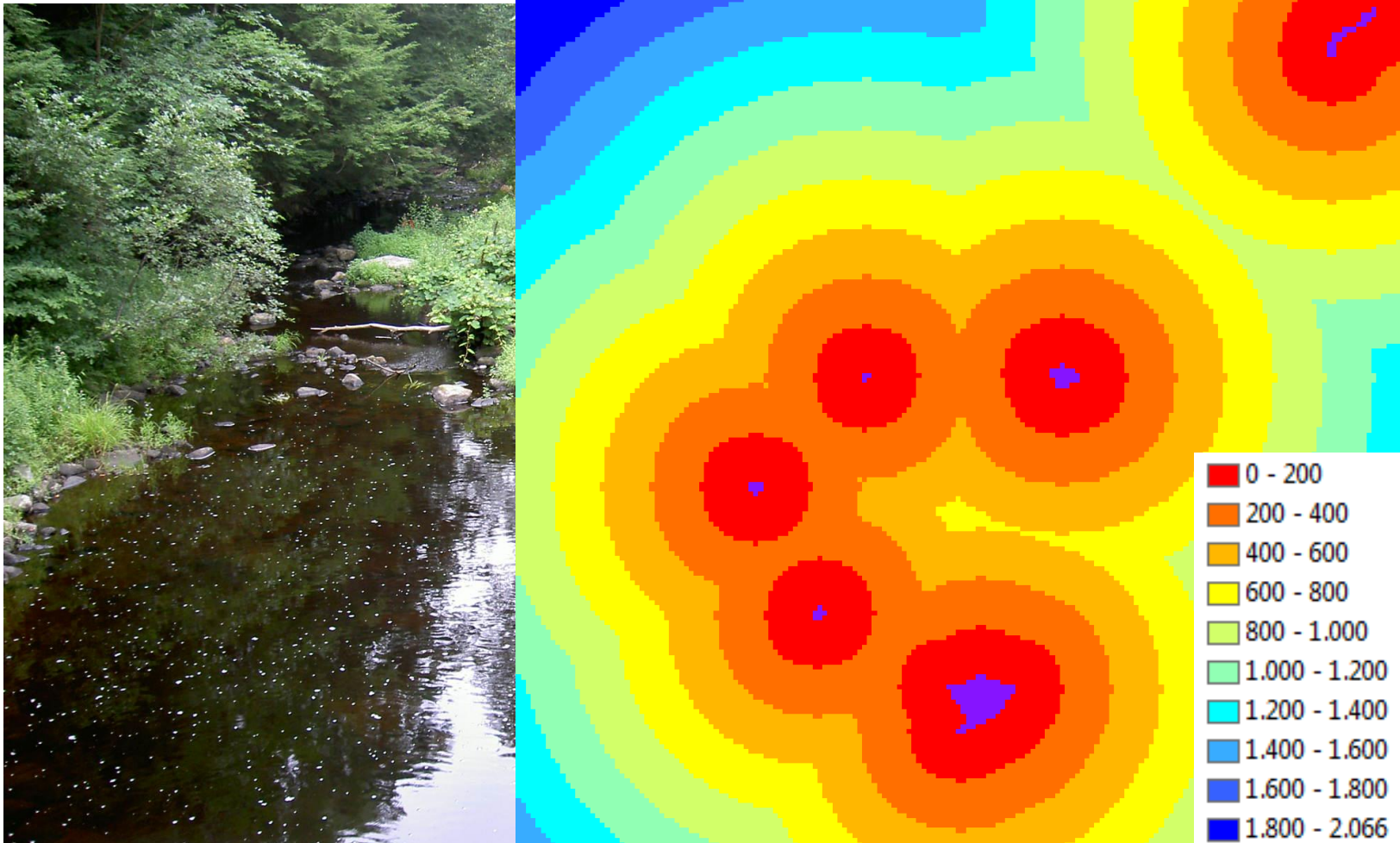


## Browns Pond, Petersham, Massachusetts

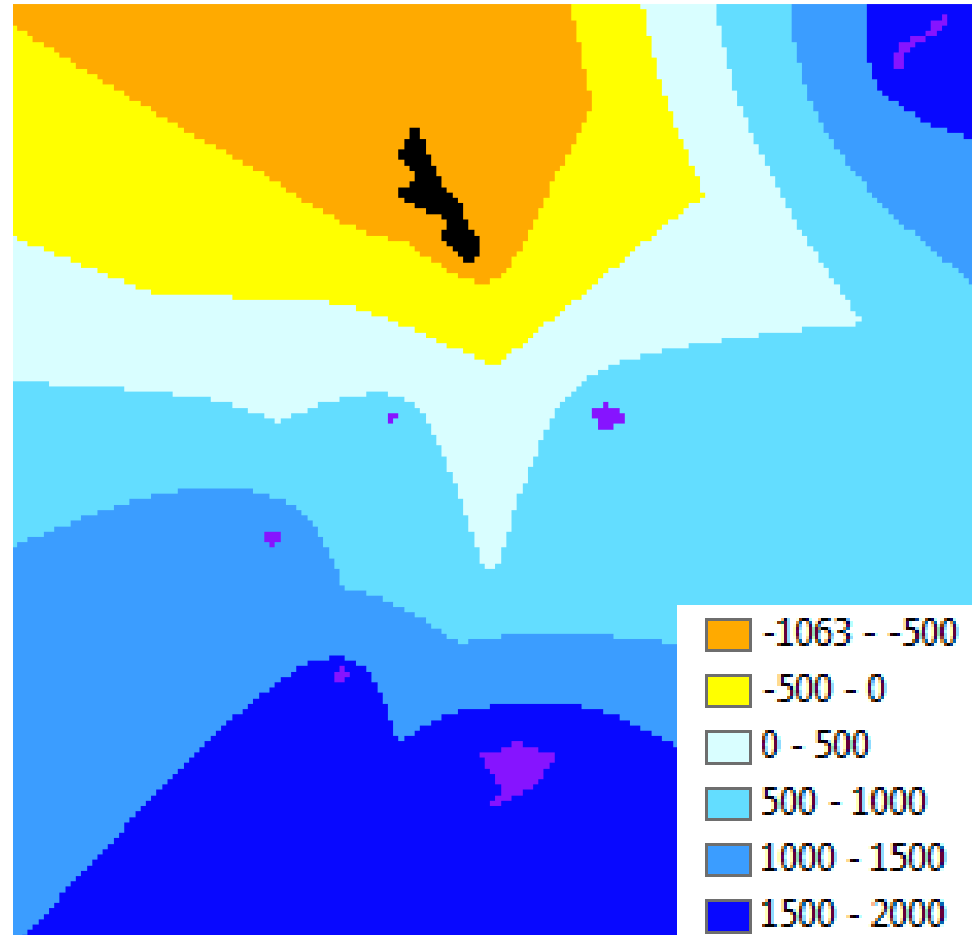
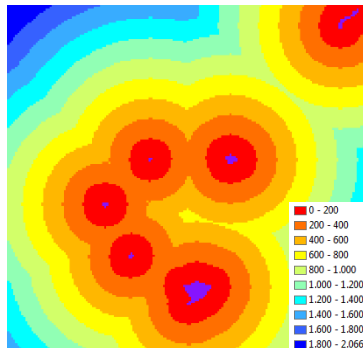
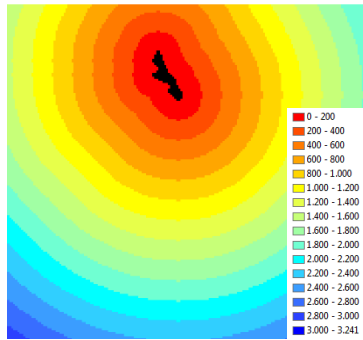




## Other ponds nearby



This figure's cells are found by subtracting the values in the OtherPonds raster from the values in the BrownPond raster. So, what do the values represent?

