
EEE - 321: Signals and Systems

Lab Assignment 3

Please carefully study this assignment before coming to the laboratory. You may begin working on it or even complete it if you wish, but you do not have to. Complete the assignment in the form of a report and turn it in to the assistant. Some of the exercises will be performed by hand and others by using MATLAB. What you should include in your report is indicated within the exercises.

Note: Along with this pdf file, you will find a .zip file containing two MATLAB functions named FT.m and IFT.m. Unzip the archive and place all files contained in it under the current directory of MATLAB.

1 PART 1

In this lab, you are going to see two common daily life applications in which the concepts you learned in the signals and systems course are used. In this part, you will see the first of these applications: transmission and detection of Dual Tone Multi Frequency (DTMF) signals. In Part 2, you will see the second application: cancelation of the echoes from a sound signal.

Dual tone multi frequency (DTMF) is the name of the standard technique used over analog telephone lines to transmit and receive the information about the dialed phone number.

| | 1209 Hz | 1336 Hz | 1477 Hz | 1633 Hz |
|--------|---------|---------|---------|---------|
| 697 Hz | 1 | 2 | 3 | A |
| 770 Hz | 4 | 5 | 6 | B |
| 852 Hz | 7 | 8 | 9 | C |
| 941 Hz | * | 0 | # | D |

Table 1: DTMF frequencies

Examine the following chart: The interpretation of this chart is as follows: Suppose you press the button for 5 on your phone for 0.25 seconds. Then, the DTMF transmitter on your phone sends the following signal

$$x(t) = \begin{cases} \cos(2\pi 770t) + \cos(2\pi 1336t) & \text{for } 0 \leq t \leq 0.25, \\ 0 & \text{otherwise} \end{cases}$$

Or if you press 9, the transmitted signal becomes

$$x(t) = \begin{cases} \cos(2\pi 852t) + \cos(2\pi 1477t) & \text{for } 0 \leq t \leq 0.25, \\ 0 & \text{otherwise} \end{cases}$$

At the receiver (that is the telephone exchange - telefon santrali), the DTMF receiver examines the incoming signal, tries to understand which frequencies were transmitted, so tries to decide which number is dialed.

1.1 DTMF Transmitter

In this part, you will write a function that prepares the analog signal to be transmitted when a phone number containing only numerical digits 0,1,...,9 is dialed.

Assume that for each button, the duration of the transmitted signal is only 0.25 seconds. Thus, for instance, if the dialed number is 2016, you should prepare the following signal:

$$x(t) = \begin{cases} \cos(2\pi 697t) + \cos(2\pi 1336t) & \text{for } 0 \leq t \leq 0.25, \\ \cos(2\pi 941t) + \cos(2\pi 1336t) & \text{for } 0.25 \leq t \leq 0.5, \\ \cos(2\pi 697t) + \cos(2\pi 1209t) & \text{for } 0.5 \leq t \leq 0.75, \\ \cos(2\pi 770t) + \cos(2\pi 1477t) & \text{for } 0.75 \leq t \leq 1, \\ 0 & \text{otherwise} \end{cases}$$

Note that if N digits are dialed, the duration of the final signal is 0.25N. Of course, in MATLAB we can only compute the samples of x(t). Your code should compute the samples within

$0 \leq t \leq 0.25N$ using the sampling period $T_s = 1/8192$.

Your function should look like function `[x]=DTMFTRA(Number)` where

- Number of size $1 \times N$ contains the phone number that is dialed. For instance, if the dialed number is 2016, you should have `Number=[2 0 1 6]`.
- x contains the samples of the transmitted signal x(t).

Once your code is ready to run, prepare the signal for your own cellular phone number and listen to it using the MATLAB command **soundsc(x,8192)**. Does what you listen to sound familiar to you? Explain your answer and compare the sounds you heard. Include your code and comments to your report.

1.2 DTMF Receiver

(**Note:** Before starting this part, clear everything in the workspace issuing the command `clear all`. Place the m-files named FT.m and IFT.m under the current directory.)

First run `x=DTMFTRA(Number)` where number includes the last 4 digits of your student number in reverse order and the number corresponding to your section (1 or 2). Therefore,

- For a student with ID: 20157234 in section 1, `Number= [4 3 2 7 1]` or
- For a student with ID 20117895 in section 2, `Number= [5 9 8 7 2]` etc.

Now, suppose we are on the receiver side, x is the received signal and assume we do not know what x includes. You can listen to it typing `soundsc(x,8192)`.

