



# Simple Parallel Calibration and 3D Reconstruction in Real-Time for RGB-D Cameras

Dr. Lau, advisor

Dr. Hastings, committee member

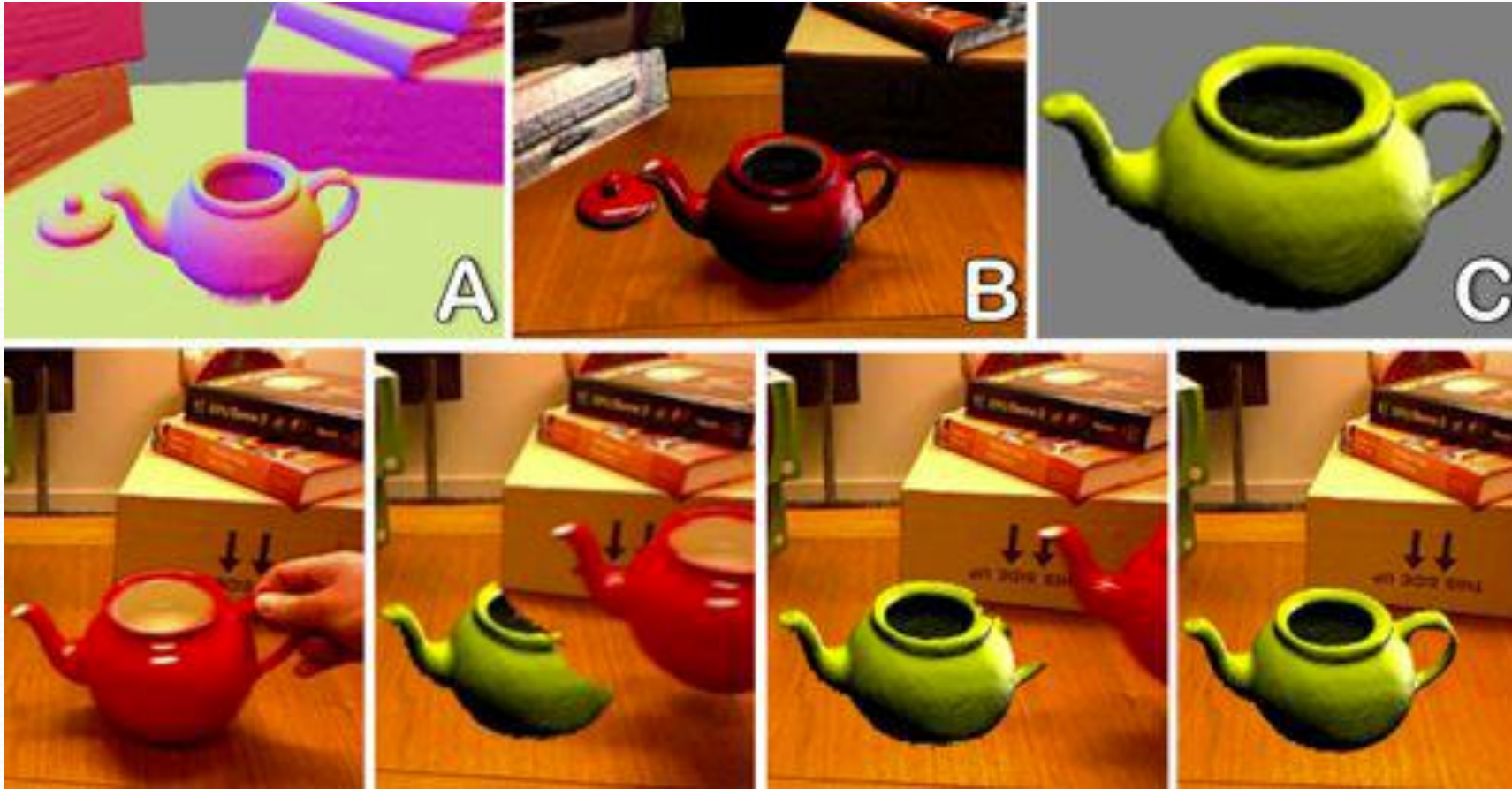
Dr. Cheung, committee member

- Presented By: Sen Li

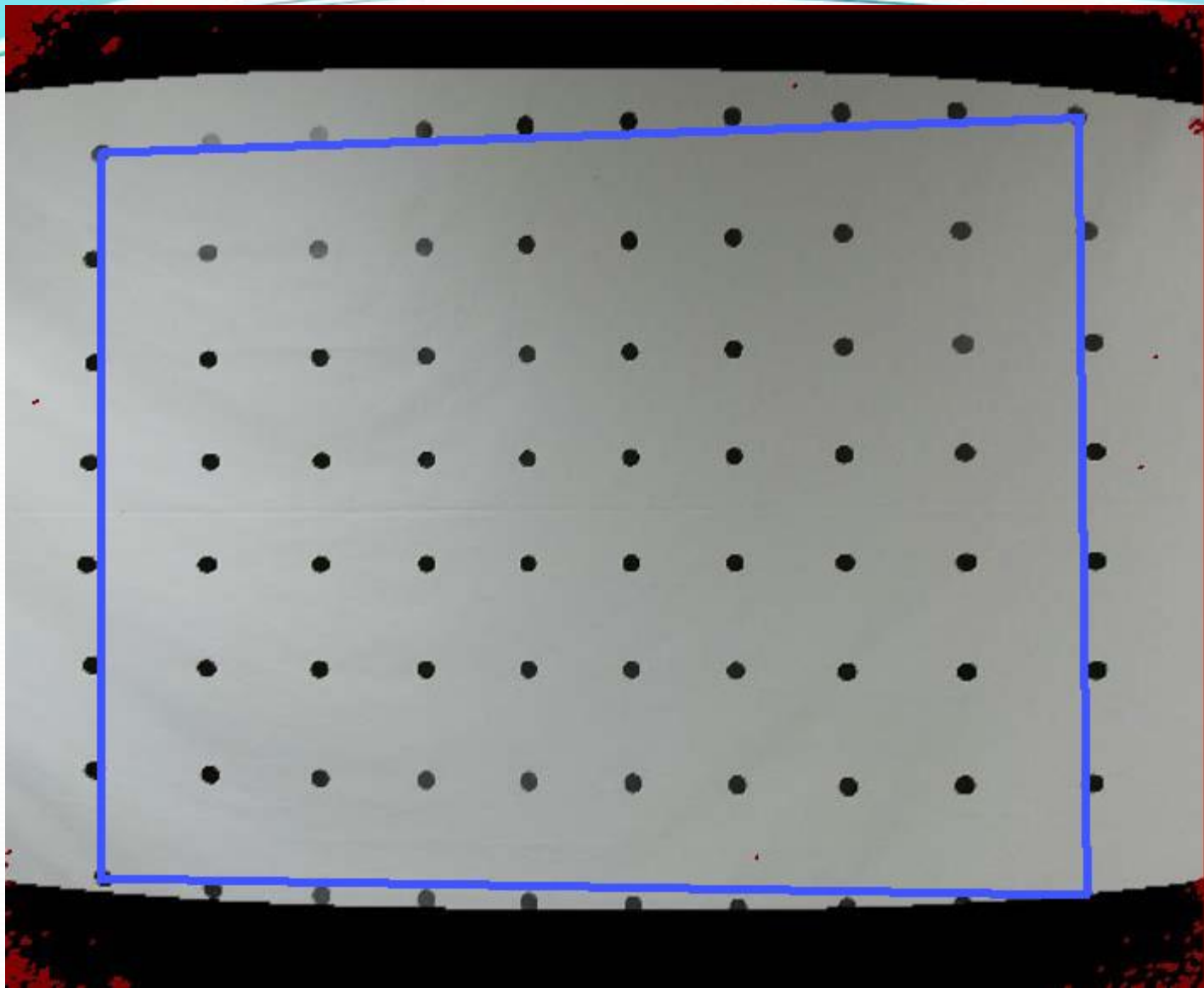
# Outline

- **Introduction**
- Academic Background:
  - Pinhole Camera Model (Camera calibration / 3D reconstruction)
  - Kai's per-pixel 3D reconstruction on GPU
  - Inspiration
- Natural GPU Calibration and Reconstruction Method:
  - Calibration system
  - Calibration procedures
  - Undistorted 3D Reconstruction
- Conclusion