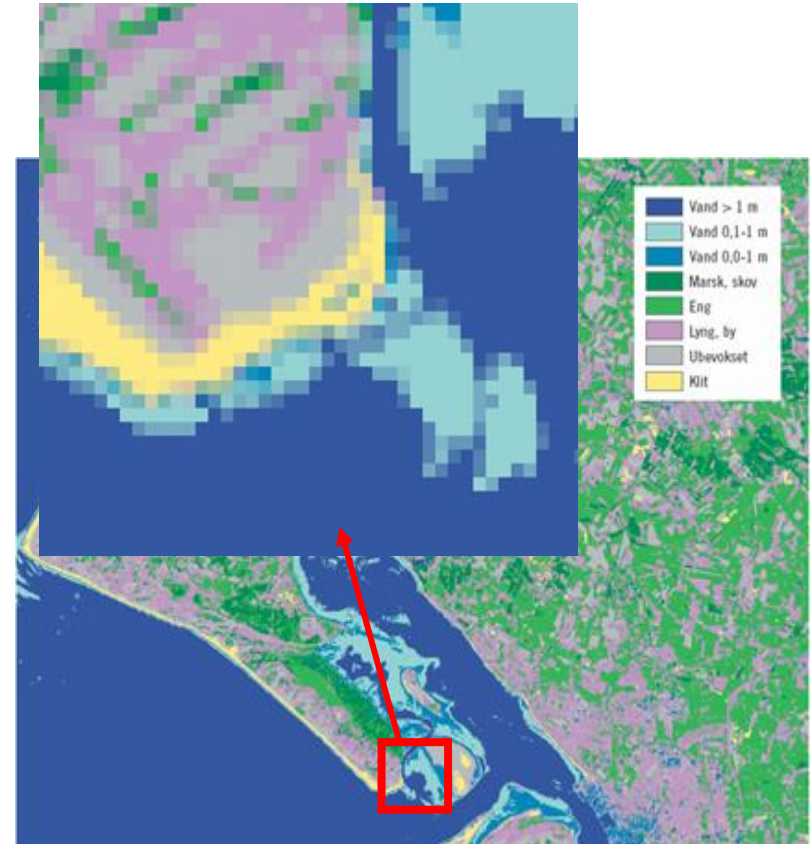


## Facts about the raster based GIS data model

- Introduced during the 1970's due to an increasing demand for analysis of digital satellite data.
- Image processing systems → development of tools for spatial analysis.
- Separate development of vector and raster based GIS data models since the 1990's.
- Today well integrated



## From pixel based classifications ...



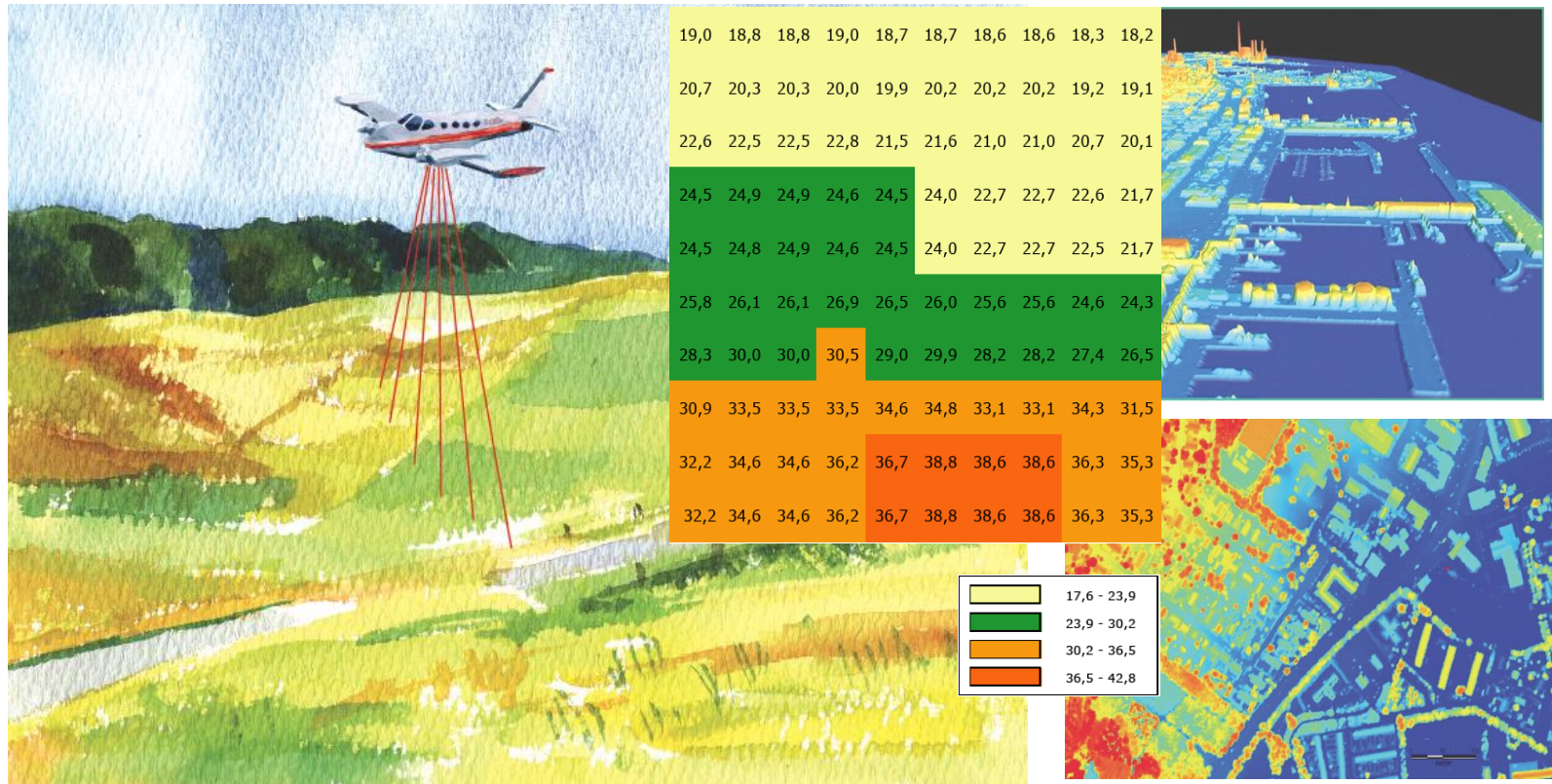


.. to object oriented feature extractions





# Analysis of laser scanned elevation models (LIDAR)



## Map Algebra functions overview

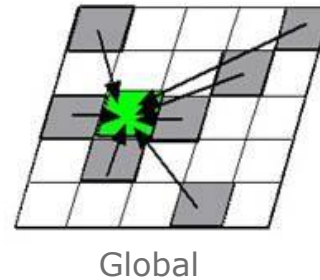
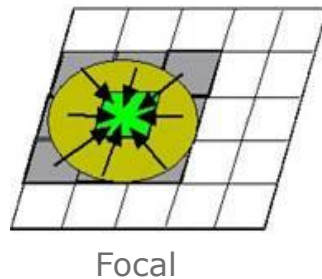
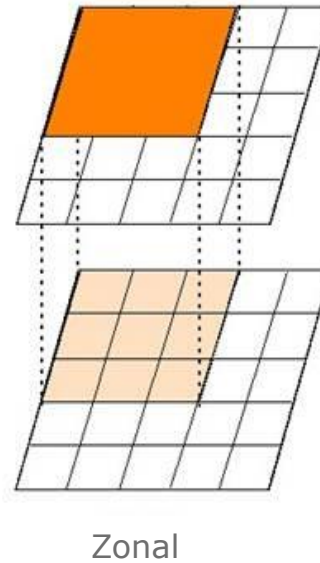
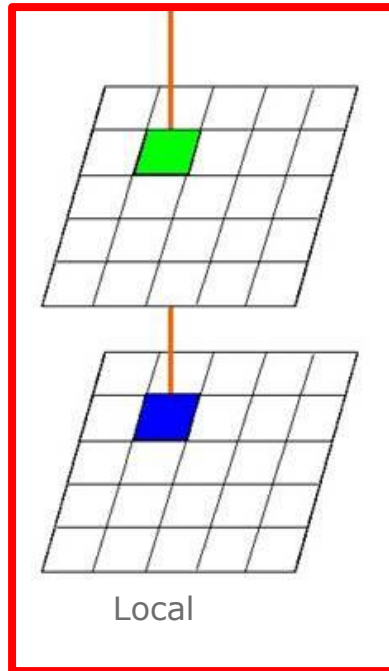
### Functions:

**Local**

Focal

Zonal

Global



## Map algebra and cartographic modelling

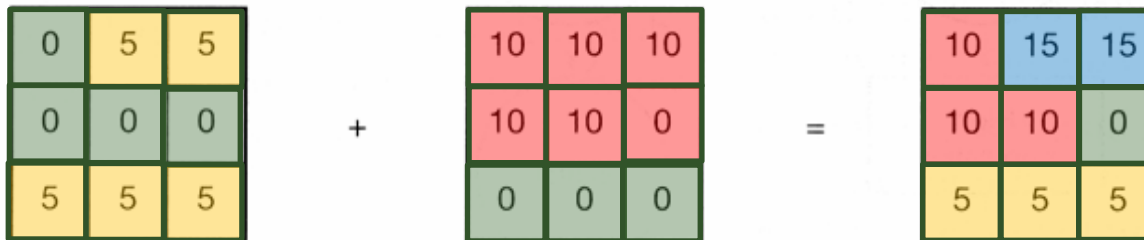
Map Algebra is a modelling language defined by C.D. Tomlin designed to manipulate raster based data.

The basic elements are **objects** and **actions**

Objects are input and output rasters

Actions are operators and functions

Exampel 1: **Local addition** of values cell by cell for two days' precipitation by simple addition of two rasters with calibrated, quantitative data values



Example 2: **Local addition** of two rasters with qualitative data values

0 = open land

0 = private

0 = open land, private, 5 = forest, private

5 = forest

10 = state

10 = open land, state, 15 = forest, state

## Local functions

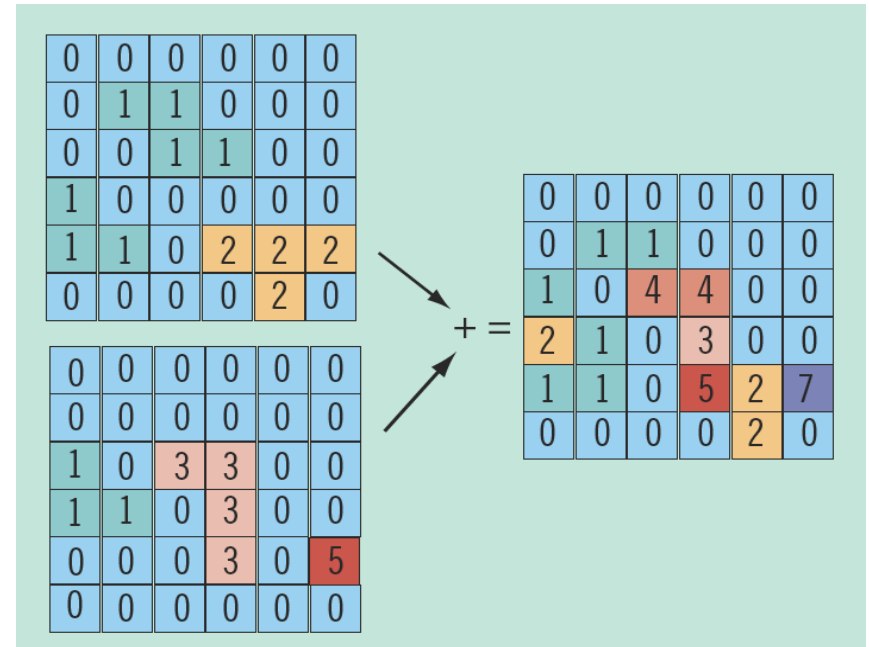
Per-cell functions that calculate a new value for each individual cell based on a mathematical function on one raster or a stack of rasters

Example:

TwoDaysPrecipitation =  
**LocalSum** of PrecipitationDay1  
 and PrecipitationDay1

Other local functions:

Trigonometric (sin, cos, tan ...),  
 logarithmic, truncate, reclassify



## Local functions: Renumbering using the Reclassify tool

16	16	16	19
16	16	19	19
12	12	19	19
12	12	12	19



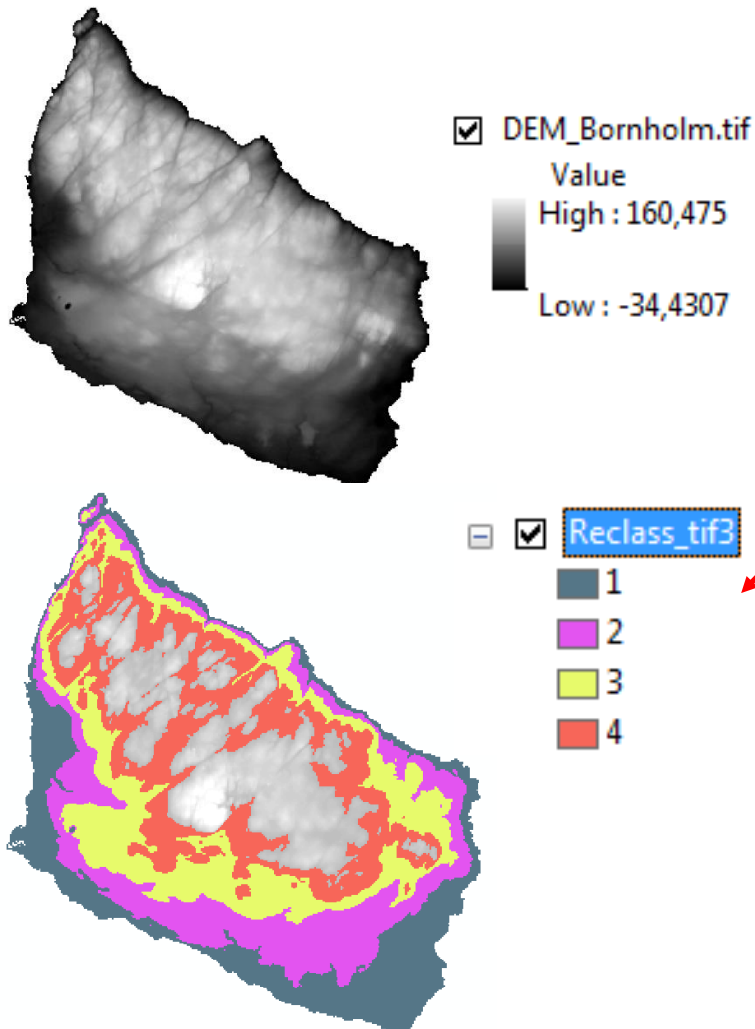
2	2	2	1
2	2	1	1
3	3	1	1
3	3	3	1

Reclassification  
schema

19  $\rightarrow$  1  
16  $\rightarrow$  2  
12  $\rightarrow$  3



## Local functions: Renumbering using the Reclassify tool



**Reclassify**

Input raster: DEM\_Bornholm.tif

Reclass field: Value

Reclassification

Old values	New values
-34,430683 - 26,897326	1
26,897326 - 52,618855	2
52,618855 - 77,659554	3
77,659554 - 100,03154	4
100,03154 - 160,475021	NoData
NoData	NoData

Buttons: Classify..., Unique, Add Entry, Delete Entries, Load..., Save..., Reverse New Values, Precision...

