

Replication of : Statistical Arbitrage and High-Frequency Data with an Application to Eurostoxx 50 Equities

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Data Summary

As used in paper

The authors used Euro Stoxx 50 data at both daily and intraday frequencies

- Daily for from 01 Jan 2000 to 17 Nov 2009
- Intraday from 03 Jul 2009 03-07-2009 to 17 Nov 2009 at 5 min, 10 min, 20 min, 30 min, 60 min frequencies

Data was adjusted for dividend payments and splits.

The authors used the intraday data as ‘out of sample’ and the daily for “in sample”.

As obtained by me

From studying the paper it was quite clear that * there is too little data for “out of sample” verification (1 to 10 ratio) * there is an opportunity to further improve the strategy by checking the real demand at the time the signals are triggered (bid/ask, volume, and, in the long run, the limit order book)

As such, I decided to get * minute data for all 50 stocks for 10 years * trades and quotes data for 1-2 years for the 6 pairs of stocks the PCA analysis will select to be accounting for 97% of the variance.

I also excluded “UNIBAIL-RODAMCO” since it is the only one in it’s category so it cannot form a pair as per the paper approach.

For the same reason, included “ESSILOR INTERNATIONAL” even though it was not used by the authors (but it is currently in the index).

In terms of provider I chose TickData.com because they provide tools to convert data for corporate actions (but also because QuantGo.com did not offer access in time).

Potential issues

- Currency: different stocks might be priced in currencies different than EUR : must check individually
 - Not clear if the authors use actual bid/ask spreads or not : on one hand they say “we do not dispose of bid and ask prices” and on the other, they use “minute data” (the tickdata.com definition of “minute data” may not contain bid/asks but just trades only)
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Tactical purchase of data

- the high cost of the data
- the above unknowns
- the fact that the rationale above is not yet verified by Brian

I chose to acquire part of the data for now and acquire more later if indeed Brian considers the approach valid and the potential worthwhile.

If indeed the daily data is enough then may choose to use free daily data from elsewhere.

Overview of data collection approach

- Compare current EURO STOXX 50 index composition and compare with the composition at the time the paper was written
 - Document differences in index composition
 - Decide the selection of stocks to obtain in order to make paper replication as faithful as possible
 - Locate the data (daily and intraday/minute) for the stocks to use
 - Ensure stock is properly identified using Quant Finance and stoxx.com (disambiguate between different symbols used by different exchanges; ended up using ISIN numbers)
 - Check which historical data providers : tickdata.com, quantquote.com, quantgo.com, eoddata.com.
 - Download and verify data
 - If stock data is obtained from different vendors or from different exchanges then convert to EUR (how (question))
 - If data is obtained from different vendors then ensure it is consistent across the various frequencies.
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Paper Summary

Introduction

Argue for the presence of arbitrage profitability in a selection of EuroStoxx 50 equities when using a novel approach combining cointegration at HFT and daily levels, time adaptable beta and a test to select pairs that account for most of the variability in the set of stocks.

Main points

- Pairs grouped by industry sector are sometimes cointegrated and can be traded with pair-trading strategies
- Using a Kalman filter to determine a time adaptable beta is superior to using OLS or DESP
- Using sampling frequencies higher than daily for cointegration tests offers investment characteristics that are more attractive than when using daily data
- Using PCA to subselect pairs which account for most of the variability improves returns

Conclusion Statistical arbitrage at daily frequencies in EuroStoxx 50 is not attractive but testing cointegration at high frequencies, using a time adaptive beta and filtering stocks with maximum variability makes strategies attractive.

Main techniques

1. Group stocks in the Eurostoxx 50 index by industry groups. Within each industry group create pairs of stocks
2. For each pair calculate time adaptive/varying betas using Kalman filters

Note: OLS (ordinary least squares) and DESP (double exponential smoothing prediction) are dropped in favor of Kalman filters.

3. The traditional simple strategy :
 - enter both positions when spread > 2 standard deviations
 - exit both positions when spread returned < 0.5 standard deviations of long term mean

Key finding Results are not attractive

4. Calculate the information ratio of the series

$$AnnualizedInformationRatio = (R/\sigma)\sqrt{Hourstradedperday * 252}$$

5. Obtain the t-stat of the ADF test of the series sampled at daily interval
6. Build a diversified portfolio of 5 pairs with the best indicator value

Key finding An indicator made from a combination of the two above produces information ratios of

- over 3 for high frequencies
- 1.3 for daily frequency

Compares favorably with the performance of Eurostoxx 50 index and the index of Market Neutral Hedge Funds.

7. Calculate the cointegration of pairs using Engle and Granger (chosen vs. the Johansen test due to simplicity and lower variance)

$$Y_t = \beta X_t + \epsilon_t$$

8. Test the hypothesis of positive correlation between the t-stat of the ADF test on the OLS residuals and the out of sample “information ratio” (uses bootstrap); the test is a PCA on a normalized matrix of t-stats from the ADF test for 176 pairs x (5, 10, 20, 30, 60) frequencies

Key finding In sample t-stat at 5min and 10 min frequencies have certain predictive power for the out of sample information ratio.

The first principal component explains 97% of the variation in the data for the overall set of pairs in the index.

9. Use the above indicators to trade the enhanced strategy on the subset of 5 pairs filtered through the PCA test.

Key finding The extra indicators heavily improved the attractiveness of the results for the pairs sampled at the high-frequency intervals.

- Almost all the information ratios are above 2 when traded at high frequencies.
- Average maximum drawdown at high frequencies is 1.58% and 4.26% at daily frequency.
- Average maximum drawdown duration at high frequencies is 22 days at high-frequencies, and 55 days for daily frequency.

Issues and possible improvements

“For daily data, the in-sample period is much longer than the out-of-sample period.” Too little out of sample data.

“For high-frequency data the in- and out-of-sample periods have the same lengths” Data is split just in two sets. Needs more sophisticated cross validation, k-fold validation, etc.

The HFT data used in the paper spans 4 months for Summer and Fall. This makes the results to seasonality of the spread. A solution would be to test with larger out of sample HFT data and seek patterns of seasonality. (“seasonal version of the Ornstein-Uhlenbeck formula”: <https://www.evernote.com/shard/s175/nl/19543423/4ad339f8-c347-43a4-a9c5-04bedd77c3e8>) Additionally, add a momentum component to the strategy to go around the assumption of mean reversion.

Hypothesis Summary

- subject: power of prediction of profitability
- independent variables: prices of the stocks in Euro Stoxx 50
- dependent variables:
- cointegration of pairs created within each industry sector
- variance of the spread between a selection of pairs that account for most of the variance

Misc Formulae

Spread

$$z_t = P_{Y_t} - \beta_t P_{X_t}$$

Half-life

$$Half\ life = -\ln(2)/k$$

O-U equation

$$dz_t = k(\mu - z_t)dt + \sigma dW_t$$

Returns

$$Ret_t = \ln(P_{X_t}/P_{X_{t-1}}) - \ln(P_{Y_t}/P_{Y_{t-1}})$$

References

Blah (see Enders and Granger 1998)

Enders, W., and Granger. 1998. "Unit-Root Tests and Asymmetric Adjustment with an Example Using the Term Structure of Interest Rates." *Journal of Business & Economic Statistics*.