

# Electric Machinery Fundamentals

Fifth Edition



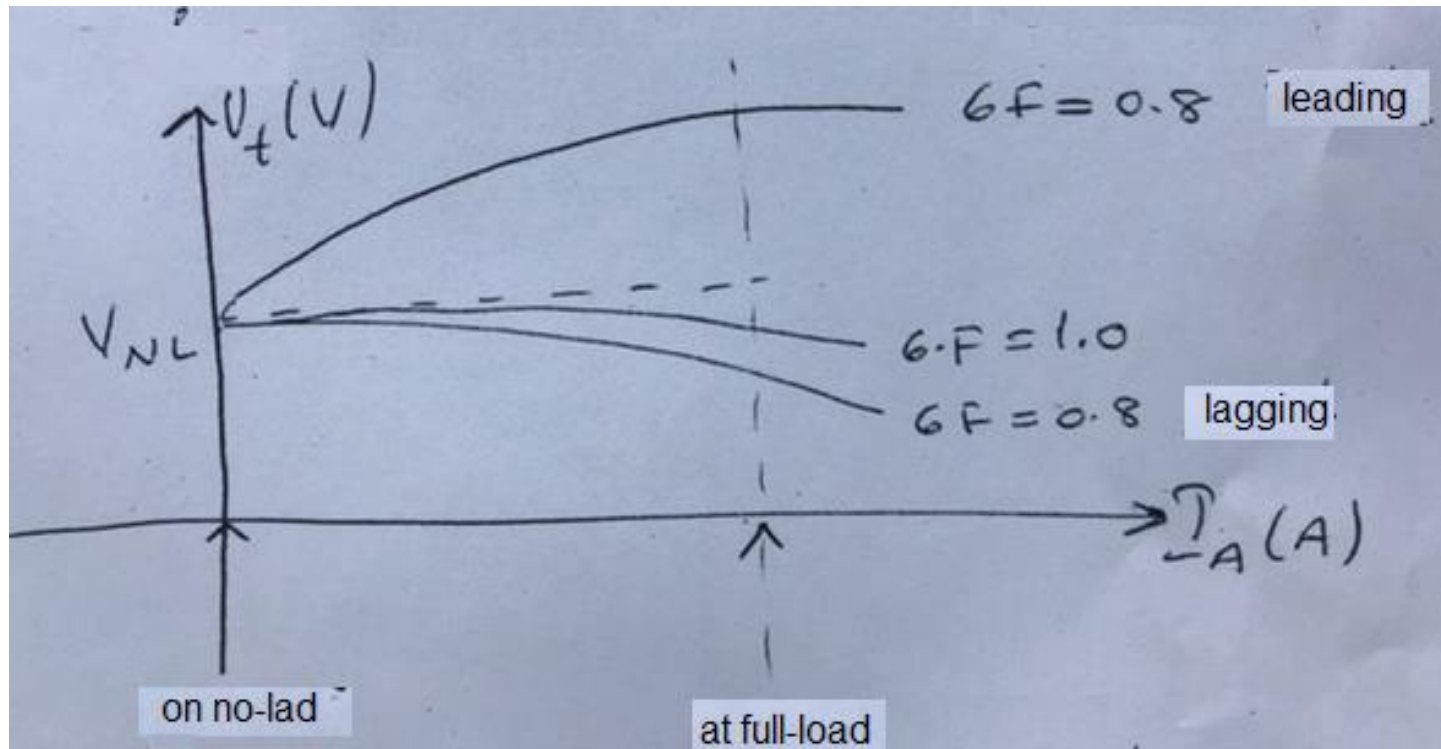
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## Synchronous Generators

# Voltage Regulation

- The synchronous generator must provide the conditions listed below before feeding a load.
  1. Since pole number of the machine is constant, the machine must be operated at right speed (synchronous speed) in order to generate voltage at required frequency.
  2. A DC field excitation is required in the rotor.
  3. The output voltage must be at desired level by adjusting the field current.

By providing these conditions, if the generator is loaded, the output voltage of the generator will be affected even the DC field excitation is constant. The voltage change of the generator depends on the load (i.e. load power factor). The output voltage will drop with resistive and inductive load increase, and it will increase with capacitive load increase.