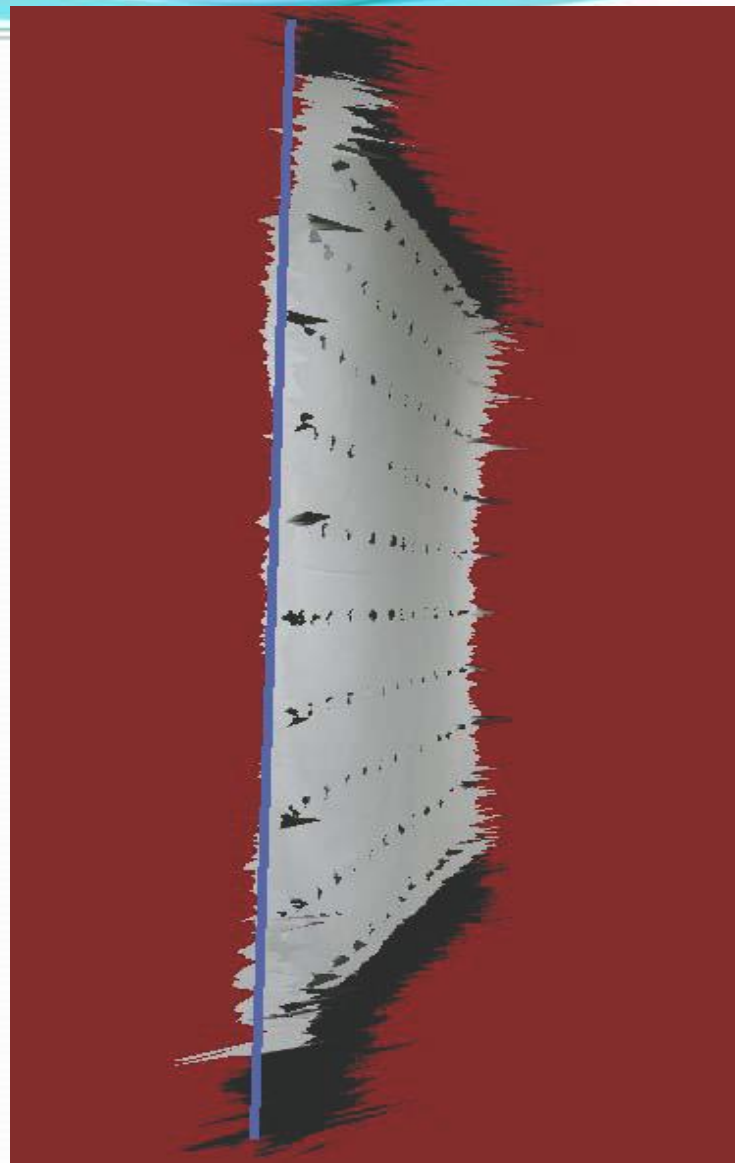
# Object Segmentation in KinectFusion



# Raw Camera Space 3D Reconstruction



lens Distortion



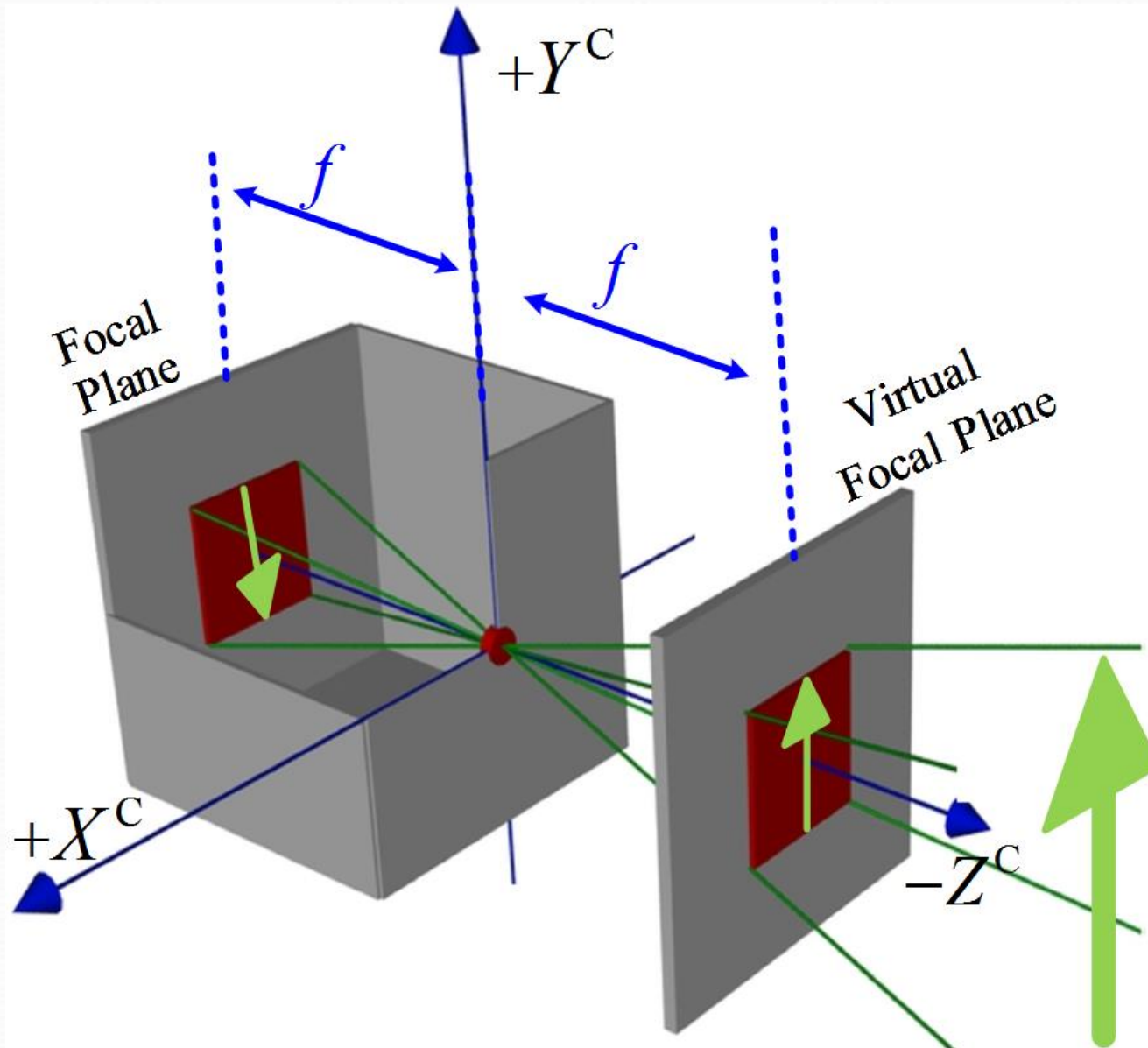
Depth Distortion



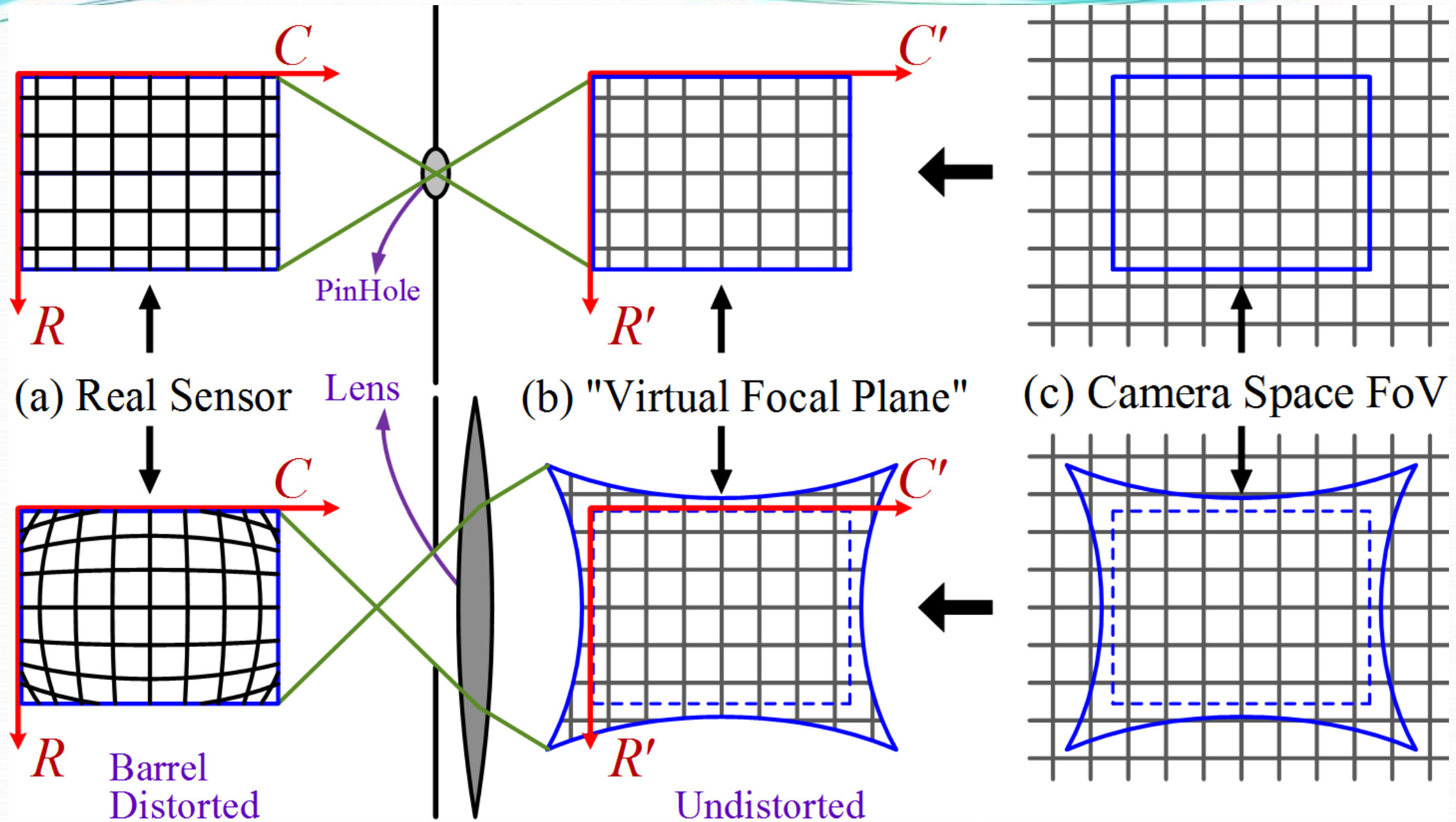
# Introduction

- Goal: given a RGB-D camera, show undistorted 3D reconstruction with color (RGB) on GPU
- Camera: KinectV2
- Streams:  
Depth, NearIR:  $424 * 512$  ; RGB :  $1080 * 1920$
- Plan:
  - determine best-fit calibration system
  - choose corresponding parallel (on GPU) calibration method
  - build models in demand
  - calibrate and reconstruct

# Pinhole-Camera Model

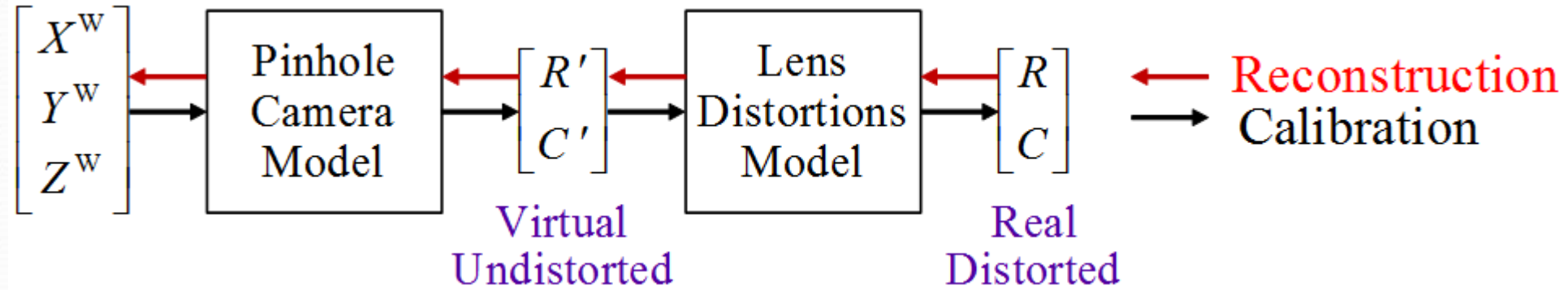


- From Camera Space to Image Space with Lens Distortions



# Academic Background

- **Pinhole-Camera Model** (Reconstruction and Calibration)



Intrinsic Matrix

$$K = \begin{bmatrix} f_c & s & t_c \\ 0 & f_r & t_r \\ 0 & 0 & 1 \end{bmatrix}$$

Extrinsic Matrix

$$\begin{bmatrix} R_{3 \times 3} & T_{3 \times 1} \end{bmatrix}$$

Pinhole Camera Matrix :

$$M = K \begin{bmatrix} R_{3 \times 3} & T_{3 \times 1} \end{bmatrix} = \begin{bmatrix} m_{11} & m_{12} & m_{13} & m_{14} \\ m_{21} & m_{22} & m_{23} & m_{24} \\ m_{31} & m_{32} & m_{33} & m_{34} \end{bmatrix}$$

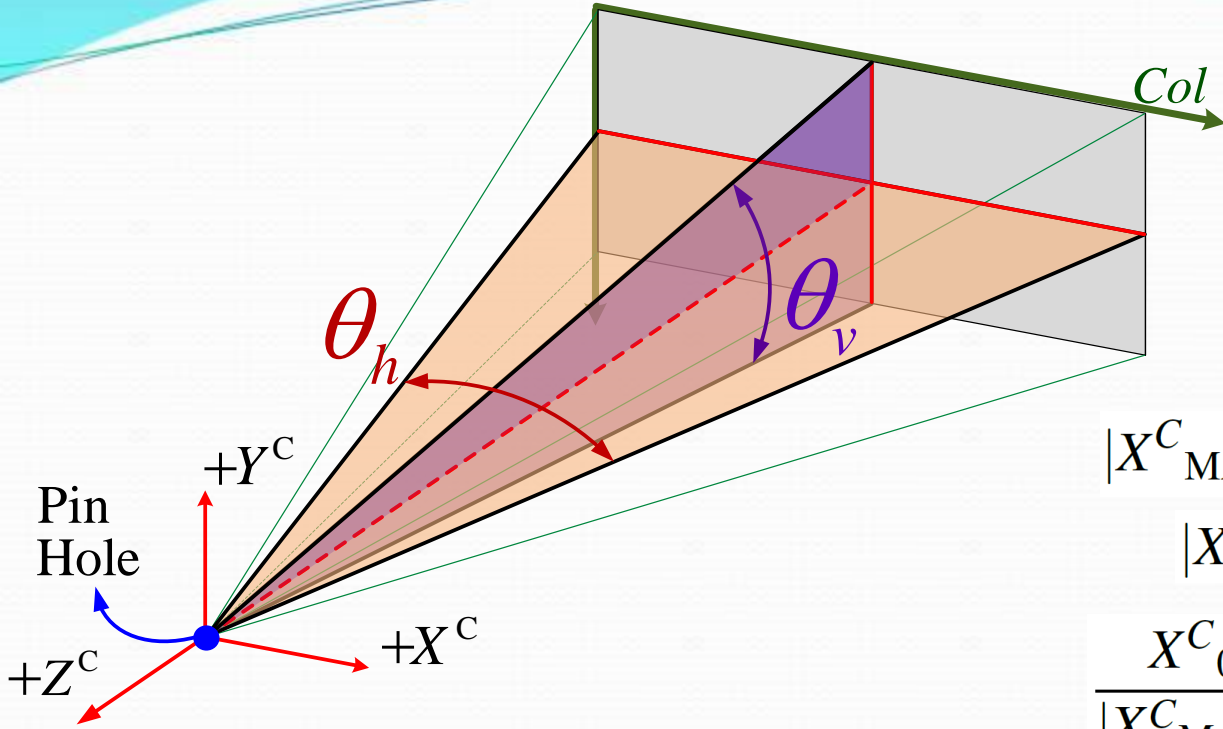
$$C' = C(1 + k_1 r^2 + k_2 r^4 + k_3 r^6) + [p_1(r^2 + 2C^2) + 2p_2 CR]$$

$$R' = R(1 + k_1 r^2 + k_2 r^4 + k_3 r^6) + [p_2(r^2 + 2R^2) + 2p_1 CR]$$

Distortion Parameters:  $k_1/k_2/k_3/p_1/p_2$



# Raw Camera Space 3D Reconstruction



$$Z^C[m, n] = -\beta D[m, n]$$

65535.0

$$X^C[m, n] = a[m, n] \cdot |Z^C[m, n]|$$

$$Y^C[m, n] = b[m, n] \cdot |Z^C[m, n]|$$

$$|X^C_{MAX}| = |Z^C_0| \cdot \tan(\theta_h/2)$$

$$|X^C_0| = |Z^C_0| \cdot \tan(\alpha_0)$$

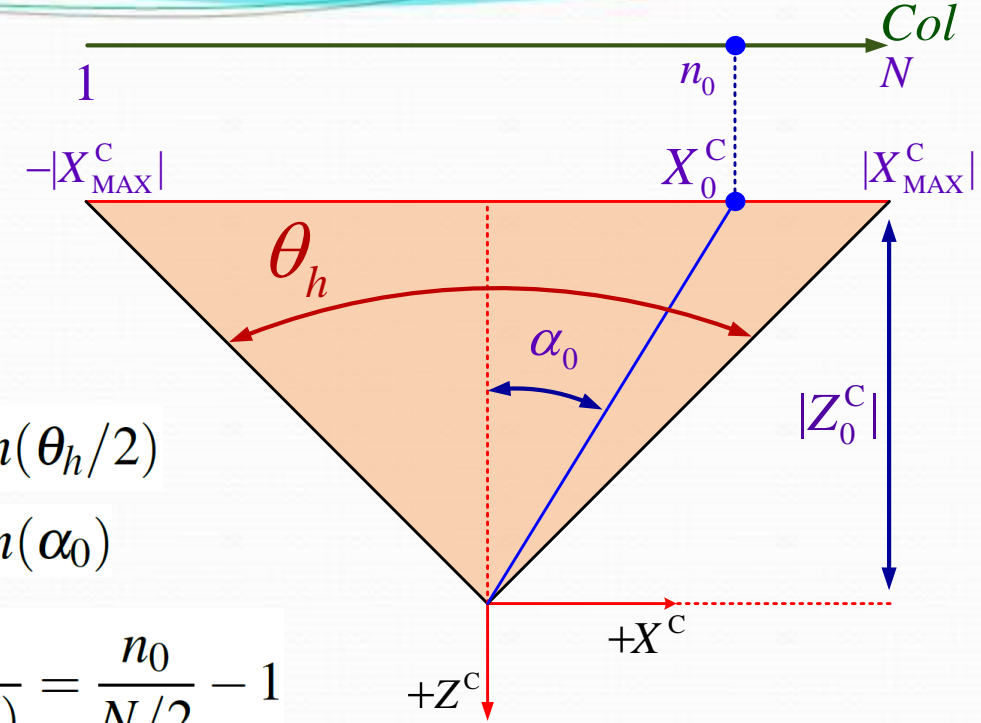
$$\frac{X^C_0}{|X^C_{MAX}|} = \frac{\tan(\alpha_0)}{\tan(\theta_h/2)} = \frac{n_0}{N/2} - 1$$

$$X^C[m, n] = \tan(\theta_h/2) \cdot \left(\frac{n}{N/2} - 1\right) \cdot |Z^C[m, n]|$$

$$Y^C[m, n] = \tan(\theta_v/2) \cdot \left(\frac{m}{M/2} - 1\right) \cdot |Z^C[m, n]|$$

$$a[m, n] = \tan(\theta_h/2) \cdot \left(\frac{n}{N/2} - 1\right)$$

$$b[m, n] = \tan(\theta_v/2) \cdot \left(\frac{m}{M/2} - 1\right)$$



- Pinhole-Camera Model (Reconstruction and Calibration)

$$M = K \begin{bmatrix} R_{3 \times 3} & T_{3 \times 1} \end{bmatrix} = \begin{bmatrix} m_{11} & m_{12} & m_{13} & m_{14} \\ m_{21} & m_{22} & m_{23} & m_{24} \\ m_{31} & m_{32} & m_{33} & m_{34} \end{bmatrix}$$

Distortion Parameters:  $k_1/k_2/k_3/p_1/p_2$

- Raw Camera Space 3D Reconstruction on GPU

$$Z^C[m, n] = -\beta D[m, n]$$

65535.0

$$X^C[m, n] = a[m, n] \cdot |Z^C[m, n]|$$

$$Y^C[m, n] = b[m, n] \cdot |Z^C[m, n]|$$

- Kai's [1] : A Natural Parallel Reconstruction

Pinhole  
Camera  
Model

$$M = \begin{bmatrix} m_{11} & m_{12} & m_{13} & m_{14} \\ m_{21} & m_{22} & m_{23} & m_{24} \\ m_{31} & m_{32} & m_{33} & m_{34} \end{bmatrix}$$