Output raster: C:\Users\Thomas\Documents\ArcGIS\Default.gdb\Reclass.tif3

☐ Change missing values to NoData (optional)

Buttons: OK, Cancel, Environments..., Show Help >>

## Local functions: Reclassify using the CON tool

Inraster

1	1	0	0
	1	2	2
4	0	0	2
4	0	1	1

If expression = True

If expression = False

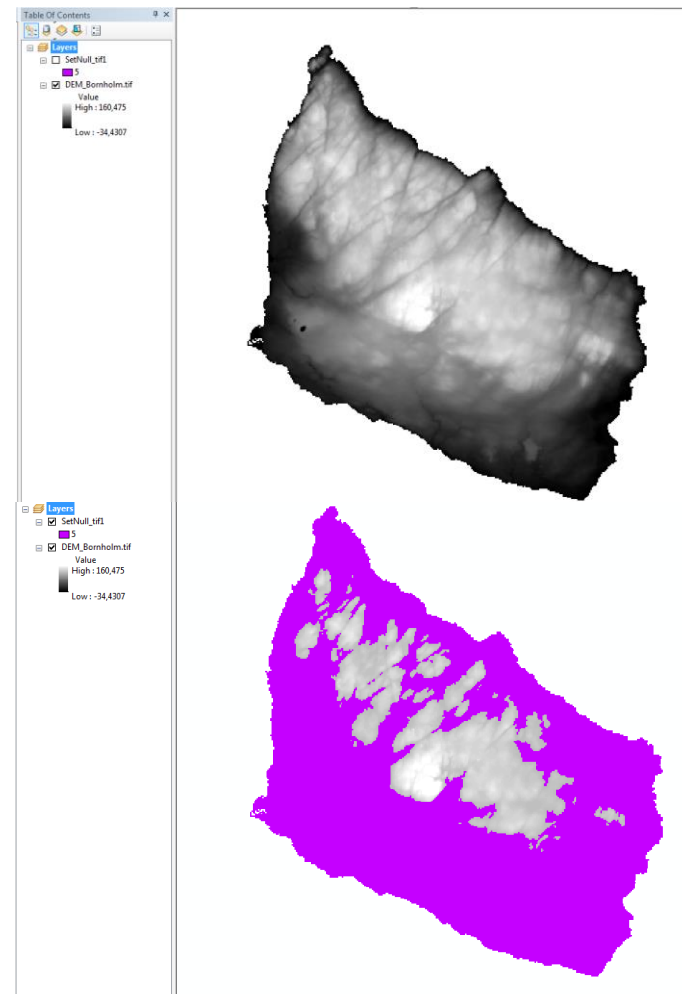
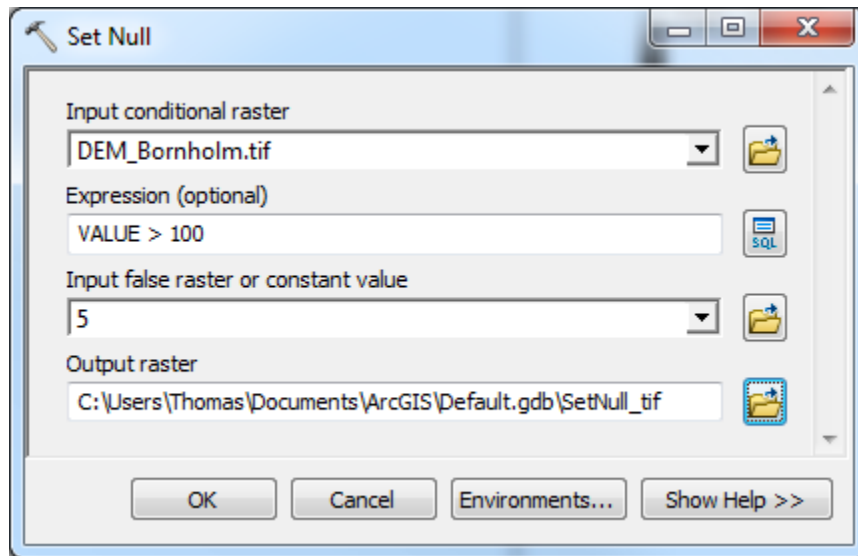
Outraster = Con(Inraster, 40, 30, "Value >=2" )

Outraster

30	30	30	30
	30	40	40
40	30	30	40
40	30	30	30

## Local functions: Reclassify using the SetNull tool

Assigns NODATA value to specific cells



# Functions - overview

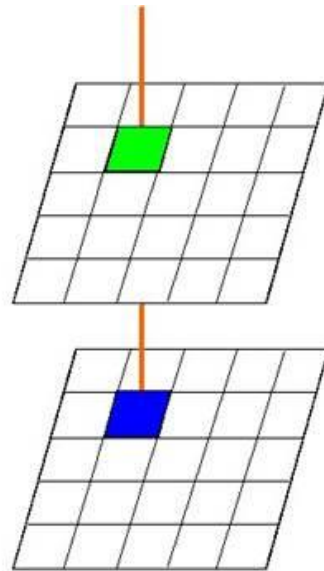
## Functions:

## Local

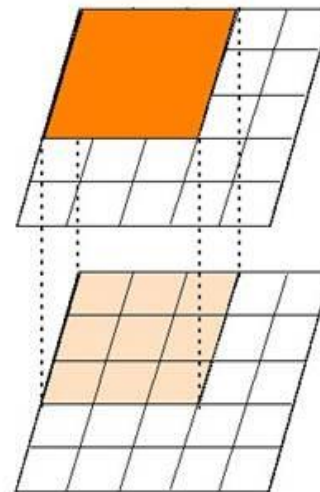
## Focal

## Zonal

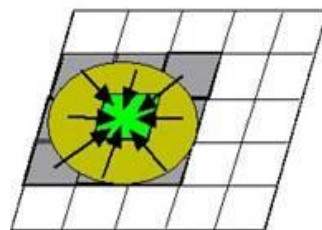
# Global



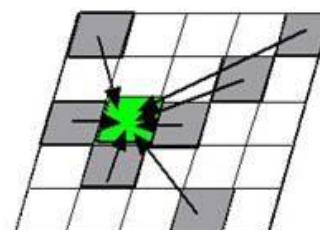
Local



## Zonal



## Focal



Global

## Focal functions

Per-neighbour functions that calculate a new value for each individual cell based on a search within a specific neighborhood.

Example:

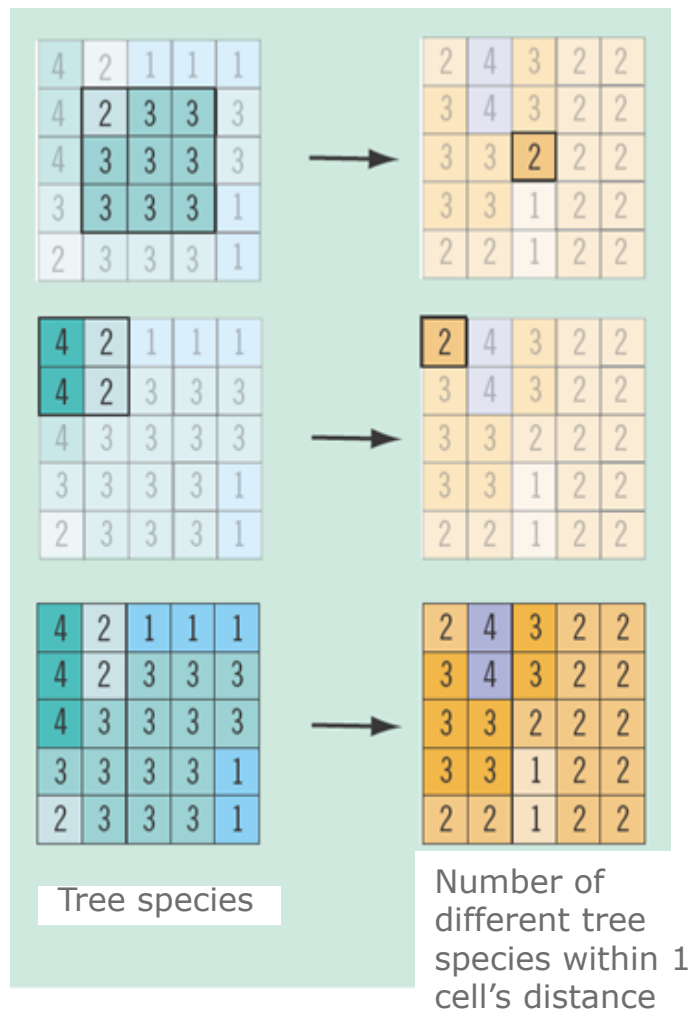
NumberOfTreeSpecies =

**FocalVariation** of Trees within 1

Other focal functions:

Sum, min, max, majority, range

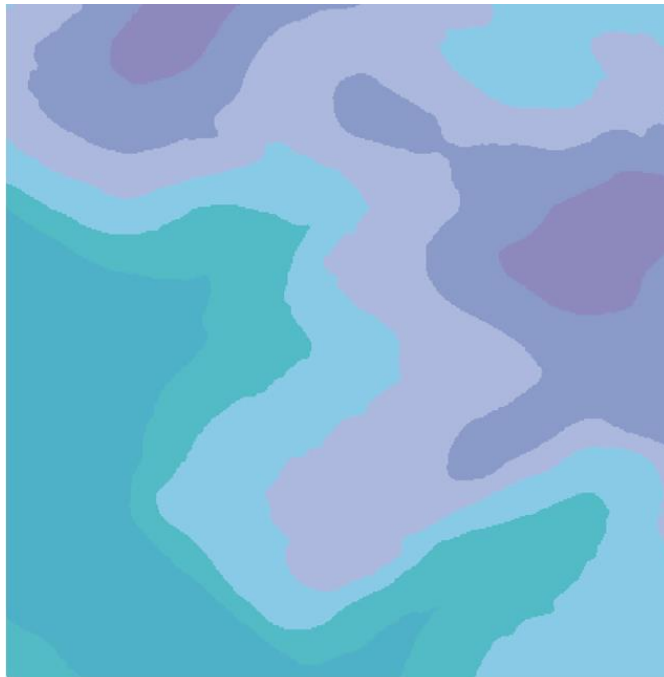
Variable 'neighborhoods'  
(donuts, wedges ...)



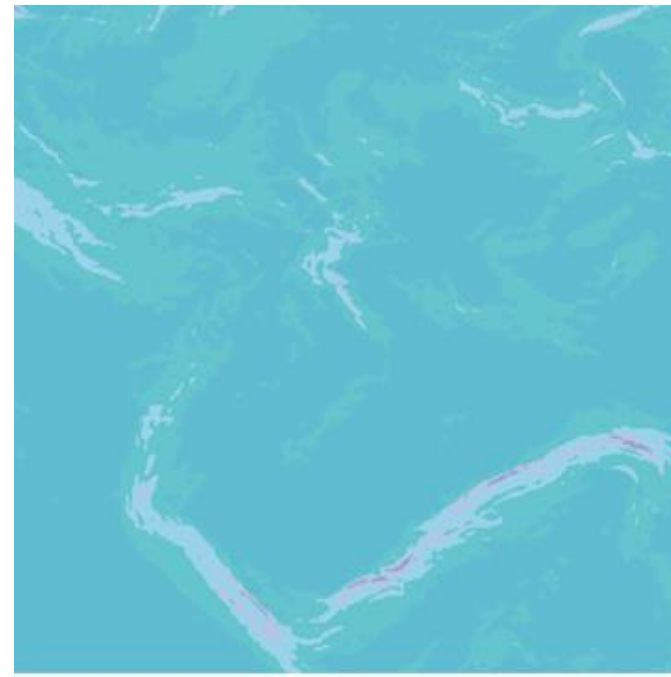


## Focal functions: Slope

Slope calculation, Vagar, The Faroe Islands (4x4 km)



Elevation, m asl.



Slopes in %



## Focal functions: Slope

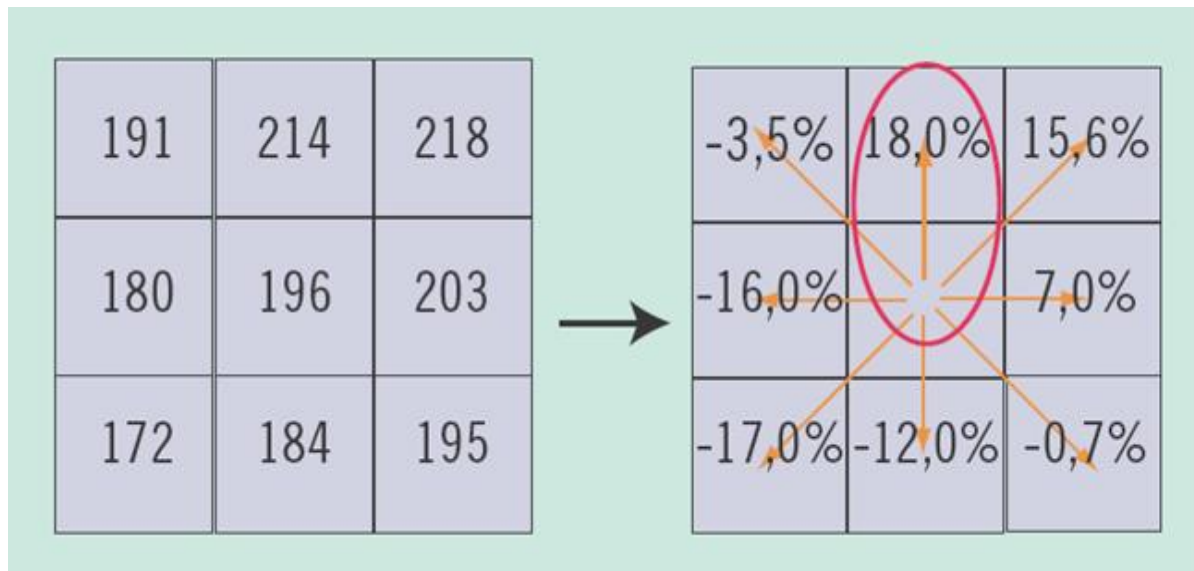
The maximum slope in percent may be determined from identifying the biggest difference in elevation values for a center cell and its 8 neighbours, and dividing this number by the horizontal distance.

191	214	218
180	196	203
172	184	195

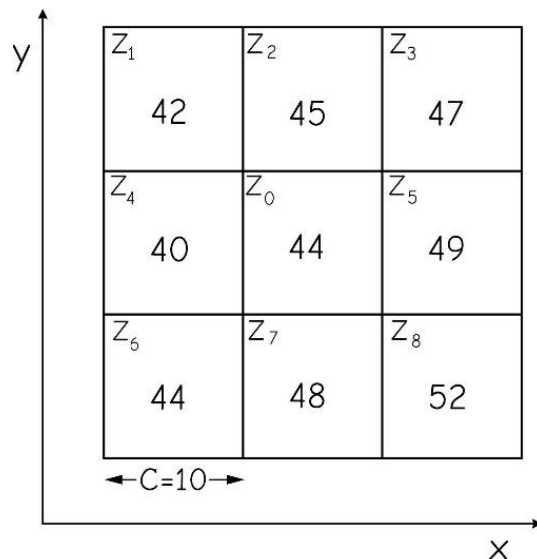
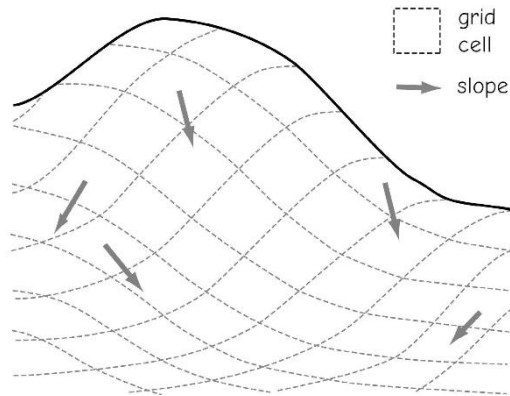
In which direction is the steepest slope (cell size is 100 meters)?

