## CSC258 Computer Organization 2015 fall Assignment 1 due Thu.Oct.8 at 6pm in BA2220

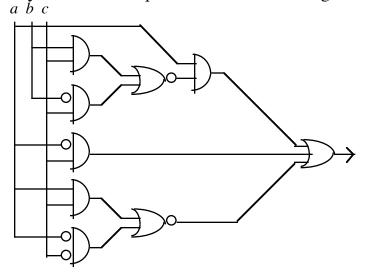
1[10] Prove that the following three expressions are equivalent.

if x then y else z

if y then  $z \lor x$  else  $z \gt x$ 

if z then  $x \le y$  else  $x \land y$ 

2[10] Find the simplest circuit you can that's equivalent to the following circuit.



- 3[5] Prove that  $\triangle$  is complete.
- 4[10] Prove that \(\pm\) is not complete. Hint: Find a systematic way to show all functions that can be created from \(\pm\), and show some function that is not created. Or find a property of all functions that can be created from \(\pm\), and show some function that does not have that property.
- 5[15] Design a circuit whose 4 bits of input represent a number x from 0 to 15, and whose bits of output represent two numbers y and z such that  $x = y \times z$  and  $y \ge z$ , and of all pairs whose product is x, the pair y and z has the smallest sum.