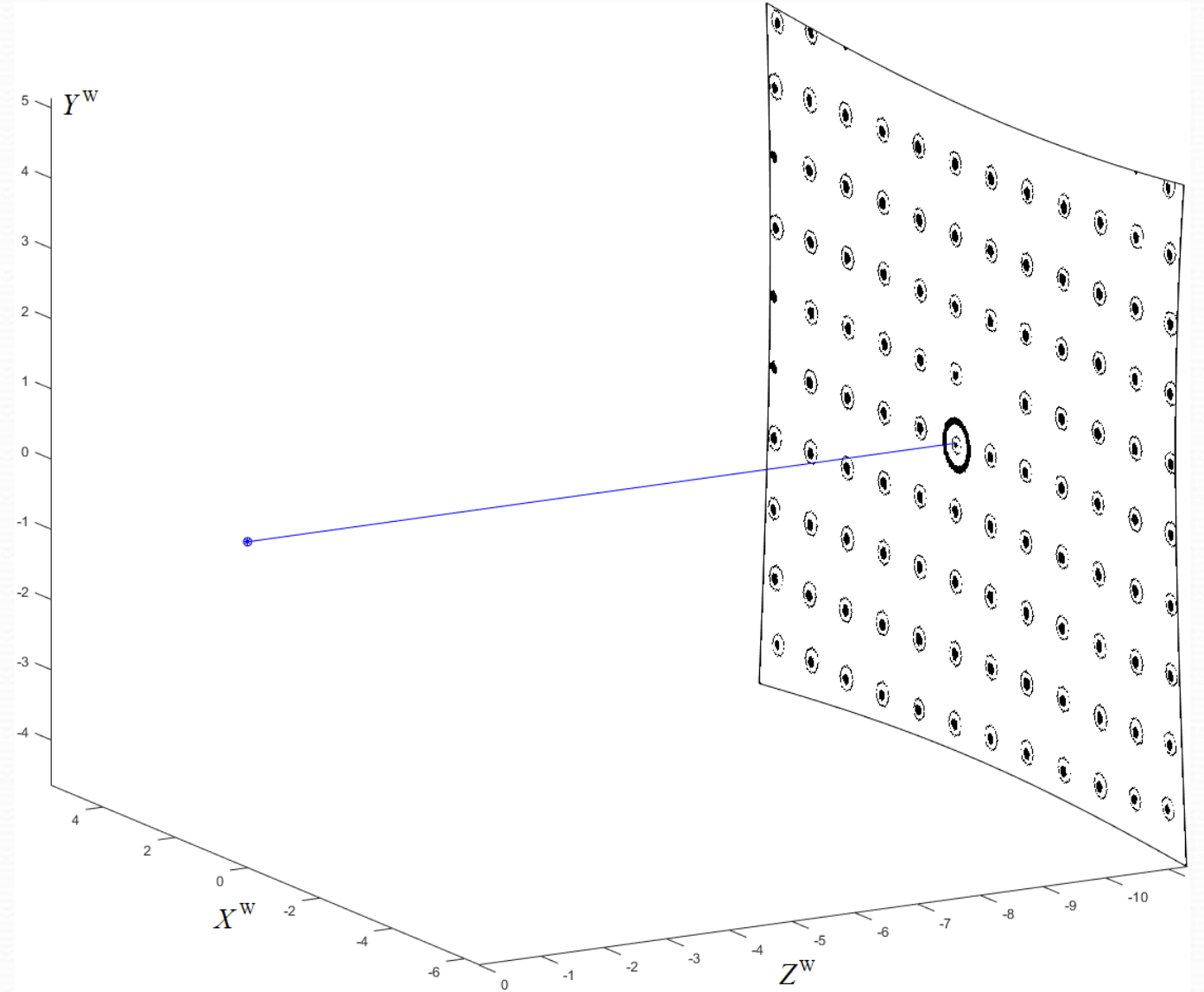
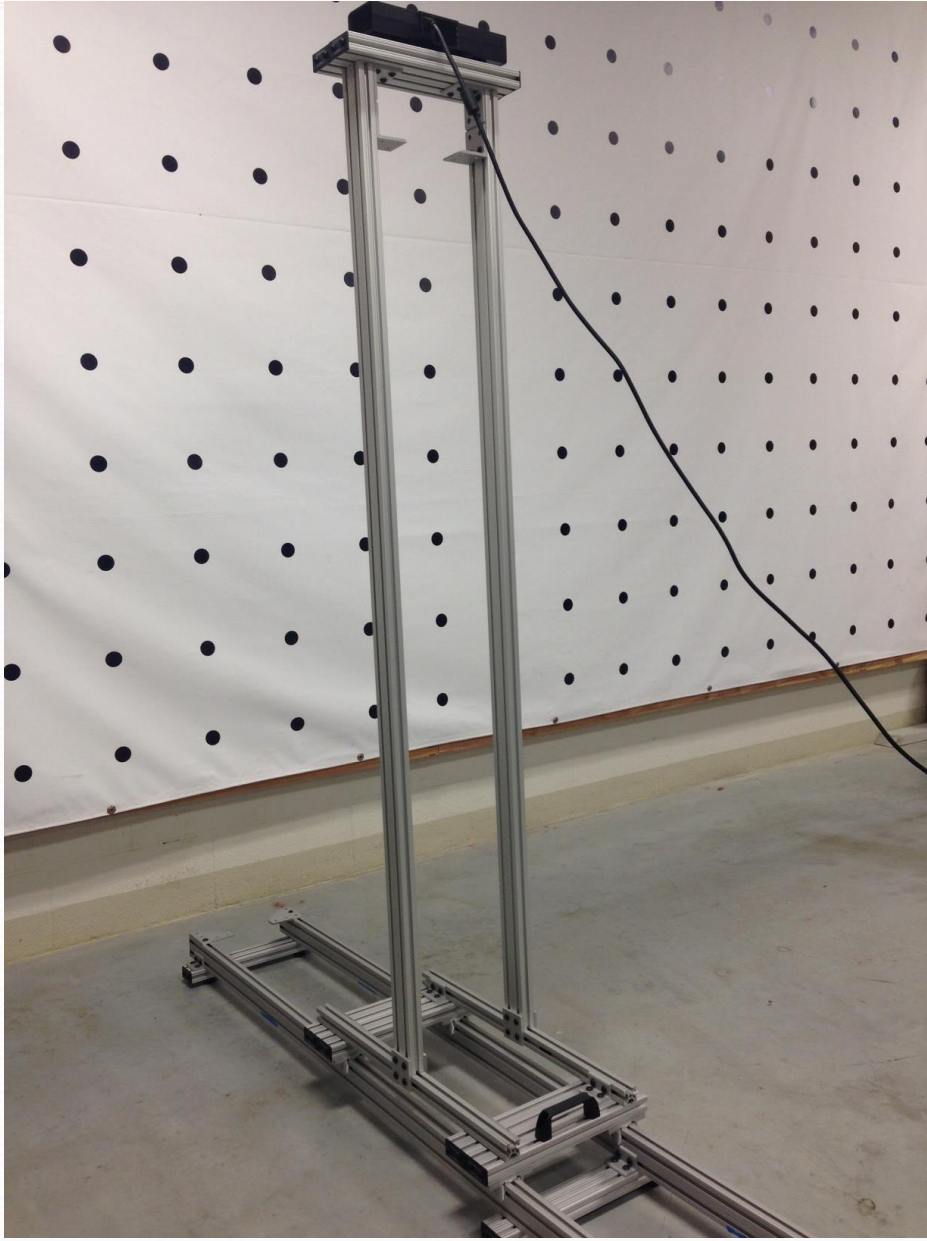


$$X^W[m, n] = a[m, n]Z^W[m, n] + b[m, n]$$

$$Y^W[m, n] = c[m, n]Z^W[m, n] + d[m, n]$$

- Inspiration: find a way to get per-pixel  $Z^W$

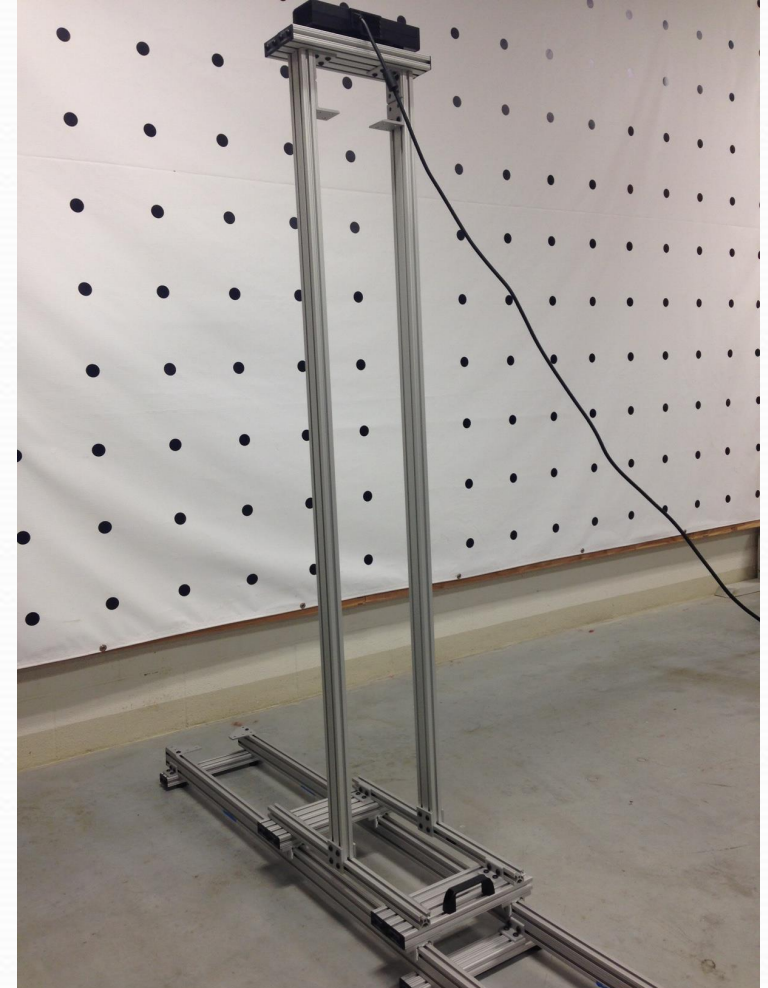
# Rail Calibration System





# Data Collection

- Mount: camera and laser distance measurer
- Want:
  - NIR:  $X^w Y^w Z^w ID$
  - RGB:  $X^w Y^w Z^w RGBD$
- Bound:
  - $Z^w$ : Laser Distance Measurer
  - $X^w Y^w$ : Uniform Round Dot Pattern
- Found (algorithms):
  - Calibration Points (*Row*, *Col*)s Extraction;
  - Corresponding World Space Address Assignment;
  - Non-Linear Dense Transformation





# Calibration Points (*Row, Col*) Extraction;

- Gray-Scaling

$$I_0[m, n] = 0.21R[m, n] + 0.72G[m, n] + 0.07B[m, n]$$

- Histogram Equalization

$$I_1[m, n] = \frac{I_0[m, n] - I_{\text{MIN}}}{I_{\text{MAX}} - I_{\text{MIN}}}$$

- Adaptive Thresholding

$$I_2[m, n] = \begin{cases} 1, & I_1[m, n] - I_b[m, n] - C_0 > 0 \\ 0, & \text{else} \end{cases}$$

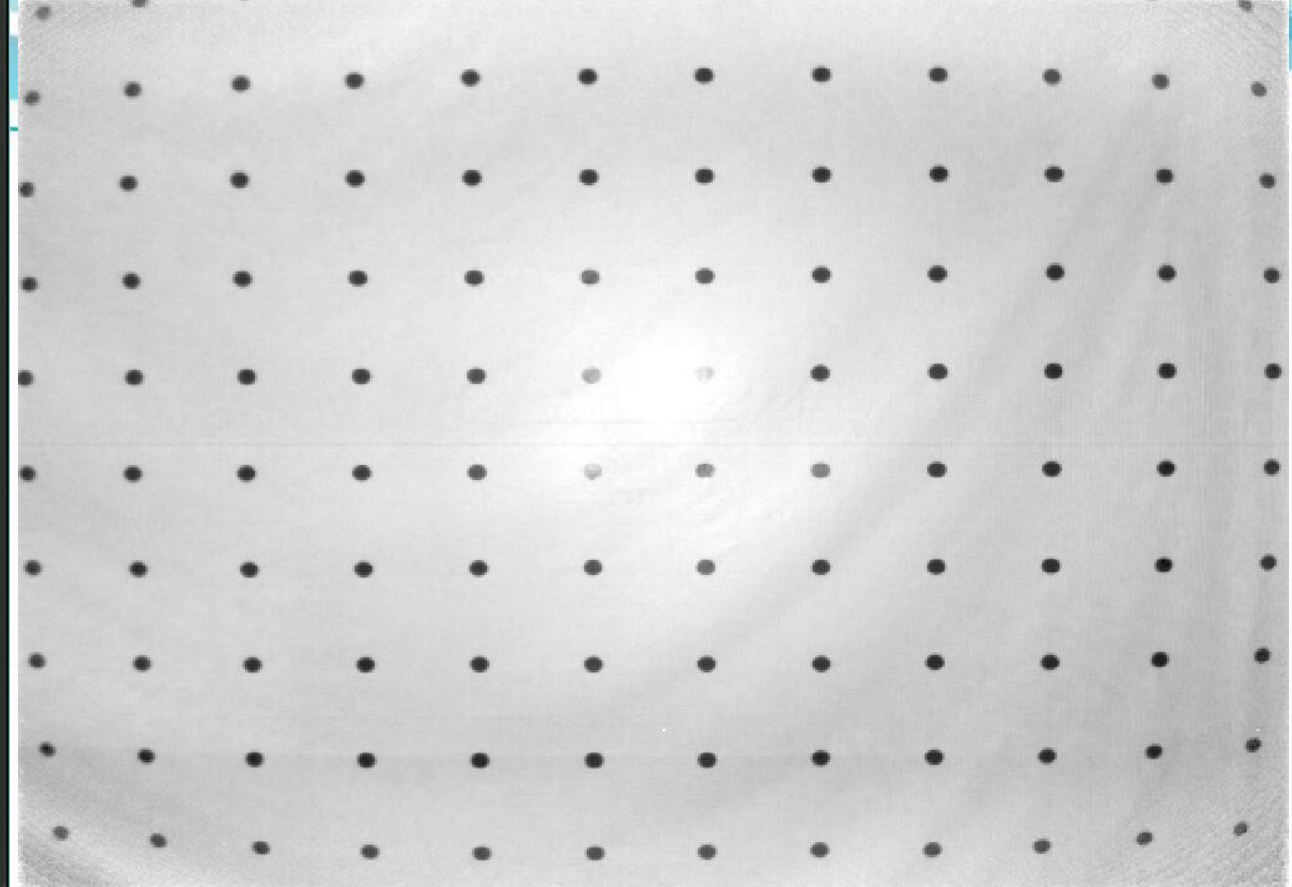
- Round Dot Tracking

<i>E</i>	<i>A</i>	<i>F</i>
<i>B</i>	<i>O</i>	<i>C</i>
<i>G</i>	<i>D</i>	<i>H</i>

$$I_3[m, n] = I_2[m, n] * \frac{(128I_A + 64I_B + 32I_C + 16I_D + 8I_E + 4I_F + 2I_G + I_H)}{255}$$