## Focal functions: Slope (former Esri method)

The maximum slope in percent may be determined from identifying the biggest difference in elevation values for a center cell and its 8 neighbours, and dividing this number by the horizontal distance.



## Focal function: Slope (alternative method, Bolstad)



for Z<sub>0</sub>:

$$dZ/dx = (49 - 40)/20 = 0.45$$

$$dZ/dy = (45 - 48)/20 = -0.15$$

$$\text{slope} = \text{atan} [(0.45)^2 + (-0.15)^2]^{0.5}$$

$$= 25.3^\circ$$

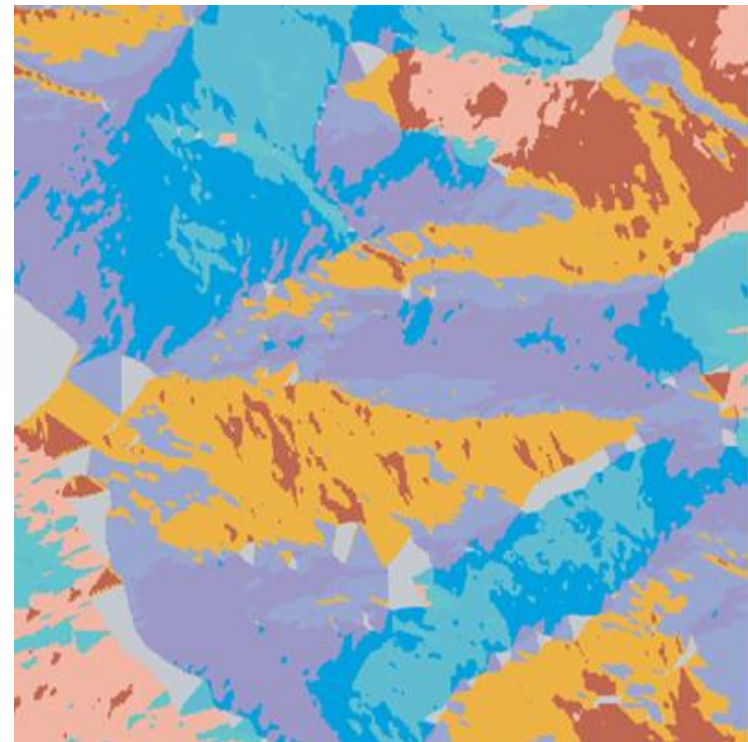
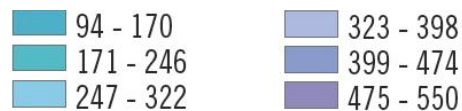
$$\text{Slope\%} = (0.45^2 + (-0.15)^2)^{0.5} * 100 = 47.3\%$$

## Focal functions: Aspect

Aspect calculation, Vagar, The Faroe Islands (4x4 km)



Elevation, m asl.



Aspects (exposures)

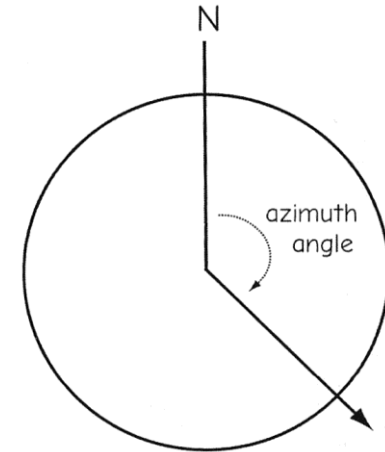




## Fokal function: Aspect

Aspect is defined as the direction of the steepest slope

$$\alpha = 180 - \operatorname{atan}\left(\frac{\left(\frac{dZ}{dy}\right)}{\left(\frac{dZ}{dx}\right)}\right) + 90\left(\frac{\left(\frac{dZ}{dx}\right)}{\left|\frac{dZ}{dx}\right|}\right)$$



When using values from Bolstad's calculation of slope:

$$a = 180 - \operatorname{atan}(-0.15/0.45) + 90(0.45/0.45)$$

$$a = 180 + 18 + 90 = 288^\circ$$

## Functions - overview

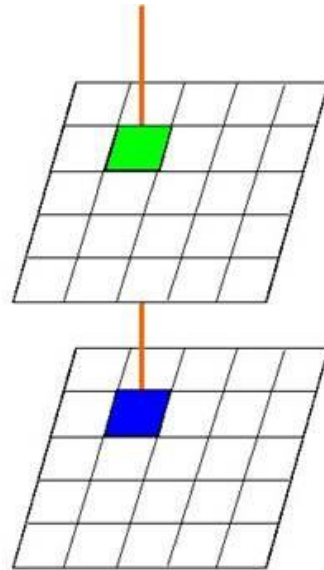
### Functions:

Local

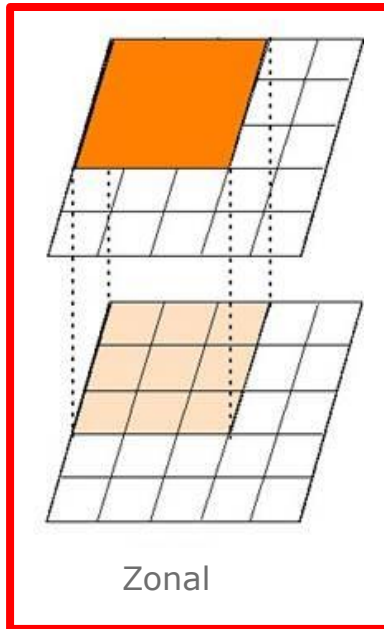
Focal

**Zonal**

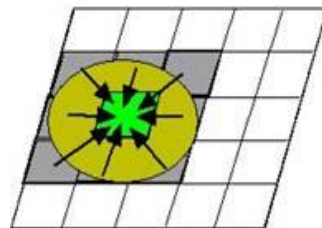
Global



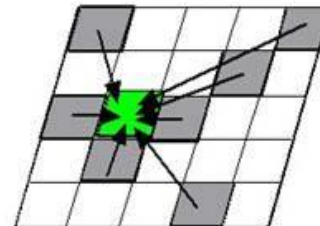
Local



Zonal



Focal



Global

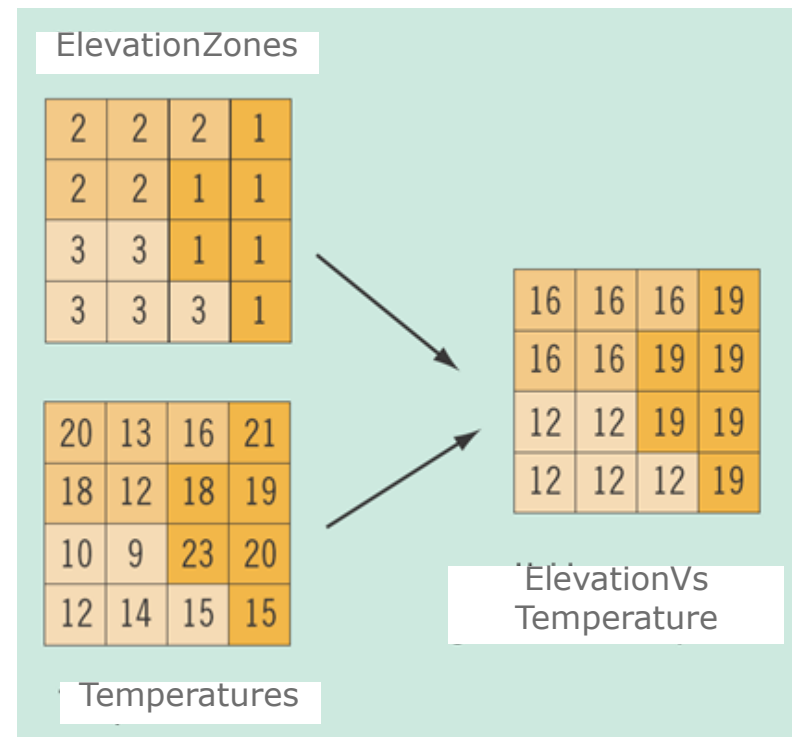
## Zonal functions

Calculates a value for each cell in one raster determined by zonal masks in a second raster

