

# Circuit Theory & Analysis

## Track: Comprehensive Program

### Goal

#### Enabling Mastery in Electrical Circuit Analysis & Simulation

This program is designed to provide a deep understanding of electrical circuits, ranging from fundamental concepts to advanced analysis techniques.

Key areas include the behavior of RLC circuits in both time and frequency domains, understanding transient and steady-state responses, and the practical application of circuit simulation tools for design and analysis.

Source: Simulating Circuits With SPICE

**Agnes**

# Program Structure & Core Pillars

## Phase 1: Foundational & Core Concepts

This initial phase establishes a robust theoretical base, focusing on fundamental principles. Learners engage with interactive online modules, gaining comprehensive knowledge of core circuit behaviors and analytical methods.

## Phase 2: Industry Immersion & Integrated Project

This immersive phase transitions to hands-on, practical application. Participants collaborate on a comprehensive project, applying learned concepts in a real-world, in-person setting.

Months 1 & 2

Online

Month 3

Offline

### Key Areas

**DC/AC Analysis:** Delve into principles of Direct and Alternating Current circuits.

**Network Theorems:** Master techniques like Thevenin's & Norton's for complex networks.

**Transient/Steady-State:** Explore dynamic and stable circuit responses over time.

**Frequency Response:** Investigate circuit behavior across different frequencies for filtering and resonance.



### Capstone Project

#### RLC Circuit Analysis & Simulation Mini Project

**In-depth Analysis:** Examine impedance, resonance, and phase in RLC circuits.

**Simulation Mastery:** Use industry software to simulate, validate, and predict circuit behavior.

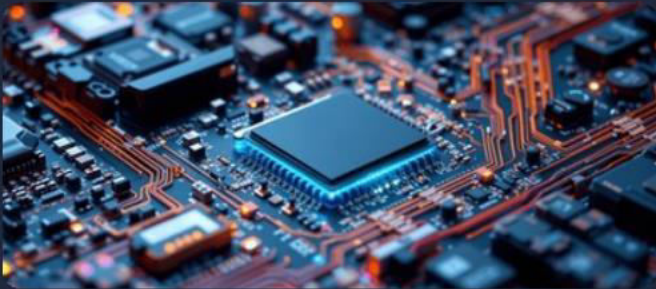
**Practical Application:** Design and troubleshoot an RLC circuit in a final, hands-on project.





# Month 1, Week 1: Basic DC Circuit Concepts & Laws

## ⚡ Circuit Elements

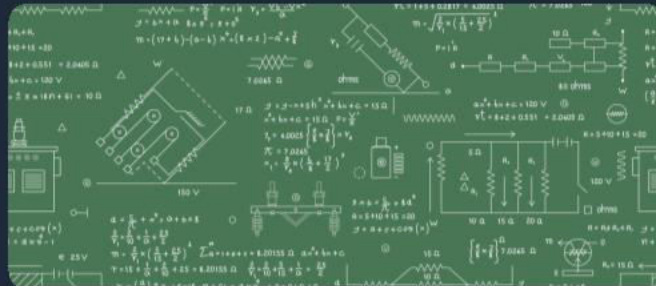


**Resistors:** Passive components opposing current flow, essential for controlling voltage and current.

**Independent Sources:** Provide constant voltage or current (e.g., batteries), their output unaffected by the circuit.

**Dependent Sources:** Output is controlled by another voltage or current in the circuit, key for modeling active devices.

## ⚡ Fundamental Laws



**Ohm's Law ( $V=IR$ ):** Defines the direct relationship between voltage, current, and resistance.

**Kirchhoff's Voltage Law (KVL):**  
The sum of voltages in any closed loop is zero, based on energy conservation.

**Kirchhoff's Current Law (KCL):**  
The sum of currents entering a node is zero, based on charge

## 🔗 Combinations & Rules

Series Resistors

Parallel Resistors

Voltage Divider

Current Divider

**Series:** Resistors connected end-to-end, creating a single current path.  
Total  $R = R_1 + R_2 + \dots$

**Parallel:** Resistors connected across the same two points, offering multiple current paths.

**Voltage Divider:** A rule to find the voltage across a specific resistor in a series circuit.

**Current Divider:** A rule to find the current through a specific resistor in a parallel setup.

# Month 1, Weeks 2-3: DC Analysis Techniques & Network Theorems

## Nodal & Mesh Analysis

### Nodal Analysis: Setting Up & Solving Equations

A powerful method applying Kirchhoff's Current Law (KCL) at each non-reference node to determine node voltages. This creates a system of linear equations to solve the entire circuit.