Raw NIR Image



After Histogram Equalization

$$I_0[m, n] = \frac{g[m, n]}{G} * (1.0 - 0.0) + 0.0 = \frac{g[m, n]}{G}$$

$$CDF(g) = \frac{\sum_{l=1}^g PMF[l]}{M \times N}$$

$$CDF(g_{\min}) = 0.01$$

$$CDF(g_{\max}) = 0.99$$

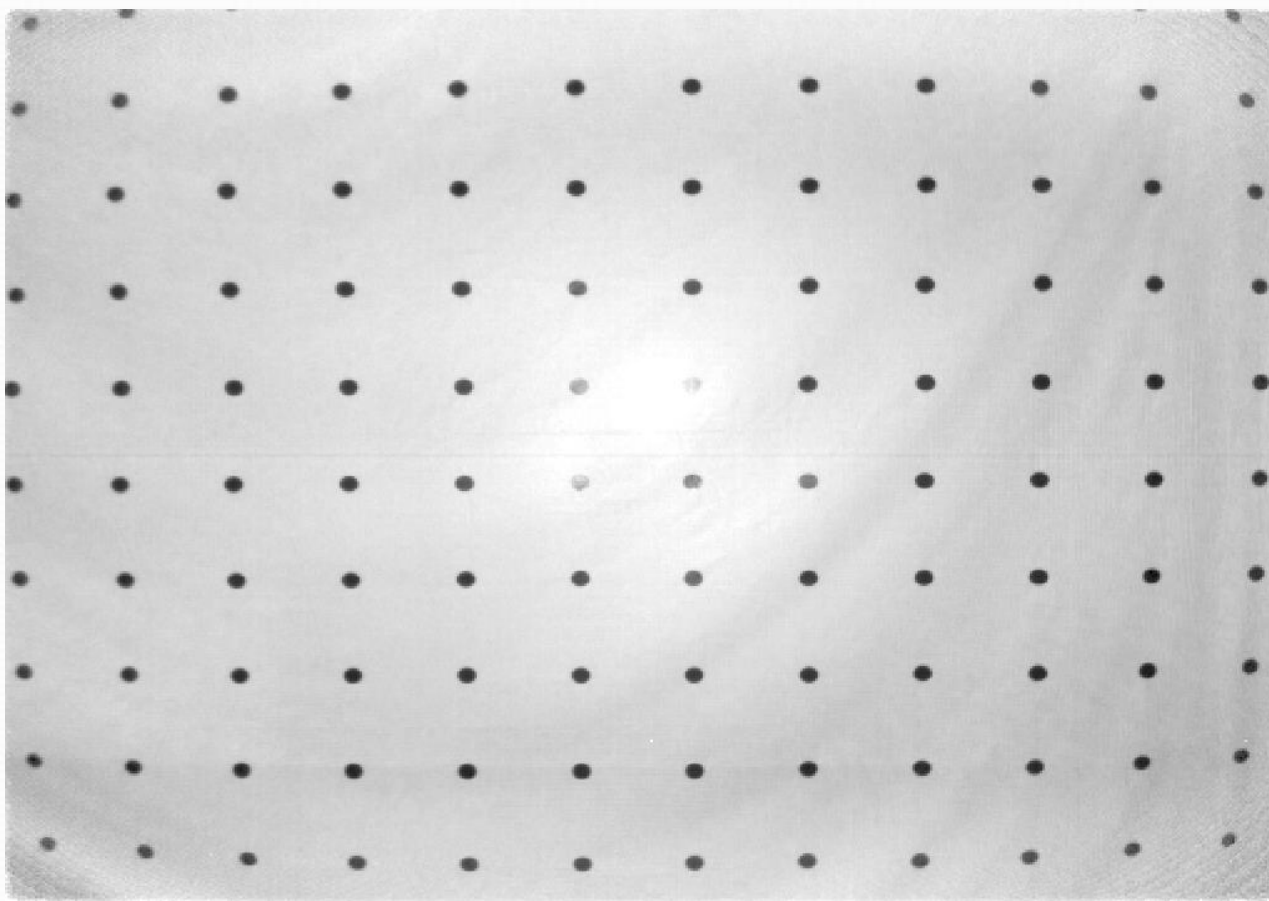
$$I_{\min} = g_{\min} / G$$

$$I_{\max} = g_{\max} / G$$

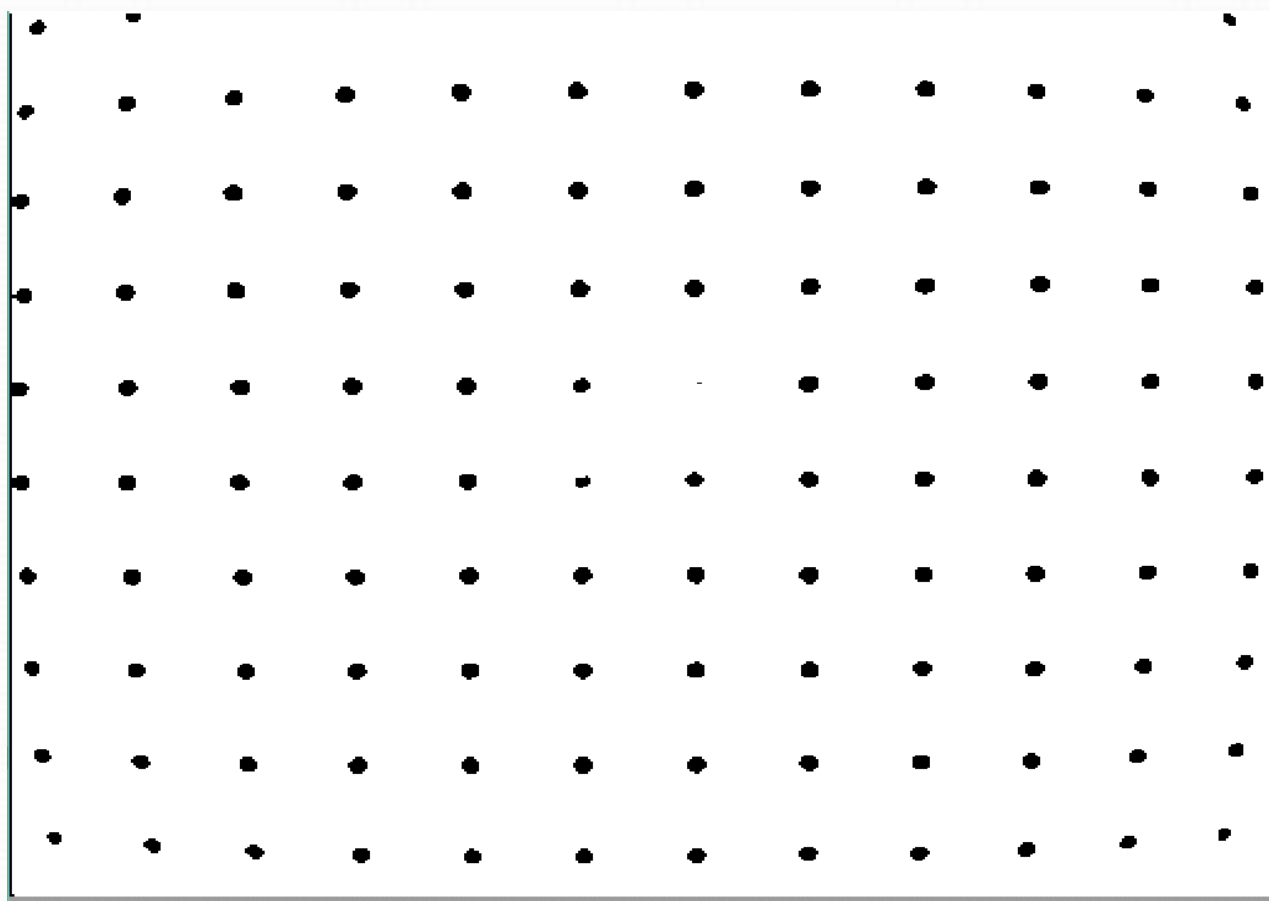
$$I_1[m, n] = \frac{I_0[m, n] - I_{\min}}{I_{\max} - I_{\min}}$$

- Adaptive Thresholding

$$I_2[m,n] = \begin{cases} 1, & I_1[m,n] - I_b[m,n] - C_0 > 0 \\ 0, & \text{else} \end{cases}$$



Histogram Equalized



Binarized

- Round Dot Tracking

<i>E</i>	<i>A</i>	<i>F</i>
<i>B</i>	<i>O</i>	<i>C</i>
<i>G</i>	<i>D</i>	<i>H</i>

$$I_3[m, n] = I_2[m, n] * \frac{(128I_A + 64I_B + 32I_C + 16I_D + 8I_E + 4I_F + 2I_G + I_H)}{255}$$

*if* ( $I_O \& 0x80 == 1$ ), *then*, marker *A* is valid ( go Up )

*if* ( $I_O \& 0x40 == 1$ ), *then*, marker *B* is valid ( go Left)

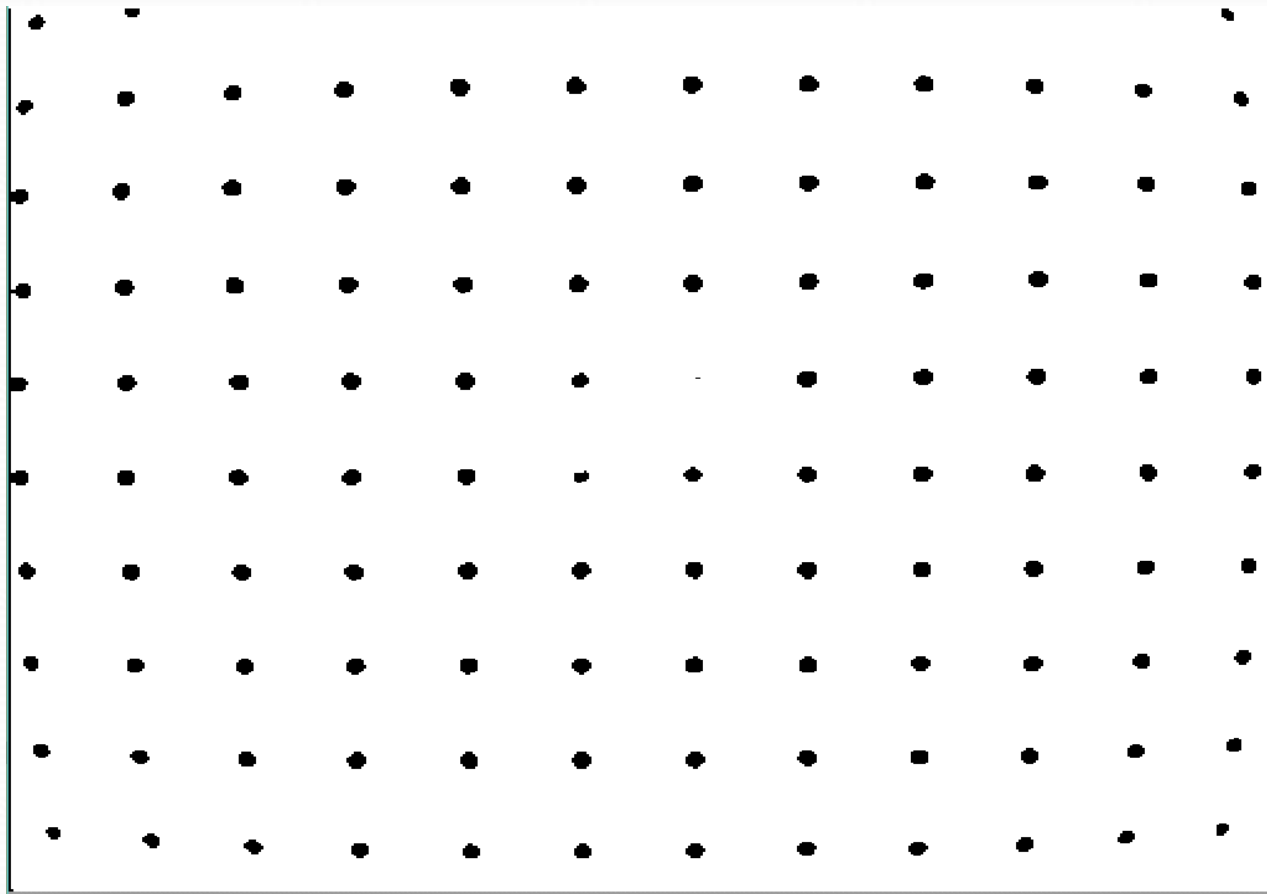
*if* ( $I_O \& 0x20 == 1$ ), *then*, marker *C* is valid ( go Right )

*if* ( $I_O \& 0x10 == 1$ ), *then*, marker *D* is valid ( go Down )

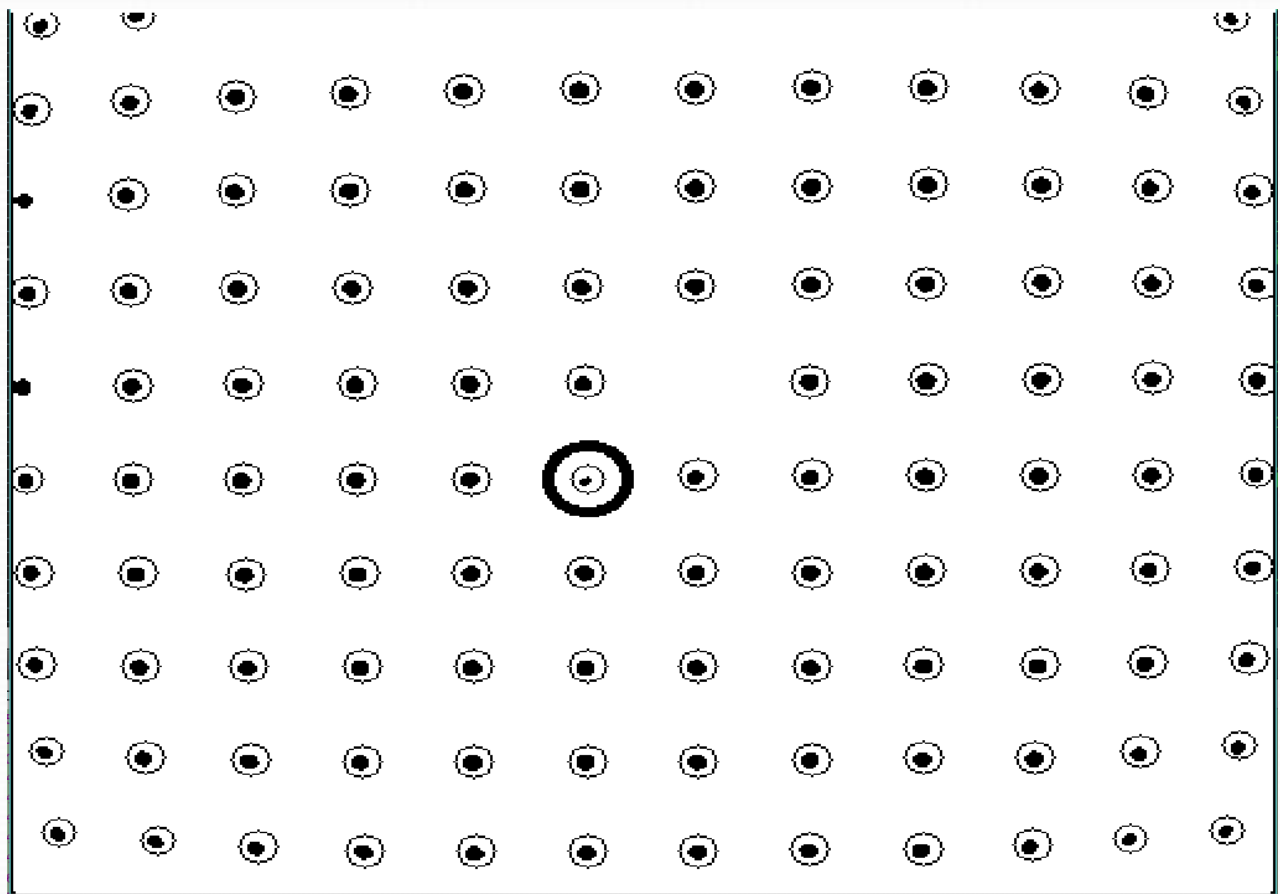
Anchor !=0 → Detect Valid → Flip Valid → Get Area + Bounding Box



# Traverse and Extract on CPU



Binarized Image



Dots' Centers Extracted

# World Space Address Assignment

- Travers every 4 Square-Shaped points and find best  $A_0$ , which corresponds to the best-fit “Unit One” (228mm) in Image Space:

Get Linear Mapping matrix  $A_0 \rightarrow$  Transform all  $(R, C)$  to  $(X^W, Y^W)$

$\rightarrow$  Count  $(N_v)$  valid points with integer  $X^W/Y^W \rightarrow$  Find best  $A_0$  who generates the largest  $N_v$ .

$$\begin{array}{cc}
 (0, 1) & (1, 1) \\
 \bullet & \bullet \\
 \bullet & \bullet \\
 (0, 0) & (1, 0)
 \end{array}
 \begin{bmatrix} zX^W \\ zY^W \\ z \end{bmatrix} = A_0 \begin{bmatrix} C \\ R \\ 1 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \begin{bmatrix} C \\ R \\ 1 \end{bmatrix}$$

- Translate Origin to the Center Dot

$$\begin{aligned}
 c_h &= (512 - 1) / 2 = 255.5 \\
 r_h &= (424 - 1) / 2 = 211.5
 \end{aligned}
 \begin{bmatrix} zx_h \\ zy_h \\ z \end{bmatrix} = A_0 \cdot \begin{bmatrix} c_h \\ r_h \\ 1 \end{bmatrix}
 \quad
 \begin{aligned}
 c_h &= \text{round}(c_h) \\
 r_h &= \text{round}(r_h)
 \end{aligned}
 \quad
 A_1 = T \cdot A_0 = \begin{bmatrix} 1 & 0 & -x_h \\ 0 & 1 & -y_h \\ 0 & 0 & 1 \end{bmatrix} \cdot A_0$$