Example:

ElevationVsTemperature =  
**ZonalMean** of Temperatures in  
 ElevationZones

Other zonal functions:  
 Sum, minimum, maximum



## Functions - overview

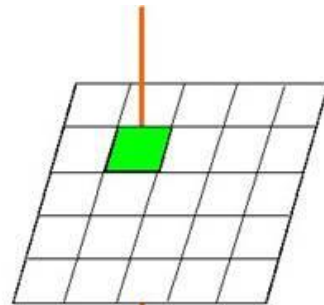
### Functions:

Local

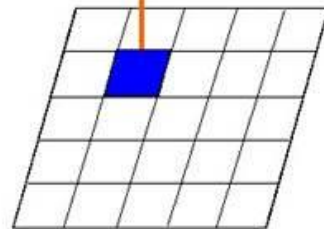
Focal

Zonal

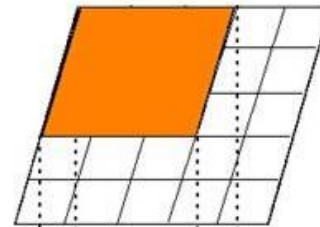
**Global**



Local



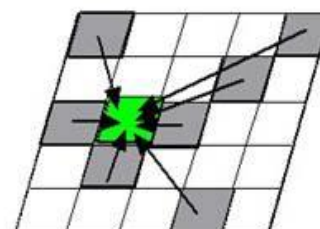
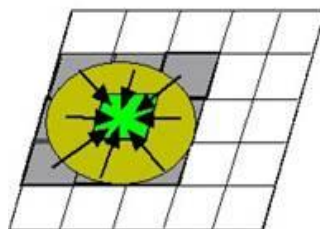
Focal



Zonal



Global

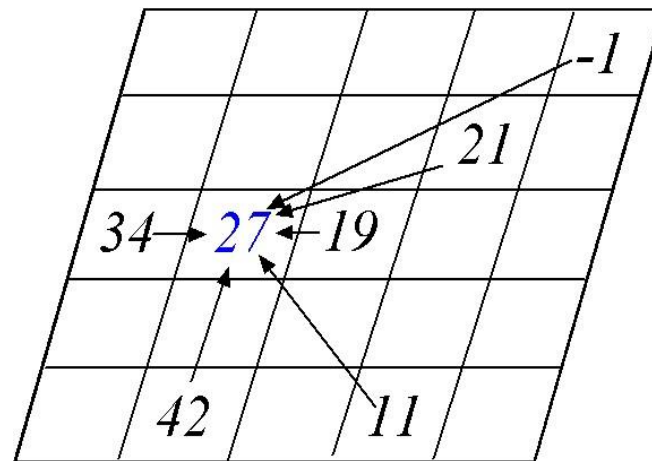


## Global functions: Interpolation

Calculate missing values based on existing ones.

Example:  
Inverse distance weighting  
interpolation.

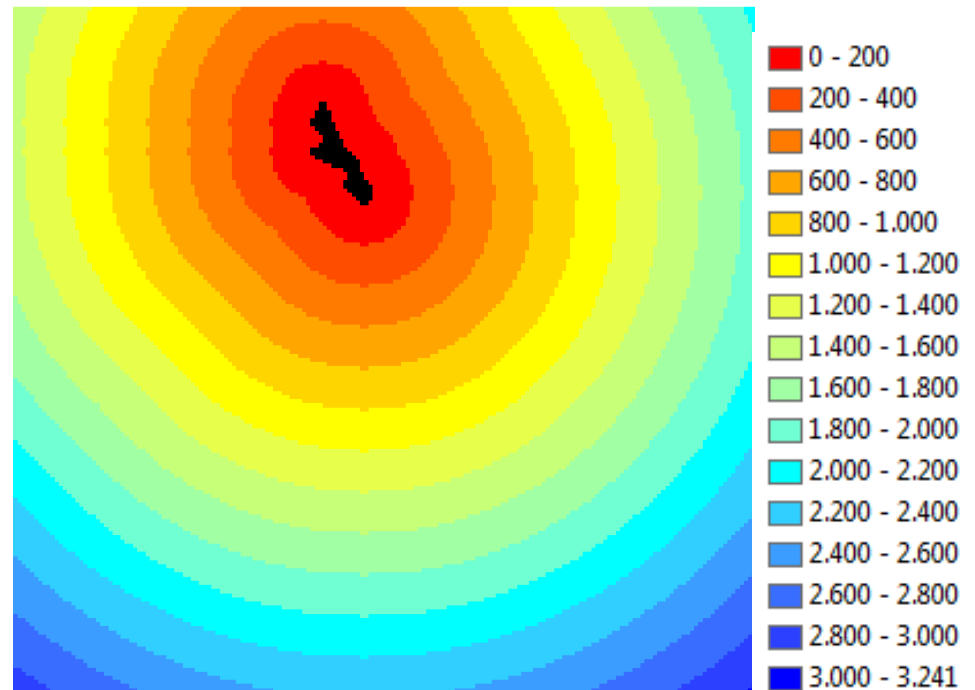
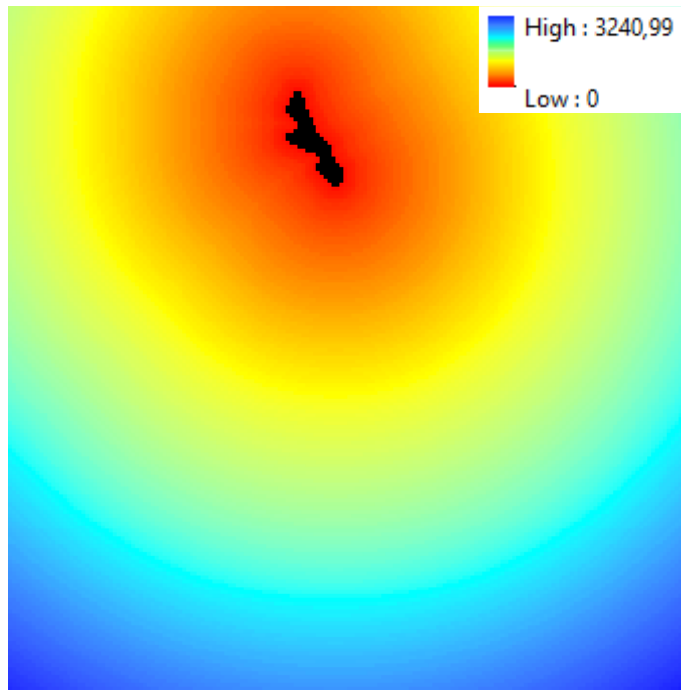
InterpolatedTemperature =  
**GlobalInterpolation** of  
Temperature



## Global functions: Euclidean distances / Distance Accumulation

Every cell gets a value telling the distance to the nearest source cell.

Next, the Reclassify tool may be used to slice the data into, say, 16 classes.





