

# Query Processing and Optimization Quiz Solution

Prof. Dr. Volker Markl

Alexander Alexandrov, Stephan Ewen,  
Kostas Tzoumas, Fabian Hueske, Max Heimel



Fachgebiet Datenbanksysteme und Informationsmanagement  
Technische Universität Berlin

<http://www.dima.tu-berlin.de/>

- Given are three relations  $R(\underline{r1}, r2, r3)$ ,  $S(\underline{r1}, \underline{t1})$ ,  $T(\underline{t1}, t2, t3)$ , where  $S.r1$  is a foreign key on  $R.r1$  and  $S.t1$  a FK on  $T.t1$ .
- Following statistics are available:
  - $|R| = 1000$
  - $|R.r2| = 50$ ,  $\min(R.r2) = 0$ ,  $\max(R.r2) = 50000$
  - $|R.r3| = 500$ ,  $\min(R.r3) = 101$ ,  $\max(R.r3) = 600$
  - $|S| = 20000$
  - $|S.r1| = 1000$
  - $|S.t1| = 200$
  - $|T| = 200$
  - $|T.t2| = 20$ ,  $\min(T.t2) = 0$ ,  $\max(T.t2) = 42$
  - $|T.t3| = 8$ ,  $\min(T.t3) = 1$ ,  $\max(T.t3) = 256$

- Given the RA expression E:

$$\pi_{r2,r3,t2}(((\sigma_{(r2=75) \vee (r3>300 \wedge r3 \leq 400)} R) \bowtie_{r1} S) \bowtie_{t1} (\sigma_{t3=0} T))$$

compute the cardinality estimates of the intermediate results for the following execution tree of E, as described in the lecture.

Assume independence and uniform distribution.

**|IR1| = 216:**

Selectivity ( $r2 = 75$ ):  $S_1 = (|R|/|R.r2|)/|R| = (1 / 50) = 0.02$

Selectivity ( $r3 > 300$  AND  $r3 \leq 400$ ):  $S_2 = (400-300)/(\max(R.r3)-\min(R.r3)+1) = 100/500 = 0.2$

Disjunctive predicate's selectivity  $S_3 = 1 - (1 - S_1)*(1 - S_2) = 1 - (1 - 0.02)*(1 - 0.2) = 0.216$

Cardinality:  $(|R| * S_3) = 1000 * 0.216 = 216$

**|IR2| = 4320:**

S.r1 is FK of R.r1

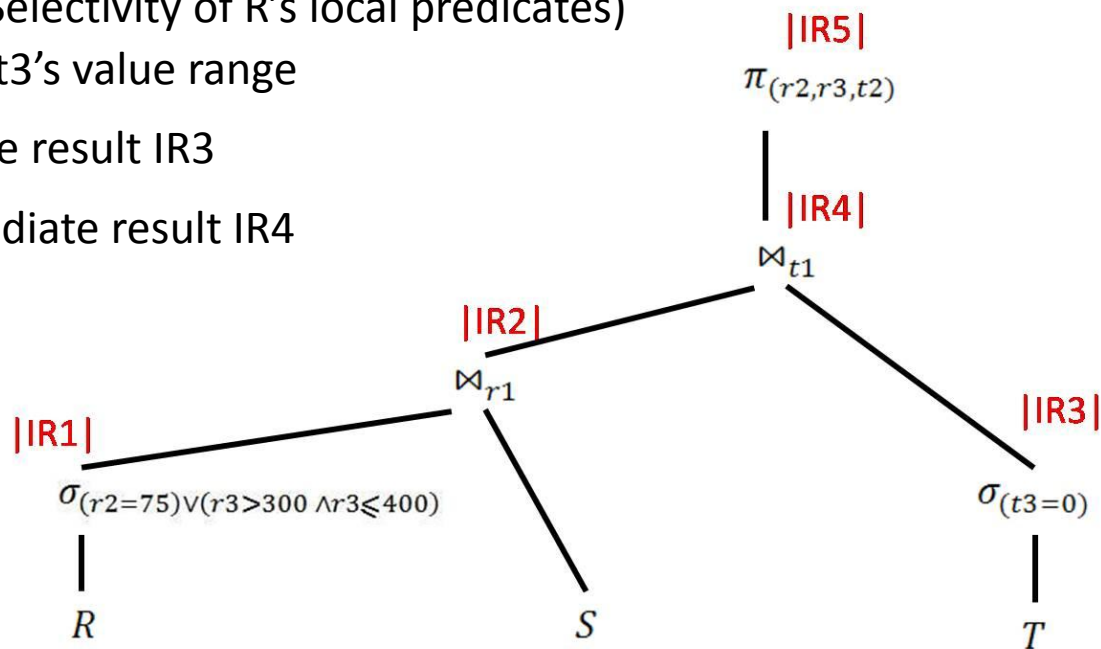
Assume uniform distribution of S.r1 and independence of R's attributes.