# World Space Address Assignment

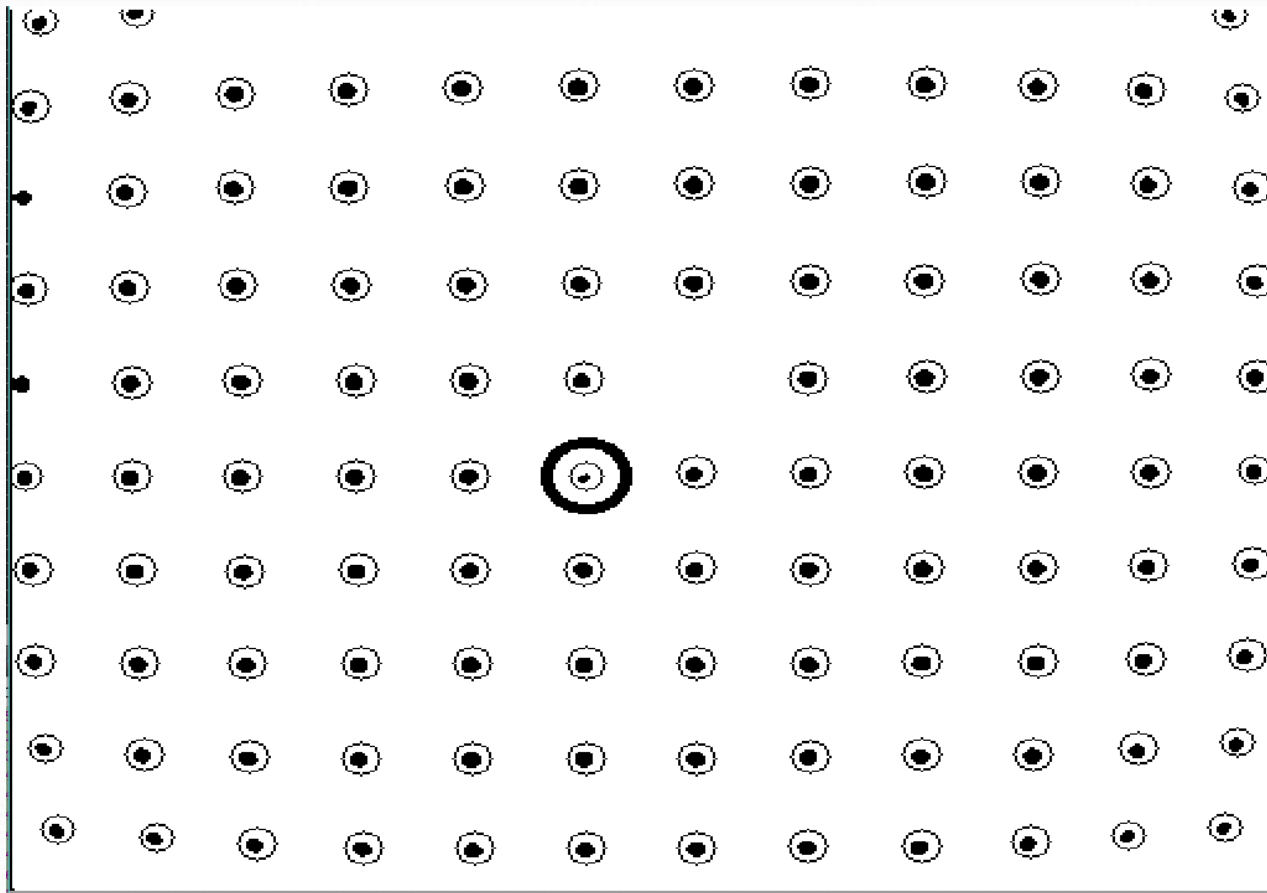
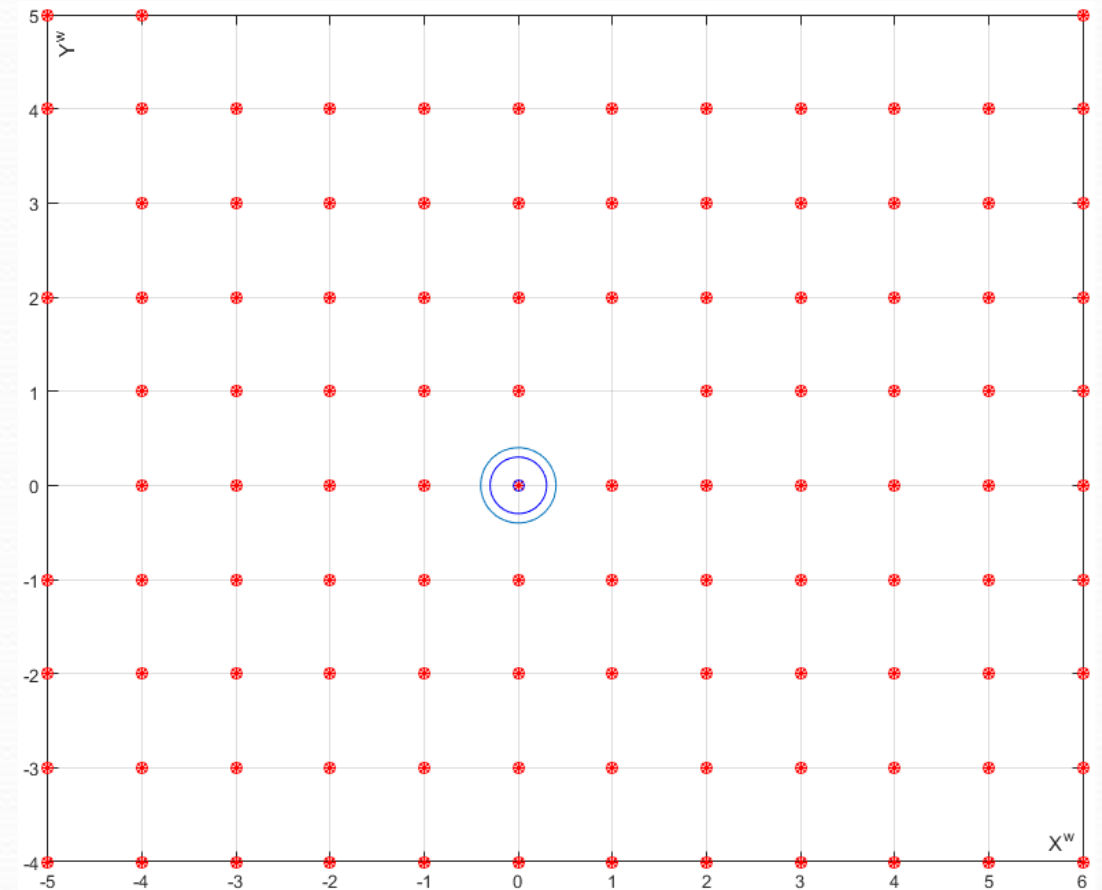


Image Space Calibration Points



Assigned World Space  $X^w Y^w$

# Two Dimensional Polynomial Mapping

- (First Order Perspective Transformation)

$$\begin{bmatrix} zX^W \\ zY^W \\ z \end{bmatrix} = A_0 \begin{bmatrix} C \\ R \\ 1 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \begin{bmatrix} C \\ R \\ 1 \end{bmatrix}$$

- Second Order

$$X^W = a_{11}C^2 + a_{12}CR + a_{13}R^2 + a_{14}C + a_{15}R + a_{16}$$

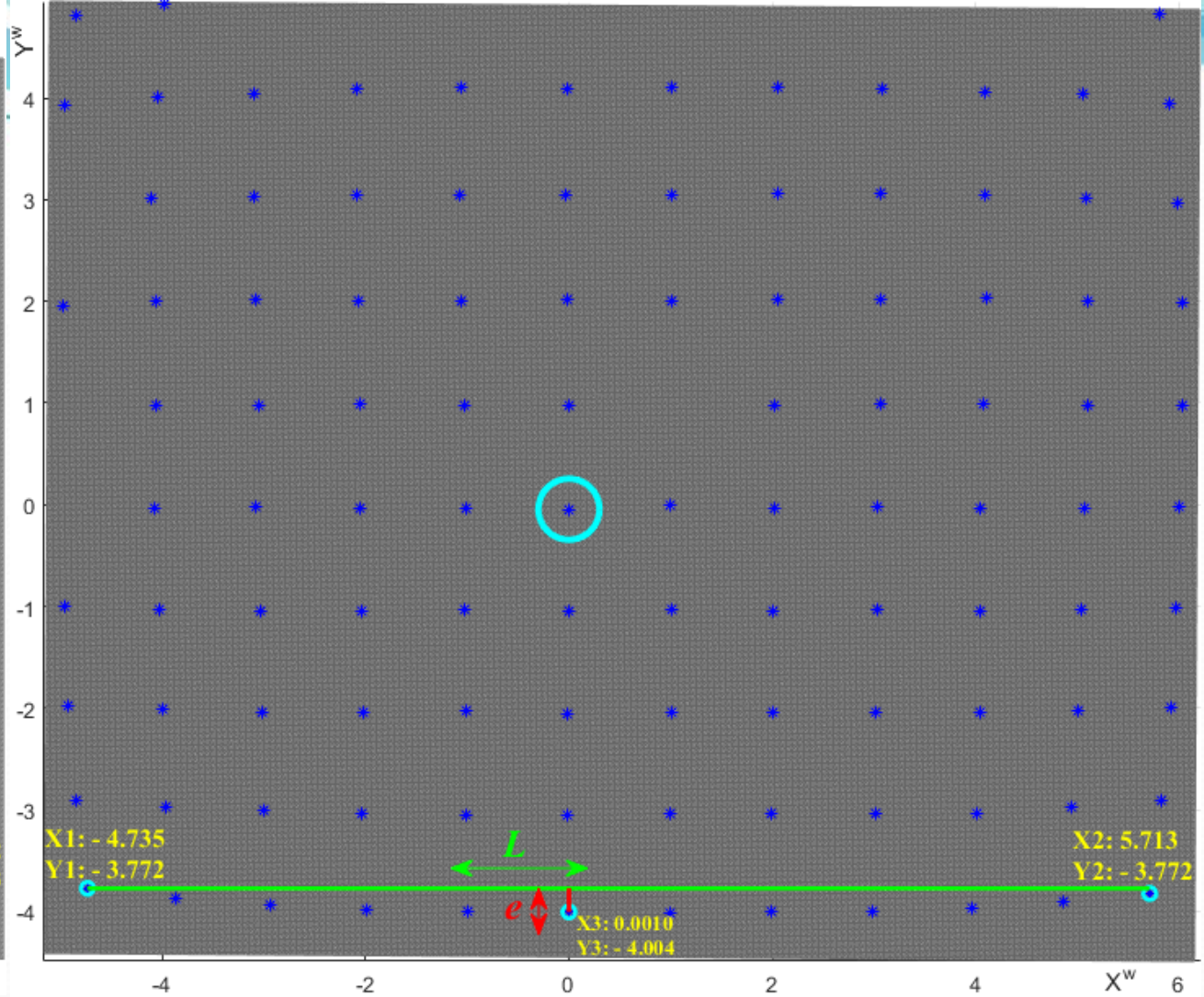
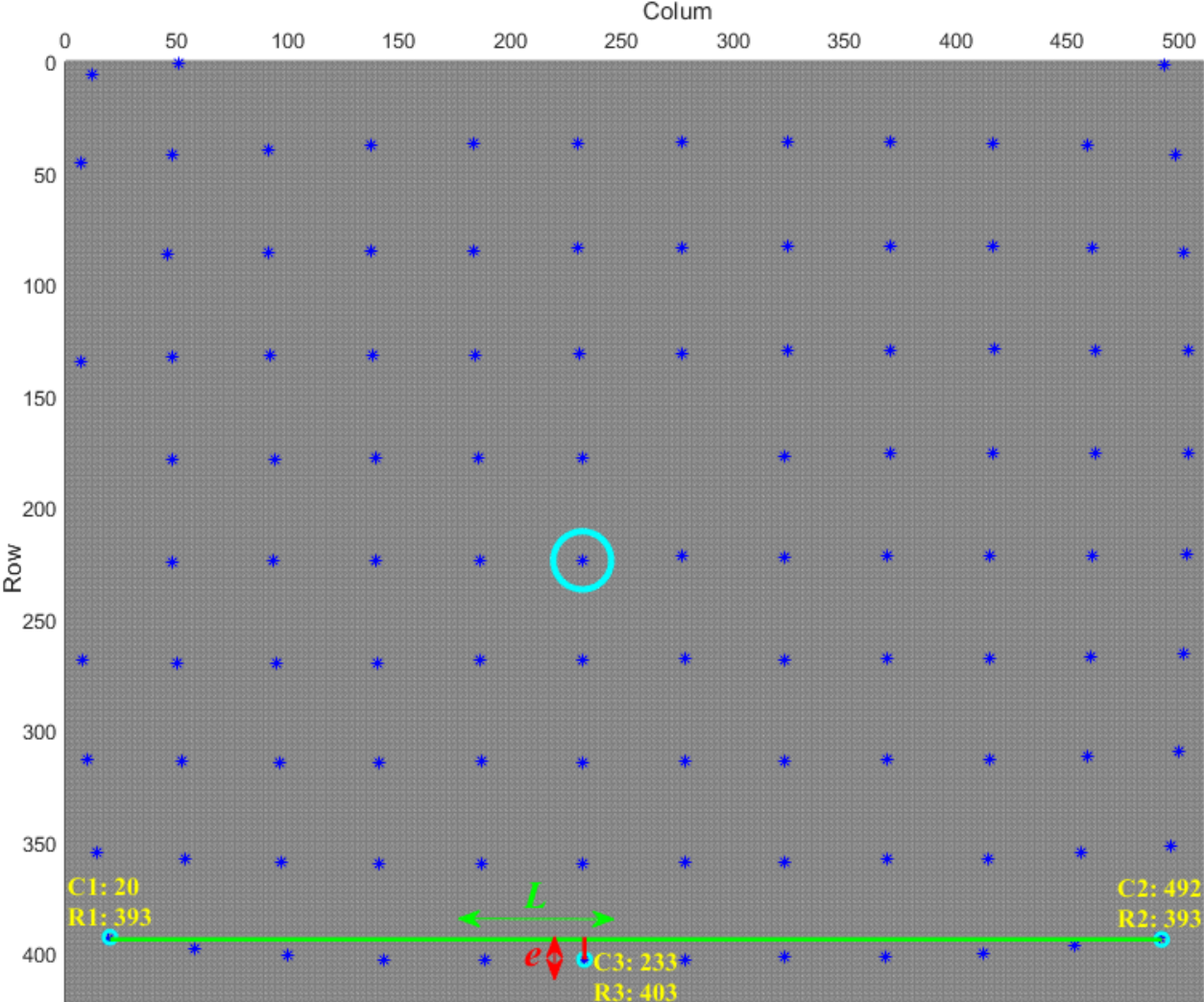
$$Y^W = a_{21}C^2 + a_{22}CR + a_{23}R^2 + a_{24}C + a_{25}R + a_{26}$$

- Fourth Order

$$\begin{aligned} X^W = & a_{11}C^4 + a_{12}C^3R + a_{13}C^2R^2 + a_{14}CR^3 + a_{15}R^4 + a_{16}C^3 + a_{17}C^2R \dots \\ & + a_{18}CR^2 + a_{19}R^3 + a_{110}C^2 + a_{111}CR + a_{112}R^2 + a_{113}C + a_{114}R + a_{115} \end{aligned}$$

$$\begin{aligned} Y^W = & a_{21}C^4 + a_{22}C^3R + a_{23}C^2R^2 + a_{24}CR^3 + a_{25}R^4 + a_{26}C^3 + a_{27}C^2R \dots \\ & + a_{28}CR^2 + a_{29}R^3 + a_{210}C^2 + a_{211}CR + a_{212}R^2 + a_{213}C + a_{214}R + a_{215} \end{aligned}$$



