

Closest Pair of Points (2D)

DnC vs Brute Force



Kelompok 4

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```
class Point{  
    public double x;  
    public double y;  
    public Point(double x,double y){  
        this.x = x;  
        this.y = y;  
    }  
    public String toString(){  
        return "("+x+","+y+"";  
    }  
}
```

Fachren

```
public Point[] getClosestPair(Point[] ps){  
    // urutkan berdasarkan absis x  
    sortPointsByX(ps);  
  
    // kemudian hitung  
    return getClosestPair(ps,0,ps.length-1);  
}
```

Winner



```
/**
 * menggunakan quick sort
 * kompleksitas:  $O(n \log n)$ 
 */
public void sortPointsByX(Point[] ps) {
    int size = ps.length;
    quickSort(ps, 0, size-1);
}
```

Hendy

```
public void quickSort(Point[] ps, int left, int right) {
    if (left >= right)
        return;
    int i = left, j = right;
    Point tmp;
    double pivot = (ps[left].x + ps[right].x) / 2;

    while (i <= j) {
        while (ps[i].x < pivot)
            i++;
        while (ps[j].x > pivot)
            j--;
        if (i <= j) {
            tmp = ps[i];
            ps[i] = ps[j];
            ps[j] = tmp;
            i++;
            j--;
        }
    }

    if (left < i - 1)
        quickSort(ps, left, i - 1);
    if (i < right)
        quickSort(ps, i, right);
}
```


Yochiko



```
/**
 * @param ps: sebelumnya udah di sort berdasarkan absis
 */
public Point[] getClosestPair(Point[] ps, int start, int end){
    if(start==end)
        return null;
    if(start+1==end)
        return new Point[]{ps[start],ps[end]};

    // menentukan medium X
    int mediumX = (start+end)/2;
```

Ghaza



```
// kemudian solve secara rekursif  
Point[] leftClosestPair = this.getClosestPair(ps, start, mediumX);  
Point[] rightClosestPair = this.getClosestPair(ps, mediumX, end);  
Point[] returnPair;  
double returnDelta;
```


Seteven

```
// cari minimal distance untuk masing-masing (sebelah kiri dan kanan)
double leftDelta = this.getDistance(leftClosestPair);
double rightDelta = this.getDistance(rightClosestPair);
double delta;
if(leftDelta < rightDelta){
    delta = leftDelta;
    returnPair = leftClosestPair;
}else{
    delta = rightDelta;
    returnPair = rightClosestPair;
}
returnDelta = delta;
```

```
// menentukan jarak minimal antara pasangan titik yg terletak di satu sisi dan yg terletak di sisi lain  
int leftEdge = this.getLeftEdgeOfDelta(ps, mediumX, leftDelta);  
if(leftEdge < start)  
    leftEdge = start;  
int rightEdge = this.getRightEdgeOfDelta(ps, mediumX, rightDelta);  
if(rightEdge > end)  
    rightEdge = end;
```

Dian

```
// urutkan points yang edge sebelah kiri dan kanan berdasarkan ordinat atau Y  
// Time:  $O(n \log n)$   
int yOrderInfo[][] = this.sortPointsByY(ps, leftEdge, rightEdge);  
int idxToOrderY[] = yOrderInfo[0];  
int orderYToIdx[] = yOrderInfo[1];
```

Rahmatul

```
// periksa apakah ada titik di [mediumX, rightEdge] yang memiliki jarak kurang dari delta ke titik ini
for(int i=leftEdge;i<=mediumX;i++){
    int orderY = idxToOrderY[i-leftEdge];
    for(int j=orderY-1;j>=0;j--){
        Point[] pair = new Point[]{ps[i],ps[orderYToIdx[j]]};
        if(this.getYDistance(pair) > delta)
            break;
        double distance = this.getDistance(pair);
        if(distance < returnDelta){
            returnDelta = distance;
            returnPair = pair;
        }
    }

    for(int j=orderY+1;j<idxToOrderY.length;j++){
        Point[] pair = new Point[]{ps[i],ps[orderYToIdx[j]]};
        if(this.getYDistance(pair) > delta)
            break;
        double distance = this.getDistance(pair);
        if(distance < returnDelta){
            returnDelta = distance;
            returnPair = pair;
        }
    }
}
return returnPair;
```

Elvina

```
// mengurutkan ordinat menggunakan quick sort, cost n log n
public int[][] sortPointsByY(Point[] ps, int leftEdge, int rightEdge) {
    int size = rightEdge - leftEdge + 1;
    int orderToIdx[] = new int[size];
    for(int i=0;i<size;i++)
        orderToIdx[i] = leftEdge+i;
    quickSortForDeltaArea(ps, orderToIdx, 0, size-1);
    int idxToOrder[] = new int[size];
    for(int i=0;i<size;i++){
        idxToOrder[orderToIdx[i]-leftEdge] = i;
    }
    return new int[][]{idxToOrder,orderToIdx};
}
```



Siti