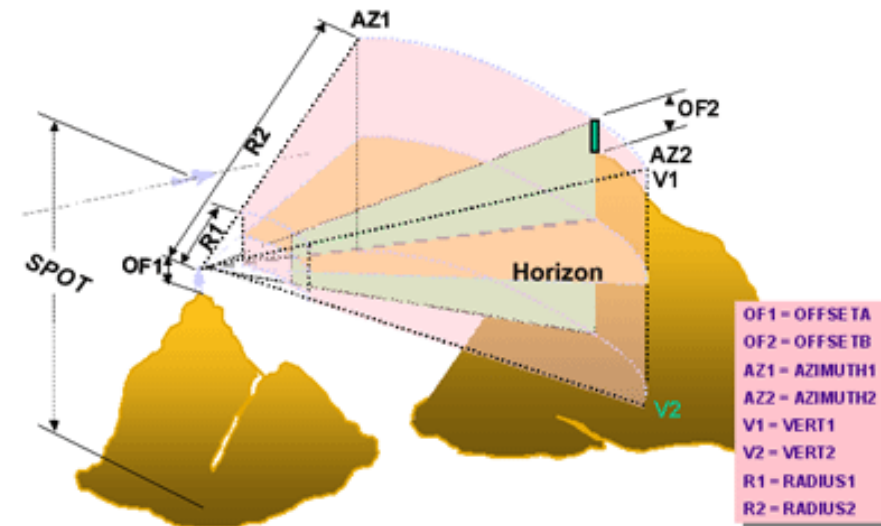
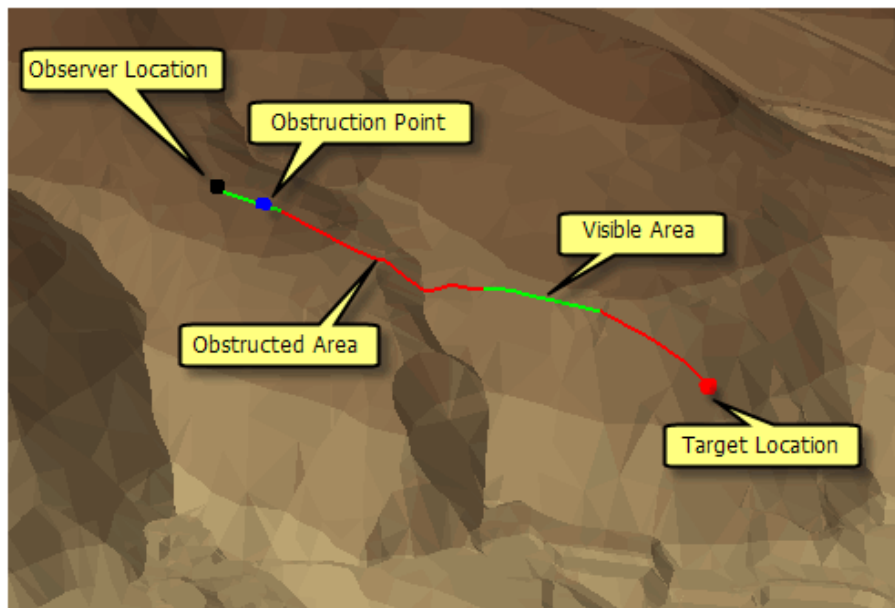
## Global functions: Nearest neighbour allocation

Every cell gets a value telling which source cell is nearest.



Method =  
Creation of Thiessen polygons

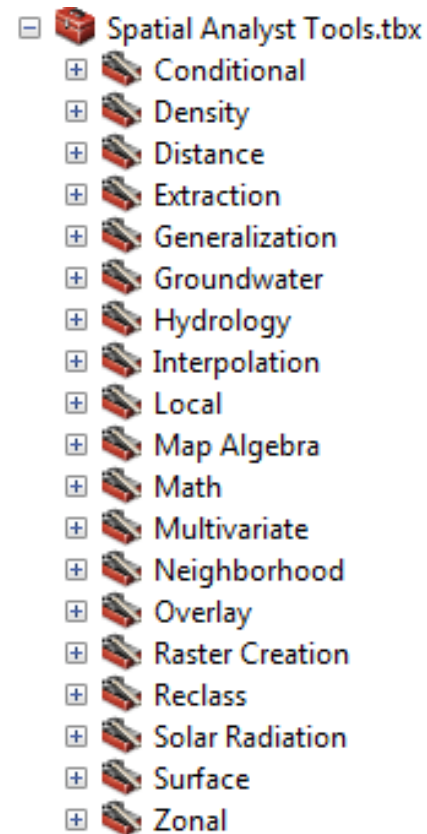
## Global functions: Visibility analysis



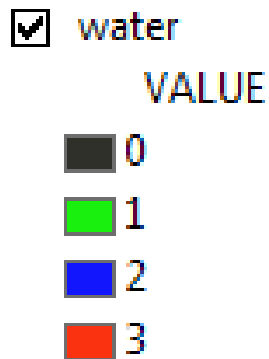
*Parameters for controlling the viewshed analysis*

## Working on rasters in ArcGIS

- Enable the Spatial Analyst extension → Locate the right tools



## Working on rasters in ArcGIS



Table

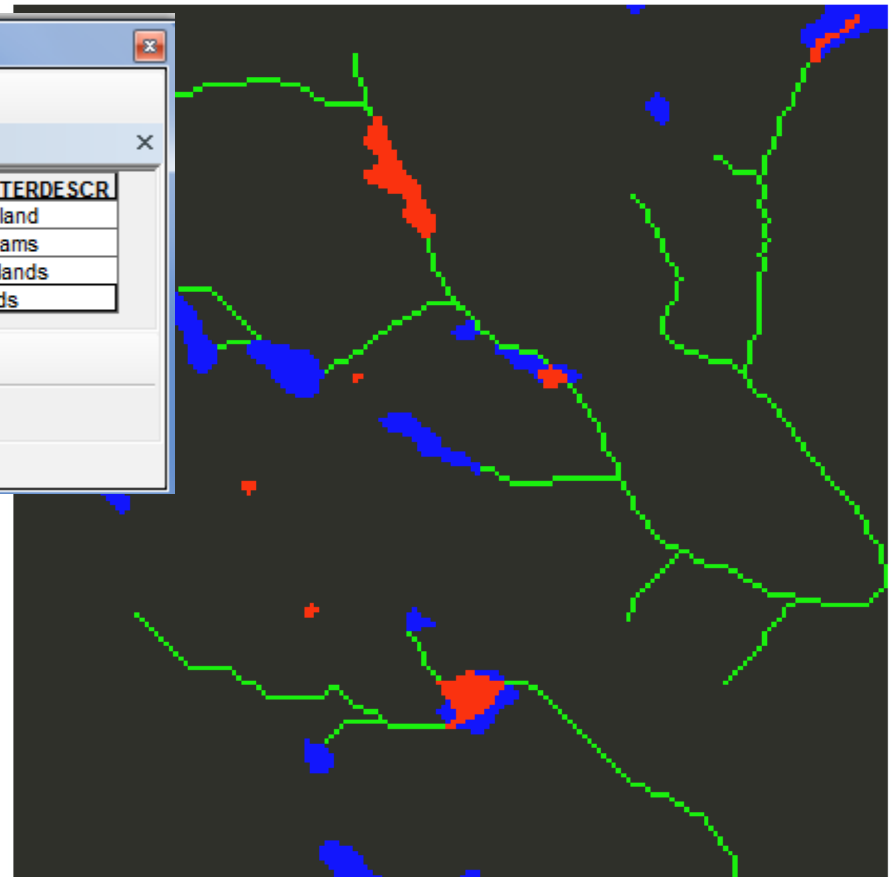
water

Rowid	VALUE	COUNT	WATERDESCR
0	0	30815	Dry land
1	1	595	Streams
2	2	707	Wetlands
3	3	283	Ponds

(0 out of 4 Selected)

water

Only integer rasters with  
< 65536 unique values  
have attribute tables.  
Use Build Raster attribute  
Table to build them



## Working on rasters in ArcGIS – layer files

