

We introduce the structure constants of  $sl_2$   
We show the Killing-Cartan metric

```
-8.00 0.00 0.00
0.00 8.00 0.00
0.00 0.00 8.00
```

and its determinant  
-512.0

In what follows we expand  $sl_2$  with all the abelian semigroups of order 2  
and identify the ones that leads to a semisimple algebra

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A semisimple algebra has been found, expanding with the semigroup #2

1 1

1 2

The metric of the expanded algebra is:

```
-8.00 -8.00 0.00 0.00 0.00 0.00
-8.00 -16.00 0.00 0.00 0.00 0.00
0.00 0.00 8.00 8.00 0.00 0.00
0.00 0.00 8.00 16.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00
0.00 0.00 0.00 0.00 8.00 16.00
```

whose determinant is: 262144.0

\*\*\*\*\*

A semisimple algebra has been found, expanding with the semigroup #4

1 2

2 1

The metric of the expanded algebra is:

```
-16.00 0.00 0.00 0.00 0.00 0.00
0.00 -16.00 0.00 0.00 0.00 0.00
0.00 0.00 16.00 0.00 0.00 0.00
0.00 0.00 0.00 16.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 16.00
```

whose determinant is: 1.6777216E7

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There are 3 commutative semigroups of order 2  
And 2 expansions that give a semisimple algebra