$4320 = 20000 * 0.216$  (Cardinality S \* Selectivity of R's local predicates)

**|IR3| = 0**, predicate value (0) is out of t3's value range

**|IR4| = 0**, join with empty intermediate result IR3

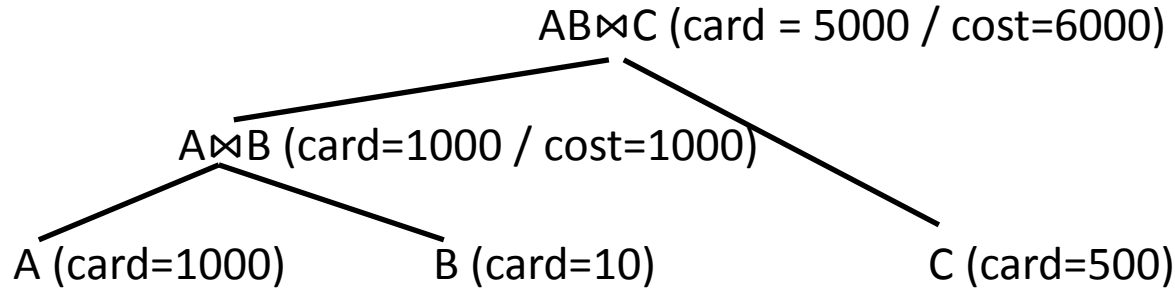
**|IR5| = 0**, projection of empty intermediate result IR4



- Given are:
  - four relations R, S, T, U  
with cardinalities  $|R| = 20$ ,  $|S| = 100000$ ,  $|T| = 1000$ ,  $|U| = 500$
  - Local predicates on R (selectivity = 0.5) and U (selectivity = 0.2)
  - The following join-selectivities (based on size of the cross product of the inputs)

2-Table Joins	Selectivity	3-Table Joins	Selectivity	4-Table Joins	Selectivity
$R \bowtie S$	0,05	$RS \bowtie T$	0,001	$RST \bowtie U$	0,002
$R \bowtie T$	1,0	$RS \bowtie U$	1,0	$RSU \bowtie T$	0,000002
$R \bowtie U$	1,0	$RT \bowtie S$	0,00005	$RTU \bowtie S$	0,00005
$S \bowtie T$	0,001	$RT \bowtie U$	0,002	$STU \bowtie R$	0,05
$S \bowtie U$	1,0	$RU \bowtie S$	0,05	$RS \bowtie TU$	0,001
$T \bowtie U$	0,002	$RU \bowtie T$	0,002	$RT \bowtie SU$	0,0000001
		$ST \bowtie R$	0,05	$RU \bowtie ST$	0,0001
		$ST \bowtie U$	0,002		
		$SU \bowtie R$	0,05		
		$SU \bowtie T$	0,000002		
		$TU \bowtie R$	1,0		
		$TU \bowtie S$	0,001		

- Compute the costs for join order using a Dynamic Programming approach
- Costs are modeled as follows:
  - Table access is free (cost = 0)
  - The cost of a join is the sum of the resulting cardinalities of all previous joins (including the cardinality of the own result)
  - Example:



- Sheet and paper solution in two steps
  - Step 1 (Preprocessing): Compute IR cardinalities
    - Removes duplicate computations in the next step
    - Independent on the join order, e.g.  
$$|(R \bowtie S) \bowtie T| = |R \bowtie (S \bowtie T)| = |(R \bowtie T) \bowtie S|$$
    - IR cardinality decomposes into base relation cardinality and local and join predicate selectivity factors
  - Step 2 (Optimization): Salinger style enumeration of plans
    - Bottom-up enumeration
      - for  $k$  in  $[1 \text{ to } N]$  tables:
        - generate all plans of  $k$  tables
    - Dynamic Programming: save and reuse results up to  $k$  for  $k+1$  tables
    - Pruning: keep only the best plan joining the same subset of  $k$  tables