- Key steps: identify nodes, choose a reference, assign unknown voltages, and write KCL equations.

### Mesh Analysis: Setting Up & Solving Equations

An alternative that uses Kirchhoff's Voltage Law (KVL) around each mesh (loop) to find mesh currents. It is particularly effective for planar circuits.

- Key steps: identify meshes, assign mesh currents, and write KVL equations for each mesh.

### Handling Supernodes & Supermeshes

Advanced techniques to simplify analysis when ideal sources are

## Network Theorems

### Superposition Theorem

In a linear circuit with multiple sources, the response in any element is the sum of responses caused by each source acting alone. This simplifies complex problems into smaller parts.

### Thevenin, Norton, & Maximum Power Transfer

Powerful equivalence theorems used to simplify complex linear circuits into simpler forms for load analysis.

- ∞ **Thevenin's Theorem:** Reduces a circuit to a voltage source ( $V_{th}$ ) in series with a resistor ( $R_{th}$ ).
- ∞ **Norton's Theorem:** Reduces a circuit to a current source ( $I_n$ ) in parallel with a resistor ( $R_n$ ).
- ∞ **Max Power Transfer:** Occurs when load resistance equals the Thevenin resistance of the source.

# Month 1, Week 4: Introduction to AC Fundamentals & Phasors

## Sinusoidal Signals

AC circuits are driven by sinusoidal sources. Understanding their properties—Amplitude, Frequency, Phase, and RMS Value—is crucial for analysis.

- **Amplitude ( $V_p$ ):** Maximum instantaneous value of the waveform.
- **Frequency ( $f$ ):** Cycles per second (Hz). Angular frequency  $\omega = 2\pi f$ .
- **Phase ( $\phi$ ):** Waveform's position relative to a reference.
- **RMS Value:** Effective AC value, equivalent to the DC value that produces the same power.  $V_{rms} = V_p / \sqrt{2}$ .

Amplitude

Frequency

Phase

RMS Value

## Phasors

Phasors are rotating vectors representing sinusoidal quantities in the frequency domain. They transform complex differential equations into simple algebraic ones.

- **Representation:** Vector length is amplitude, angle is phase.
- **Simplification:** Converts time-domain  $v(t)$  to phasor  $V$ .

## Complex Numbers Review

A key mathematical tool to simplify AC circuit analysis from differential equations to algebra.

- **Rectangular Form:**  $a + jb$  (for addition/subtraction).
- **Polar Form:**  $M\angle\theta$  (for multiplication/division).
- **Conversion:** Convert between forms for efficient calculation.

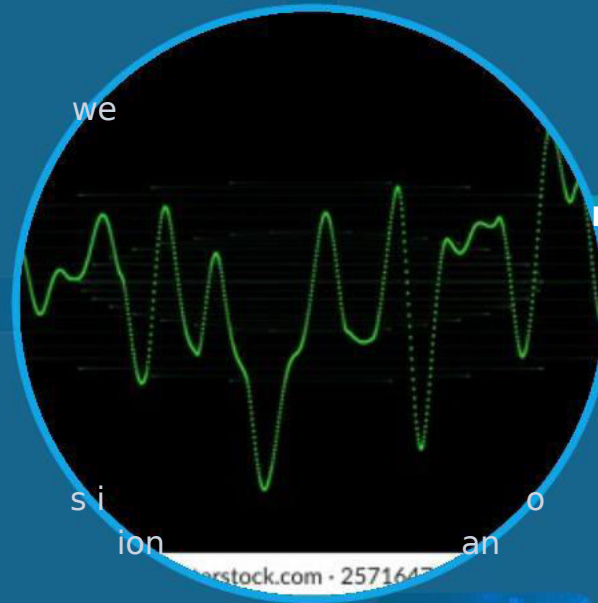
Polar Form

Mathematical Tool

## Impedance ( $Z$ )

AC current ( $Z = R + jX$ ), analogous to resistance in DC.

