```
We introduce the structure constants of sl2
We show the Killing-Cartan metric
 -8.00 0.00 0.00
0.00 8.00 0.00
0.00 0.00 8.00
and its determinant
-512.0
In what follows we expand sl2 with all the abelian semigroups of order 5 having
zero element and identify the ones that leads to a semisimple algebra.
A semisimple algebra has been found, expanding with the semigroup #680
1 1 1 1 1
1 1 3 1 1
11141
1 1 1 1 5
whose zero element is: 1.
The metric of the reduced algebra is:
0.00\ 0.00\ -8.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00\ 0.00\ 0.00\ -8.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00 0.00 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00
and its determinant
6.8719476736E10
A semisimple algebra has been found, expanding with the semigroup #683
1 1 1 1 1
1 2 1 1 1
1 1 3 1 1
1 1 1 4 4
1 1 1 4 5
whose zero element is: 1.
The metric of the reduced algebra is:
0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 16.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00
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and its determinant

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*******
A semisimple algebra has been found, expanding with the semigroup #685
1 1 1 1 1
1 2 1 1 1
1 1 3 1 1
1 1 1 4 5
1 1 1 5 4
whose zero element is: 1.
The metric of the reduced algebra is:
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00
and its determinant
4.398046511104E12
******
A semisimple algebra has been found, expanding with the semigroup #689
1 1 1 1 1
1 2 1 1 1
1 1 3 1 3
1 1 1 4 4
1 1 3 4 5
whose zero element is: 1.
The metric of the reduced algebra is:
0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 8.00 0.00 8.00 0.00 0.00 0.00 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 24.00 0.00 0.00 0.00 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 24.00
and its determinant
6.8719476736E10
A semisimple algebra has been found, expanding with the semigroup #704
1 2 1 1 1
1 1 3 3 3
1 1 3 4 3
1 1 3 3 5
whose zero element is: 1.
The metric of the reduced algebra is:
```

6.8719476736E10

```
0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00
and its determinant
6.8719476736F10
A semisimple algebra has been found, expanding with the semigroup #707
1 1 1 1 1
1 2 1 1 1
1 1 3 3 3
1 1 3 4 4
1 1 3 4 5
whose zero element is: 1.
The metric of the reduced algebra is:
0.00 \ -8.00 \ -16.00 \ -16.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00
and its determinant
6.8719476736E10
A semisimple algebra has been found, expanding with the semigroup #709
1 2 1 1 1
1 1 3 3 3
1 1 3 4 5
1 1 3 5 4
whose zero element is: 1.
The metric of the reduced algebra is:
0.00 \ -8.00 \ -24.00 \ -8.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00
0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 8.00 24.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 8.00 24.00 0.00 0.00 0.00 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 24.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 24.00
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and its determinant
4.398046511104F12
******
A semisimple algebra has been found, expanding with the semigroup #714
1 1 1 1 1
1 2 1 1 1
1 1 3 3 5
1 1 3 4 5
1 1 5 5 3
whose zero element is: 1.
The metric of the reduced algebra is:
0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 16.00 24.00 0.00 0.00 0.00 0.00 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 24.00 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 16.00
and its determinant
4.398046511104E12
A semisimple algebra has been found, expanding with the semigroup #722
1 2 1 1 1
1 1 3 4 5
1 1 4 5 3
11534
whose zero element is: 1.
The metric of the reduced algebra is:
0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00 0.00
and its determinant
-1.352605460594688E15
A semisimple algebra has been found, expanding with the semigroup #734
1 1 1 1 1
1 2 1 1 2
1 1 3 1 3
1 1 1 4 4
1 2 3 4 5
whose zero element is: 1.
```

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The metric of the reduced algebra is:
 -8.00\ 0.00\ 0.00\ -8.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
 0.00 0.00 0.00 0.00 8.00 0.00 0.00 8.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 0.00 8.00 0.00 8.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 8.00 8.00 8.00 32.00 0.00 0.00 0.00
 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 8.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 32.00
and its determinant
6.8719476736E10
******
A semisimple algebra has been found, expanding with the semigroup #740
1 2 1 1 2
1 1 3 3 1
1 1 3 4 1
1 2 1 1 5
whose zero element is: 1.
The metric of the reduced algebra is:
 -8.00\ 0.00\ 0.00\ -8.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
 0.00 \ -8.00 \ -8.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00
 0.00 0.00 0.00 0.00 8.00 0.00 0.00 8.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 0.00 8.00 8.00 0.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 0.00 8.00 16.00 0.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 8.00 0.00 0.00 16.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 8.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 0.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 0.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00 16.00
and its determinant
6.8719476736E10
A semisimple algebra has been found, expanding with the semigroup #746
11111
1 2 1 1 2
1 1 3 3 3
1 1 3 4 3
1 2 3 3 5
whose zero element is: 1.
```