2-Table Joins	Cardinality	3-Table Joins	Cardinality	4-Table Joins	Cardinality
$R \bowtie S$	50000	$R \bowtie S \bowtie T$	50000	$R \bowtie S \bowtie T \bowtie U$	10000
$R \bowtie T$	10000	$R \bowtie S \bowtie U$	5000000		
$R \bowtie U$	1000	$R \bowtie T \bowtie U$	2000		
$S \bowtie T$	100000	$S \bowtie T \bowtie U$	20000		
$S \bowtie U$	10000000				
$T \bowtie U$	200				

2-Tables	Card.	Cost	3-Tables	Card.	Cost	4-Tables	Card.	Cost
$R \bowtie S$	$5 \cdot 10^4$	$5 \cdot 10^4$	<del><math>RS \bowtie T</math></del>	$5 \cdot 10^4$	$1 \cdot 10^5$	<del><math>RST \bowtie U</math></del>	$1 \cdot 10^4$	$7 \cdot 10^4$
$R \bowtie T$	$1 \cdot 10^4$	$1 \cdot 10^4$	<del><math>RS \bowtie U</math></del>	$5 \cdot 10^6$	$505 \cdot 10^4$	<del><math>RSU \bowtie T</math></del>	$1 \cdot 10^4$	$5011 \cdot 10^3$
$R \bowtie U$	$1 \cdot 10^3$	$1 \cdot 10^3$	$RT \bowtie S$	$5 \cdot 10^4$	$6 \cdot 10^4$	$RTU \bowtie S$	$1 \cdot 10^4$	$122 \cdot 10^2$
$S \bowtie T$	$1 \cdot 10^5$	$1 \cdot 10^5$	<del><math>RT \bowtie U</math></del>	$2 \cdot 10^3$	$12 \cdot 10^3$	<del><math>STU \bowtie R</math></del>	$1 \cdot 10^4$	$302 \cdot 10^2$
$S \bowtie U$	$1 \cdot 10^7$	$1 \cdot 10^7$	$RU \bowtie S$	$5 \cdot 10^6$	$5001 \cdot 10^3$	<del><math>RS \bowtie TU</math></del>	$1 \cdot 10^4$	$602 \cdot 10^2$
$T \bowtie U$	$2 \cdot 10^2$	$2 \cdot 10^2$	<del><math>RU \bowtie T</math></del>	$2 \cdot 10^3$	$3 \cdot 10^3$	<del><math>RT \bowtie SU</math></del>	$1 \cdot 10^4$	$1002 \cdot 10^4$
			<del><math>ST \bowtie R</math></del>	$5 \cdot 10^4$	$15 \cdot 10^4$	<del><math>RU \bowtie ST</math></del>	$1 \cdot 10^4$	$111 \cdot 10^3$
			<del><math>ST \bowtie U</math></del>	$2 \cdot 10^4$	$12 \cdot 10^4$			
			<del><math>SU \bowtie R</math></del>	$5 \cdot 10^6$	$15 \cdot 10^6$			
			<del><math>SU \bowtie T</math></del>	$2 \cdot 10^4$	$102 \cdot 10^4$			
			$TU \bowtie R$	$2 \cdot 10^3$	$22 \cdot 10^2$			
			$TU \bowtie S$	$2 \cdot 10^4$	$202 \cdot 10^2$			



- Q 5.6 Best left-deep plan:  
 $((T \bowtie U) \bowtie R) \bowtie S \rightarrow 200 + 2000 + 10000 = 12200$
- Q 5.7 Worst left-deep plan (pruned in the table on the prev. slide):  
 $((S \bowtie U) \bowtie R) \bowtie T \rightarrow 10000000 + 5000000 + 10000 = 15010000$
- Q 5.8 Best bushy plan:  
 $(T \bowtie U) \bowtie (R \bowtie S) \rightarrow 200 + 50000 + 10000 = 60200$
- Q 5.9 Worst bushy plan:  
 $(S \bowtie U) \bowtie (T \bowtie R) \rightarrow 10000000 + 10000 + 10000 = 10020000$

- Given is a relation R with tuple size of 256 Byte.  
Block size of the disc is 4KB and 128MB of memory are available.  
Assume for simplicity that blocks have no header, 1MB=1024KB,  
1KB=1024Byte
- What is the max cardinality of R to sort it with a single pass method?

Answer: **524288**

Memory size / Tuple size:

$$128 \text{ MB} / 256 \text{ B} = 524288 = 2^{19}$$

- Given is a relation R with tuple size of 256 Byte.  
Block size of the disc is 4KB and 128MB of memory are available.  
Assume for simplicity that blocks have no header, 1MB=1024KB,  
1KB=1024Byte  
(same as in 5.1)
- What is the max. cardinality of R to sort it with a TPMMS?

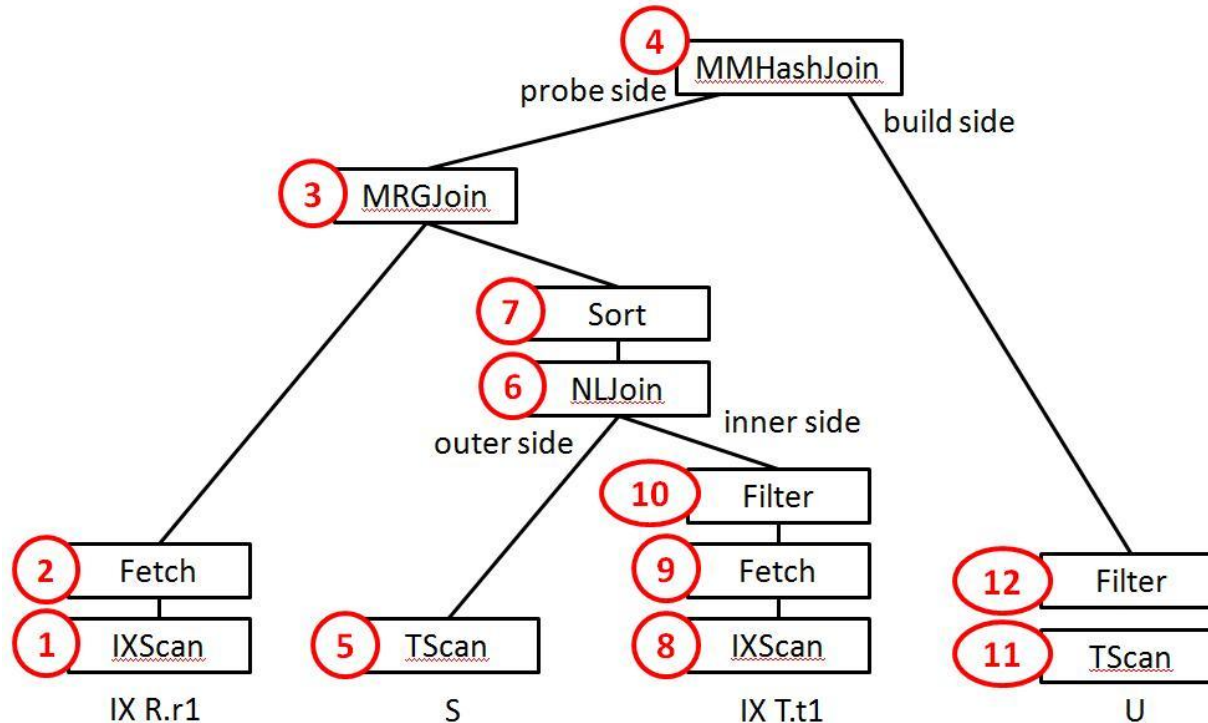
Answer: 17179344896

1. Data is sorted in memory (see 5.1) and spilled to disk
2. Sorted chunks are read from disk (one block per chunk) and merged

#Tuples sortable in memory (see 5.1) \* Number of blocks in memory  
 $2^{19} * ((128 \text{ MB} / 4 \text{ KB}) - 1) = 17179344896 \approx 2^{39}$

