

GPU Computing

Homework 1: Matrix Transposition

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1 Problem Description

The goal of this homework is to implement a matrix transposition algorithm, where the transpose of a matrix is an operator which flips the matrix over its diagonal. That is, if A is a matrix of size $m \times n$, then the transpose of A is a matrix of size $n \times m$ where the element at row i and column j is the element, also denoted as A^T .

Additionally, we are asked to measure the effective bandwidth of our implementation, considering also the usage of different optimization flags such as: `-O0`, `-O1`, `-O2`, `-O3`.

Furthermore an analysis of the cache behavior of the algorithm is required, for this purpose we are going to use `valgrind`.

1.1 Algorithm

In order to dimostrare qualcosa, two algorithms have been implemented: the first one is a naïve approach, which consists in iterating over the matrix and swapping the elements, while the second one is a more optimized version which takes advantage of a block mechanism to reduce the number of cache misses.

Algorithm 1 Naïve Matrix Transposition

```
1:  $src \leftarrow create\_matrix(size)$ 
2: for  $i = 0$  to  $size$  do
3:   for  $j = 0$  to  $size$  do
4:      $dest[j * size + i] = src[i * size + j]$ 
5:   end for
6: end for
```

2 Bo da decidere

2.1 Hardware

1. Desktop PC

- **CPU:** AMD Ryzen 5 5600X
 - **Cores:** 6
 - **Threads:** 12
 - **Base Clock:** 3.7 GHz
 - **L1 Cache:** 64 KB (per core)
 - **L2 Cache:** 512 KB (per core)
 - **L3 Cache:** 32 MB
- **RAM:** 16 GB DDR4
- **OS:** Ubuntu 22.04 (on WSL2)

2. MacBook Air M1

- **CPU:** Apple M1
 - **Cores:** 8 (4 Firestorm + 4 Icestorm)
 - **Threads:** 8
 - **Base Clock:** 3.2 GHz
 - **L1 Cache Firestorm:** 192 + 128 KB (instructions + data, per core)
 - **L2 Cache Firestorm:** 12 MB (shared)
 - **L1 Cache Icestorm:** 128 + 64 KB (instructions + data, per core)
 - **L2 Cache Icestorm:** 4 MB (shared)
- **RAM:** 8 GB LPDDR4X
- **OS:** macOS Ventura 13.2.1

2.2 Results

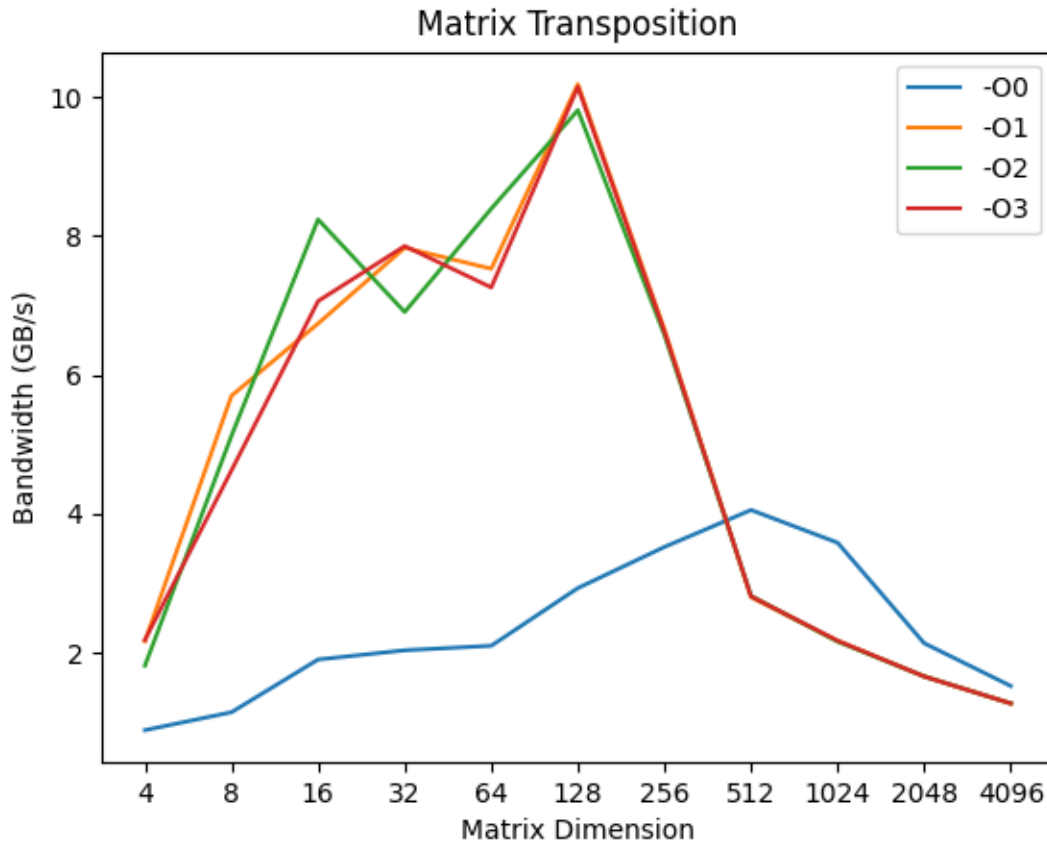


Figure 1: