Dsl.scala: creating library-defined keywords from ad-hoc polymorphic delimited continuations

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The semantics of a programming language are defined by its keywords, which traditionally require special treatment by the compiler. Thus, the capacity of the programming language is not extensible by libraries, unless using compiler plug-ins, AST macros, code generation, or other metaprogramming technologies.

Our goal is making the control flow of a programming language extensible. We discovered a novel approach to create library-defined keywords used in control flow. Those keywords are interpreted by libraries instead of the compiler. No metaprogramming knowledge is required for keyword authors.

Library-defined keywords are collaborative. An application developer can create a single function that contains interleaved keywords from different libraries, along with ordinary language control flows.

Additional Key Words and Phrases: type class, scala

1 INTRODUCTION

Traditionally, the capacity of a general purpose language can be extended to special domain by creating an embedded DSL (Domain-Specific Language). For example, Akka provides a DSL to create finite-state machines [Lightbend, Inc. 2017], which consists of some domain-specific operators including when, goto, stay, etc. Although those operators looks similar to native control flow, they are not embeddable in native **if**, **while** or **try** blocks, because the DSL code is split into small closures, preventing ordinary control flow from crossing the boundary of those closures. Thus, this kind of DSLs reinvent incompatible control flow to the meta-languages. TensorFlow's control flow operations [Abadi et al. 2016] and Caolan's async library [McMahon 2017] are other examples of reinventing control flow in eDSLs.

Instead of reinventing the whole set of control flow for each DSL, a more general approach is implementing a minimal interface for control flow for each domain, while other control flow operations are derived from the interface, shared between different domains. In Haskell and other functional programming language, monads are used as the generic interface of control flow [Jones and Duponcheel 1993; Wadler 1990, 1992]. Scala implementations of monads are provided by Scalaz [Yoshida et al. 2017], Cats [Typelevel 2017], Monix [Nedelcu et al. 2017] and Algebird [Twitter, Inc. 2016]. A DSL author only have to implement bind and point functions in Monad type class, and all the derived control flow operations like whileM or ifM are available. In addition, those monadic data type can be created and composed from do notation [Jones et al. 1998] or for comprehension [Odersky et al. 2004]. For example, you can use the same scalaz.syntax or for comprehension to create random value generators [Nilsson 2015] and data-binding expressions [Yang 2016], as long as there are Monad instances for data types org.scalacheck.Gen and com.thoughtworks.binding.Binding respectively.

An idea to avoid incompatible domain-specific control flow is converting direct style control flow to domain-specific control flow at compiler time. For example, Scala Async provides a macro to generate asynchronous control flow [Haller and Zaugg 2013], allowing normal sequential code inside a scala.async block to run asynchronously. This approach can be generalized to any monadic data types. ThoughtWorks Each [Yang 2015], Monadless [Brasil 2017], effectful [Crockett 2013] and !-notation in Idris [Brady 2013a] are compiler-time transformers to convert source code of direct style control flow to monadic control flow. For example, with the help of ThoughtWorks

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Each, Binding.scala[Yang 2016] can be used to create reactive HTML template from ordinary direct style code.

Another generic interface of control flow is continuation, which is known as the mother of all monads [Piponi 2008], where specific control flow in specific domain can be supported by specific answer types of continuations. Scala Continuations [Rompf et al. 2009] and Stateless Future [Yang 2014a] are two delimited continuation implementations in Scala. Both projects can convert direct style control flow to continuation-passing style closure chains at compiler time. For example, Stateless Future Akka [Yang 2014b], based on Stateless Future, provides a special answer type for akka actors. Unlike reinvented control flow in akka.actor.AbstractFSM, users can create complex finite-state machines from simple direct style control flow along with Stateless Future Akka's domain-specific operator nextMessage.

All the previous approaches lack of the ability to collaborate with other DSLs. Each of the above DSLs can be exclusively enabled in a code block. Scala Continuations enables calls to @cps method in reset blocks, and ThoughtWorks Each enables the magic each method [Yang 2015] for scalaz. Monad in monadic blocks. It was impossible to enable both DSL in one function.

[Kiselyov et al. 2013] introduced effect handlers to solve the collaboration problem. However, the solution is heavy weight, only expressions written in the special Eff language are able to use DSLs defined in effect handlers.

This paper describes a lighter-weight approach to resolve the collaboration problem, and presents an implementation in Scala, the framework *Dsl.scala*.

Dsl.scala allows library authors to create special keywords for language features that were usually implemented by the compiler. Those library-defined keywords (LDKs) are adaptive to the enclosing DSL, as a library user can create one function that contains interleaved LDKs from different vendors, along with ordinary Scala control flow. Unlike Eff, an LDK is non-intrusive, can be added into an existing function as an optional first-class feature.

Dsl.scala ships with some built-in LDKs, including:

- The Shift LDK for asynchronous programming, similar to the await and async keywords in C#, Python and JavaScript.
- The Yield LDK for generating lazy streams, similar to the yield keyword in C#, Python and JavaScript.
- The Each LDK for traversing each element of a collection, similar to for, yield keywords for Scala collections.
- The Fork LDK for duplicating current thread, similar to the fork system call in POSIX.
- The AutoClose LDK to automatically close resources when exiting a scope, similar to the destructor feature in C++.
- The Monadic LDK for creating Scalaz [Yoshida et al. 2017] or Cats [Typelevel 2017] monadic control flow, similar to the !-notation in Idris[Brady 2013a].

2 USING LIBRARY-DEFINED KEYWORDS

In this section, we will show some use cases from the perspective of the user of LDKs.

2.1 Creating generators

 Suppose Alice is creating an Xorshift pseudo-random number generator [Marsaglia et al. 2003], and she wants to store the generated numbers in a lazily evaluated infinite stream.

The usage of Alice's pseudo-random number generator is shown as below:

```
val generatedNumbers = aliceRandomGenerator(seed = 2463534242)
println(generatedNumbers(0))
```

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```
println(generatedNumbers(1))
println(generatedNumbers(2))
```

Listing 1. Using Alice's pseudo-random number generator

Alice is a functional programming language developer. She wants to avoid mutable variables in the implementation. Unfortunately, a pseudo-random number generator usually has an internal state that are changed during generate new random number.

With the help of the built-in LDK Yield from *Dsl.scala*, Alice can implement the generator as a recursive function that produce the next random number in each iteration.