1 block reserved for the output

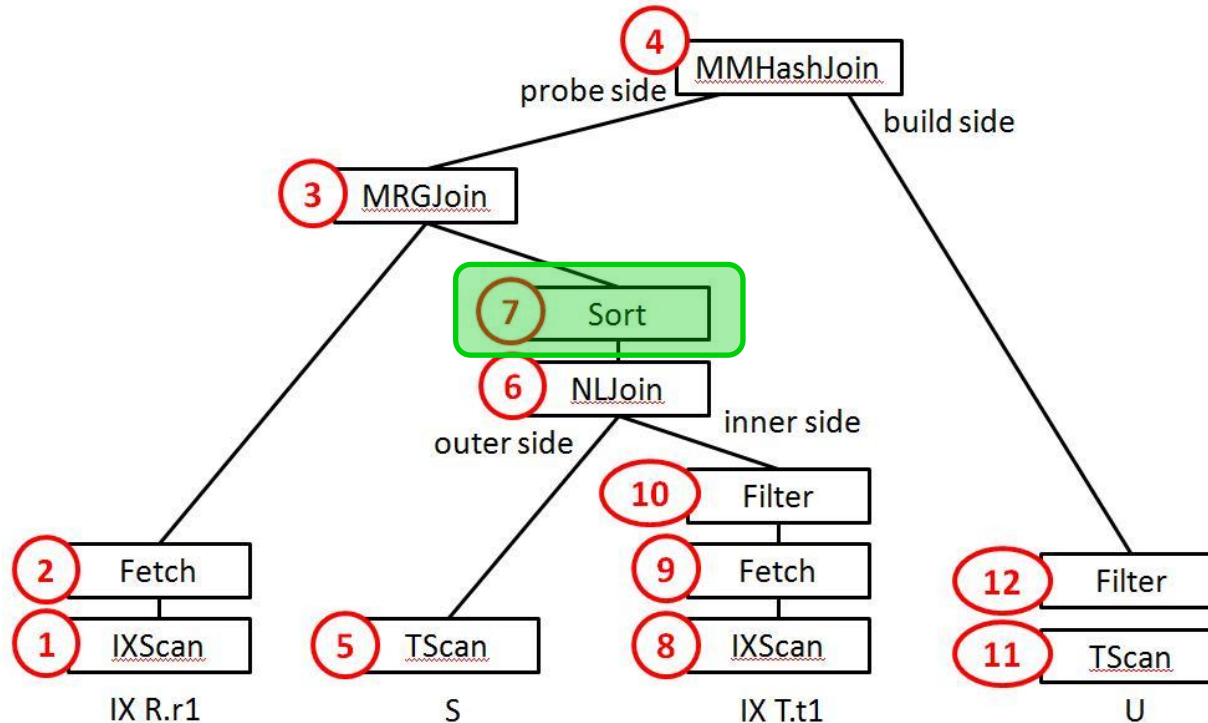
- Given the following query execution plan:



- Decide which operator acts as the first dam for the tuples of R. Operator IDs are given in red, if none operator is damping answer 0.