- **Figure 6:** The output voltage vs load current for various load power factor.

- As we know before, factors such as voltage drop in the armature resistance and flux change due to the armature reaction affect the output voltage. The third factor affecting the output voltage of the synchronous generator is the voltage drop in the armature reactance. This is because of the armature inductance,  $L_A$ .
- $$X_A = 2\pi f L_A \text{ (}\Omega\text{)}$$
- Where;
- $L_A$  : armature winding inductance per phase (H)
- $\omega = 2\pi f$ : Angular frequency in rad/s.

$$\text{voltage regulation} = \frac{V_{NL} - V_{FL}}{V_{FL}} \cdot 100$$

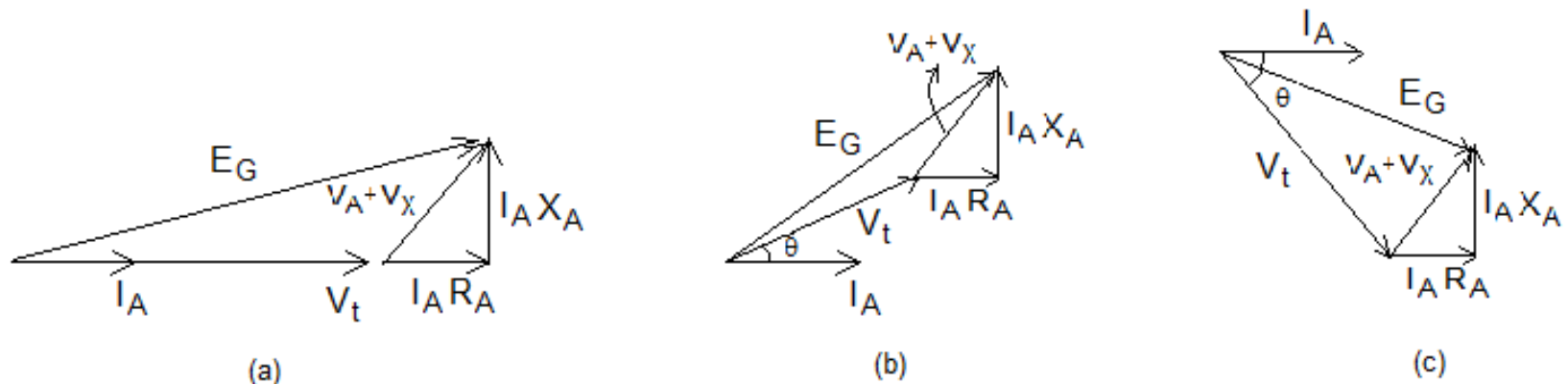
- $V_{NL}$ : Voltage on no-load (V)
- $V_{FL}$ : Voltage at full-load (V).

- In case the power factor is leading, the voltage regulation will be negative, which means that the voltage increases with the increase of the load.
- In general, the output voltage increases considerably when the load is extracted in AC generators. For this reason, voltage regulators are used together with synchronous generators.
- The voltage change in synchronous generators because of the armature reaction and reactance is much bigger than that of DC machines. The generators normally feeds long transmission lines having transformers resulting in extra voltage drops. All these negative factors result in unacceptable voltage changes with load changes in power delivery systems. For this reason, by using special designed regulators, the voltage drop is compensated by increasing DC field excitation current.

# Voltage Drop in The Generator

- For example as a load, if a three-phase motor is supplied by the generator, a current in the armature winding of the generator will start to flow. The armature winding has a resistance,  $R_A$  per phase. Therefore, a voltage drop occurs in that resistance as;
  - $V_A = I_A.R_A$  (Volt/Phase)
- Since three-phase is symmetrical, the voltage drop and therefore phase currents are same in all phases.
- The voltage drop does not only consist of the voltage on the resistance. In addition, a reactive voltage drop occurs because of the armature winding inductance.
  - $V_X = I_A.X_A$  (Volt/Phase)
- $X_A$ : Reactance per phase ( $\Omega$ /Phase)

- It is not enough to know these voltage drops to determine the generated voltage. These voltages are added in vector to the output voltage to find the generated voltage. Therefore, it is required to know the character of the load and power factor.



