

1. (a) For truth table enumeration
time complexity: $O(2^n)$
space complexity: $O(n)$
 n is the # of symbols

(b) forward chaining

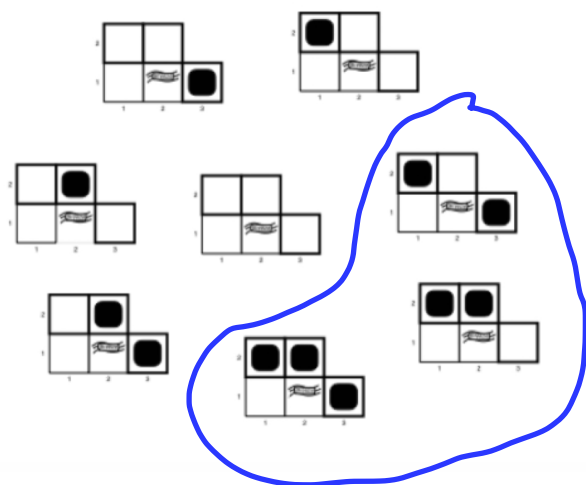
time complexity: $O(n)$
space complexity: $O(n)$
 n is the # of horn clause

(c) Resolution

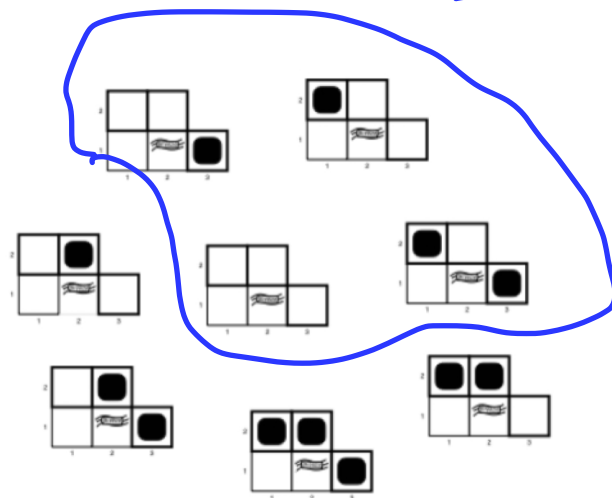
time complexity: $O(n^2)$
space complexity: $O(n^2)$
 n is the # of clauses

2.

KB:



α : $[1,2]$ is safe



breaze in $[1,1]$ and $[2,1]$

conclusion: KB do not entail α

3.

$$(A \wedge B \Rightarrow C) \wedge \neg C \quad \neg A \wedge \neg B$$

A	B	C	$\neg A$	$\neg B$	$\neg C$	$A \wedge B \Rightarrow C$
true	true	true	false	false	false	true
true	false	true	false	true	false	true
false	true	true	true	false	false	true
true	true	false	false	false	false	false
false	false	true	true	true	true	true
false	true	false	true	false	false	true
true	false	false	false	true	true	true
false	false	false	true	true	true	true

\downarrow	\downarrow
KB	α
false	false
false	true
false	true
false	false
false	true
true	true
true	true
true	true

When KB is true α is true

$\therefore KB \models \alpha$

4.

(a)

Rules:

$$\begin{aligned} B(1,1) &\Rightarrow P(2,1) \vee P(1,2) \\ B(1,2) &\Rightarrow P(1,1) \vee P(2,2) \\ B(2,1) &\Rightarrow P(1,1) \vee P(2,2) \\ B(2,2) &\Rightarrow P(2,1) \vee P(1,2) \end{aligned}$$

Observation:

$$\begin{aligned} &B(2,1) \quad \neg P(2,1) \\ &\neg B(1,1) \\ &\neg P(1,1) \end{aligned}$$

(b)

$$B(1,1) \leftrightarrow (P(2,1) \vee P(1,2))$$

$$\Rightarrow (B(1,1) \rightarrow (P(2,1) \vee P(1,2))) \wedge ((P(2,1) \vee P(1,2)) \rightarrow B(1,1))$$

- by conditional elimination

$$\Rightarrow (\neg B(1,1) \vee (P(2,1) \vee P(1,2))) \wedge \neg((P(2,1) \vee P(1,2)) \vee B(1,1))$$

- de Morgan law

$$\Rightarrow (\neg B(1,1) \vee P(2,1) \vee P(1,2)) \wedge (\neg P(2,1) \wedge \neg P(1,2)) \vee B(1,1)$$

- distribution law

$$\Rightarrow \neg B(1,1) \vee P(2,1) \vee P(1,2) \quad \bigwedge \quad \neg P(2,1) \vee B(1,1) \quad \bigwedge \quad \neg P(1,2) \vee B(1,1)$$

$$\Downarrow (\neg P(2,1) \wedge \neg B(1,1)) \text{ from observation}$$

$$\neg B(1,1) \vee P(1,2) \wedge \neg P(2,1) \wedge \neg P(1,2)$$

$$\Rightarrow \neg B(1,1) \wedge \neg P(2,1) \wedge \neg P(1,2) \quad \textcircled{1}$$

By the same process, ② will be

$$\neg B(1,2) \vee P(1,1) \vee P(2,2) \wedge \neg P(1,1) \vee B(1,2) \wedge \neg P(2,2) \vee B(1,2)$$

from observation: $\neg P(1,1)$

$$\Rightarrow \neg B(1,2) \vee P(2,2) \wedge \neg P(1,1) \vee B(1,2) \wedge \neg P(2,2) \vee B(1,2) \quad \textcircled{2}$$

By the same process as ①, ③ will be

$$\neg B(2,1) \vee P(1,1) \vee P(2,2) \wedge \neg P(1,1) \vee B(2,1) \wedge \neg P(2,2) \vee B(2,1)$$

from observation $(B(2,1) \wedge \neg P(1,1))$

So $P(2,2)$ must be true

$$5. \quad G: \neg R \wedge I$$

$$KB: \begin{array}{l} \neg L \Rightarrow \neg R \quad \rightarrow \quad LV - R \\ D \Rightarrow \neg L \quad \rightarrow \quad -DV - L \end{array}$$

$$\therefore KB: \underline{LV - R} \wedge \underline{-DV - L} \wedge \textcircled{D} \wedge \textcircled{A} \wedge \underline{I} \wedge \textcircled{A}$$

$$\Rightarrow \cancel{LV - R} \wedge \textcircled{-L} \wedge D \wedge A \wedge I$$

$$\Rightarrow \textcolor{yellow}{\neg R} \wedge \textcolor{yellow}{-L} \wedge D \wedge A \wedge \textcolor{yellow}{I}$$

$$\therefore KB \models G$$