We know that the form of the signal we receive is as follows:

$$x(t) = \begin{cases} \cos(2\pi f r_1 t) + \cos(2\pi f c_1 t) & \text{for } 0 \leq t \leq 0.25 \\ \cos(2\pi f r_2 t) + \cos(2\pi f c_2 t) & \text{for } 0.25 \leq t \leq 0.5 \\ \cos(2\pi f r_3 t) + \cos(2\pi f c_3 t) & \text{for } 0.5 \leq t \leq 0.75 \\ \cos(2\pi f r_4 t) + \cos(2\pi f c_4 t) & \text{for } 0.75 \leq t \leq 1 \\ \cos(2\pi f r_5 t) + \cos(2\pi f c_5 t) & \text{for } 1 \leq t \leq 1.25 \\ 0, & \text{otherwise} \end{cases}$$

where $(f r_1, f c_1)$ determine the first digit, ..., $(f r_5, f c_5)$ determine the last digit. To understand the phone number we need to find $(f r_1, f c_1), \dots, (f r_5, f c_5)$.

The Fourier transform operation is a powerful tool to analyze the frequency content of signals, and we will make use of it to understand the frequency content of the received signal.

The Fourier transform of $x(t)$ denoted by $X(\omega)$ is defined as:

$$X(\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt \quad (1)$$

For any particular frequency ω , $X(\omega)$ denotes the contribution of the complex exponential $e^{j\omega t}$ to the signal $x(t)$. As an analogy, $X(\omega)$ shows how many grams of $e^{j\omega t}$ we need to use to form $x(t)$.

Answer the following questions and include the answers to your report. You can directly use the result given in the book for part a. For the other parts show your work clearly. In these parts, you can directly use the definition of the Fourier transform. However, if it is possible, it is recommended to use the properties of the Fourier transform.

- a) Let $x(t) = \exp(j2\pi f_0 t)$. What is $X(\omega)$?
- b) Let $x(t) = \cos(2\pi f_0 t)$. What is $X(\omega)$?
- c) Let $x(t) = \sin(2\pi f_0 t)$. What is $X(\omega)$?
- d) Let $x(t) = \text{rect}\left(\frac{t}{T_0}\right)$. What is $X(\omega)$?
- e) Let $x(t) = \exp(j2\pi f_0 t) \text{rect}\left(\frac{t}{T_0}\right)$. What is $X(\omega)$?
- f) Let $x(t) = \cos(2\pi f_0 t) \text{rect}\left(\frac{t}{T_0}\right)$. What is $X(\omega)$?
- g) Let $x(t) = \text{rect}\left(\frac{t-t_0}{T_0}\right)$. What is $X(\omega)$?
- h) Let $x(t) = \exp(j2\pi f_0 t) \text{rect}\left(\frac{t-t_0}{T_0}\right)$. What is $X(\omega)$?
- i) Let $x(t) = \cos(2\pi f_0 t) \text{rect}\left(\frac{t-t_0}{T_0}\right)$. What is $X(\omega)$?

Type **X=FT(x)**. Then create a frequency array using the following code:

```
omega=linspace(-8192*pi,8192*pi,10241);
omega=omega(1:10240);
```

This piece of code will create a frequency array in angular frequency. You will learn the details of this code when you learn the details of sampling. Then type `plot(omega,abs(X))`. You will obtain the plot of the magnitude of the Fourier transform of $x(t)$ computed over the grid specified by ω . Include the plot to the report. Examine the figure, in particular, determine the frequencies where you see the peaks. Are the frequencies where the peaks occur the ones used by DTMF transceivers? (Here you should consider the conversion of cyclic frequency (with units of Hertz) to angular frequency (with units of rad/sec)). If yes, can you understand ONLY from this figure what the dialed number is? Include your answers to the report.

Now, define a new signal as

$$x_1(t) = \begin{cases} x(t) & \text{for } 0 \leq t \leq 0.25 \\ 0 & \text{for } 0.25 \leq t \leq 1.25 \\ 0 & \text{otherwise} \end{cases}$$

This operation can be seen as a multiplication of $x(t)$ by a rectangular signal. First write the analytical expression of this rectangular signal. Then, in Matlab, generate this rectangular signal and by multiplying by $x(t)$, create $x_1(t)$. Make sure that the size of the array for $x_1(t)$ is the same with the size of the array for $x(t)$. Include your code to the report.

Now compute $X_1(\omega)$ using the FT.m function and plot its magnitude against ω . Include the plot to the report. Look again to the frequencies where the peaks occur. This time, can you understand what is the first digit that is dialed? Include the answer to your report. Continue in this manner and find the remaining four digits. Explain these steps clearly.

