Assignment No.1

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Download all python codes from

https://github.com/Sekharjala/Assignments/blob/main/code

and pdf from

https://github.com/Sekharjala/Assignments/blob/main/Assignment1.pdf

1 Question No.Matrices 1.76.1

Question: Find equation of line joining (1,2) and (3,6) using determinants.

2 Solution

To construct a line joining $\mathbf{A} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$ and $\mathbf{B} = \begin{pmatrix} 3 \\ 6 \end{pmatrix}$, let \mathbf{n} be the normal vector then

$$\mathbf{n}^{\mathrm{T}}\mathbf{A} = c \tag{2.0.1}$$

$$\mathbf{n}^{\mathsf{T}}\mathbf{B} = c \tag{2.0.2}$$

from Equations(2.0.1) and (2.0.2)

$$\mathbf{A}^T \mathbf{n} = c \tag{2.0.3}$$

$$\mathbf{B}^T \mathbf{n} = c \tag{2.0.4}$$

$$\begin{pmatrix} \mathbf{A}^T \\ \mathbf{B}^T \end{pmatrix} \mathbf{n} = \begin{pmatrix} c \\ c \end{pmatrix} \tag{2.0.5}$$

$$\begin{pmatrix} 1 & 2 \\ 3 & 6 \end{pmatrix} \mathbf{n} = \begin{pmatrix} c \\ c \end{pmatrix} \tag{2.0.6}$$

Augmented vector is

$$\begin{pmatrix} 1 & 2 & c \\ 3 & 6 & c \end{pmatrix} = 0 \tag{2.0.7}$$

$$\begin{pmatrix} 1 & 2 & c \\ 3 & 6 & c \end{pmatrix} \tag{2.0.8}$$

$$\stackrel{3r_1-r_2\to r_2}{\longrightarrow} \begin{pmatrix} 1 & 2 & c \\ 0 & 0 & -2c \end{pmatrix} \tag{2.0.9}$$

Thus, from the above row reduced form we can conclude that the given system of lines has solution iff "c=0" and points are collinear.

$$\begin{pmatrix} 1 & 2 & 0 \\ 0 & 0 & 0 \end{pmatrix} \tag{2.0.10}$$

$$\begin{pmatrix} 1 & 2 \end{pmatrix} \mathbf{n} = 0 \tag{2.0.11}$$

The normal vector n to a line is orthogonal to the direction vector m then

$$\mathbf{m}^T \mathbf{n} = 0 \tag{2.0.12}$$

Directional vector is

$$\mathbf{m} = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \tag{2.0.13}$$

Normal vector

$$\mathbf{n} = \begin{pmatrix} -2\\1 \end{pmatrix} \tag{2.0.14}$$

Equation of straight line is from (2.0.1) is

$$\begin{pmatrix} -2 & 1 \end{pmatrix} \mathbf{X} = 0 \tag{2.0.15}$$

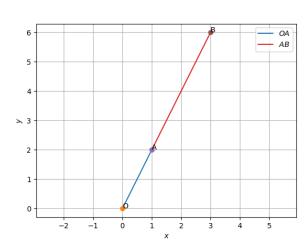


Fig. 0: line formed with points(1,2) and (3,6) using Python