```
// quick sort untuk delta area, kiri medium & kanan medium
public void quickSortForDeltaArea(Point[] ps,int[] indexs, int left, int right) {
    if (left >= right)
        return;
    int i = left, j = right;
    int tmp;
    double pivot = ( ps[indexs[left]].y + ps[indexs[right]].y) / 2;

    while (i <= j) {
        while (ps[indexs[i]].y < pivot)
            i++;
        while (ps[indexs[j]].y > pivot)
            j--;
        if (i <= j) {
            tmp = indexs[i];
            indexs[i] = indexs[j];
            indexs[j] = tmp;
            i++;
            j--;
        }
    }

    if (left < i - 1)
        quickSortForDeltaArea(ps, indexs, left, i - 1);
    if (i < right)
        quickSortForDeltaArea(ps, indexs, i, right);
}
```


Chiko

```
// hitung tepi kanan area delta
public int getRightEdgeOfDelta(Point[] ps, int mediumX, double rightDelta) {
    for(int i=mediumX;i<ps.length;i++){
        if(ps[i].x - ps[mediumX].x>rightDelta)
            return i-1;
    }
    return ps.length-1;
}
```

Winner

```
// hitung tepi kiri area delta
public int getLeftEdgeOfDelta(Point[] ps, int mediumX, double leftDelta) {
    for(int i=mediumX;i>=0;i--){
        if(ps[mediumX].x - ps[i].x>leftDelta)
            return i+1;
    }
    return 0;
}
```


Ghaza



```
// =  $\sqrt{(x_2-x_1)^2+(y_2-y_1)^2}$ 
public double getDistance(Point[] ps) {
    if(ps==null||ps.length!=2){
        return -1;
    }
    return Math.pow(
        (ps[0].x-ps[1].x) * (ps[0].x-ps[1].x) +
        (ps[0].y-ps[1].y) * (ps[0].y-ps[1].y), 0.5);
}
```

Hendy

```
// generate titik acak
public Point[] generateRandomPoints(int size, double maxX, double minX, double maxY, double minY){
    Point[] points = new Point[size];
    for(int i=0; i<size; i++){
        points[i] = new Point(
            Math.random()*(maxX-minX) + minX,
            Math.random()*(maxY-minY) + minY);
    }
    return points;
}
```



Seteven

```
// kebutuhan log, input, dan waktu
logs = new StringBuilder();
int totalLoop = Integer.parseInt(points.getText());
int totalPointsPerLoop = Integer.parseInt(loops.getText());

double minX = Double.parseDouble(minx.getText());
double maxX = Double.parseDouble(maxx.getText());
double minY = Double.parseDouble(miny.getText());
double maxY = Double.parseDouble(maxy.getText());

int passed = 0;
long nlognTime = 0;
long nsqTime = 0;
long startTime;
```



Siti

```
indikator.setText("Done");  
log.setText(logs.toString());  
sukses.setText(passed + "/" + totalLoop);  
bft.setText(String.valueOf(nsqTime));  
dnct.setText(String.valueOf(nlognTime));
```

```
private void resetActionPerformed(java.awt.event.ActionEvent evt) {//GEN-FIRST:event_resetActionPerformed  
    // set button  
    points.setText("");  
    loops.setText("");  
    minx.setText("");  
    miny.setText("");  
    maxx.setText("");  
    maxy.setText("");  
    indikator.setText("");  
    log.setText("");  
    sukses.setText("");  
    bft.setText("");  
    dnct.setText("");  
}
```

```
for(int k=0;k<totalLoop;k++){
    Point[] ps = cpp.generateRandomPoints(totalPointsPerLoop, maxX, minX, maxY, minY);
    startTime = new Date().getTime();

    Point[] pair = cpp.getClosestPair(ps);
    nlognTime += (new Date().getTime() - startTime);

    double distance = cpp.getDistance(pair);
    logs.append("[ok] = " + pair[0].toString() + "," + pair[1].toString() + " = " + distance + "\n");

    startTime = new Date().getTime();
    pair = cpp.bruteForce(ps);

    nsqTime += (new Date().getTime() - startTime);
    double distance2 = cpp.getDistance(pair);
    if(distance==distance2){
        passed++;
    }
}
```

Closest Pair of Points Problem ~ DnC vs Brute Force

Masukkan Banyak perulangan

Masukkan banyak points per perulangan

Min x Min y

Max x Max y

Sukses

Total Waktu Brute Force ms

Total Waktu DnC ms



DEMO

Nobody:
Bugs right before a demo:



Efisiensi

Setiap instance permasalahan akan terjadi N pass untuk setiap titik dan masing-masing pass akan meninjau kembali n titik. Sehingga kompleksitas untuk algoritma brute force $O(n^2)$ nested loop

Fungsi conquer, memiliki kompleksitas $O(n)$, namun pada awal fungsi conquer, titik disekitar garis pembagi diurutkan berdasarkan ordinat, (asumsi algo berorder $n \log n$, maka kompleksitas total algoritmanya adalah $O(n \log n)$)

Kelebihan & Kekurangan

- *Brute force* Cukup baik untuk N nya yang tidak terlalu besar
- Untuk N yg besar ($n > 100.000$), komputasi dengan algoritma *brute force* ini akan memakan waktu yg lama
- Karena Algoritma *DnC* memiliki kompleksitas $O(n \log n)$, untuk N yang besar masih cukup mangkus untuk digunakan



Thanks