```
0.00 0.00 0.00 0.00 8.00 0.00 0.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 8.00 24.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 24.00
and its determinant
6.8719476736E10
A semisimple algebra has been found, expanding with the semigroup #747
1 1 1 1 1
1 2 1 1 2
1 1 3 3 3
1 1 3 4 4
1 2 3 4 5
whose zero element is: 1.
The metric of the reduced algebra is:
0.00 \ -8.00 \ -16.00 \ -16.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00 \ 0.00
0.00 0.00 0.00 0.00 8.00 0.00 0.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 16.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 32.00
and its determinant
6.8719476736E10
A semisimple algebra has been found, expanding with the semigroup #752
11111
1 2 1 1 2
1 1 3 4 1
1 1 4 3 1
1 2 1 1 5
whose zero element is: 1.
The metric of the reduced algebra is:
0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 8.00 0.00 0.00 16.00 0.00 0.00 0.00 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 0.00\ 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 0.00 16.00
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and its determinant
4.398046511104F12
******
A semisimple algebra has been found, expanding with the semigroup #757
1 1 1 1 1
1 2 1 1 2
1 1 3 4 3
1 1 4 3 4
1 2 3 4 5
whose zero element is: 1.
The metric of the reduced algebra is:
0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 8.00 16.00 0.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 0.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 0.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 0.00 32.00
and its determinant
4.398046511104E12
A semisimple algebra has been found, expanding with the semigroup #770
1 2 1 1 5
1 1 3 4 1
1 1 4 3 1
15112
whose zero element is: 1.
The metric of the reduced algebra is:
0.00\ 0.00\ 0.00\ 0.00\ 16.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00
and its determinant
2.81474976710656E14
******
A semisimple algebra has been found, expanding with the semigroup #777
1 1 1 1 1
1 2 1 2 2
1 1 3 3 3
1 2 3 4 4
1 2 3 4 5
whose zero element is: 1.
```

```
The metric of the reduced algebra is:
  -8.00 \; -8.00 \; -24.00 \; -32.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0
  0.00 0.00 0.00 0.00 8.00 0.00 8.00 0.00 0.00 0.00 0.00
  0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 8.00\ 24.00\ 24.00\ 0.00\ 0.00\ 0.00\ 0.00
  0.00 0.00 0.00 0.00 8.00 8.00 24.00 32.00 0.00 0.00 0.00 0.00
  0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
  0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 8.00
  0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 24.00 24.00
  0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 24.00 32.00
and its determinant
6.8719476736E10
*******
A semisimple algebra has been found, expanding with the semigroup #779
1 2 1 2 2
1 1 3 3 3
1 2 3 4 5
1 2 3 5 4
whose zero element is: 1.
The metric of the reduced algebra is:
  0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 0.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00
  0.00 0.00 0.00 0.00 8.00 8.00 32.00 16.00 0.00 0.00 0.00 0.00
  0.00 0.00 0.00 0.00 8.00 8.00 16.00 32.00 0.00 0.00 0.00 0.00
  0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
  0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
  0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 32.00 16.00
  0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 32.00
and its determinant
4.398046511104E12
A semisimple algebra has been found, expanding with the semigroup #893
11111
1 2 2 2 2
1 2 3 2 2
1 2 2 4 2
1 2 2 2 5
whose zero element is: 1.
```

```
-8.00 \; -8.00 \; -16.00 \; -8.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.
  0.00 0.00 0.00 0.00 8.00 16.00 8.00 8.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 8.00 8.00 16.00 8.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 8.00 8.00 8.00 16.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 8.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 8.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 16.00
and its determinant
6.8719476736E10
A semisimple algebra has been found, expanding with the semigroup #896
1 1 1 1 1
1 2 2 2 2
1 2 3 2 2
1 2 2 4 4
1 2 2 4 5
whose zero element is: 1.
The metric of the reduced algebra is:
 -8.00 \; -8.00 \; -8.00 \; -8.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00
 0.00 0.00 0.00 0.00 8.00 16.00 8.00 8.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 8.00 8.00 16.00 16.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 8.00 8.00 16.00 24.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 8.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 16.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 16.00 24.00
and its determinant
6.8719476736E10
A semisimple algebra has been found, expanding with the semigroup #898
11111
1 2 2 2 2
1 2 3 2 2
1 2 2 4 5
1 2 2 5 4
whose zero element is: 1.
The metric of the reduced algebra is:
 0.00 0.00 0.00 0.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00
 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 16.00\ 8.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00
 0.00 0.00 0.00 0.00 8.00 8.00 24.00 8.00 0.00 0.00 0.00 0.00
 0.00 0.00 0.00 0.00 8.00 8.00 8.00 24.00 0.00 0.00 0.00 0.00
 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 8.00\ 8.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 8.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 24.00 8.00
 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 24.00
```