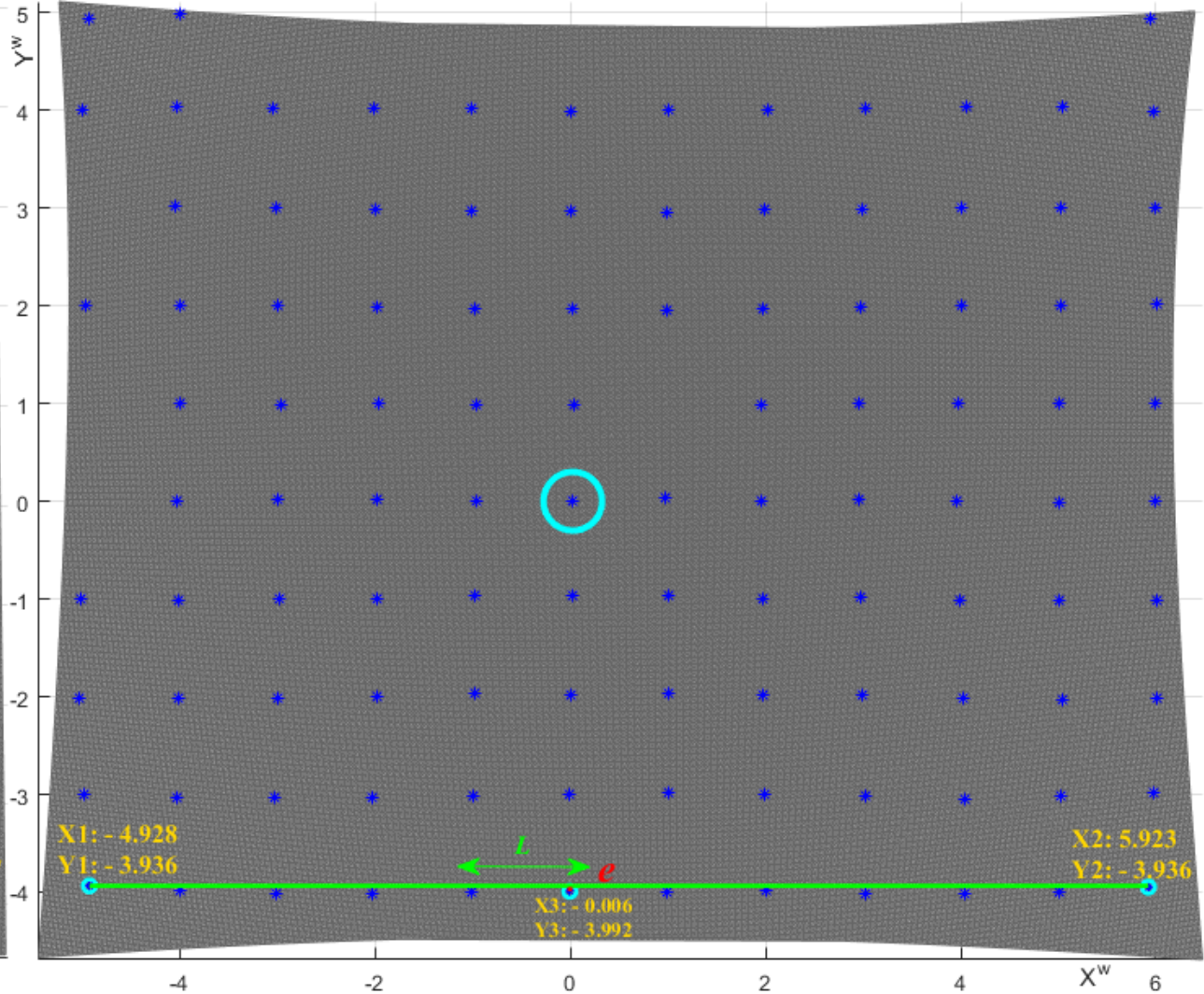
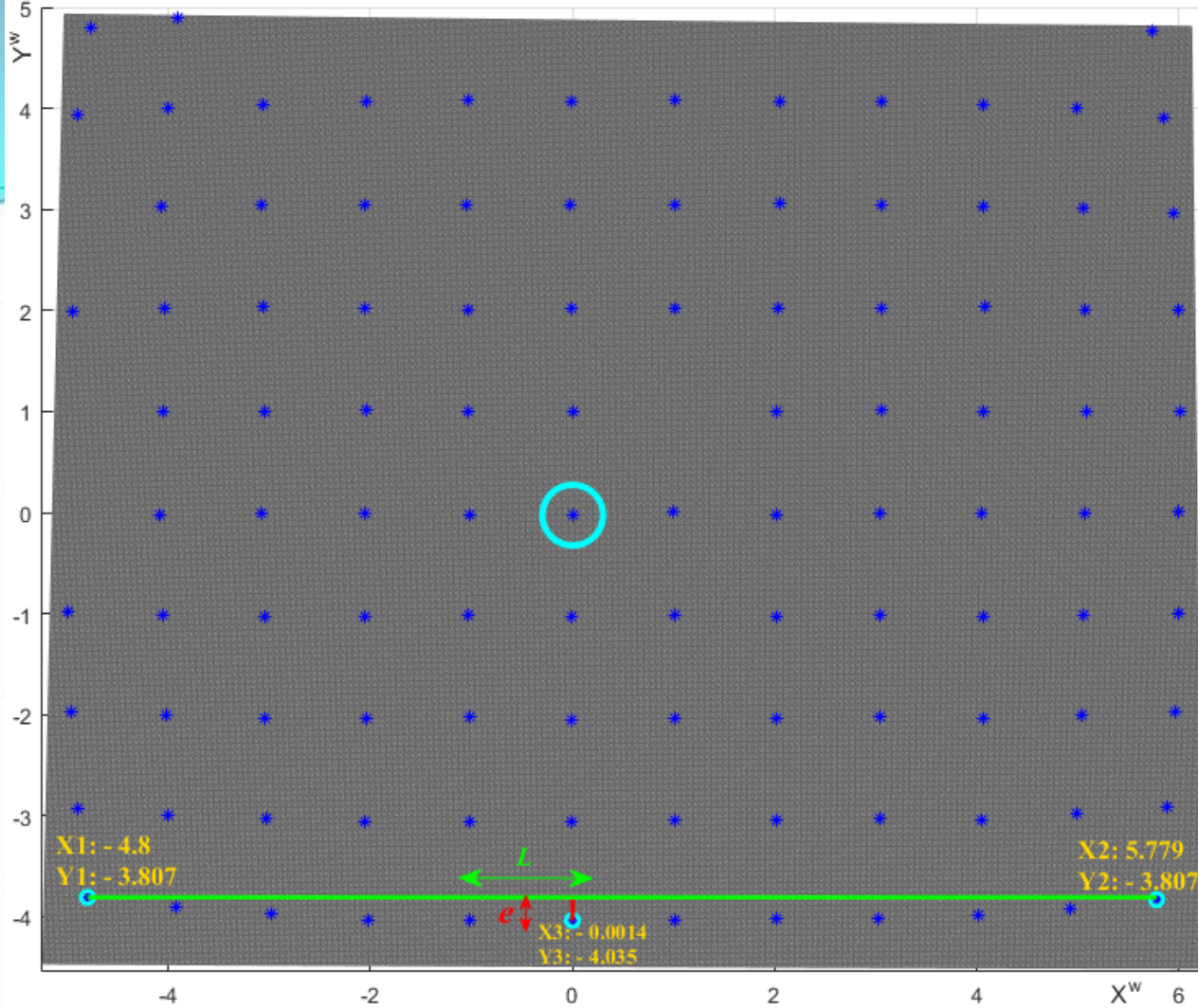


$$d(\%) = e / L$$

$$d_0 = (R3 - R1) / (C2 - C1) = (403 - 393) / (492 - 20) = 2.1\%$$

$$d_1 = (Y1 - Y3) / (X2 - X1) = [-3.772 + 4.004] / [5.713 + 4.735] = 2.2\%$$

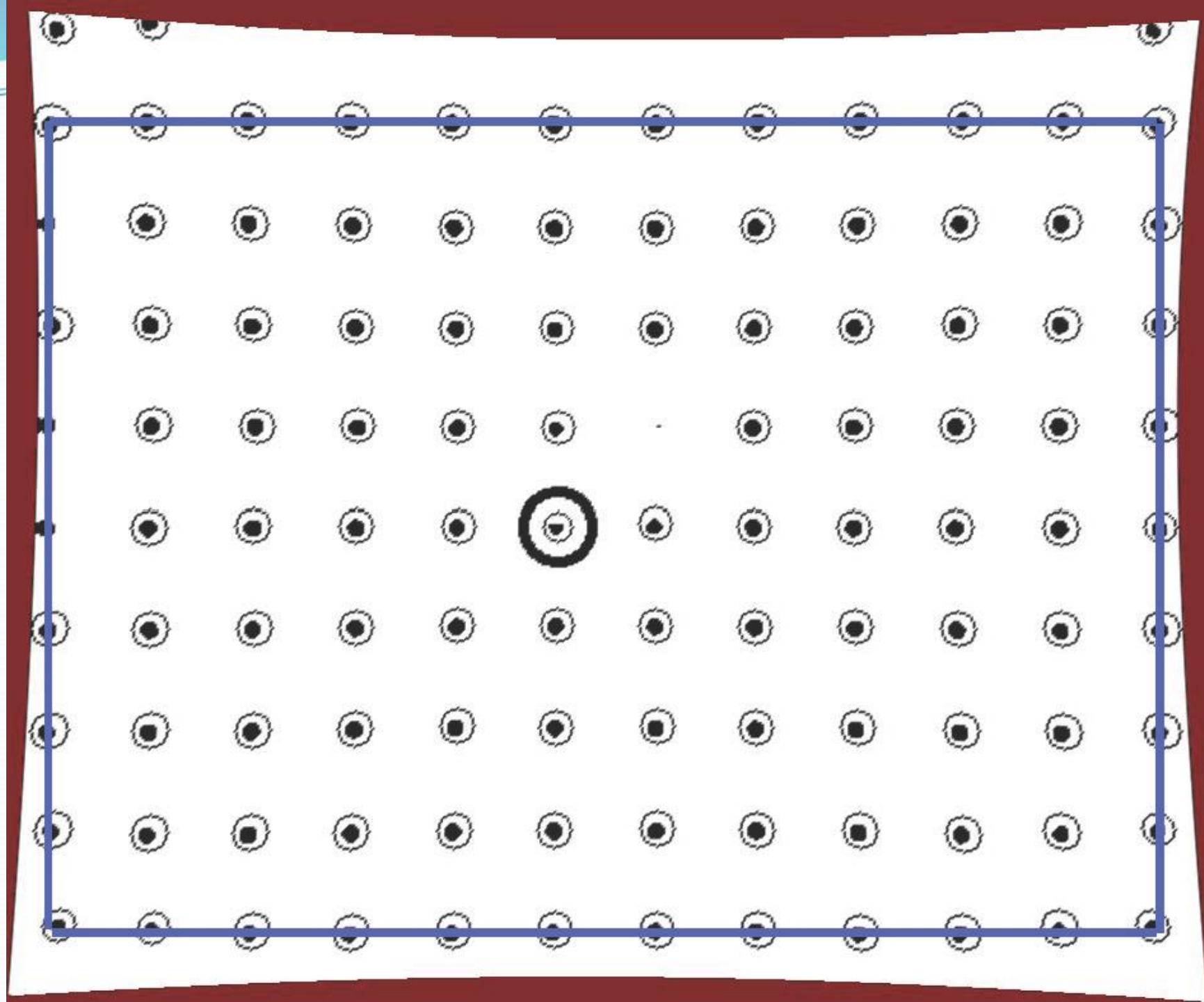




$$d(\%) = e / L$$

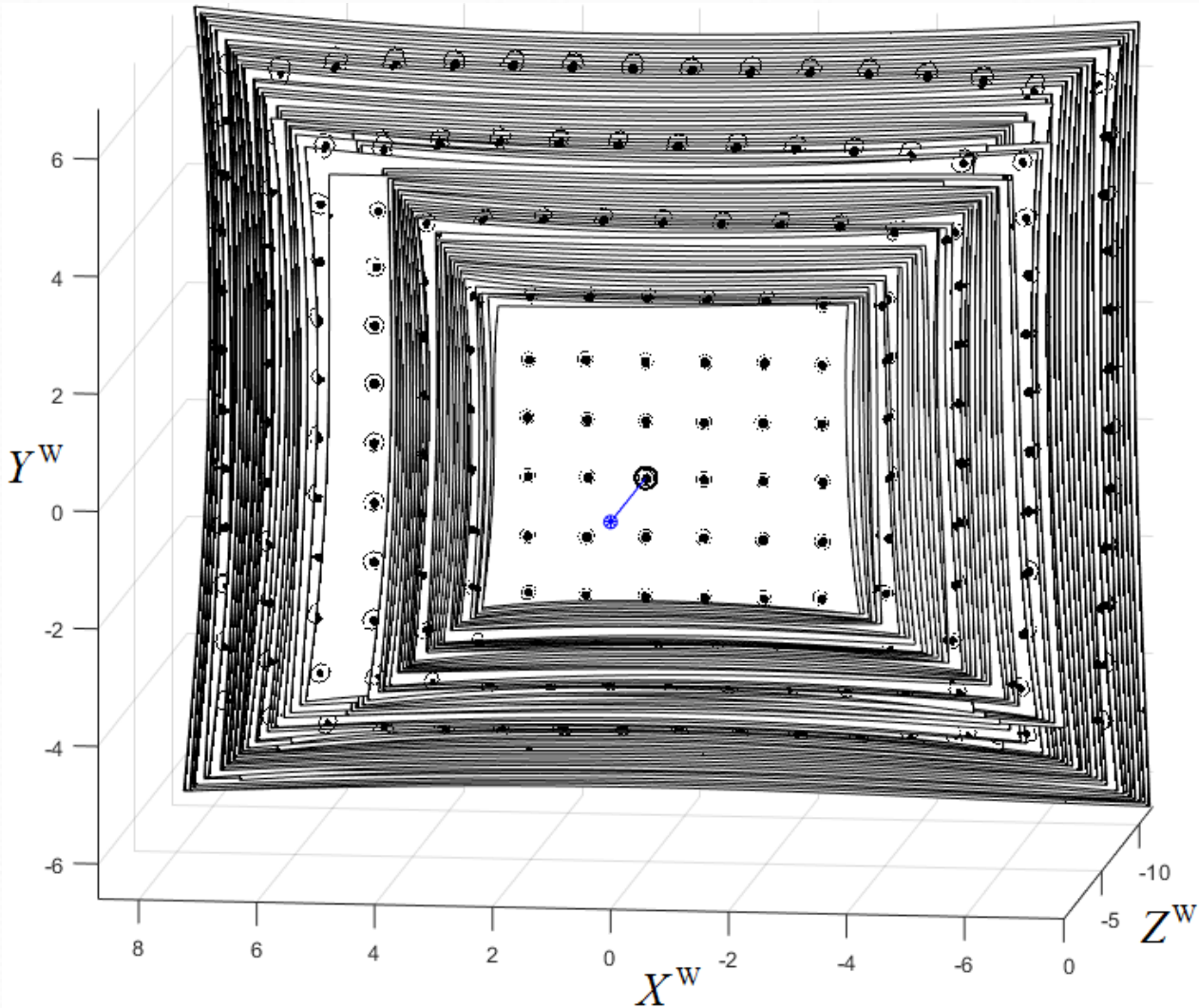
$$d_2 = [-3.807 - (-4.035)] = [5.779 - (-4.8)] = 2.1\%$$