- Figure 7:** The effect of the power factor on the generated voltage by considering only the armature resistance and reactance. (a)  $PF=1.0$ ; (b)  $PF=\text{Lagging}$ ; (c)  $PF=\text{Leading}$

- The relationship between the power factor and the generated voltage is shown in Fig.7. The generated voltage ( $E_G$ ) is bigger than the output voltage ( $V_t$ ) at unity and lagging power factors. However, the output voltage  $V_t$  is bigger than the generated voltage  $E_G$  at leading power factor. If the figure is examined carefully,  $E_G$  voltage is always leading the  $V_t$  voltage for all power factors.



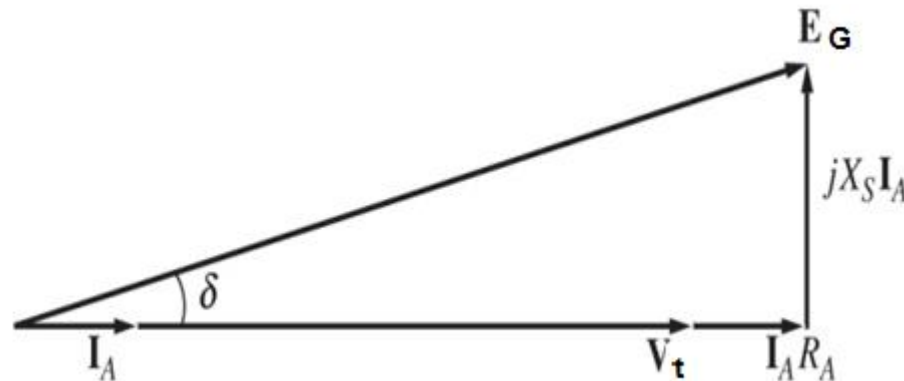
# The Phasor Diagram of a Synchronous Generator

The Kirchhoff's voltage law equation for the armature circuit is;

