## – Problem Set 1 –

## 1. The following two propositions are given:

A: "It is cold outside."

B: "It is raining outside.".

Write the following compound propositions in natural language:  $(a) \neg A$ ,  $(b) A \wedge B$ ,

(c)  $A \vee B$ , (d)  $B \vee \neg A$ .

## 2. The following two propositions are given:

A: "Janez is rich."

B "Janez is happy."

Write the following propositions symbolically:

- (a) If Janez is rich, then he is unhappy.
- (b) Janez is neither happy nor rich.
- (c) Janez is happy only if he is poor.
- (d) Janez is poor if and only if he is unhappy.

## 3. Find truth tables for the examples from the previous task.

- 4. Solve the following problems about knights and servants (knights are always telling the truth, while servants always lie):
  - (i) Artur: It is not true that Cene is a servant.

Bine: Cene is a knight or I am a knight.

Cene: Bine is a servant.

For each of them determine whether they are knights or servants!

(ii) Artur: Cene is a servant or Bine is a servant.

Bine: Cene is a knight and Artur is a knight.

For each of them determine whether they are knights or servants!

Rešitev. Označimo: A – Arthur je vitez, B – Bine je vitez, C – Cene je vitez.

(i) Velja naslednja sestavljena izjava

$$(A \Leftrightarrow C) \land (B \Leftrightarrow C \lor B) \land (C \Leftrightarrow \neg B).$$

S pomočjo pravilnostne tabele vidimo, da je izjava pravilna le za nabor A=1 in B=C=0.

(ii) Velja naslednja sestavljena izjava

$$(A \Leftrightarrow \neg C \vee \neg B) \wedge (B \Leftrightarrow C \wedge A).$$

S pomočjo pravilnostne tabele vidimo, da je izjava pravilna le za nabor A=1 in B=C=0.

- 5. Using basic connectives  $\neg$  and  $\land$  express the following compound propositions:
  - (i)  $A \vee B$
  - (ii)  $A \Rightarrow B$
  - (iii)  $A \Leftrightarrow B$
- 6. Verify the validity of the following equivalences:
  - (i)  $A \land (B \lor C) \Leftrightarrow \neg(A \land B) \Rightarrow (A \land C)$
  - (ii)  $\neg A \land (A \Rightarrow B) \Leftrightarrow A \Rightarrow \neg A \land B$
  - (iii)  $A \lor B \lor C \Leftrightarrow \neg(A \lor B) \Rightarrow C$
  - (iv)  $(A \Rightarrow B) \land (B \Rightarrow A) \Leftrightarrow (A \land B) \lor (\neg A \land \neg B)$