```
and its determinant
4.398046511104F12
******
A semisimple algebra has been found, expanding with the semigroup #902
1 1 1 1 1
1 2 2 2 2
1 2 3 2 3
1 2 2 4 4
1 2 3 4 5
whose zero element is: 1.
The metric of the reduced algebra is:
0.00 0.00 0.00 0.00 8.00 8.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 8.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 16.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 8.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00
and its determinant
6.8719476736E10
A semisimple algebra has been found, expanding with the semigroup #917
1 2 2 2 2
1 2 3 3 3
1 2 3 4 3
1 2 3 3 5
whose zero element is: 1.
The metric of the reduced algebra is:
0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 8.00\ 8.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 8.00 16.00 24.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 24.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 24.00
and its determinant
6.8719476736E10
A semisimple algebra has been found, expanding with the semigroup #920
1 1 1 1 1
1 2 2 2 2
1 2 3 3 3
1 2 3 4 4
1 2 3 4 5
whose zero element is: 1.
```

```
The metric of the reduced algebra is:
0.00\ 0.00\ 0.00\ 0.00\ 8.00\ 16.00\ 24.00\ 24.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 8.00 16.00 24.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 24.00 32.00
and its determinant
6.8719476736E10
*******
A semisimple algebra has been found, expanding with the semigroup #922
1 2 2 2 2
1 2 3 3 3
1 2 3 4 5
1 2 3 5 4
whose zero element is: 1.
The metric of the reduced algebra is:
0.00 0.00 0.00 0.00 8.00 16.00 32.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 32.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 16.00 16.00 32.00
and its determinant
4.398046511104E12
A semisimple algebra has been found, expanding with the semigroup #927
11111
1 2 2 2 2
1 2 3 3 5
1 2 3 4 5
1 2 5 5 3
whose zero element is: 1.
```

```
9.00 0.00 0.00 0.00 8.00 24.00 24.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 24.00 32.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 8.00 24.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 24.00 24.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 24.00 32.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 24.00
and its determinant
4.398046511104E12
*******
A semisimple algebra has been found, expanding with the semigroup #933
1 1 1 1 1
1 2 2 2 2
1 2 3 4 5
1 2 4 5 3
1 2 5 3 4
whose zero element is: 1.
The metric of the reduced algebra is:
-8.00 \; -8.00 \; -8.00 \; -8.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00 \; 0.00
0.00 0.00 0.00 0.00 8.00 32.00 8.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 8.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 8.00 8.00 32.00 8.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 32.00 8.00 8.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 8.00 32.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 8.00 8.00 32.00 8.00
and its determinant
-1.352605460594688E15
A semisimple algebra has been found, expanding with the semigroup #949
1 1 1 1 1
1 2 2 2 5
1 2 3 2 5
1 2 2 4 5
15552
whose zero element is: 1.
The metric of the reduced algebra is:
0.00 0.00 0.00 0.00 16.00 24.00 16.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 16.00 24.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 24.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 24.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00
```

```
and its determinant
4.398046511104F12
******
A semisimple algebra has been found, expanding with the semigroup #954
1 1 1 1 1
1 2 2 2 5
1 2 3 3 5
1 2 3 4 5
1 5 5 5 2
whose zero element is: 1.
The metric of the reduced algebra is:
0.00 0.00 0.00 0.00 16.00 24.00 32.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 24.00 24.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 24.00 32.00 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 16.00
and its determinant
4.398046511104E12
A semisimple algebra has been found, expanding with the semigroup #959
1 2 2 2 5
1 2 3 4 5
1 2 4 3 5
1 5 5 5 2
whose zero element is: 1.
The metric of the reduced algebra is:
0.00 0.00 0.00 0.00 16.00 32.00 16.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 16.00 16.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 32.00 16.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00 32.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00
and its determinant
2.81474976710656E14
******
A semisimple algebra has been found, expanding with the semigroup #968
1 1 1 1 1
1 2 2 4 4
1 2 3 4 5
1 4 4 2 2
1 4 5 2 3
whose zero element is: 1.
```

```
The metric of the reduced algebra is:
0.00 0.00 0.00 0.00 16.00 32.00 0.00 0.00 0.00 0.00 0.00
0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 16.00\ 16.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 0.00 0.00 16.00 32.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 32.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 16.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 16.00 32.00
and its determinant
2.81474976710656E14
A semisimple algebra has been found, expanding with the semigroup #979
1 2 2 4 5
1 2 3 4 5
1 4 4 5 2
1 5 5 2 4
whose zero element is: 1.
The metric of the reduced algebra is:
0.00\ 0.00\ 0.00\ 0.00\ 24.00\ 24.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
0.00 0.00 0.00 0.00 24.00 32.00 0.00 0.00 0.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00 32.00 0.00 0.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 24.00 0.00
and its determinant
-1.352605460594688E15
A semisimple algebra has been found, expanding with the semigroup #990
11111
1 2 3 4 5
1 3 2 5 4
1 4 5 2 3
1 5 4 3 2
whose zero element is: 1.
```

## and its determinant 1.15292150460684698E18

\*\*\*\*\*\*

A semisimple algebra has been found, expanding with the semigroup #991

- 1 1 1 1 1
- 1 2 3 4 5
- 1 3 2 5 4
- 1 4 5 3 2
- 1 5 4 2 3

whose zero element is: 1.

The metric of the reduced algebra is:

There are 226 semigroups of order 5 with zero element. And 34 of them leads to a semisimple algebra.