

We introduce the structure constants of sl2
We show the Killing-Cartan metric

```
-8.00 0.00 0.00
0.00 8.00 0.00
0.00 0.00 8.00
```

and its determinant
-512.0

In what follows we expand sl2 with all the abelian semigroups of order 6 having
a resonance; and identify the ones that leads to a semisimple algebra.

A semisimple algebra has been found, expanding with the semigroup #12097

```
1 1 1 1 1 1
1 2 1 1 1 6
1 1 3 3 3 1
1 1 3 4 5 1
1 1 3 5 4 1
1 6 1 1 1 2
```

whith the resonance:

S0: 1 2 3 4

S1: 1 3 5 6

The metric of the reduction of the resonant subalgebra is:

```
-8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -16.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 24.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 8.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 16.00
```

and its determinant
6.8719476736E10

A semisimple algebra has been found, expanding with the semigroup #12151

```
1 1 1 1 1 1
1 2 1 1 2 2
1 1 3 1 3 3
1 1 1 4 4 4
1 2 3 4 5 6
1 2 3 4 6 5
```

whith the resonance:

S0: 1 2 3 4 5

S1: 1 2 3 4 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -8.00 -8.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -16.00 -8.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -8.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -16.00 -40.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 8.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 8.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 16.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00 40.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 8.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 8.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00 40.00

```

and its determinant

-3.5184372088832E13

A semisimple algebra has been found, expanding with the semigroup #12218

```

1 1 1 1 1 1
1 2 1 1 2 2
1 1 3 3 3 3
1 1 3 4 4 4
1 2 3 4 5 6
1 2 3 4 6 5

```

whith the resonance:

S0: 1 2 3 4 5

S1: 1 2 3 4 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -8.00 -8.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -16.00 -24.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -24.00 -40.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 8.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 24.00 24.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 24.00 40.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 8.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 24.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 24.00 40.00

```

and its determinant

-3.5184372088832E13

A semisimple algebra has been found, expanding with the semigroup #12262

```

1 1 1 1 1 1
1 2 1 1 2 2
1 1 3 4 3 4
1 1 4 3 4 3
1 2 3 4 5 6
1 2 4 3 6 5

```

whith the resonance:

S0: 1 2 3 5

S1: 1 2 4 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -8.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 8.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 16.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00

```

and its determinant

6.8719476736E10

A semisimple algebra has been found, expanding with the semigroup #12400

```

1 1 1 1 1 1
1 2 1 2 2 2
1 1 3 3 3 3
1 2 3 4 4 4
1 2 3 4 5 6
1 2 3 4 6 5

```

whith the resonance:

S0: 1 2 3 4 5

S1: 1 2 3 4 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -8.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -32.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -32.00 -40.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 16.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00 32.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00 40.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00 32.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00 40.00

```

and its determinant

-3.5184372088832E13

A semisimple algebra has been found, expanding with the semigroup #13679

```

1 1 1 1 1 1
1 2 2 2 2 2
1 2 3 2 2 6
1 2 2 4 5 2
1 2 2 5 4 2
1 2 6 2 2 3

```

whith the resonance:

S0: 1 2 3 4

S1: 1 2 5 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -24.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 24.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 24.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 24.00

```

and its determinant

6.8719476736E10

A semisimple algebra has been found, expanding with the semigroup #13688

```

1 1 1 1 1 1
1 2 2 2 2 2
1 2 3 2 3 3
1 2 2 4 4 4
1 2 3 4 5 6
1 2 3 4 6 5

```

whith the resonance:

S0: 1 2 3 4 5

S1: 1 2 3 4 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -24.00 -16.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -24.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -24.00 -24.00 -40.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 16.00 24.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 24.00 24.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 24.00 40.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 16.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 24.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 24.00 40.00

```

and its determinant

-3.5184372088832E13

A semisimple algebra has been found, expanding with the semigroup #13831

```

1 1 1 1 1 1
1 2 2 2 2 2
1 2 3 3 3 3
1 2 3 4 4 4
1 2 3 4 5 6
1 2 3 4 6 5

```

whith the resonance:

S0: 1 2 3 4 5

S1: 1 2 3 4 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -24.00 -24.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -24.00 -32.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -24.00 -32.00 -40.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 24.00 24.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 32.00 32.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 32.00 40.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 24.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 32.00 32.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 32.00 40.00

```

and its determinant

-3.5184372088832E13

A semisimple algebra has been found, expanding with the semigroup #13877

1 1 1 1 1 1

1 2 2 2 2 2

1 2 3 3 5 5

1 2 3 4 5 6

1 2 5 5 3 3

1 2 5 6 3 4

with the resonance:

S0: 1 2 3 4

S1: 1 2 5 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -24.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -24.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 24.00 24.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 24.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 32.00

```

and its determinant

6.8719476736E10

A semisimple algebra has been found, expanding with the semigroup #13899

1 1 1 1 1 1

1 2 2 2 2 2

1 2 3 4 5 6

1 2 4 3 6 5

1 2 5 6 3 4

1 2 6 5 4 3

with the resonance:

S0: 1 2 3 6

S1: 1 2 4 5

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -32.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 32.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 32.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00

```

and its determinant

4.398046511104E12

A semisimple algebra has been found, expanding with the semigroup #13900

```

1 1 1 1 1 1
1 2 2 2 2 2
1 2 3 4 5 6
1 2 4 3 6 5
1 2 5 6 4 3
1 2 6 5 3 4

```

whith the resonance:

S0: 1 2 3 4

S1: 1 2 5 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -32.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 32.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 32.00 16.00

```

and its determinant

4.398046511104E12

A semisimple algebra has been found, expanding with the semigroup #14212

```

1 1 1 1 1 1
1 2 2 2 5 6
1 2 3 4 5 6
1 2 4 3 5 6
1 5 5 5 6 2
1 6 6 6 2 5

```

whith the resonance:

S0: 1 2 3 5 6

S1: 1 2 4 5 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -32.00 -32.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -32.00 -40.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -8.00 -8.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -8.00 -32.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 32.00 32.00 8.00 8.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 32.00 40.00 8.00 8.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 32.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 32.00 8.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 32.00 32.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 32.00 40.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00 32.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 32.00 8.00

```

and its determinant

6.9253399582448026E17

A semisimple algebra has been found, expanding with the semigroup #14815

```

1 1 1 1 1 6
1 2 1 1 5 6
1 1 3 4 1 6
1 1 4 3 1 6
1 5 1 1 2 6
6 6 6 6 6 1

```

with the resonance:

S0: 1 2 3 6

S1: 1 4 5 6

The metric of the reduction of the resonant subalgebra is:

```

-16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-16.00 -24.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-16.00 -16.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 24.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 16.00 24.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 24.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 24.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00

```

and its determinant

4.398046511104E12

A semisimple algebra has been found, expanding with the semigroup #14937

```

1 1 1 1 1 6
1 2 2 4 4 6
1 2 3 4 5 6
1 4 4 2 2 6
1 4 5 2 3 6
6 6 6 6 6 1

```

with the resonance:

S0: 1 2 3 6

S1: 1 4 5 6

The metric of the reduction of the resonant subalgebra is:

```

-16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-16.00 -24.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-16.00 -24.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 24.00 24.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 24.00 32.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 24.00 24.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 24.00 32.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00

```

and its determinant

4.398046511104E12

A semisimple algebra has been found, expanding with the semigroup #14944

```

1 1 1 1 1 6
1 2 3 4 5 6
1 3 2 5 4 6
1 4 5 2 3 6
1 5 4 3 2 6
6 6 6 6 6 1

```

whith the resonance:

S0: 1 2 5 6

S1: 1 3 4 6

The metric of the reduction of the resonant subalgebra is:

```

-16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-16.00 -32.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-16.00 -16.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 32.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 16.00 32.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 32.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 32.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00

```

and its determinant

2.81474976710656E14

A semisimple algebra has been found, expanding with the semigroup #14945

```

1 1 1 1 1 6
1 2 3 4 5 6
1 3 2 5 4 6
1 4 5 3 2 6
1 5 4 2 3 6
6 6 6 6 6 1

```

whith the resonance:

S0: 1 2 3 6

S1: 1 4 5 6

The metric of the reduction of the resonant subalgebra is:


```

-16.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-16.00 -32.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-16.00 -16.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 16.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 16.00 32.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 32.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 32.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 32.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00

```

and its determinant

2.81474976710656E14

A semisimple algebra has been found, expanding with the semigroup #15448

1 1 1 1 5 6

1 2 2 2 5 6

1 2 3 4 5 6

1 2 4 3 5 6

5 5 5 5 6 1

6 6 6 6 1 5

with the resonance:

S0: 1 2 3 5 6

S1: 1 2 4 5 6

The metric of the reduction of the resonant subalgebra is:

```

-24.00 -24.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-24.00 -32.00 -32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-24.00 -32.00 -40.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 24.00 24.00 24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 24.00 32.00 32.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 24.00 32.00 40.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00 24.00 24.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00 32.00 32.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00 32.00 40.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00 0.00

```

and its determinant

6.9253399582448026E17

A semisimple algebra has been found, expanding with the semigroup #15619

1 1 1 4 4 4

1 2 1 4 4 6

1 1 3 4 5 4

4 4 4 1 1 1

4 4 5 1 3 1

4 6 4 1 1 2

with the resonance:

S0: 1 2 3

S1: 4 5 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 8.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 16.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 8.00 16.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00

```

and its determinant

-1.34217728E8

A semisimple algebra has been found, expanding with the semigroup #15696

```

1 1 1 4 4 4
1 2 2 4 5 5
1 2 3 4 5 6
4 4 4 1 1 1
4 5 5 1 2 2
4 5 6 1 2 3

```

whith the resonance:

S0: 1 2 3

S1: 4 5 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 8.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 16.00 16.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 16.00 24.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00

```

and its determinant

-1.34217728E8

A semisimple algebra has been found, expanding with the semigroup #15725

```

1 1 1 4 4 4
1 2 3 4 5 6
1 3 2 4 6 5
4 4 4 1 1 1
4 5 6 1 2 3
4 6 5 1 3 2

```

whith the resonance:

S0: 1 2 3

S1: 4 5 6

The metric of the reduction of the resonant subalgebra is:

```

-8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -24.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 8.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 24.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 8.00 24.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 24.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 24.00

```

and its determinant

-8.589934592E9

A semisimple algebra has been found, expanding with the semigroup #15726

1 1 1 4 4 4

1 2 3 4 5 6

1 3 2 4 6 5

4 4 4 1 1 1

4 5 6 1 3 2

4 6 5 1 2 3

whith the resonance:

S0: 1 2 3

S1: 4 5 6

The metric of the reduction of the resonant subalgebra is:

```
-8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -24.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -8.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 8.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 8.00 24.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 24.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 24.00 8.00
```

and its determinant

-8.589934592E9

A semisimple algebra has been found, expanding with the semigroup #15947

1 1 3 3 5 6

1 2 3 4 5 6

3 3 1 1 6 5

3 4 1 2 6 5

5 5 6 6 1 3

6 6 5 5 3 1

whith the resonance:

S0: 1 2 6

S1: 3 4 5

The metric of the reduction of the resonant subalgebra is:

```
-16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
-16.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 16.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 16.00 24.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 16.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 16.00 24.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00
```

and its determinant

-8.589934592E9

A semisimple algebra has been found, expanding with the semigroup #15972

1 2 3 4 5 6

2 1 4 3 6 5

3 4 5 6 1 2

4 3 6 5 2 1

5 6 1 2 3 4

6 5 2 1 4 3

whith the resonance:

S0: 1 3 5

S1: 2 4 6

The metric of the reduction of the resonant subalgebra is:

```
-24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 24.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 24.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 24.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 24.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00 0.00
```

and its determinant

2.641807540224E12

There are 2059 semigroups of order 6 at least one resonant decomposition.

In total, there are 25512 different resonant decompositions.

And 23 of them leads to a semisimple algebra.

There are 0 semigroups having more than one resonance and
leading to semisimple algebras with all those resonances.