```
import dsl.keywords.Yield
def aliceRandomGenerator(seed: Int): Stream[Int] = {
  val tmp1 = seed ^ (seed << 13)
  val tmp2 = tmp1 ^ (tmp1 >>> 17)
  val tmp3 = tmp2 ^ (tmp2 << 5)
  !Yield(tmp3)
  aliceRandomGenerator(tmp3)
}</pre>
```

Listing 2. The implementation of Alice's pseudo-random number generator

aliceRandomGenerator does not throw a StackOverflowError, because the execution of aliceRandomGenerator will be paused at the LDK Yield, and it will be resumed when the caller is looking for the next number.

Yield is an LDK to produce a value for a lazily evaluated Stream, similar to the yield keyword in C#, JavaScript or Python. That is to say, Stream is the domain where the domain-specific LDK Yield can be used. More generally, all LDKs are domain-specific, where the word "domain" stands for the return type of the enclosing function.

2.2 Creating generators with an additional return value

In this use case, we will demonstrate how to add logging to existing functions using the Yield LDK.

Suppose Bob has a function to parse JSON text. The parser is fault-tolerant, since it returns the defaultValue for invalid input (Listing 3).

```
import scala.util.parsing.json._
def bobParser(jsonContent: String, defaultValue: JSONType): JSONType = {
    JSON.parseRaw(jsonContent) match {
        case Some(json) =>
            callback(json)
        case None =>
            callback(defaultValue)
    }
}
```

Listing 3. The original implementation of Bob's parser

Then, Bob wants to add some logs to his existing parser. He learned from Alice's use case, and wonders if he can Yield log messages to a Stream[String] during parsing.

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However, unlike Alice's case, Bob's parser should return both the parsed JSON objects and the collected logs. It's impossible in C#'s yield, because yield does not work in a method that returns a JSON object.

Bob resolves the problem by creating a delimited continuation. The parsed JSON object is handled by a callback function instead of return value. Thus the return value is still a Stream, allowing Yielding log messages (Listing 4).

Listing 4. The implementation of Bob's logging parser

The return type of Bob's new parser is (Stream[String] !! JSONType), which is an alias to the delimited continuation ((JSONType => Stream[String]) => Stream[String]), indicating it produces both a scala.util.parsing.json.JSONType and a Stream of logs.

After Bob created the first version of delimited continuation, he then found that the closure can be simplified with the help of Scala's placeholder syntax (Listing 5).

Listing 5. The implementation of Bob's logging parser, the underscore placeholder version

Alternately, Bob can use the pre-defined function reset instead of the underscore placeholder (Listing 6).

```
def reset[R, A](a: => A): R !! A = _(a)

def bobLoggingParserReset(jsonContent: String, defaultValue: JSONType): Stream[
    String] !! JSONType = reset {
```

```
!Yield(s"I_am_going_to_parse_the_JSON_text_$jsonContent...")
JSON.parseRaw(jsonContent) match {
   case Some(json) =>
    !Yield(s"Succeeded_to_parse_$jsonContent")
        json
   case None =>
    !Yield(s"Failed_to_parse_$jsonContent")
        defaultValue
}
```

Listing 6. The implementation of Bob's logging parser, the reset version

Then, the user of Bob's parser calls bobLoggingParserReset to handle both results (Listing 7):

- (1) The JSON result in a callback function.
- (2) The logs from return value.

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Listing 7. Using Bob's parser

The use case of Bob's parser demonstrates how to enable additional LDKs into existing ordinary functions. Generally, an LDK user can introduce a new domain that supports more LDKs to an existing method with the two changes:

- (1) Inserting a NewDomain!! prefix to the return type (Stream[String]!! in Bob's case).
- (2) Inserting an underscore or a reset before the method body.

2.3 Using multiple LDKs at once

In this use case, we will demonstrate how to use multiple library-defined keywords in one function. Suppose Carol is creating a line splitter from a file. Carol wants to lazily read each line of a file to a Stream, and automatically close the file handle after reading the last line, and finally return the total number of lines.

Carol will use the Yield LDK to append a line to the Stream, and the AutoClose LDK to manage the life-cycle of the file handle.

Yield LDK is only available in a function that returns Stream or (Stream[_] !! _) as we already knows. Similarly, the AutoClose LDK is only available in a function that returns (_ !! Throwable !! _). So, Carol makes her line splitter return (Stream[String] !! Throwable !! Int) to enable both LDKs (Listing 8).

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```
import dsl.Dsl.!!
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     import dsl.keywords.AutoClose
     import dsl.keywords.Yield
     import dsl.keywords.Shift
     import java.nio.file._, Files._
251
     def carolLineSplitter(path: Path): Stream[String] !! Throwable !! Int = reset {
253
       val reader = !AutoClose(newBufferedReader(path))
255
       def loop(lineNumber: Int): Stream[String] !! Throwable !! Int = _ {
         reader.readLine() match {
257
            case null =>
              lineNumber
259
            case line =>
              !Yield(line)
261
              !Shift(loop(lineNumber + 1))
          }
263
       }
265
       !loop(0)
266
267
268
```

Listing 8. Carol's line splitter

Note that the return type of loop, (Stream[String] !! Throwable !! Int), is a delimited continuation, Carol needs Shift LDK as the first-class delimited continuation operator[Asai 2009; Danvy and Filinski 1990] to invoke loop recursively.

The type (Stream[String] !! Throwable !! Int) returned from carolLineSplitter contains the following data:

- A Stream of each lines of the file, as the final return value.
- An optional Throwable of the exception thrown during reading the file, which can be handled by a callback function.
- An Int of the total number of lines in the file, which can be handled by another callback function.

The example code of using Carol's line splitter is shown in Listing 9.

```
val allLines: Stream[String] = carolLineSplitter(Paths.get("multiline.txt")) {
    numberOfLines: Int =>
    println(s"There_are_${numberOfLines}_lines_in_multiline.txt")
    Function.const(Stream.empty)(_)
} { e: Throwable =>
    println("An_error_occurred_during_splitting_multiline.txt")
}
```

Listing 9. Using Carol's line splitter

In this use case, Carol created a function from three library-defined keywords.

(1) AutoClose for resource management, similar to C++'s RAII feature.

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- (2) Yield for lazily append values to a Stream, similar to Python, C# or ECMAScript's yield keyword.
- (3) Shift for awaiting a value from a task, similar to Python, C# or ECMAScript's await keyword.

