

We introduce the structure constants of sl2  
We show the Killing-Cartan metric

```
-8.00 0.00 0.00
0.00 8.00 0.00
0.00 0.00 8.00
```

and its determinant  
-512.0

In what follows we expand sl2 with all the abelian semigroups of order 4 having  
a resonance; and identify the ones that leads to a semisimple algebra.

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A semisimple algebra has been found, expanding with the semigroup #88

```
1 1 1 1
1 2 2 2
1 2 3 4
1 2 4 3
```

whith the resonance:

S0: 1 2 3

S1: 1 2 4

The metric of the reduction of the resonant subalgebra is:

```
-8.00 -8.00 -8.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -16.00 0.00 0.00 0.00 0.00 0.00 0.00
-8.00 -16.00 -24.00 0.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 8.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 16.00 16.00 0.00 0.00 0.00
0.00 0.00 0.00 8.00 16.00 24.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00
```

and its determinant

-1.34217728E8

\*\*\*\*\*

A semisimple algebra has been found, expanding with the semigroup #118

```
1 1 3 3
1 2 3 4
3 3 1 1
3 4 1 2
```

whith the resonance:

S0: 1 2

S1: 3 4

The metric of the reduction of the resonant subalgebra is:

```
-8.00 -8.00 0.00 0.00 0.00 0.00
-8.00 -16.00 0.00 0.00 0.00 0.00
0.00 0.00 8.00 8.00 0.00 0.00
0.00 0.00 8.00 16.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00
0.00 0.00 0.00 0.00 8.00 16.00
```

and its determinant

262144.0

\*\*\*\*\*

A semisimple algebra has been found, expanding with the semigroup #125

1 2 3 4

2 1 4 3

3 4 1 2

4 3 2 1

whith the resonance:

S0: 1 4

S1: 2 3

The metric of the reduction of the resonant subalgebra is:

```
-16.00 0.00 0.00 0.00 0.00 0.00
0.00 -16.00 0.00 0.00 0.00 0.00
0.00 0.00 16.00 0.00 0.00 0.00
0.00 0.00 0.00 16.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 16.00
```

and its determinant

1.6777216E7

\*\*\*\*\*

A semisimple algebra has been found, expanding with the semigroup #126

1 2 3 4

2 1 4 3

3 4 2 1

4 3 1 2

whith the resonance:

S0: 1 2

S1: 3 4

The metric of the reduction of the resonant subalgebra is:

```
-16.00 0.00 0.00 0.00 0.00 0.00
0.00 -16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 16.00 0.00 0.00
0.00 0.00 16.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 16.00
0.00 0.00 0.00 0.00 16.00 0.00
```

and its determinant

1.6777216E7

\*\*\*\*\*

There are 48 semigroups of order 4 at least one resonant decomposition.

In total, there are 124 different resonant decompositions.

And 4 of them leads to a semisimple algebra.

There are 0 semigroups having more than one resonance and  
leading to semisimple algebras with all those resonances.