- **Resistor ( $R$ ):**  $Z_R = R\angle 0^\circ$
- **Inductor ( $L$ ):**  $Z_L = j\omega L = \omega L\angle 90^\circ$
- **Capacitor ( $C$ ):**  $Z_C = 1/j\omega C = (1/\omega C)\angle -90^\circ$



# Month 2, Week 5: Advanced AC Circuit Analysis

## Σ Phasor Domain Laws

### Extending Fundamental Laws to AC:

Fundamental laws like Ohm's Law, KVL, and KCL are applied using phasors, transforming time-domain differential equations into simpler algebraic equations with complex numbers.

### Key Principles:

- **Ohm's Law:**  $V = I * Z$  (Phasor Voltage = Phasor Current  $\times$  Complex Impedance).
- **KVL:** The algebraic sum of phasor voltages around any closed loop is zero.
- **KCL:** The algebraic sum of phasor currents entering any node is zero.

Phasor Domain

KVL (AC)

KCL (AC)

Ohm's Law (AC)

## Series & Parallel Impedance

**Simplifying Complex Circuits:** Complex impedances ( $Z$ ) are combined to find an equivalent impedance, simplifying network analysis.



Source: Rlc Circuit Images - Freepik

### Combination Rules:

- **Series:**  $Z_{eq} = Z_1 + Z_2 + \dots$
- **Parallel:**  $1/Z_{eq} = 1/Z_1 + 1/Z_2 + \dots$

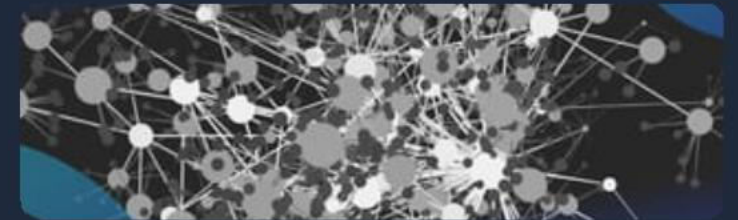
Series Impedance

Parallel Impedance

RLC Combinations

## AC Nodal & Mesh Analysis

**Systematic Problem Solving:** Nodal and Mesh analysis are extended to AC circuits, using complex algebra to solve systems of equations with phasor voltages and currents.



Source: Graph Theory Defined and Applications

- **AC Nodal Analysis:** Applies KCL to find unknown nodal phasor voltages.
- **AC Mesh Analysis:** Applies KVL to find unknown mesh phasor currents.