What is interesting is that our library-defined keywords are more like first-class features than compiler-defined keywords. Despite the fact that Python 3.5, C# and ECMAScript do not support automatic resource management, they also do not support using both yield and await in one function, even when yield and await are supported respectively, and Python 3.6 needs a special implementation of Asynchronous Generators [Selivanov 2016] to use both yield and await, while our library-defined keywords can collaborate with arbitrary other LDKs by composing extra domains on the return type.

2.4 Fork / join in asynchronous programming

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We provided a type alias **type** Task[A] = TailRec[Unit] !! Throwable !! A for asynchronous programming.

For example, Suppose Dave is creating an HTTP client. He can implement the HTTP protocol in the Task domain shown in Listing 10.

```
312
     import dsl.task._
     import dsl.keywords._, Shift.implicitShift, AsynchronousIo._
313
314
     import java.io._
     import java.net._
315
     import java.nio._, channels._
316
317
     def readAll(channel: AsynchronousByteChannel, destination: ByteBuffer): Task[
318
         Unitl = {
319
       if (destination.remaining > 0) {
320
         val numberOfBytesRead: Int = !Read(channel, destination)
321
         numberOfBytesRead match {
322
323
            case -1 =>
            case _ => !readAll(channel, destination)
324
         }
325
       } else {
326
          throw new IOException("The_response_is_too_big_to_read.")
327
328
     }
329
330
     def writeAll[Domain](channel: AsynchronousByteChannel, destination: ByteBuffer)
331
          : Task[Unit] = _ {
332
       while (destination.remaining > 0) {
333
          !Write(channel, destination)
334
       }
335
     }
336
337
     def daveHttpClient(url: URL): Task[String] = _ {
338
       val socket = AsynchronousSocketChannel.open()
339
       try {
340
         val port = if (url.getPort == -1) 80 else url.getPort
341
         val address = new InetSocketAddress(url.getHost, port)
342
```

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Listing 10. Dave's HTTP client

Dave's HTTP client is built from Connect, Read and Write LDKs. Those are asynchronous Java NIO.2 IO operators defined in dsl.keywords.AsynchronousIo, working with dsl.task.Task domain.

In this example, Dave imported implicitShift, which is an implicit conversion, which automatically converts Task or other CPS functions to Shift LDKs. Therefore, !Shift(writeAll(...)) becomes unnecessary, in favor of !writeAll(...).

The usage of Task can be similar to previous examples in Section 2.3, but we also provide blockingAwait and some other utilities under the implicit class dsl.task.TaskOps to ease the usage (Listing 11).

```
val fileContent = daveHttpClient(new URL("http://ftp.debian.org/debian/")).
    blockingAwait
fileContent should startWith("HTTP/1.1_200_OK")
```

Listing 11. Using Dave's http client

Another useful LDK for asynchronous programming is Fork, which duplicate the current control flow, and the child control flow are executed in parallel, similar to the POSIX fork system call.

Dave puts Fork inside a join block, which collects the result of each forked control flow in parallel (Listing 12).

```
import dsl.keywords.Fork
val Urls = Seq(
   new URL("http://ftp.debian.org/debian/README.CD-manufacture"),
   new URL("http://ftp.debian.org/debian/README")
)
def parallelTask: Task[Seq[String]] = Task.join {
   val url: URL = !Fork(Urls)
   !daveHttpClient(url)
}

val Seq(fileContent0, fileContent1) = parallelTask.blockingAwait
fileContent0 should startWith("HTTP/1.1_200_OK")
fileContent1 should startWith("HTTP/1.1_200_OK")
```

Listing 12. Using Dave's http client in parallel

In addition to Fork, we also provide the Each LDK, whose type signature is identical with Fork, to sequentially execute tasks. If Dave replaces the Fork to Each, those URLs will be fetched in sequentially. Other usage of Each LDK will be introduced in Section 2.5.

The Task implemented in *Dsl.scala* is light-weight and faster. See section 4 for the performance benchmark between dsl.task.Task, scala.concurrent.Future, scalaz.concurrent.Task and monix.eval.Task.

2.5 Monadic programming

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Despite LDKs directly implemented in *Dsl.scala*, we also provide some LDKs as adapters to monads and other type classes.

The built-in Monadic LDK can be used as an adapter to scalaz. Monad, to create monadic code from imperative syntax, similar to the !-notation in Idris.

For example, suppose Erin is creating a program that counts lines of code under a directory. She uses the Monadic LDK store the result in a Stream of line count of each file (Listing 13).

```
import java.io.File
import dsl.keywords.Monadic
import dsl.domains.scalaz._
import scalaz.std.stream._
def erinMonadicCounter(file: File): Stream[Int] = Stream {
  if (file.isDirectory) {
    file.listFiles() match {
      case null =>
        // Unable to open `file`
        !Monadic(Stream.empty[Int])
      case children =>
        // Import this implicit conversion to omit the Monadic keyword
        import dsl.keywords.Monadic.implicitMonadic
        val child: File = !children.toStream
        !erinMonadicCounter(child)
    }
  } else {
    scala.io.Source.fromFile(file).getLines.size
  }
}
```

Listing 13. Erin's line of code counter, the monadic version

The previous code requires a toStream conversion on children, because children's type Array[File] does not fit the F type parameter in scalaz. Monad.bind [Yoshida et al. 2017].

There is a Each LDK in *Dsl.scala* to extract each element in a Scala collection, based on CanBuild-From type class instead of monads. The Each behavior is similar to Monadic, except the collection type can vary.

Thus, Erin can extract each element from an Array with the help of Each LDK in Listing 14, even when the enclosing domain is still a Stream.

```
import java.io.File
import dsl.keywords.Monadic, Monadic.implicitMonadic
```

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```
import dsl.keywords.Each
     import dsl.domains.scalaz._
443
     import scalaz.std.stream._
     def erinMixedCounter(file: File): Stream[Int] = Stream {
445
       if (file.isDirectory) {
         file.listFiles() match {
447
           case null =>
449
              // Unable to open `file`
              !Stream.empty[Int]
           case children =>
451
              val child: File = !Each(children)
              !erinMixedCounter(child)
          }
       } else {
455
          scala.io.Source.fromFile(file).getLines.size
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       }
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```

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Listing 14. Erin's line of code counter, mixed Monad-based and CanBuildFrom-based LDKs

As shown the erinMixedCounter, Dsl.scala allows Each and other non-monadic LDKs to work along with monads, which is impossible in Haskell's do-notation or Idris's !-notation.