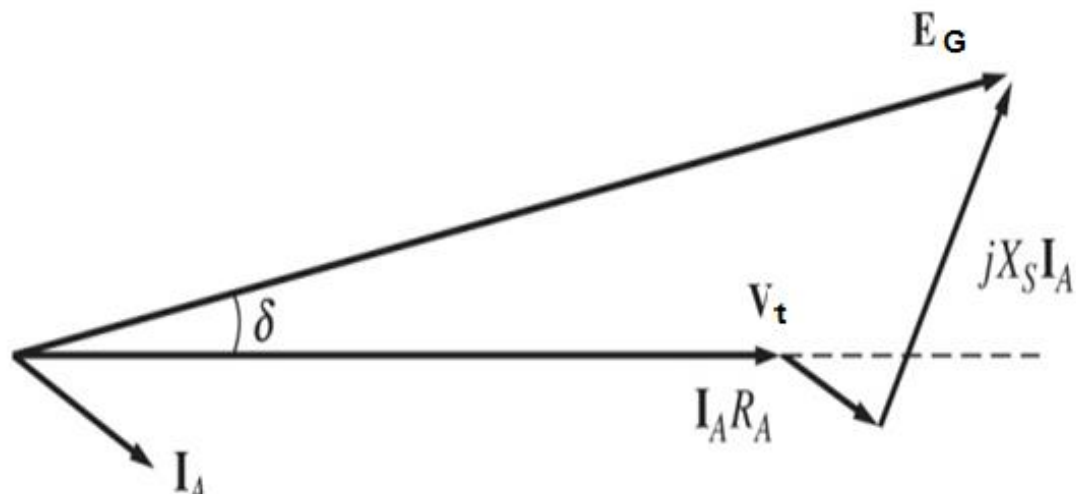
$$E_G = V_t + I_A(R_A + jX_S)$$

Where;  $X_S = X_A + X_{AR}$

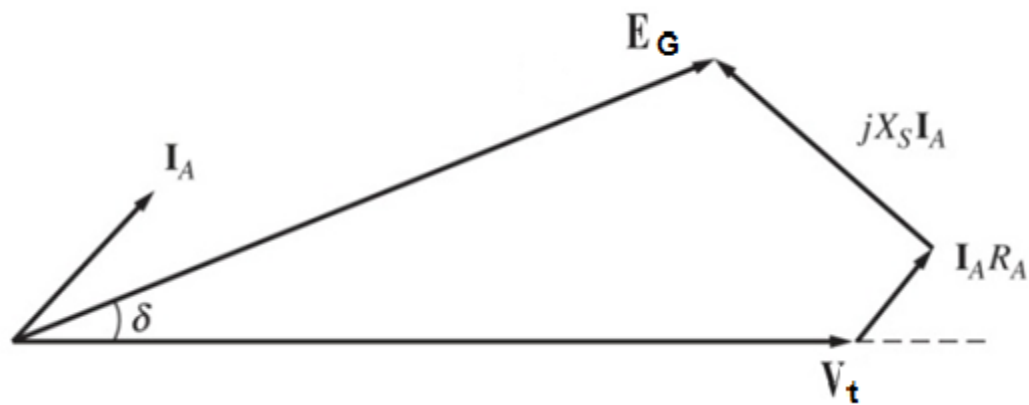
The phasor diagrams for unity, lagging, and leading power factors load are shown here:



(a) PF=1



**(b)** PF= Lagging



**(c)** PF= Leading

**Figure 8:**

- For unity power factor (Fig.8(a)),  $E_G$  voltage is bigger than  $V_t$ . For lagging power factor (Fig.8(b)),  $E_G$  is much bigger than  $V_t$  comparing to the unity power factor. However, for leading power factor (Fig.8(c)),  $V_t$  is bigger than  $E_G$ . That is; if the power factor is leading and the machine operates at full-load, the output voltage  $V_t$  is bigger than the voltage at no-load,  $E_G$ .
- $I_A X_s$  voltage drop is known as synchronous reactance voltage and here,  $X_s$  is called as “synchronous reactance”. In Fig.8, the angle,  $\delta$  between  $E_G$  and  $V_t$  is called as “power angle” or “torque angle”. This angle depends on the load and it is a measure of the airgap power.
- In the phasor diagrams drawn for pure inductive or capacitive loads, the angle  $\delta$  is zero since there is no active power dissipated.

## The Equivalent Circuit of a Synchronous Generator

- When generator is not loaded, the internal generated voltage  $E_A$  is the same as the voltage appearing at the terminals of the generator,  $V_t$ .
- When generator is loaded, a balanced 3-phase current will flow which results in the stator rotating magnetic field  $B_S$ . The net air gap flux density is the sum of the rotor and stator magnetic fields:

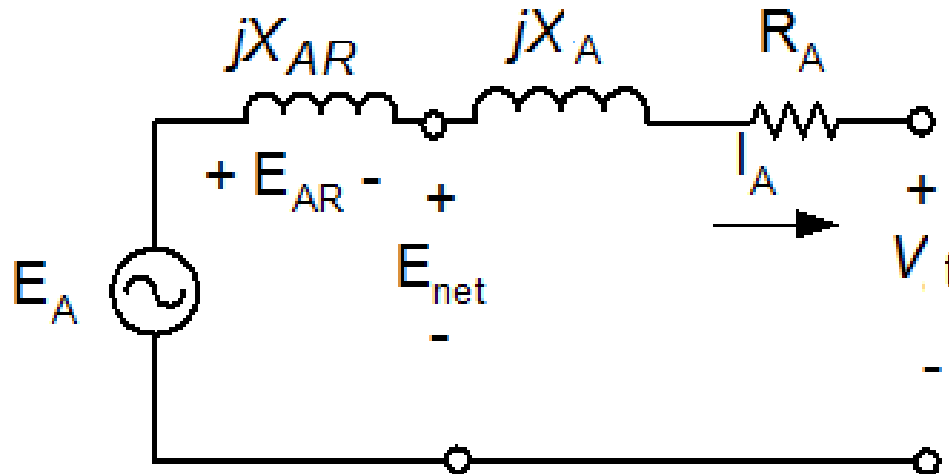
$$\mathbf{B}_{net} = \mathbf{B}_R + \mathbf{B}_S$$

