

Math 305 Homework 4

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April 2023

Problem 1

- Colley Ratings: Where C = Colley rating of a team
 W = number of wins by the team
 P = number of opponents the team has played
 G = number of games played by the team

$$- C_1 = \frac{W_1 + P_1}{2G_1} = \frac{5+3}{12} = .66$$

$$- C_2 = \frac{W_2 + P_2}{2G_2} = \frac{3+3}{12} = .5$$

$$- C_3 = \frac{W_3 + P_3}{2G_3} = \frac{3+3}{12} = .5$$

$$- C_4 = \frac{W_4 + P_4}{2G_4} = \frac{1+3}{12} = .33$$

- Massey Ratings: (Not sure)

Problem 2

Experienced chess players A and B both start with a rating of 2600. They play two games, first A beats B, then B beats A. Will the rating of A equal the rating of B after these two games? Should the ratings be equal? Describe your thoughts.

No, the ratings would not be equal, because although they begin at the same place, after player A beats B, their rating goes up, whereas player B's rating goes down. Therefore, for the next game, when player B wins, they are beating a higher rated player, therefore gaining more elo than if they were both the same.

Problem 3

Two chess players have Elo ratings that differ by $400n$, where n is a non-negative integer. How likely is the higher rated player to win for different values of n ? How much more likely is the higher rated player to win than the lower rated

one for different values of n ? (Consider $n = 0, 1, 2, \dots, 4$ to see a pattern or analyze the formula for win probability.)

- $n = 0, P = 50\%$
- $n = 1, P = 90.91\%$
- $n = 2, P = 99\%$
- $n = 3, P = 99.9\%$
- $n = 4, P = 99.99\%$
- $n = i, P = \frac{1}{1+10^{-i}}$

Problem 4

Suppose a truck rental company has locations in Dallas, TX, Raleigh, NC and Miami, FL. The company permits one-way rentals and knows that based on previous experience that during a typical week the following truck movements occur: Of the trucks that start in Dallas:

- 50% stay in Dallas
- 25% travel to Raleigh
- 25% travel to Miami

Of the trucks that start in Raleigh:

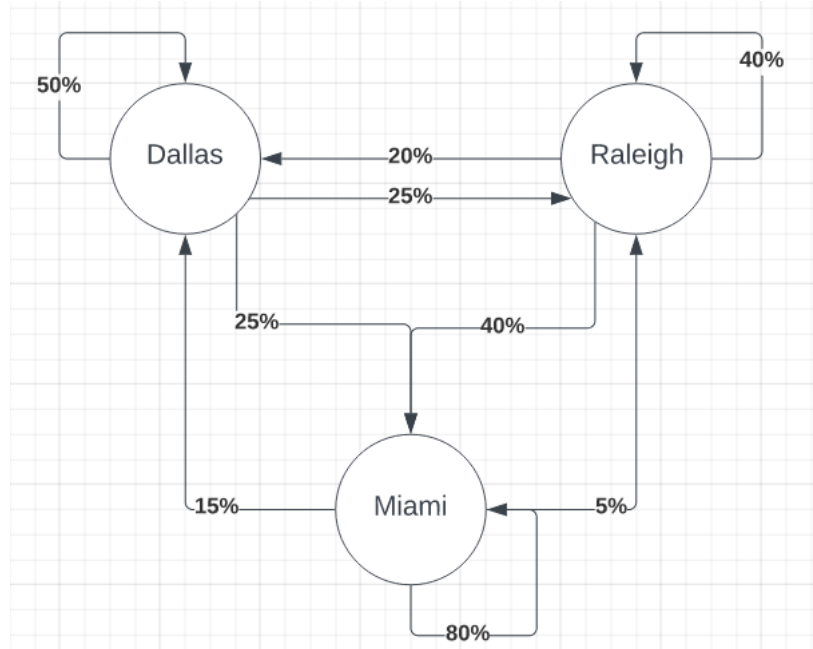
- 40% stay in Raleigh
- 20% travel to Dallas
- 40% travel to Miami

Of the trucks that start in Miami:

- 80% stay in Miami
- 15% travel to Dallas
- 5% travel to Raleigh

Draw a transition diagram for the model adding the given probabilities. If 150 trucks start in each city, use MATLAB to determine the long-term numbers of

trucks in each city (steady-state)



$$A = \begin{pmatrix} .5 & .25 & .25 \\ .2 & .4 & .4 \\ .15 & .05 & .8 \end{pmatrix}$$

$$\lambda_1 = 1$$

$$v_1 = (1 \ 1 \ 1)$$

Therefore all 3 cities will have 150 trucks as time goes on.