



# ML - PM mid2. exe:

1. Decision trees.

200:  $p(T) = \frac{4}{5} = 0.8$   
 $p(F) = \frac{1}{5} = 0.2$

201:  $p(T) = \frac{5}{20} \cdot \frac{3}{8} + \frac{15}{20} \cdot \frac{8}{15} = 0.15 + 0.25 = 0.44$

$p(F) = \frac{5}{20} \cdot \frac{2}{8} + \frac{15}{20} \cdot \frac{8}{15} = 0.1 + 0.46 = 0.56$

202:  $p(T) = \frac{15}{15} \cdot \frac{5}{15} + \frac{2}{15} \cdot 1 = 0.33 + 0.13 = 0.46$

$p(F) = \frac{15}{15} \cdot \frac{3}{15} + \frac{2}{15} \cdot 0 = 0.53$

Using Decision Rules (PRISM)

2. IF (Att<sub>2</sub> = n) AND (Att<sub>4</sub> = 0) AND (Att<sub>3</sub> = -) THEN T

we do not count the row containing the values, delete it.

choose biggest → Att<sub>2</sub>(n): [3/5] ~ 0.6 ✓

Att<sub>2</sub>(y): [1/5] ~ 0.2

Att<sub>3</sub>(+): [3/6] ~ 0.5

Att<sub>3</sub>(-): [1/4] ~ 0.25

Att<sub>4</sub>(x): [2/5] ~ 0.4

Att<sub>4</sub>(0): [2/5] ~ 0.4

Total: 4/10

number of class = T

consider rows that have Att<sub>2</sub> = n

Att<sub>3</sub> = + [2/3]

Att<sub>3</sub> = - [1/2]

Att<sub>4</sub> = x [1/2]

Att<sub>4</sub> = 0 [2/3]

Total: 3/5

number of rows where class = T

for Att<sub>3</sub> = +

Att<sub>4</sub> = x [0/0]

Att<sub>4</sub> = 0 [2/3]

number of rows with Att<sub>4</sub> = 0 & class = T

3. IF (Att<sub>2</sub> = n) AND (Att<sub>3</sub> = +) AND (Att<sub>4</sub> = 0) THEN T

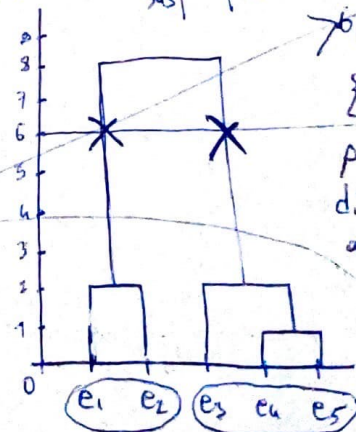
1	2	3	4	5
1	0	2	7	8
2		0	5	6
3			0	1
4				0
5				0

1	2	3	4	5
1	0	2	7	8
2		0	5	6
3			0	1
4				0
5				0

1	2	3	4	5
1	0	2	7	8
2		0	5	6
3			0	1
4				0
5				0

1	2	3	4	5
1	0	2	7	8
2		0	5	6
3			0	1
4				0
5				0

2 groups:



pick biggest distance, as at the end of this arrow

using:

- hierarchical agglomerative
- manhattan distance
- complete linkage (when joining, take the biggest distance)
- if using single linkage, take smallest distance



10	441	2	3	4
200	<del>200</del>	-	-	-

if att<sub>1</sub>, att<sub>2</sub>, att<sub>3</sub> are different for every id for 300, write 1, else 0, you get:

Big table	$\sqrt{0^2 + 1^2 + 1^2 + 0^2} = \sqrt{2}$
2004.401	$\sqrt{1} = 1 \leftarrow$
2015.735	$\sqrt{0} \leftarrow$
2020.000	$\sqrt{1} = 1 \leftarrow$
2019.188	$\sqrt{0} \leftarrow$

find average  
we pick a smallest because our  $k = 4$ .  
this is if the class? or attribute are nominal. If they are numeric, pick most dominant id.

$$\frac{2004.401 + 2015.735 + 2020 + 2019.188}{4} = 2014.83275$$

- we divide by the number of closest neighbours, not with  $k$ .
- if attribute from small table has the same value for attribute from big table, then 0, 1 otherwise. ex:

ID	Att <sub>1</sub>	Att <sub>2</sub>	Att <sub>3</sub>	Att <sub>4</sub>	Class
110	2008.7	(Y)	(-)	(0)	F
300		(A)	(+)	(0)	T

$\sqrt{1^2 + 1^2 + 0^2 + 1^2} = \sqrt{3}$

c)  $\{A, B, P\}$ : minimum confidence = 0.8 (80%)

$$A \rightarrow BP: \frac{2}{3} = 0.6$$

$$B \rightarrow AP: \frac{3}{3} = 1 \checkmark$$

$$P \rightarrow AB: \frac{3}{4} = 0.75$$

$$BP \rightarrow A: \frac{3}{3} = 1 \checkmark$$

$$AP \rightarrow B: \frac{3}{4} = 0.75$$

$$AB \rightarrow P: \frac{2}{3} = 0.6 \checkmark$$

$$\text{confidence}(A \rightarrow BP) = \frac{\sigma(\{A, B, P\})}{\sigma(\{A\})}$$

upper part is how many items have all A, B, P attributes, and lower part is number of occurrences of the set left of the arrow.

TID	Products
22149	A, B, C, L, P, Q, U, X
33277	A, B, C, P, R, X
44305	A, C, T, V, X
57473	A, P, V, X
58511	A, B, P, V, X

⑤ Association rules.

a)  $k$ -itemsets, minimum support 60% = 0.6

1-itemsets	2-itemsets	3-itemsets
A	AB, BE, EV	ABE, ACV, BCP, BVX
B	AB, BP, CX	ABP, ACX, BCP, CPV
C	AP, BV, PX	ABV, APV, BCP, CPX
	AV, DX, PX	ABX, APX, BCP, CPX
	AX, EP, VX	ACP, AVX, BCP, CPX
6	9	5

4-itemsets

BPCX  
APCX  
ABCX  
ADPE  
ADPX

$$6 + 9 + 5 + 1 = 21 \text{ itemsets}$$

$$6 \cdot 0 + 9 \cdot 2 + 5 \cdot 6 + 1 \cdot 19 = 62 \text{ associated rules}$$

2 to the power of which itemset

multiply number of  $k$ -itemsets, we got above 6 for 1-itemset, 9 for 2-itemset, with 2 to the power of  $k$ .

we multiply 6 with 0 because  $2^1 - 2 = 0$ , 9 with two because  $2^2 - 2 = 2$ .

$$d) \text{Lift}(A \rightarrow BP) = \frac{\text{conf.}(A \rightarrow BP)}{\sigma(\{B, P\})}$$

$$B \rightarrow AP: \frac{1/4}{3/4} = \frac{1}{3} = 1.25 \checkmark (\{B, P\})$$

$$BP \rightarrow A: \frac{1/3}{1} = 1$$

$$AB \rightarrow P: \frac{1/4}{2/4} = \frac{1}{2} = 1.25 \checkmark$$

"enough" = lift > 1