AC Nodal Analysis

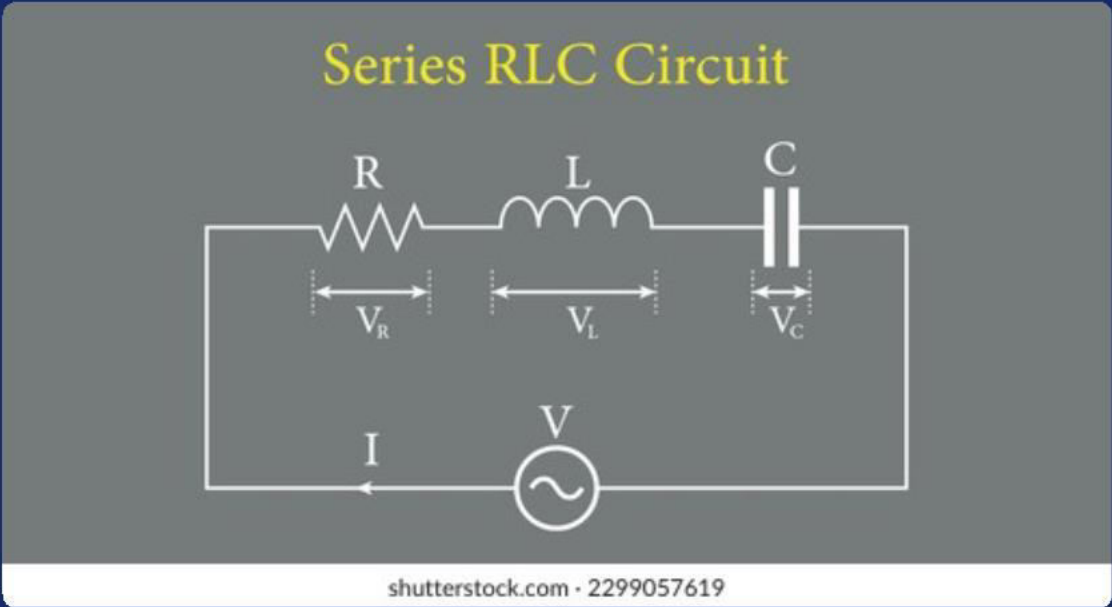
AC Mesh Analysis

Systematic Approach

## 🔌 Power in AC Circuits: A Comprehensive Overview

# Month 2, Week 6: Resonance & Filters in AC Circuits

## Series Resonance



Resonance occurs when inductive reactance ( $X_L$ ) equals capacitive reactance ( $X_C$ ), leading to unique circuit behavior.

**Resonant Frequency ( $f_0$ ):** The frequency where reactances cancel.  
 $f_0 = 1 / (2\pi\sqrt{LC})$

**Impedance (Z):** At resonance, impedance is at its **MINIMUM** ( $Z = R$ ), allowing **MAXIMUM** current flow.

**Q-Factor & Bandwidth (BW):** Q-Factor measures selectivity. A higher Q means a sharper resonance peak and narrower bandwidth ( $BW = f_0 / Q$ ).

## Parallel Resonance (Anti-Resonance)

In parallel RLC circuits, resonance results in maximum impedance, also known as anti-resonance.

**Impedance (Z):** At resonance, impedance is at its **MAXIMUM**, acting like an open circuit.

**Current:** The total current from the source is at its **MINIMUM**, making it a "tank circuit".

### Series vs. Parallel Comparison

Characteristic	Series Resonance	Parallel Resonance
Impedance at $f_0$	Minimum ( $Z=R$ )	Maximum ( $Z_{max}$ )
Current at $f_0$	Maximum	Minimum
Application	Current Amplification	Voltage Amplification



# Month 2, Week 7: Transient Analysis of First-Order Circuits

## 💡 Unveiling Dynamic Circuit Behavior

**Understanding Transient Response:** Transient analysis examines the dynamic behavior of circuits immediately after a sudden change in input. Unlike steady-state analysis, it focuses on the temporary period where voltages and currents transition from one state to another.

**Focus on First-Order Circuits:** These circuits contain one energy storage element (inductor or capacitor). Their behavior is described by a first-order differential equation, making them fundamental for understanding transient phenomena in RL (Resistor-Inductor) and RC (Resistor-Capacitor) circuits.

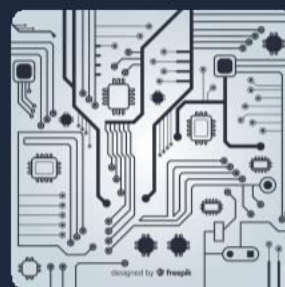


## ⇄ Dissecting Circuit Responses

**Natural Response:** Behavior from stored energy with no external sources active. It's the circuit's inherent, decaying response.

**Forced Response:** Long-term behavior dictated by external sources, representing the steady-state.

**Complete Response:** The total observed response, calculated as: Complete = Natural + Forced.



Natural Response

Forced Response

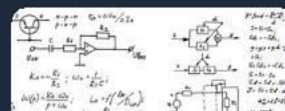
Complete Response

Transient

## ↗ Analyzing Sudden Changes

**Step Input:** An abrupt change in voltage or current, used to analyze how a circuit behaves when suddenly energized.

**General Form:** The response  $v(t)$  follows the form:  $v(t) = v_{ss} + (v(0) - v_{ss})e^{-t/\tau}$



## 🕒 The Heartbeat of Transients

**Definition:** The time constant ( $\tau$ ) quantifies the speed of the circuit's response to change. A larger  $\tau$  means a slower response.

**Calculation:** For RL circuits,  $\tau = L/R$ . For RC circuits,  $\tau = RC$ .

**Interpretation:** After  $5\tau$ , a circuit is considered to have reached its steady-state, with the transient decayed by over 99%.



Time Constant ( $\tau$ )

RL Circuits

RC Circuits

Exponential Decay

## 🕒 The Circuit's "Memory"

**Energy Storage:** Inductors and capacitors "remember" their state by storing energy. This stored energy defines the initial conditions.

