

1.

A - Recurrence Formula:

$$t(n) = \begin{cases} c & \text{for } 0 \leq n \leq 2 \\ n + \max(t(n-2), t(n-3)) & \text{for value } n < 3 \\ \max(t(n-2), t(n-3)) & \text{for value } n < 0 \end{cases}$$

B - Pseudocode:

```
def max_independent_set(array):
    memo = []
    three_back = []
    two_back = []
    one_back = []          #set variables to hold returns and tracking
    if len(array) < 3
        if length = 0
            return empty memo
        if length = 1
            append array[0] to memo and return memo
            or if array[0] < 0 just return empty memo
        if length = 2
            append max (array[0],array[1]) to memo
            or if both negative, return empty memo
    else:                  # all arrays length 3+
        if array[2] is negative
            append three_back to array[0]
            append two back to array[1]
            append one back to array[0]      #since 2 is negative and skipped
            add correct current sums to memo
        if array[0] is negative
            append three_back to array[0]
            append two back to array[1]
            append one back to array[2]
            add correct current sums to memo
        if array[1] is negative, and array[0] and array[2] are not:
            append three_back to array[0]
            append two back to array[1]
            append one back to array[2]
            add correct current sums to memo

    for i in range 3-array length
        if array[i] is not negative
            append memo with max(memo[i-3],memo[i-2])
            if memo[i-3] greater
                store three_back in array temp
                move all back variables one step back
                one_back becomes temp
            else memo[i-2] greater
                store two_back in array temp
                move all back variables one step back
                one_back becomes temp
```

```

else if array[i] is positive
    append memo with (array[i] + max(memo[i-3],memo[i-2]))
    if memo[i-3] greater
        store three_back in array temp
        move all back variables one step back
        one_back becomes temp
    else memo[i-2] greater
        store two_back in array temp
        move all back variables one step back
        one_back becomes temp

#memo stores the max sum at each location in the array
#we only need to check the last 2 for what is max, and then return
#one_back or two_back

if memo[len(memo)-1] > memo[len(memo)-2]
    return one_back
else:
    return two_back

```

C - Time Complexity:  $O(n)$

The code uses one for loop that goes the length of the array passed to it. everything else is if statements running in constant time.

2.

B - Time Complexity  $O(2^n)$

Every additional element of the set makes it run exponentially longer.

Debrief:

1. About 15 hours this week on the course. The assignment was 8 hours and about 7 on the explorations and third party resources to try and understand the material. I ended up not using the knapsack technique for the first problem because I was not very comfortable with the way it was explained.

2. Moderate+

3. 50% maybe. I understand this specific instance of it, but I don't feel confident in the subject overall.

4. I really wish there was some more examples for the problems we cover in the explorations. I feel that one simple look at the problem from a theoretical approach and then one specific example that's more in depth would be helpful.