

We introduce the structure constants of sl2  
We show the Killing-Cartan metric

```
-8.00 0.00 0.00
0.00 8.00 0.00
0.00 0.00 8.00
```

and its determinant  
-512.0

In what follows we expand sl2 with all the abelian semigroups of order 5 having zero element and a resonance; and identify the ones that leads to a semisimple algebra.

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A semisimple algebra has been found, expanding with the semigroup #770

```
1 1 1 1 1
1 2 1 1 5
1 1 3 4 1
1 1 4 3 1
1 5 1 1 2
```

which has the zero element 1 and the resonance:

S0: 1 2 3

S1: 1 4 5

The metric of the reduction of the resonant subalgebra is:

```
-8.00 0.00 0.00 0.00 0.00 0.00
0.00 -8.00 0.00 0.00 0.00 0.00
0.00 0.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00
```

and its determinant  
262144.0

\*\*\*\*\*

A semisimple algebra has been found, expanding with the semigroup #779

```
1 1 1 1 1
1 2 1 2 2
1 1 3 3 3
1 2 3 4 5
1 2 3 5 4
```

which has the zero element 1 and the resonance:

S0: 1 2 3 4

S1: 1 2 3 5

The metric of the reduction of the resonant subalgebra is:

```
-8.00 0.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 0.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 8.00 24.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00
```

0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 24.00

and its determinant

-1.34217728E8

\*\*\*\*\*

A semisimple algebra has been found, expanding with the semigroup #922

1 1 1 1 1

1 2 2 2 2

1 2 3 3 3

1 2 3 4 5

1 2 3 5 4

which has the zero element 1 and the resonance:

S0: 1 2 3 4

S1: 1 2 3 5

The metric of the reduction of the resonant subalgebra is:

-8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00  
-8.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00  
-8.00 -16.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00  
0.00 0.00 0.00 8.00 8.00 8.00 0.00 0.00 0.00  
0.00 0.00 0.00 8.00 16.00 16.00 0.00 0.00 0.00  
0.00 0.00 0.00 8.00 16.00 24.00 0.00 0.00 0.00  
0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00  
0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00  
0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00

and its determinant

-1.34217728E8

\*\*\*\*\*

A semisimple algebra has been found, expanding with the semigroup #968

1 1 1 1 1

1 2 2 4 4

1 2 3 4 5

1 4 4 2 2

1 4 5 2 3

which has the zero element 1 and the resonance:

S0: 1 2 3

S1: 1 4 5

The metric of the reduction of the resonant subalgebra is:

-8.00 -8.00 0.00 0.00 0.00 0.00  
-8.00 -16.00 0.00 0.00 0.00 0.00  
0.00 0.00 8.00 8.00 0.00 0.00  
0.00 0.00 8.00 16.00 0.00 0.00  
0.00 0.00 0.00 0.00 8.00 8.00  
0.00 0.00 0.00 0.00 8.00 16.00

and its determinant

262144.0

\*\*\*\*\*

A semisimple algebra has been found, expanding with the semigroup #990

1 1 1 1 1

1 2 3 4 5

1 3 2 5 4

1 4 5 2 3

1 5 4 3 2

which has the zero element 1 and the resonance:

S0: 1 2 5

S1: 1 3 4

The metric of the reduction of the resonant subalgebra is:

```
-16.00 0.00 0.00 0.00 0.00 0.00
0.00 -16.00 0.00 0.00 0.00 0.00
0.00 0.00 16.00 0.00 0.00 0.00
0.00 0.00 0.00 16.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 16.00
```

and its determinant

1.6777216E7

\*\*\*\*\*

A semisimple algebra has been found, expanding with the semigroup #991

1 1 1 1 1

1 2 3 4 5

1 3 2 5 4

1 4 5 3 2

1 5 4 2 3

which has the zero element 1 and the resonance:

S0: 1 2 3

S1: 1 4 5

The metric of the reduction of the resonant subalgebra is:

```
-16.00 0.00 0.00 0.00 0.00 0.00
0.00 -16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 16.00 0.00 0.00
0.00 0.00 16.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 16.00
0.00 0.00 0.00 0.00 16.00 0.00
```

and its determinant

1.6777216E7

\*\*\*\*\*

There are 204 semigroups of order 5 with zero element and at least one resonant decomposition.

In total, there are 1295 different resonant decompositions.

And 6 of them leads to a semisimple algebra.

There are 0 semigroups with zero element, having more than one resonance and leading to semisimple algebras with all those resonances.