**Continuity Principles:** Capacitor voltage  $v_C(0^-) = v_C(0^+)$  and inductor current  $i_L(0^-) = i_L(0^+)$



# Month 2, Week 8: Second-Order Circuits & Two-Port Networks

## 🔗 Second-Order RLC Circuits

Second-order RLC circuits contain two energy storage elements, leading to characteristic responses described by second-order differential equations. Their natural response is crucial for designing stable and predictable systems.

### Natural Response Forms:

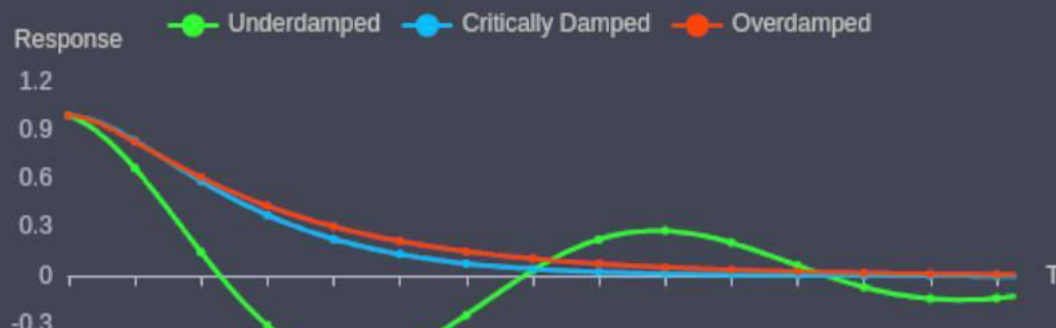
**Underdamped ( $\zeta < 1$ )** An oscillatory decay.

**Critically Damped ( $\zeta = 1$ )** Fastest decay, no oscillation.

**Overdamped ( $\zeta > 1$ )** Slow, non-oscillatory decay.



Second-Order RLC Natural Responses



## 🔗 Two-Port Networks

A "black box" model that simplifies the analysis of complex systems like amplifiers by focusing on input/output port relationships.

### Key Parameter Sets:

Z-Parameters

Y-Parameters

H-Parameters

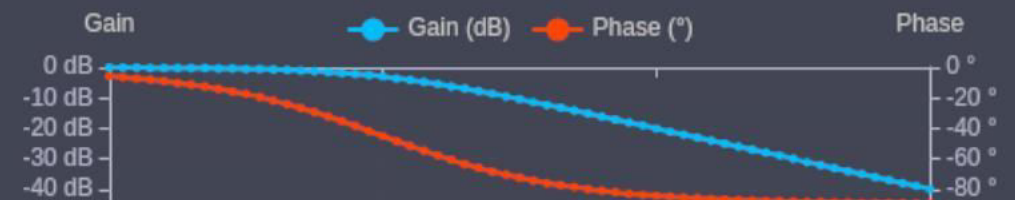
G-Parameters



## 📈 Frequency Response

Describes output behavior as input frequency changes, visualized with **Gain** & **Phase** plots (Bode Plots).

### Conceptual Frequency Response



# Month 3, Week 9: Capstone Project Kick-off: RLC Analysis

## Your Capstone Journey Begins!

Welcome to the culmination of your circuit analysis training! This Capstone Project provides a hands-on, immersive experience where you will apply all learned principles to conduct an in-depth RLC circuit analysis. This week marks the official kick-off, focusing on foundational setup and defining your project scope.



## Phase 1: Onboarding & Team Synergy

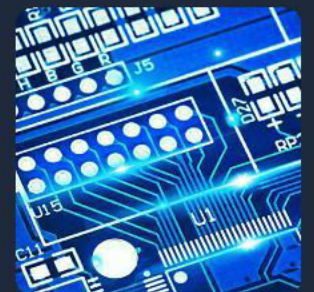
**Arrival & Orientation:** Begin with a comprehensive orientation to familiarize yourselves with project guidelines, resources, and safety protocols for a smooth transition.

**Team Formation & Mentor Allocation:** Form collaborative teams and get paired with an expert mentor for guidance and technical support throughout the project.

## Phase 2: Defining Your RLC Challenge

**Selecting Configurations:** Choose specific series, parallel, or mixed RLC circuits for analysis, defining component values and input sources.

**Focus Areas:** Decide whether to analyze behavior in the **time domain** (transient) or **frequency domain** (AC steady-state).