- The voltage induced in the armature would be the sum of the voltages induced by rotor field ( $E_A$ ) and the voltage induced by the stator field ( $E_{AR}$ , or armature-reaction voltage).

$$\mathbf{E}_{net} = \mathbf{E}_A + \mathbf{E}_{AR}$$

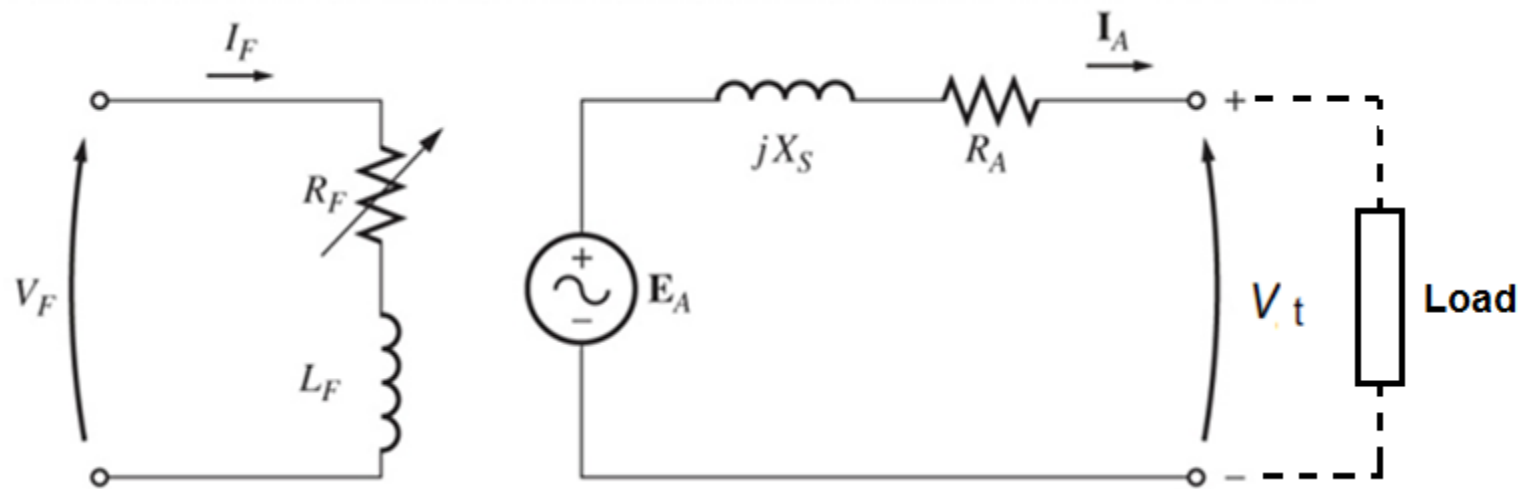
Two other voltage drops must be considered:

- Self (or leakage) inductance of the armature coils.
- Resistance of the armature coils
- The armature-reaction voltage may be represented by an inductive voltage drop across an armature–reaction reactance  $X_{AR}$ , as shown here.



The two reactances may be combined into a single reactance called the synchronous reactance of the machine:

$$X_S = X_A + X_{AR}$$



**Figure 9:**

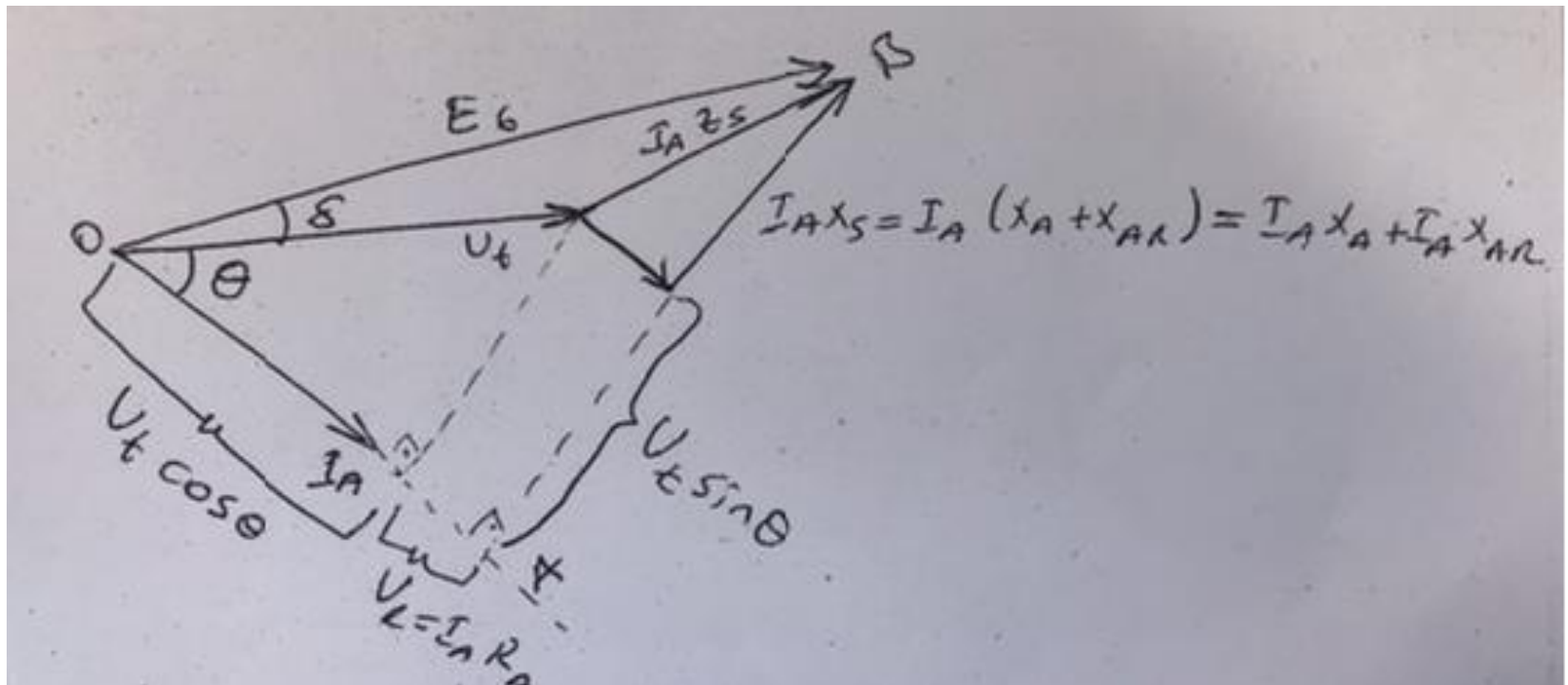
The per phase equivalent circuit of a synchronous generator.

If  $X_S = X_A + X_{AR}$

Then;

$$I_A X_A + I_A X_{AR} = I_A X_S$$

Therefore, if  $V_t$  is taken as reference phasor, then the phasor diagram can be drawn as;



$$\bar{E}_G = \bar{I}_A \bar{Z}_S + \bar{V}_t$$

- Where  $Z_S$  is the armature impedance per phase.

$$Z_S = R_A + jX_S \rightarrow Z_S = \sqrt{R_A^2 + X_S^2}$$

- As can be seen from Fig.9, a synchronous generator can be modelled by an R-L circuit. In this circuit,  $R_A$  represents the armature resistance and  $X_S$  represents the synchronous reactance. The power factor angle,  $\theta$  is determined by the load. The power dissipated on the load;
- $P_L = V_t \cdot I_A \cdot \cos\theta$  (Watt/Phase)
- Since the machine is a three-phase machine;
- $P_L = 3 \cdot V_t \cdot I_A \cdot \cos\theta$



- The power is usually represented by line current and line voltage. In this case, winding connection type must be known. If the armature windings are connected in star;

$$I_A = I_L \text{ and } V_t = \frac{V_L}{\sqrt{3}}$$

$$P_L = 3 \frac{V_L}{\sqrt{3}} I_L \cos \theta = \sqrt{3} V_L I_L \cos \theta$$

- This is a general expression of three-phase power and it is independent of armature or load connection type.

$$\bar{I}_A = I_A (\cos \theta - j \sin \theta)$$

$$\bar{Z}_S = R_A + jX_S$$

- For inductive load characteristic;

$$E_G = V_t + I_A(\cos\theta - j\sin\theta).(R_A + jX_S)$$

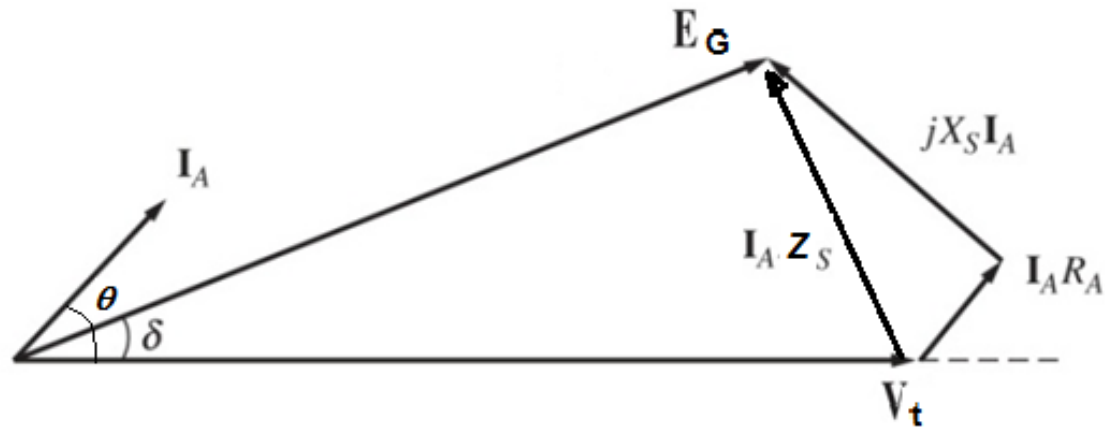
If  $V_t = V_t \angle 0$  is taken as reference phasor and consider the phasor diagram;

$$OA = V_t \cos\theta + V_R \text{ and } AB = V_t \sin\theta + V_S$$

Since  $E_G = OB$  then;

$$E_G = [(V_t \cos\theta + V_R)^2 + (V_t \sin\theta + V_S)^2]^{1/2}$$

If the load is capacitive, the phasor diagram will be as;



- By the help of the phasor diagram it can be obtain that;

$$E_G = [(V_t \cos \theta + V_R)^2 + (V_t \sin \theta - V_S)^2]^{1/2}$$

- If the load is pure resistive load, then  $PF = \cos \theta = 1$  and  $\sin \theta = 0$ . Then;

$$E_G = [(V_t + V_R)^2 + (V_S)^2]^{1/2}$$

- $R_A$  is usually much smaller than  $X_S$  (specially at high rated machines). Therefore,  $V_R$  voltage can be neglected comparing to  $V_S$ .

- **Example:**
- Figure given below shows the equivalent circuit and phasor diagram of a 250 kVA, 660 V, 60 Hz, a three-phase and star connected synchronous generator. Armature resistance and synchronous reactance of the generator is 0.1  $\Omega$ /Phase and 1.4  $\Omega$ /Phase, respectively. A load with power factor of 0.866 (lagging) is connected to the output of the generator. Calculate the voltage regulation.

- **Solution:**

$$I_A = \frac{250000}{\sqrt{3} \cdot 660} = 219 \text{ A}$$

$$V_t = \frac{V_L}{\sqrt{3}} = \frac{660}{\sqrt{3}} = 381 \text{ V}$$

$$I_A R_A = 219 * 0.1 = 21.9 \text{ V}$$

$$I_A X_S = 219 * 1.4 = 306.6 \text{ V}$$

$$\cos\theta = 0.866 \text{ and } \sin\theta = 0.5 \text{ (lagging)}$$

$$E_G = [(381 * 0.866 + 21.9)^2 + (381 * 0.5 + 306.6)^2]^{\frac{1}{2}} = 609 \text{ V}$$

$$\text{Voltage Regulation} = \frac{609 - 381}{381} * 100 = 59.8\%$$