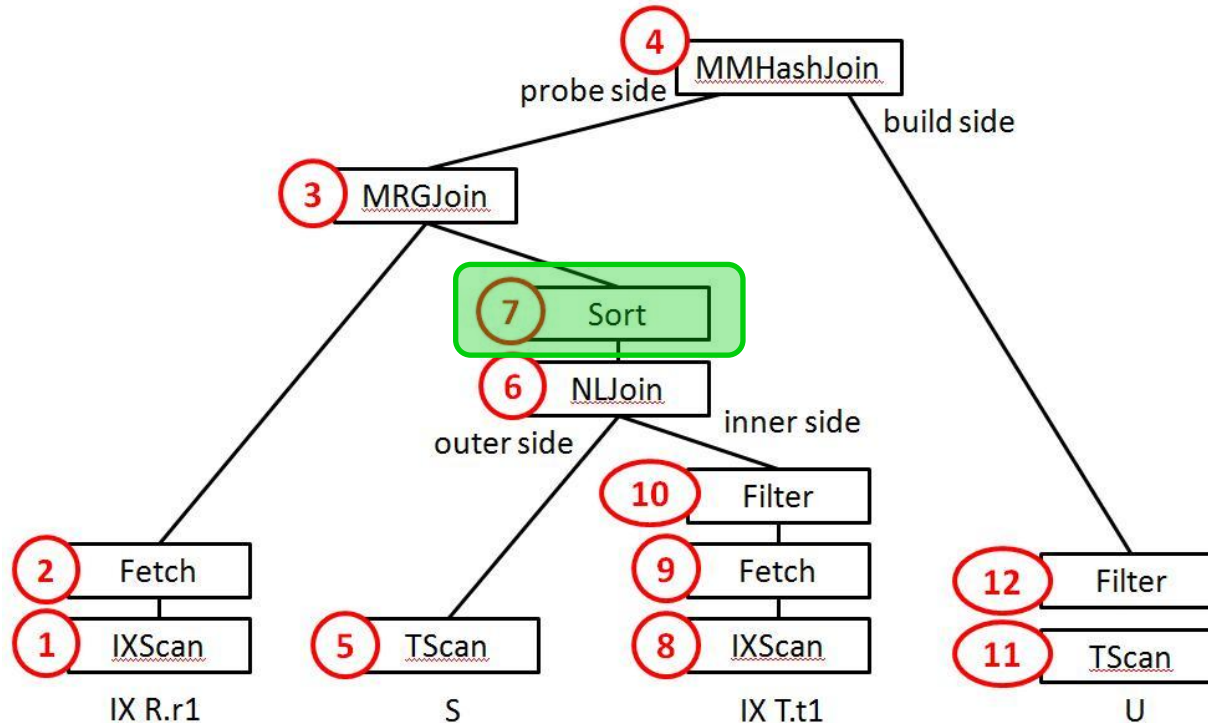
Answer: 0, R is completely pipelined

- Given the following query execution plan:



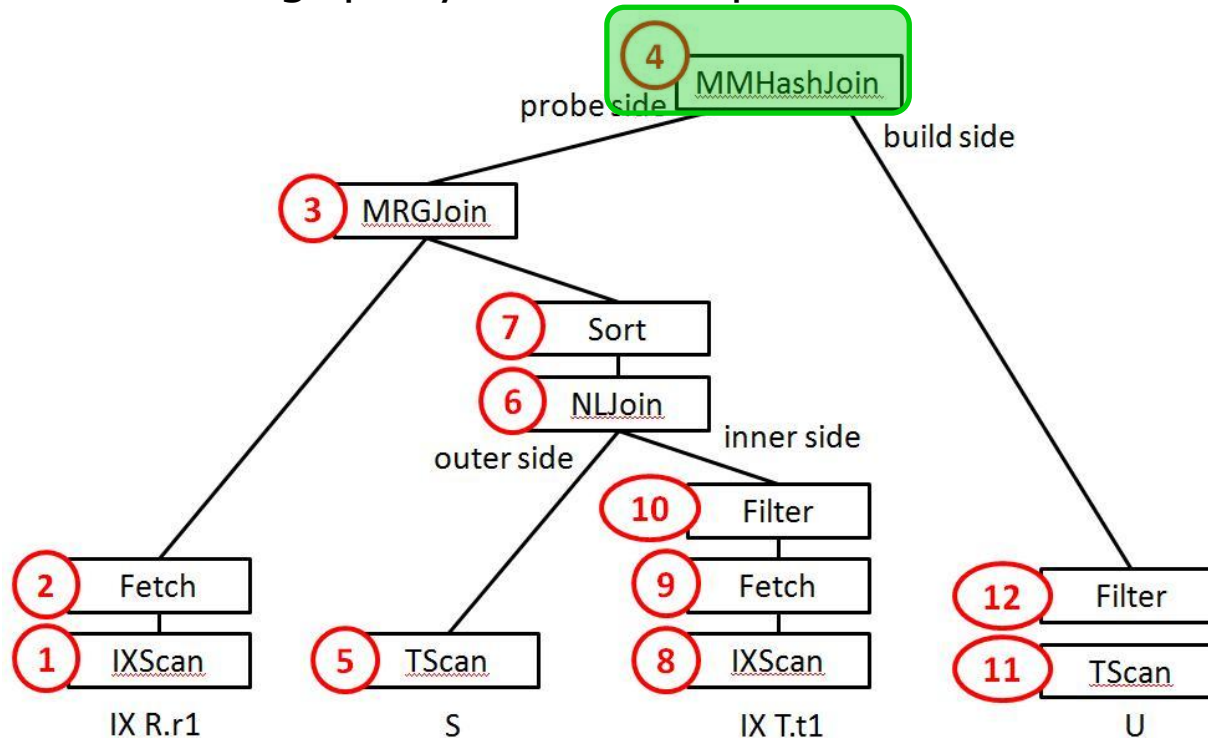
- Decide which operator acts as the first dam for the tuples of S. Operator IDs are given in red, if none operator is damping answer 0.

- Given the following query execution plan:



- Decide which operator acts as the first dam for the tuples of T. Operator IDs are given in red, if none operator is damping answer 0.

- Given the following query execution plan:



- Decide which operator acts as the first dam for the tuples of U. Operator IDs are given in red, if none operator is damming answer 0.