# Month 3, Week 10: RLC Circuit Simulation & Validation

## Advanced Simulation Environment Setup

This week focuses on proficiency with industry-standard software for complex circuit design, detailed analysis, and predictive modeling, accelerating the design cycle.

**LTSpice:** A high-performance SPICE simulator known for its speed and accuracy in analog circuit design.

**NI Multisim:** An intuitive environment with an integrated approach to circuit design, simulation, and PCB layout.

**OrCAD PSpice:** A leading simulator for mixed-signal simulation, behavior modeling, and robust design analysis.

LTSpice

Multisim

OrCAD PSpice

SPICE

Schematic Capture

Waveform Viewer

Mixed-Mode

## Transient Simulation: Dynamic Behavior

Observe how RLC circuits react to sudden changes and settle to a new steady state, revealing intrinsic damping characteristics.



## Validation: Theory Meets Simulation

Validation is the cornerstone of design, involving rigorous comparison of simulated output against theoretical predictions to confirm accuracy and understanding.

### Methodology:

- Extract data (waveforms, frequencies) from the simulation.
- Perform theoretical calculations (e.g.,  $f_0 = 1 / (2\pi\sqrt{LC})$ ).
- Compare results to identify and analyze discrepancies.

### Benefits of Validation:

- Verifies theoretical knowledge and analytical methods.
- Helps troubleshoot errors in design or simulation setup.



# Month 3, Week 11: Advanced RLC Applications & Practicalities

## RLC Filters: Design

### Purpose & Types

RLC circuits form the basis of passive filters to pass or attenuate specific frequency ranges. Common types include Low-Pass (LPF), High-Pass (HPF), Band-Pass (BPF), and Band-Stop (BSF) filters.

### Design Considerations

- › **Cutoff Frequency:** Dictates the boundary where signals are attenuated.
- › **Bandwidth:** The range of frequencies passed/stopped, related to the Q-factor.
- › **Roll-off Rate:** How sharply the filter attenuates frequencies (dB/decade).

### Application

Crucial for audio processing, communication systems, and noise reduction.

Low-Pass

High-Pass

Band-Pass

Band-Stop

Resonance

## RLC in Real-World Applications

### Signal Integrity

RLC elements impact transmission lines, reflections, and ringing. Proper RLC networks are critical to maintain signal quality in high-speed circuits.

### EMI/EMC Basics

RLC circuits are fundamental in Electromagnetic Interference/Compatibility design, used in filters to suppress unwanted noise and block interference.

### Oscillators & Tuners

Resonant RLC circuits are the heart of oscillators (signal generation) and tuners (frequency selection in radios), where  $f_0 = 1 / (2\pi\sqrt{LC})$  is key.

Signal Integrity

EMI/EMC

Oscillators

Tuners

## Practical Component Effects

### Beyond Ideal Models

Real-world components exhibit non-ideal behaviors that impact performance, especially at high frequencies.

### Equivalent Series Resistance (ESR)

Intrinsic resistance in capacitors and inductors. Causes power loss (heating), reduces Q-factor, and broadens filter responses.

### Parasitics (ESL & Capacitance)

- › **ESL:** Series inductance in capacitors limits high-frequency use.
- › **Parasitic C:** Unintended capacitance creates unwanted resonances.

Non-Ideal

ESR

Parasitics

Q-Factor

# Project Showcase & Career Launchpad



## Final Project Showcase: Mastery & Innovation

### Culmination of Technical Expertise

This capstone represents the pinnacle of your learning, showcasing your ability to conduct comprehensive RLC circuit analysis and simulation. You will present your chosen circuit's design, theoretical derivations, and detailed simulation results.

### Validation and Insights

Emphasize the validation process, comparing simulated data against theoretical predictions, and discuss practical insights gained from troubleshooting and optimization. This demonstrates a robust understanding of both ideal and real-world circuit behaviors.

### Comprehensive Documentation

Your project culminates in meticulous documentation, including schematic diagrams, analytical reports, and performance graphs. This artifact serves as a tangible demonstration of your technical capabilities for your professional portfolio.

Capstone Project

RLC Analysis

Circuit Simulation

Documentation

Portfolio

Technical Mastery

Validation



### Career Workshops

- **Resume Enhancement:** Craft a



### Mock Interviews

- **Technical Drills:** Rigorous interviews



### Graduation & Certification