However, Erin still wants to add one more feature to the LOC counter. Considering the line counter implemented in previous example may be failed for some files, due to permission issue or other IO problem, Erin wants to use an OptionT monad transformer to mark those failed file as a None (Listing 15).

```
468
     import scalaz._
469
     import java.io.File
470
     import dsl.keywords.Monadic, Monadic.implicitMonadic
471
     import dsl.domains.scalaz._
472
     import scalaz.std.stream._
473
     def erinTransformerCounter(file: File): OptionT[Stream, Int] = OptionT.some {
474
       if (file.isDirectory) {
475
          file.listFiles() match {
476
            case null =>
477
              // Unable to open `file`
              !OptionT.none[Stream, Int]
479
            case children =>
480
              val child: File = !Stream(children: _*)
              !erinTransformerCounter(child)
482
          }
483
       } else {
484
          scala.io.Source.fromFile(file).getLines.size
485
       }
486
     }
```

Listing 15. Erin's line of code counter, using an OptionT monad transformer

Note that our LDKs are adaptive to the domain it belongs to. Thus, instead of explicit lifting as !Monadic(OptionT.optionTMonadTrans.liftM(Stream(children: _*))), Erin can simply write !Stream(children: _*). This implicit lifting feature looks like Idris's effect monads [Brady 2013b], though the mechanisms is different from **implicit** lift in Idris.

3 CREATING LIBRARY-DEFINED KEYWORDS

LDKs introduced in Section 2 are optional libraries, activated by common compiler-time CPS-transform rules, which are implemented as a Scala compiler plug-in. In this section, we will present the implementation of some LDKs, and the compiler-time generated code for !-notations written by LDK users.

Dsl.scala ships with a compiler plug-in that supports both nonadaptive LDKs and adapters LDKs. A nonadaptive LDK must belongs to in an exact domain, while an adaptive LDK works in various types of domains.

3.1 Nonadaptive LDKs

 A Nonadaptive LDK is simply a delimited continuation, along with a syntactic unary_! method for !-notation. For example, the Yield LDK described at Section 2.1 can be implemented as shown in Listing 16.

Listing 16. The Yield LDK, the nonadaptive version

Calls to unary_! method will be translated to cpsApply calls by our compiler plug-in. For example, aliceRandomGenerator in Listing 2 will be translated to the code shown in Listing 17 by our compiler plug-in:

```
def aliceRandomGenerator(seed: Int): Stream[Int] = {
  val tmp1 = seed ^ (seed << 13)
  val tmp2 = tmp1 ^ (tmp1 >>> 17)
  val tmp3 = tmp2 ^ (tmp2 << 5)
  Yield(tmp3).cpsApply { _: Unit =>
    aliceRandomGenerator(tmp3)
  }
}
```

Listing 17. The translated code for Alice's pseudo-random number generator

And Listing 4 or Listing 5 will be translated to Listing 18:

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```
import dsl.Dsl.!!
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     def bobLoggingParser(jsonContent: String, defaultValue: JSONType): Stream[
         String] !! JSONType = { (callback: JSONType => Stream[String]) =>
543
       Yield(s"I_am_going_to_parse_the_JSON_text_$jsonContent...").cpsApply { _:
           Unit =>
545
         JSON.parseRaw(jsonContent) match {
           case Some(json) =>
547
              Yield(s"Succeeded_to_parse_$jsonContent").cpsApply { _: Unit =>
                callback(json)
549
              }
           case None =>
              Yield(s"Failed_to_parse_$jsonContent").cpsApply { _: Unit =>
                callback(defaultValue)
553
              }
         }
555
       }
     }
557
```

Listing 18. The translated code for Bob's parser

Our compiler plug-in performs CPS-transform in a similar approach to Scala Continuations [Rompf et al. 2009], with some minor differences.

- (1) Compiler-time instruction reset is not necessary in our implementation, as the boundary of a delimited continuation is by default the enclosing function. Instead, reset can be implemented as an ordinary Scala function shown in Listing 6.
- (2) All return types are kept as is in our implementation, instead of hijacking on the @cps type.
- (3) Our implementation only performs CPS-transform explicitly on the !-notation, instead of implicit conversion between **@**cps type and ordinary type.

Because of (2), CPS-translated function produced by our compiler plug-in always has the same answer type as the return type, which is called the "domain" of a DSL. Even then, our approach still allows explicit answer type by using the underscore trick shown in Listing 5.

3.2 Adaptive LDKs

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587 588 All *Dsl.scala* built-in LDKs are adaptive, which can collaborate with other LDKs. For example, Yield is adaptive, since it works not only in functions that return Stream[_], but also (Stream[_] !! _), (Stream[_] !! _ !! _), etc.

Those LDKs are adaptive because they all extends the **trait** Keyword, which has a ad-hoc polymorphic cpsApply method (Listing 19).

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}

} }

```
dsl.interpret(this, handler)
       }
     }
                            Listing 19. The ad-hoc polymorphism in Keyword
       The functionality of cpsApply is implemented in type class instances of Dsl (Listing 20).
     trait Dsl[Keyword, Domain, Value] {
       def interpret(keyword: Keyword, handler: Value => Domain): Domain
     }
                             Listing 20. The type class to interpret cpsApply
       The adaptive version of Yield LDK ships with a type class instance of Dsl[Yield[Element
     ], Stream[Element], Unit], allowing the !Yield notation in functions that return Stream[
     Element]
     case class Yield[Element](element: Element) extends Keyword[Yield[Element],
     object Yield {
       implicit def yieldDsl[Element]: Dsl[Yield[Element], Stream[Element], Unit] =
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          new Dsl[Yield[Element], Stream[Element], Unit] {
            def interpret(keyword: Yield[Element], mapper: Unit => Stream[Element]):
                Stream[Element] = {
              new Stream.Cons(keyword.element, mapper(()))
```

Listing 21. The Yield LDK, the adaptive version

To make Yield LDK available for another domain, just provide a Dsl type class instance for other types.

Listing 22 shows a Dsl that allows an LDK be available for Domain!!Value as long as the LDK is available for Domain. 1

```
implicit def continuationDsl[Keyword, Domain, Value, KeywordValue](
  implicit restDsl: Dsl[Keyword, Domain, KeywordValue]
): Dsl[Keyword, Domain !! Value, KeywordValue] = {
  new Dsl[Keyword, Domain !! Value, KeywordValue] {
    def interpret(keyword: Keyword, handler: KeywordValue => Domain !! Value):
        Domain !! Value = {
      (continue: Value => Domain) =>
        restDsl.interpret(keyword, { a =>
          handler(a)(continue)
        })
    }
  }
```

¹LDKs is also adaptive to domains other than continuations, such as a heterogeneous list that contains multiple sub-domains.

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}

Listing 22. The Yield LDK, the adaptive version

Therefore, the Yield LDK can be used in (Stream[String] !! JsonType) domain as shown in Listing 6, because the type class Dsl[Yield[String], Stream !! JsonType, Unit] can be implicitly resolved as continuationDsl(yieldDsl).

4 BENCHMARK

We created some benchmarks to evaluate the computational performance of code generated by our compiler plug-in for LDKs, especially, we are interesting how LDKs and other direct style DSL affect the performance in an effect system that support both asynchronous and synchronous effects.

In spite of LDKs of adapters to monads or other effect systems (see Section 2.5), the preferred effect system for LDKs is Task, the type alias of vanilla continuation-passing style function (Listing 23):

```
type !![Domain, Value] = (Value => Domain) => Domain
type TaskDomain = TailRec[Unit] !! Throwable
type Task[Value] = TaskDomain !! Value
```

Listing 23. The definition of Task, the preferred effect system using with LDKs

Our benchmarks measured the performance of LDKs in the Task domain, along with other combination of effect system with direct style DSL, listed in Table 1:

| Effect System | direct style DSL |
|--|-------------------------------------|
| vanilla continuation-passing style functions | LDKs provided by Dsl.scala |
| Scala Future [Haller et al. 2012] | Scala Async [Haller and Zaugg 2013] |
| Scala Continuation library [Rompf et al. 2009] | Scala Continuation compiler plug-in |
| Monix tasks [Nedelcu et al. 2017] | for comprehension |
| Cats effects [Typelevel 2017] | for comprehension |
| Scalaz Concurrent [Yoshida et al. 2017] | for comprehension |

Table 1. The combination of effect system and direct style DSL being benchmarked

4.1 The performance of recursive functions in effect systems

The purpose of the first benchmark is to determine the performance of recursive functions in various effect system, especially when a direct style DSL is used.

- 4.1.1 The performance baseline. In order to measure the performance impact due to direct style DSLs, we have to measure the performance baseline of different effect systems at first. We created some benchmarks for the most efficient implementation of a sum function in each effect system. These benchmarks perform the following computation:
 - Creating a List[X[Int]] of 1000 tasks, where X is the data type of task in the effect system.
 - Performing recursive right-associated "binds" on each element to add the Int to an accumulator, and finally produce a X[Int] as a task of the sum result.
 - Running the task and blocking awaiting the result.

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Note that the tasks in the list is executed in the current thread or in a thread pool. We keep each task returning a simple pure value, because we want to measure the overhead of effect systems, not the task itself.

The "bind" operation means the primitive operation of each effect system. For Monix tasks, Cats effects, Scalaz Concurrent and Scala Continuations library, the "bind" operation is flatMap; for Dsl.scala, the "bind" operation is cpsApply, which may or may not be equivalent to flatMap according to the type of the current domain.

We use the !-notation to perform the cpsApply in Dsl.scala. The !-notation results the exact same Java bytecode to manually passing a callback function to cpsApply (Listing 24).

```
def loop(tasks: List[Task[Int]], accumulator: Int = 0)(callback: Int =>
    TaskDomain): TaskDomain = {
  tasks match {
    case head :: tail =>
      // Expand to: implicitShift(head).cpsApply(i => loop(tail, i +
          accumulator)(callback))
      loop(tail, !head + accumulator)(callback)
    case Nil =>
      callback(accumulator)
  }
}
```

Listing 24. The most efficient implementation of sum based on vanilla CPS function

However, direct style DSLs for other effect systems are not used in favor of raw flatMap calls, in case of decay of the performance. Listing 25 shows the benchmark code for Scala Futures. The code for all the other effect systems are similar to it.

```
def loop(tasks: List[Future[Int]], accumulator: Int = 0): Future[Int] = {
  tasks match {
    case head :: tail =>
      head.flatMap { i =>
        loop(tail, i + accumulator)
    case Nil =>
      Future.successful(accumulator)
  }
```

Listing 25. The most efficient implementation of sum based on Scala Futures

The benchmark result is shown in Table 2 (larger score is better):

The Task alias of continuation-passing style function used with Dsl.scala is quite fast. Dsl.scala, Monix and Cats Effects score on top 3 positions for either tasks running in the current thread or in a thread pool.

The performance impact of direct style DSLs. In this section, we will present the performance impact when different syntax notations are introduced. For vanilla CPS functions, we added

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| Benchmark | executedIn | size | Score, | ops/s |
|--------------------------|----------------|------|-----------|-----------|
| RawSum.cats | thread-pool | 1000 | 799.072 | ± 3.094 |
| RawSum.cats | current-thread | 1000 | 26932.907 | ± 845.715 |
| RawSum.dsl | thread-pool | 1000 | 729.947 | ± 4.359 |
| RawSum.dsl | current-thread | 1000 | 31161.171 | ± 589.935 |
| RawSum.future | thread-pool | 1000 | 575.403 | ± 3.567 |
| RawSum.future | current-thread | 1000 | 876.377 | ± 8.525 |
| RawSum.monix | thread-pool | 1000 | 743.340 | ± 11.314 |
| RawSum.monix | current-thread | 1000 | 55421.452 | ± 251.530 |
| RawSum.scalaContinuation | thread-pool | 1000 | 808.671 | ± 3.917 |
| RawSum.scalaContinuation | current-thread | 1000 | 17391.684 | ± 385.138 |
| RawSum.scalaz | thread-pool | 1000 | 722.743 | ± 11.234 |
| RawSum.scalaz | current-thread | 1000 | 15895.606 | ± 235.992 |

Table 2. The benchmark result of sum for performance baseline

one more !-notation to avoid manually passing the callback in the previous benchmark (Listing 26, 27). For other effect systems, we refactored the previous sum benchmarks to use Scala Async, Scala Continuation's @cps annotations, and for comprehension, respectively (Listing 28, 29, 30, 31, 32, 33).

Listing 26. Left-associated sum based on LDKs of Dsl.scala

```
def loop(tasks: List[Task[Int]], accumulator: Int = 0): Task[Int] = _ {
   tasks match {
    case head :: tail =>
      !loop(tail, !head + accumulator)
    case Nil =>
      accumulator
   }
}
```

Listing 27. Right-associated sum based on LDKs of Dsl.scala

Note that reduced sum can be implemented in either left-associated recursion or right-associated recursion. The above code contains benchmark for both cases. The benchmark result is shown in Table 3, 4:

```
def loop(tasks: List[Future[Int]]): Future[Int] = async {
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        tasks match {
786
          case head :: tail =>
            await(head) + await(loop(tail))
          case Nil =>
        }
791
792
      }
793
                            Listing 28. Left-associated sum based on Scala Async
794
795
796
     def loop(tasks: List[Future[Int]], accumulator: Int = 0): Future[Int] = async {
        tasks match {
798
          case head :: tail =>
            await(loop(tail, await(head) + accumulator))
800
          case Nil =>
            accumulator
802
        }
      }
804
                            Listing 29. Right-associated sum based on Scala Async
805
806
807
     def loop(tasks: List[() => Int @suspendable]): Int @suspendable = {
808
        tasks match {
809
          case head :: tail =>
810
            head() + loop(tail)
811
          case Nil =>
812
813
        }
814
815
                      Listing 30. Left-associated sum based on Scala Continuation plug-in
816
817
818
     def loop(tasks: List[() => Int @suspendable], accumulator: Int = 0): Int @
819
          suspendable = {
820
        tasks match {
821
          case head :: tail =>
822
            loop(tail, head() + accumulator)
823
          case Nil =>
824
            accumulator
825
        }
826
      }
```

Listing 31. Right-associated sum based on Scala Continuation plug-in

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832 833 The result demonstrates that the !-notation provided by *Dsl.scala* is faster than all other direct style DSLs in the right-associated sum benchmark. The *Dsl.scala* version sum consumes a constant

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Listing 32. Left-associated sum based on for comprehension

```
def loop(tasks: List[Task[Int]], accumulator: Int = 0): Task[Int] = {
   tasks match {
     case head :: tail =>
        for {
        i <- head
            r <- loop(tail, i + accumulator)
        } yield r
     case Nil =>
        Task.now(accumulator)
   }
}
```

Listing 33. Right-associated sum based on for comprehension

| Benchmark | executedIn | size | Score, c | ps/s |
|---|----------------|------|-----------|-----------|
| LeftAssociatedSum.cats | thread-pool | 1000 | 707.940 | ± 10.497 |
| LeftAssociatedSum.cats | current-thread | 1000 | 16165.442 | ± 298.072 |
| LeftAssociatedSum.dsl | thread-pool | 1000 | 729.122 | ± 7.492 |
| LeftAssociatedSum.dsl | current-thread | 1000 | 19856.493 | ± 386.225 |
| LeftAssociatedSum.future | thread-pool | 1000 | 339.415 | ±1.486 |
| LeftAssociatedSum.future | current-thread | 1000 | 410.785 | ± 1.535 |
| LeftAssociatedSum.monix | thread-pool | 1000 | 742.836 | ± 9.904 |
| LeftAssociatedSum.monix | current-thread | 1000 | 19976.847 | ± 84.222 |
| Left Associated Sum. scala Continuation | thread-pool | 1000 | 657.721 | ± 9.453 |
| LeftAssociatedSum.scalaContinuation | current-thread | 1000 | 15103.883 | ± 255.780 |
| LeftAssociatedSum.scalaz | thread-pool | 1000 | 670.725 | ± 8.957 |
| LeftAssociatedSum.scalaz | current-thread | 1000 | 5113.980 | ± 110.272 |

Table 3. The benchmark result of left-associated sum in direct style DSLs

number of memory during the loop, because we implemented a tail-call detection in our CPS-transform compiler plug-in, and the Ds1 interpreter for Task use a trampoline technique [Tarditi et al. 1992]. On the other hand, the benchmark result of Monix Tasks, Cats Effects and Scalaz Concurrent

posed a significant performance decay, because they costs O(n) memory due to the map call generated by **for** comprehension, although those effect systems also built in trampolines. In general, the performance of recursive monadic binds in a **for** comprehension is always underoptimized due to the inefficient map.

4.2 The performance of collection manipulation in effect systems

The previous sum benchmarks measured the performance of manually written loops, but usually we may want to use higher-ordered functions to manipulate collections. We want to know how those higher-ordered functions can be expressed in direct style DSLs, and how would the performance be affected by direct style DSLs.

In this section, we will present the benchmark result for computing the Cartesian product of lists.

4.2.1 The performance baseline. As we did in sum benchmarks, we created some benchmarks to maximize the performance for Cartesian product. Our benchmarks create the Cartesian product from traverseM for Scala Future, Cats Effect, Scalaz Concurrent and Monix Tasks. Listing 34 shows the benchmark code for Scala Future.

Scala Async or **for** comprehension is used in element-wise task cellTask, but the collection manipulation listTask is kept as manually written higher order function calls, because neither Scala Async nor **for** comprehension supports traverseM.

The benchmark for *Dsl.scala* is entirely written in LDKs (Listing 35):

The Each LDK is available here because it is adaptive. Each LDK can be used in not only List[_] domain, but also (_ !! Coll[_]) domain as long as Coll is a Scala collection type that supports CanBuildFrom type class.

We didn't benchmark Scala Continuation here because all higher ordered functions for List do not work with Scala Continuation.

The benchmark result is shown in Table 5.

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930 931 Monix tasks, Cats Effects and vanilla CPS functions created from *Dsl.scala* are still the top 3 scored effect systems.

4.2.2 The performance of collection manipulation in direct style DSLs. We then refactored the benchmarks to direct style DSLs. Listing 36 is the code for Scala Future, written in ListT monad

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```
import scala.concurrent.Future
932
     import scalaz.std.list._
933
     import scalaz.std.scalaFuture._
     import scalaz.syntax.all._
935
     def cellTask(taskX: Future[Int], taskY: Future[Int]): Future[List[Int]] = async
937
       List(await(taskX), await(taskY))
939
     }
940
941
     def listTask(rows: List[Future[Int]], columns: List[Future[Int]]): Future[List[
942
         Int]] = {
943
       rows.traverseM { taskX =>
         columns.traverseM { taskY =>
945
           cellTask(taskX, taskY)
         }
947
       }
948
     }
949
```

Listing 34. Cartesian product for Scala Future, based on traverseM

Listing 35. Cartesian product for vanilla CPS functions, based on Dsl.scala

| Benchmark | executedIn | size | Score, | ops/s |
|----------------------------|----------------|------|----------|----------|
| RawCartesianProduct.cats | thread-pool | 50 | 136.415 | ± 1.939 |
| RawCartesianProduct.cats | current-thread | 50 | 1346.874 | ± 7.475 |
| RawCartesianProduct.dsl | thread-pool | 50 | 140.098 | ± 2.062 |
| RawCartesianProduct.dsl | current-thread | 50 | 1580.876 | ± 27.513 |
| RawCartesianProduct.future | thread-pool | 50 | 100.340 | ± 1.894 |
| RawCartesianProduct.future | current-thread | 50 | 93.678 | ± 1.829 |
| RawCartesianProduct.monix | thread-pool | 50 | 142.071 | ± 1.299 |
| RawCartesianProduct.monix | current-thread | 50 | 1750.869 | ± 18.365 |
| RawCartesianProduct.scalaz | thread-pool | 50 | 78.588 | ± 0.623 |
| RawCartesianProduct.scalaz | current-thread | 50 | 357.357 | ± 2.102 |

Table 5. The benchmark result of Cartesian product for performance baseline

Dsl.scala: creating library-defined keywords from ad-hoc polymorphic delimited continuation 21

transformer provided by Scalaz. The benchmarks for Monix tasks, Scalaz Concurrent are also rewritten in the similar style.

```
import _root_.scalaz.syntax.all._
984
      import _root_.scalaz.ListT
985
      import _root_.scalaz.std.scalaFuture._
     def listTask(rows: List[Future[Int]], columns: List[Future[Int]]): Future[List[
988
          Int]] = {
        for {
990
          taskX <- ListT(Future.successful(rows))</pre>
          taskY <- ListT(Future.successful(columns))</pre>
992
          x <- taskX.liftM[ListT]</pre>
          y <- taskY.liftM[ListT]</pre>
994
          r <- ListT(Future.successful(List(x, y)))</pre>
        } yield r
996
      }.run
997
998
```

Listing 36. Cartesian product for Scala Future, based on ListT transformer

With the help of ListT monad transformer, we are able to merge cellTask and listTask into one function in a direct style **for** comprehension, avoiding any manual written callback functions. We also merged cellTask and listTask in the *Dsl.scala* version of benchmark (Listing 37).

```
def listTask: Task[List[Int]] = reset {
   List(!(!Each(inputDslTasks)), !(!Each(inputDslTasks)))
}
```

Listing 37. Cartesian product for vanilla CPS functions, in one function

This time, Cats Effects are not benchmarked due to lack of ListT in Cats. The benchmark result are shown in Table 6.

| Benchmark | executedIn | size | Score, | ops/s |
|-------------------------|----------------|------|----------|----------|
| CartesianProduct.dsl | thread-pool | 50 | 283.450 | ± 3.042 |
| CartesianProduct.dsl | current-thread | 50 | 1884.514 | ± 47.792 |
| CartesianProduct.future | thread-pool | 50 | 91.233 | ± 1.333 |
| CartesianProduct.future | current-thread | 50 | 150.234 | ± 20.396 |
| CartesianProduct.monix | thread-pool | 50 | 28.597 | ± 0.265 |
| CartesianProduct.monix | current-thread | 50 | 120.068 | ± 17.676 |
| CartesianProduct.scalaz | thread-pool | 50 | 31.110 | ± 0.662 |
| CartesianProduct.scalaz | current-thread | 50 | 87.404 | ± 1.734 |

Table 6. The benchmark result of Cartesian product in direct style DSLs

Despite the trivial manual lift calls in **for** comprehension, the monad transformer approach causes terrible computational performance in comparison to manually called traverseM. In contrast, the performance of *Dsl.scala* even got improved when cellTask is inlined into listTask.

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5 DISCUSSION AND CONCLUSION

 This paper presents a novel approach to build embedded DSLs in control flow. The approach is based on three assumptions:

- (1) The return type is the specific domain of a DSL.
- (2) A DSL feature should be adaptive to various domains.
- (3) Native control flow of the meta-language should be supported in a DSL.

By combining of the three assumptions, we defined the concept LDK (Library-Defined Keyword). An LDK is merely an ad-hoc polymorphic delimited continuation, interpreted by a domain-specific type class, as described in Section 3.

But what interesting is that an LDK can be considered as a more general version of monadic bind operation as well. The interpreter of an LDK is a triple parametric Ds1 type class (Listing 20), which contains only one interpret function, whose type signature is $(K, (A \Rightarrow D)) \Rightarrow D$, which is exactly as same as monadic bind operation when K is F[A] and D is F[B]. Thus, the interpreter for Monadic LDK (See section 2.5) can be implemented as a trivial forwarder to the bind operation, as shown in Listing 38. In contrast, the reverse adapter is quite difficult, if not impossible, to be implemented.

```
implicit def monadDsl[F[_], A, B](implicit monad: Monad[F]): Dsl[Monadic[F, A],
    F[B], A] =
new Dsl[Monadic[F, A], F[B], A] {
    def interpret(keyword: Monadic[F, A], handler: A => F[B]): F[B] = {
        monad.bind(keyword.fa)(handler)
    }
}
```

Listing 38. The implementation of interpreter for Monadic LDK

The benchmarks in Section 4 demonstrated that our approach of triple parametric polymorphism improves both the extensibility and computational performance, in comparison to ordinary delimited continuations, monads or other direct style DSLs (Table 7).

| Direct style DSL | Control flow | Extensibility | Performance |
|--|--------------|---------------------------|--------------|
| LDKs provided by Dsl.scala | supported | automatically adapted | good |
| Scala Async | supported | unsupported | good |
| Delimited continuation | supported | unsupported | good |
| for comprehension + monad | unsupported | requires manually lifting | not good |
| transformer | | | |
| Compiler-defined keywords yield, async and await in C#, Python or ECMAScript | supported | unsupported | uncomparable |

Table 7. The comparison of direct style DSLs

The capacity of LDKs is the superset of both monads and ordinary delimited continuations, thus LDKs can be used in various domains as they can be, including asynchronous or parallel programming, lazy stream generation, collection manipulation, resource management, etc. But unlike monads or ordinary delimited continuations, an LDK user can use multiple LDKs for

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REFERENCES

1128

1161

11751176

- Martín Abadi, Paul Barham, Jianmin Chen, Zhifeng Chen, Andy Davis, Jeffrey Dean, Matthieu Devin, Sanjay Ghemawat,
 Geoffrey Irving, Michael Isard, et al. 2016. TensorFlow: A System for Large-Scale Machine Learning.. In OSDI, Vol. 16.
 265–283.
- Kenichi Asai. 2009. On typing delimited continuations: three new solutions to the printf problem. *Higher-Order and Symbolic Computation* 22, 3 (2009), 275–291.
- Edwin Brady. 2013a. Idris, a general-purpose dependently typed programming language: Design and implementation.

