

3C 1)

append operation's amortise time is $O(1)$ because it ~~doesn't~~ ^{doesn't} need to go ~~to~~ through the list but the end, even sometimes need to ^(enlarge) resize, the average performance is still $O(1)$ constant time

$\left. \begin{array}{l} \text{append}(1) \\ \text{append}(2) \\ \dots \\ \text{append}(n) \end{array} \right\} \begin{array}{l} O(1) \times n \\ O(n) \end{array}$

pop() (~~default~~)'s amortise time is $O(1)$ because it add item in the end of list, even sometimes need to shrink the list, the average performance is still $O(1)$, constant time

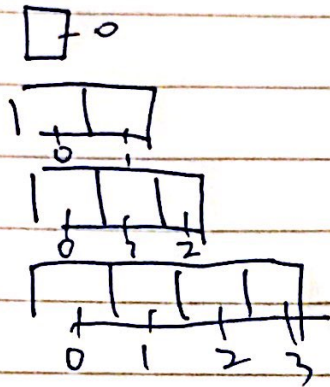
$\left. \begin{array}{l} \text{pop}() \\ \vdots \\ \times n \\ \vdots \\ \text{pop}() \end{array} \right\} \begin{array}{l} O(1) \times n \\ O(n) \end{array}$

$O(n) + O(n) \Rightarrow 2n$ operation

2) ① if the list goes shrinking ^{to half} when the actual size of list is less than half of the capacity, the runtime will increase to $2n$ from $\frac{3}{4}n$, but will save storage

shrink $\frac{1}{2}$ $\left| \begin{array}{l} 16 \\ 8 \\ 4 \\ 2 \\ 1 \end{array} \right|$ of pop $\left| \begin{array}{l} 16 \\ 8 \\ 4 \\ 2 \\ 1 \end{array} \right|$ shrink $\frac{1}{4}$

② if we append object by just increase one capacity to resize, it will be a $O(n^2)$ operation:



$$1+2+3+4+\dots+n = O(n^2)$$

also, if we shrink in every $\text{pop}()$ operation, it will be $O(n^2)$

4b: Separate loop ~~of~~ operations for three times
 $O(3n) \Rightarrow O(n)$

5a: while loop ^{worst} (n)
 inside remove operation go through list ^{worst} (n)
 worst $O(n^2)$

5c: worst case go through two separate while loops, $O(2n)$