Why do you think that the first method (looking at $X(\omega)$ at once) does not work but the second method (looking at $X_1(\omega)$, ..., $X_5(\omega)$ separately) works? Write your answer to the report.

2 PART 2

(**Note:** Before starting this part, clear everything in the workspace issuing the command `clear all`. Place the m-files named FT.m and IFT.m under the current directory.)

Suppose you are in a room with no furniture or carpet inside, and suppose all the windows and the door is closed. We know from our common daily life experience that, when you speak in the room, the acoustical waves you produce with your vocal chords will hit the walls of the room and reflect back. As a result, you will hear the echoes of your speech. Note that echoes are essentially delayed and possibly amplitude scaled versions of the original signal. Suppose there is a microphone in the room which records your speech. The recording will consist of the echoes as well.

This echo issue may cause problems in some applications, for example, ultrasound imaging, communication systems etc. Our purpose in this part is to eliminate these echoes from the recording.

You will first create a Matlab array which includes your speech. For this purpose, you will use a microphone, which can be a webcam microphone, the one that you produced in EE 211 course or another one. By using this microphone, record your speech for 10 seconds. You can record your voice directly in Matlab by creating an array, or use another program to save your voice to a file and then read it in Matlab. For this recording issue, you may need to do some google search. During your recording, the number of the samples per second, in other words, the sampling rate, should be 8192. Generate this array with the name x. Note that the length of the array should be 8192×12 . If the length of the array that you produced exceeds 98304, you can crop it to have the length 98304. What you spoke to the microphone is up to you. It can be, for example, 'my name is john doe', 'my ID is 20151028', 'this is signals and systems course', etc. When you create x, listen to it in Matlab in order to make sure that your recording is successful. Include your code and your speech to the report.

Now you will artificially create the signal y which suffers from echo. This signal will represent the one which is described in the first paragraph of this part. It can be represented as

$$y(t) = x(t) + \sum_{i=1}^M A_i x(t - t_i) \quad , \quad (2)$$

where the summation simulates the environment which causes the echo. M represent the number of the echo, A_i denotes the amplitude of the i th echo and t_i denotes the time delay for the i th echo with $A_i > 0$ and $t_i > 0$. (If there is no amplifier in the environment, we expect $A_i < 1$ due to the power loss.)

First, answer the following questions and include your answers to your report together with a clear derivation.

- a) Find $h(t)$ such that $y(t) = x(t)*h(t)$ where $*$ denotes the convolution operation. Note that in this way, we describe the process that relates $x(t)$ to $y(t)$ as a linear time invariant (LTI) system. The impulse response of this LTI system is $h(t)$.
- b) What is the frequency response of this system? That is, what is $H(\omega)$, i.e., the Fourier transform of $h(t)$?
- c) What is the relation between $X(\omega)$, $Y(\omega)$ and $H(\omega)$? (Write the mathematical relation of them and explain it.)
- d) Given $Y(\omega)$ and $H(\omega)$, how can you determine $X(\omega)$?

Now, generate the time variable t by issuing the command

t=0:1/8192:12-1/8192;

This variable indicates the sampling points in time of your voice. Then generate y from x by assuming $M = 6$, $A_i = 0.65, 0.50, 0.30, 0.22, 0.15, 0.1$ and $t_i = 0.25, 0.75, 1, 1.25, 2, 3.25$ seconds. Crop the delayed signals so that each of them is 12 seconds long. Plot $x(t)$ vs. t and $y(t)$ vs. t in separate figures. Clearly indicate the titles and labels. Also listen to $y(t)$ and describe the sound that you listened.

Now you will extract the original signal from the disturbed signal using Fourier domain relations. In order to do this, compute the Fourier transform of $y(t)$ using the command

Y=FT(y). Then, compute $H(\omega)$ over the grid specified by ω , which will be generated typing

```
omega=linspace(-8192*pi,8192*pi,98305);  
omega=omega(1:98304);
```

Next, compute $h(t)$ typing **h=IFT(H)**. Plot $h(t)$ vs. t and $|H(\omega)|$ vs. ω in separate figures. Include your plots to your report together with the appropriate labels and titles. Then, using your result in item d, compute $X_e(\omega)$, where e indicates estimated X . Finally, compute $x_e(t)$ from $X_e(\omega)$ typing **xe=IFT(Xe)**. Then listen to $x_e(t)$. Is the estimated speech different than your original speech? Plot $x_e(t)$ and include the plot to your report. Also include your comments and observations in the report. Compare them and explain the differences if exist.