 Journal of Functional Programming 23, 5 (2013), 552–593.
- Edwin Brady. 2013b. Programming and reasoning with algebraic effects and dependent types. In *ACM SIGPLAN Notices*, Vol. 48. ACM, 133–144.
- Flavio Brasil. 2017. Monadless: Syntactic sugar for monad composition. http://monadless.io/
- Tom Crockett. 2013. Effectful: A syntax for type-safe effectful computations in Scala. https://github.com/pelotom/effectful
- Olivier Danvy and Andrzej Filinski. 1990. Abstracting control. In *Proceedings of the 1990 ACM conference on LISP and functional programming*. ACM, 151–160.
- Philipp Haller, Aleksandar Prokopec, Heather Miller, Viktor Klang, Roland Kuhn, , and Vojin Jovanovic. 2012. SIP-14 Futures and Promises. (2012). https://docs.scala-lang.org/sips/futures-promises.html
- Philipp Haller and Jason Zaugg. 2013. SIP-22 Async. (2013). http://docs.scala-lang.org/sips/pending/async.html
- Mark P Jones and Luc Duponcheel. 1993. *Composing monads*. Technical Report. Technical Report YALEU/DCS/RR-1004, Department of Computer Science. Yale University.
- S Peyton Jones, John Hughes, Lennart Augustsson, Dave Barton, Brian Boutel, Warren Burton, Joseph Fasel, Kevin Hammond, Ralf Hinze, Paul Hudak, et al. 1998. *Haskell 98 report*. Technical Report. https://www.haskell.org/onlinereport/
- Oleg Kiselyov, Amr Sabry, and Cameron Swords. 2013. Extensible effects: an alternative to monad transformers. In *ACM SIGPLAN Notices*, Vol. 48. ACM, 59–70.
- Lightbend, Inc. 2017. Akka FSM. Lightbend, Inc. https://doc.akka.io/docs/akka/2.5.10/fsm.html
- George Marsaglia et al. 2003. Xorshift RNGs. Journal of Statistical Software 8, 14 (2003), 1-6.
- 1149 Caolan McMahon. 2017. TensorFlow Control Flow. https://www.tensorflow.org/api_guides/python/control_flow_ops
- Alexandru Nedelcu, Sorin Chiprian, Mihai Soloi, Andrei OpriÈŽan, Jisoo Park, Dawid Dworak, Omar Mainegra, Piotr
 GawryÅŻ, A. Alonso Dominguez, Leandro Bolivar, Ryo Fukumuro, Ian McIntosh, Denys Zadorozhnyi, and Oleg Pyzhcov.
 2017. Monix: Asynchronous, Reactive Programming for Scala and Scala.js. https://monix.io/
- Rickard Nilsson. 2015. ScalaCheck: Property-based testing for Scala. (2015). https://www.scalacheck.org/
- Martin Odersky, Philippe Altherr, Vincent Cremet, Burak Emir, Stphane Micheloud, Nikolay Mihaylov, Michel Schinz,
 Erik Stenman, and Matthias Zenger. 2004. *The Scala language specification*. https://www.scala-lang.org/docu/files/
 ScalaReference.pdf
- Dan Piponi. 2008. The Mother of all Monads. (2008). https://www.schoolofhaskell.com/user/dpiponi/ the-mother-of-all-monads
- Tiark Rompf, Ingo Maier, and Martin Odersky. 2009. Implementing first-class polymorphic delimited continuations by a type-directed selective CPS-transform. In *ACM Sigplan Notices*, Vol. 44. ACM, 317–328.
- Yury Selivanov. 2016. PEP 525 Asynchronous Generators. *Python.org* (2016). https://www.python.org/dev/peps/pep-0525/ David Tarditi, Peter Lee, and Anurag Acharya. 1992. No assembly required: Compiling Standard ML to C. *ACM Letters on*
- Twitter, Inc. 2016. Algebird: Abstract Algebra for Scala. Twitter, Inc. https://twitter.github.io/algebird/

Programming Languages and Systems (LOPLAS) 1, 2 (1992), 161-177.

- Typelevel 2017. typelevel/cats: Lightweight, modular, and extensible library for functional programming. Typelevel. https://github.com/typelevel/cats
- Philip Wadler. 1990. Comprehending monads. In *Proceedings of the 1990 ACM conference on LISP and functional programming*.
 ACM, 61–78.
- Philip Wadler. 1992. The essence of functional programming. In *Proceedings of the 19th ACM SIGPLAN-SIGACT symposium* on *Principles of programming languages*. ACM, 1–14.
 - Bo Yang, 2014a. Stateless Future. Shenzhen QiFun Network Corp., LTD. https://github.com/qifun/stateless-future
- Bo Yang. 2014b. Stateless Future Akka. Shenzhen QiFun Network Corp., LTD. https://github.com/qifun/stateless-future-akka
- Bo Yang. 2015. ThoughtWorks Each: A macro library that converts native imperative syntax to scalaz's monadic expressions.
 ThoughtWorks, Inc. https://github.com/ThoughtWorksInc/each
- Bo Yang. 2016. Binding.scala: Reactive data-binding for Scala. ThoughtWorks, Inc. https://github.com/ThoughtWorksInc/Binding.scala
- Kenji Yoshida, Alexey Romanov, Derek Williams, Edward Kmett, Heiko Seeberger, retronym, Mark Hibberd, Nick Partridge, runarorama, Richard Wallace, void, and Tony Morris. 2017. Scalaz: An extension to the core scala library. https://scalaz.github.io/scalaz/