$$d_4 = [-3.936 - (-3.992)] = [5.923 - (-4.928)] = 0.516\%$$

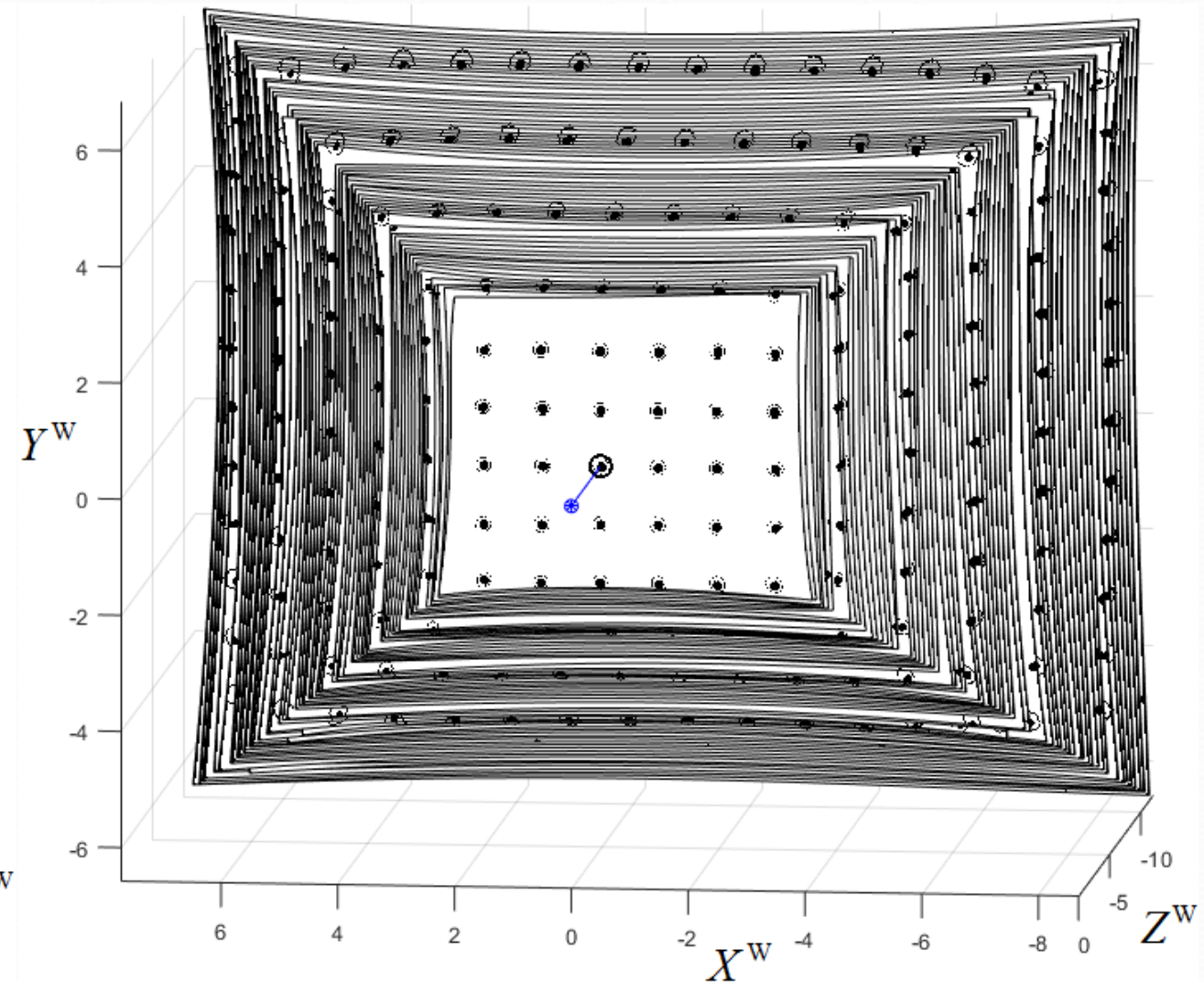




63 frames from 1.165m to 2.565m, 25mm / frame



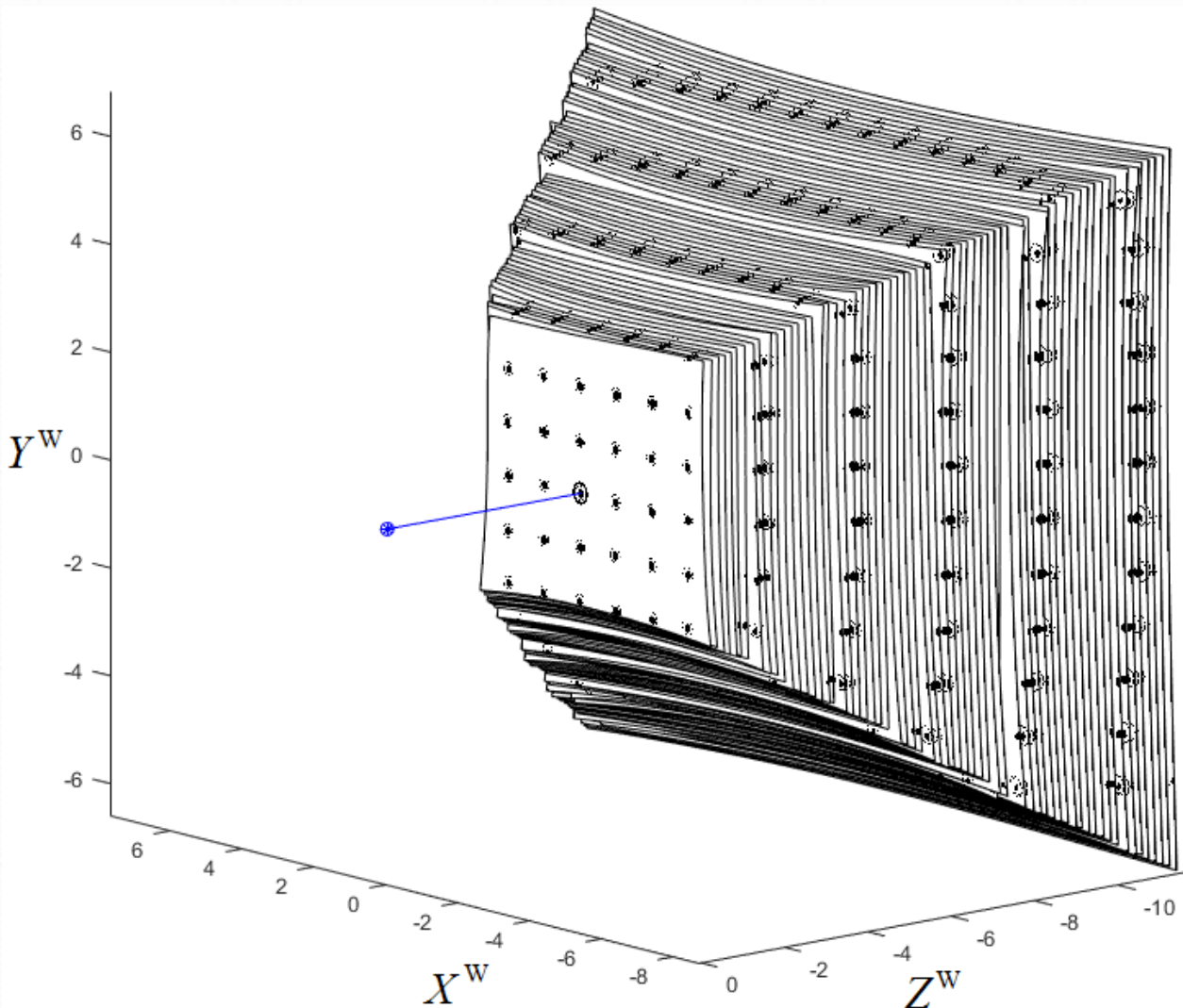
Staggered



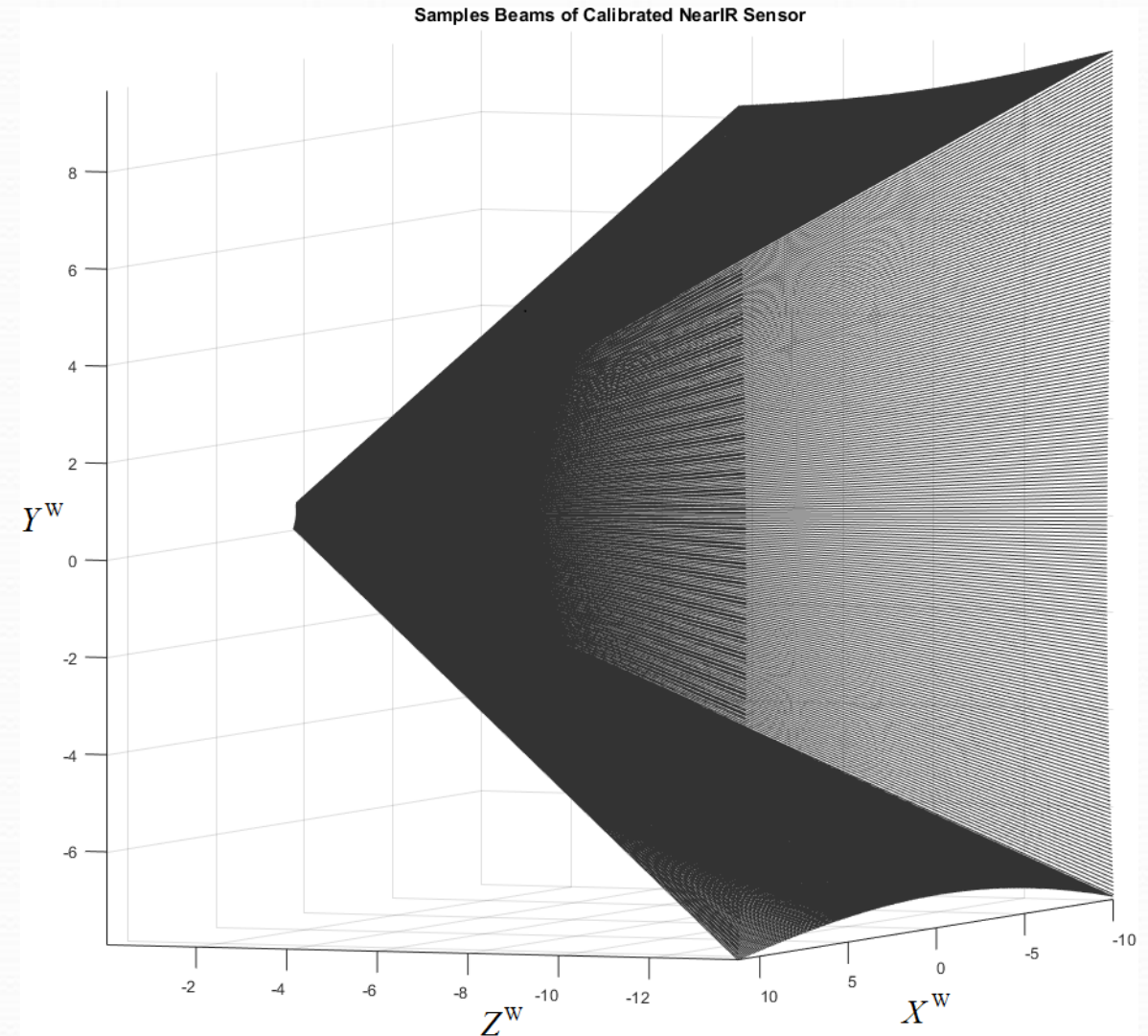
Unified



# 63 frames, generate Pixels' Beam Equations

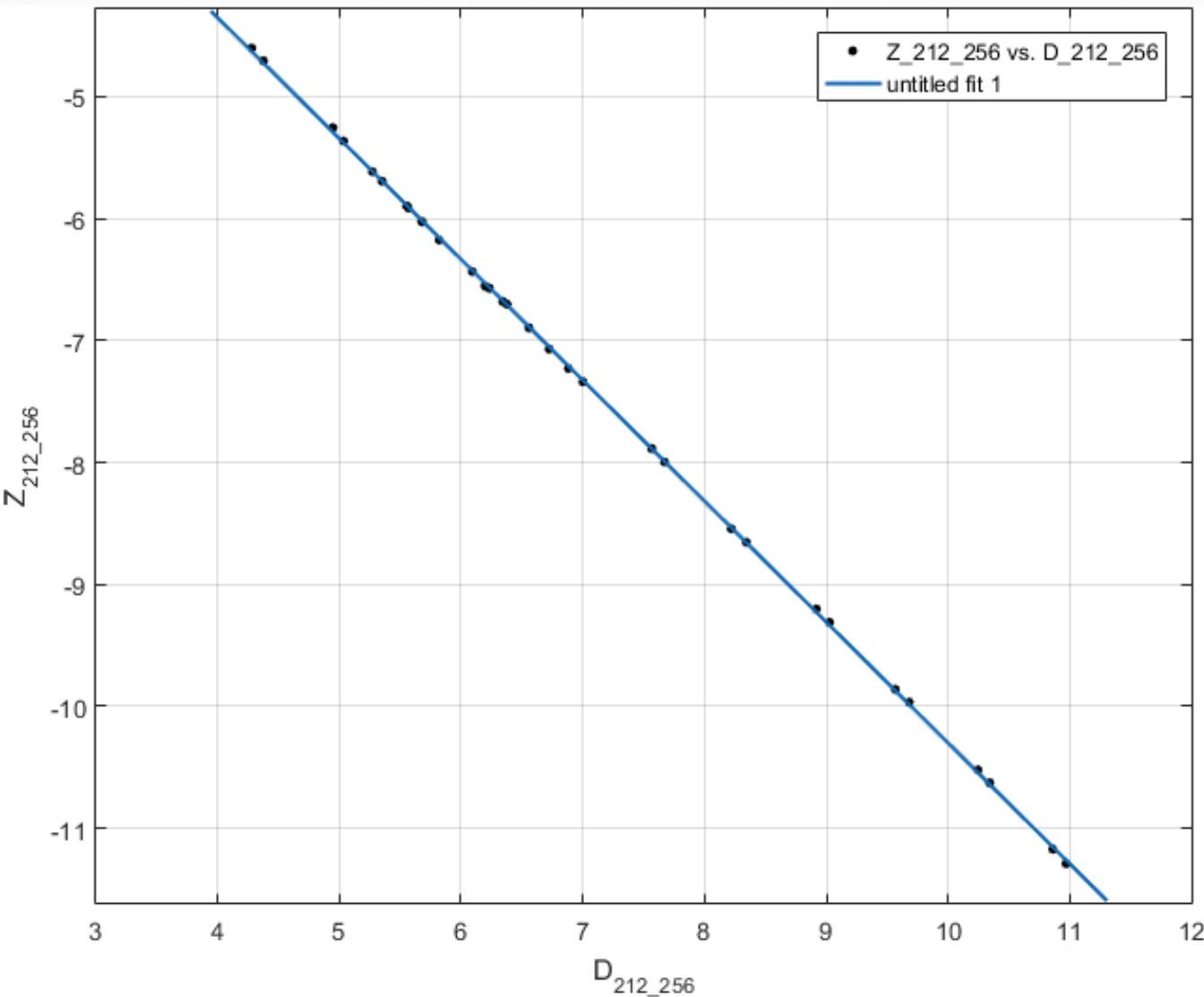


Frustum



Linear  $Z^w$  to  $X^w Y^w$  : Pixels' View

# Per-Pixel $D$ to $Z^W$ mapping



$D$  to  $Z^W$  Polynomial Fit

Data at pixel (212, 256)  
from 32 frames



*Linear*



$$Z^W[m, n] = e[m, n]D[m, n] + f[m, n]$$

# Generate Look-Up Table

- Size: *Width - Height - 6* (512\*424\*6)
- Data:  $X^W Y^W Z^W D$
- Pre-Process: (for every frame)
  - Find best-fit plane equation  $D = aX^W + bY^W + c$
  - Throw away 10% pixels of worst  $D$

- Mappings:

Fragment Shader: 3 per-pixel linear mappings, 6 parameters

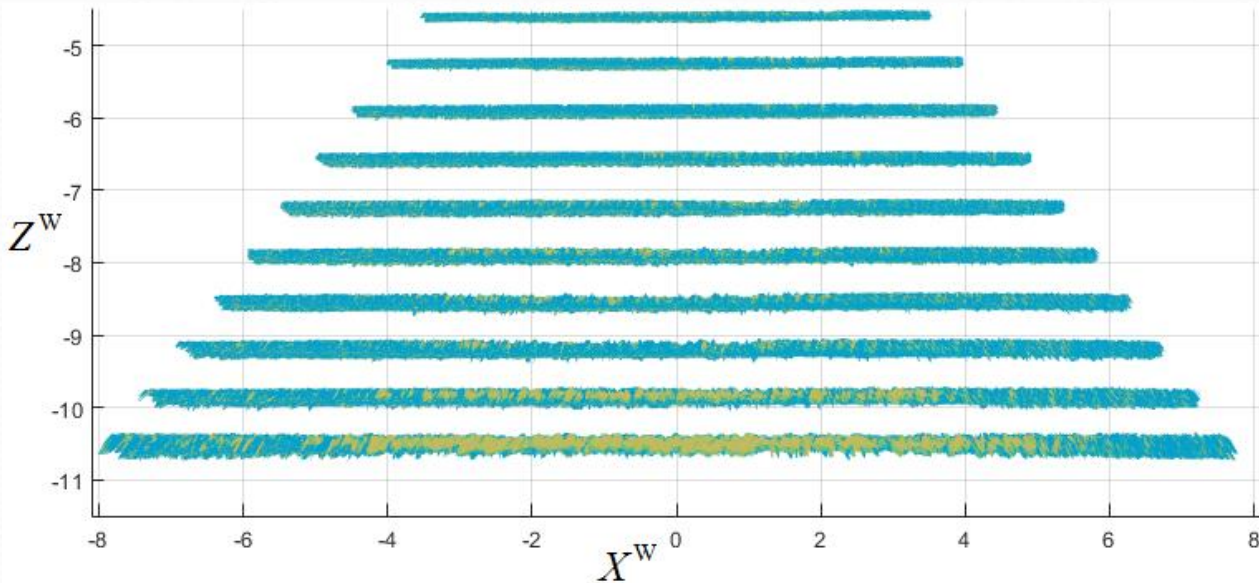
$$X^W[m, n] = a[m, n]Z^W[m, n] + b[m, n]$$

$$Y^W[m, n] = c[m, n]Z^W[m, n] + d[m, n]$$

$$Z^W[m, n] = e[m, n]D[m, n] + f[m, n]$$



# Depth Distortion Correction

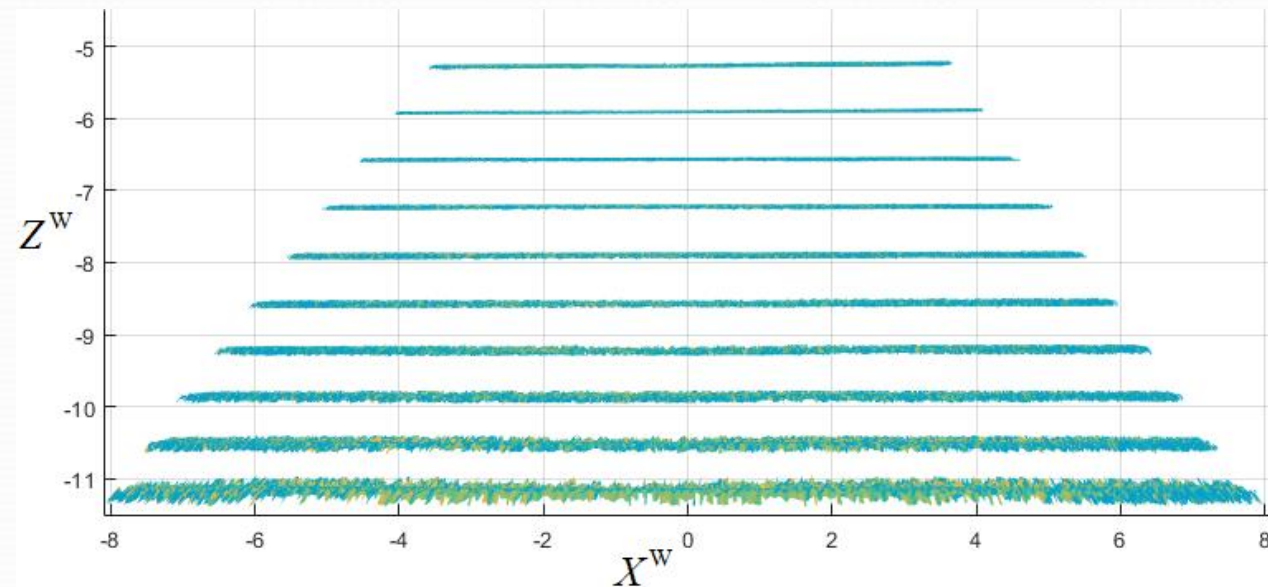


Raw Pin-Hole Reconstructions

Transformed  
into World Space

By

Best-Fit *Rotation and Translation*

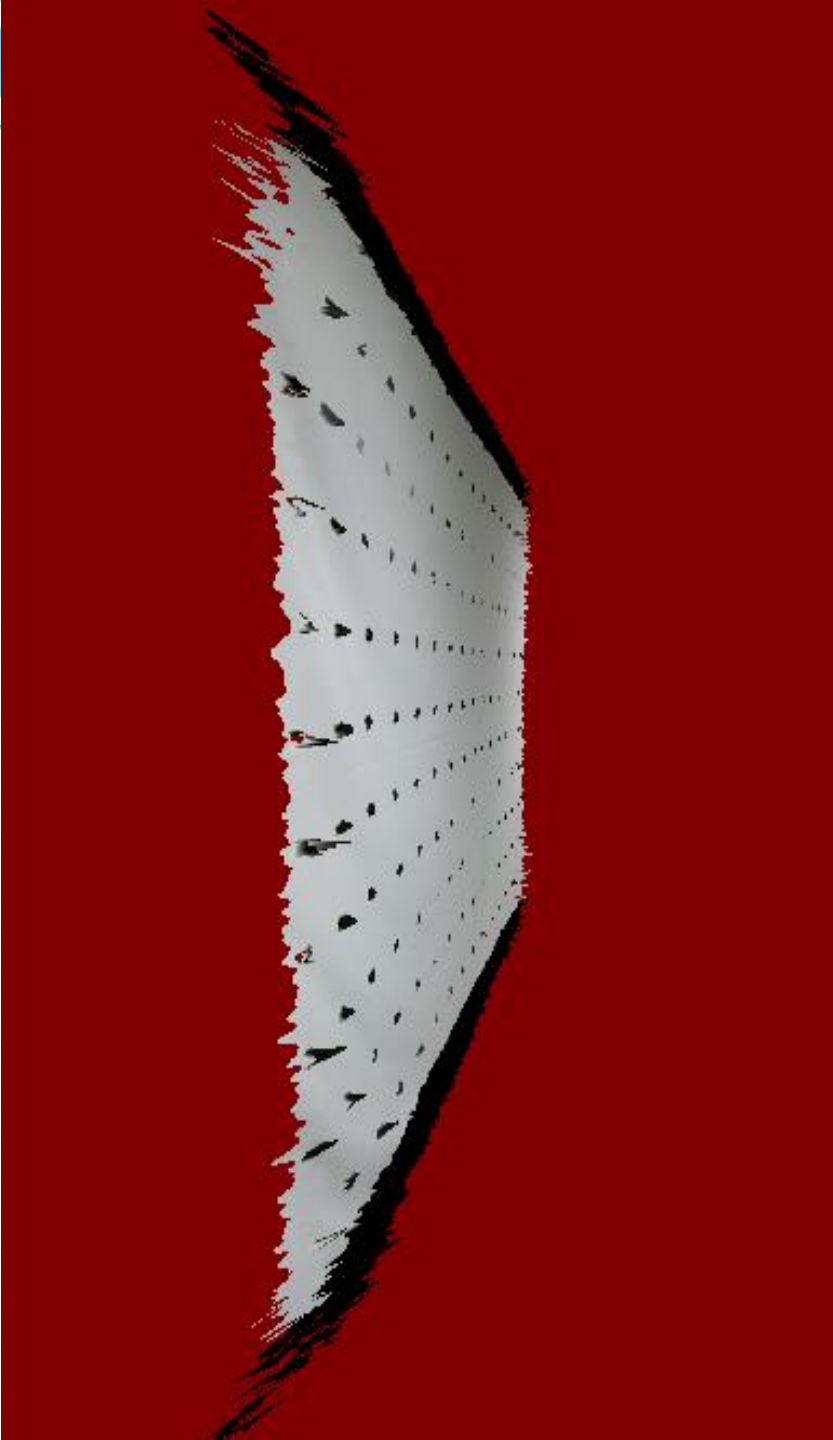
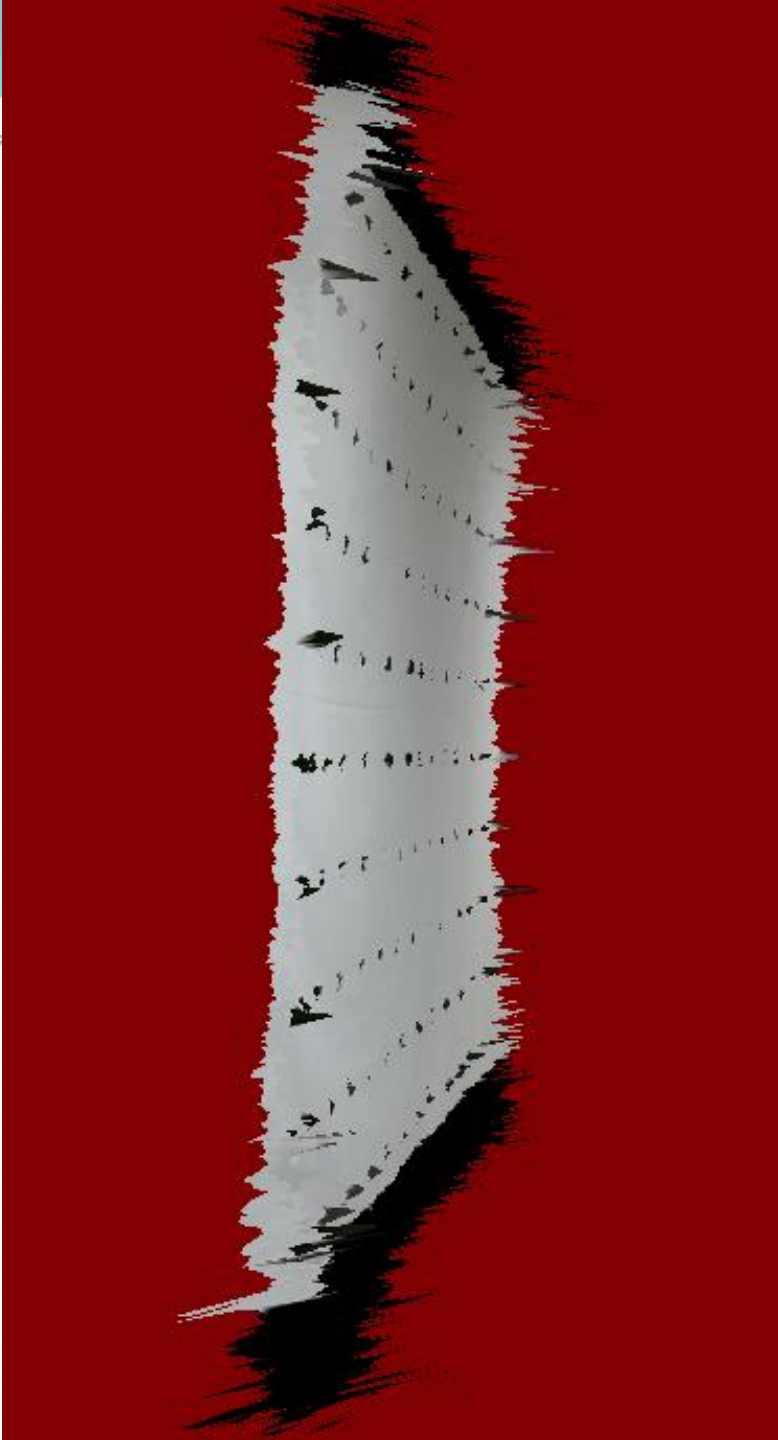


Calibrated LUT Reconstructions



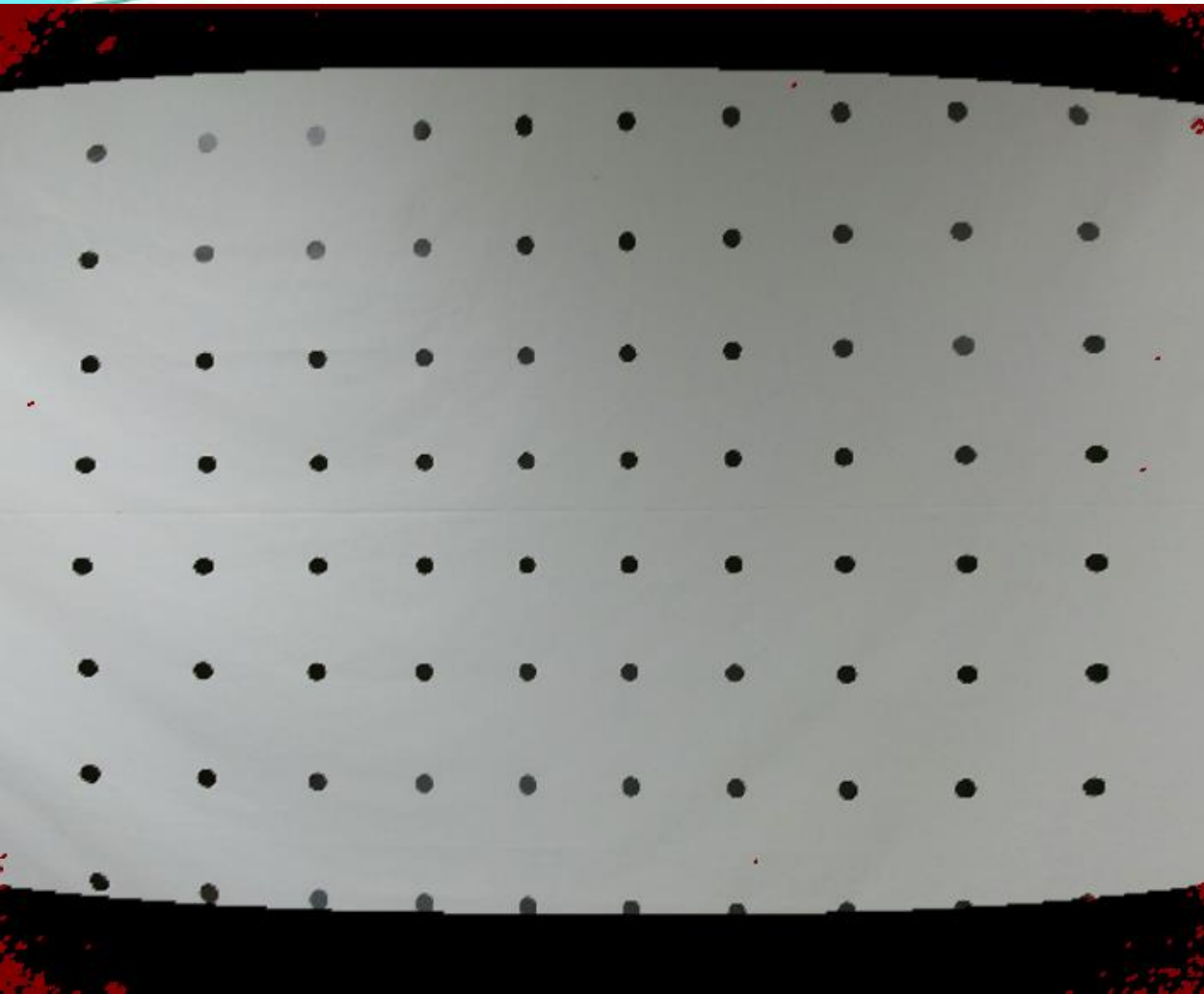


Before  
Calibration

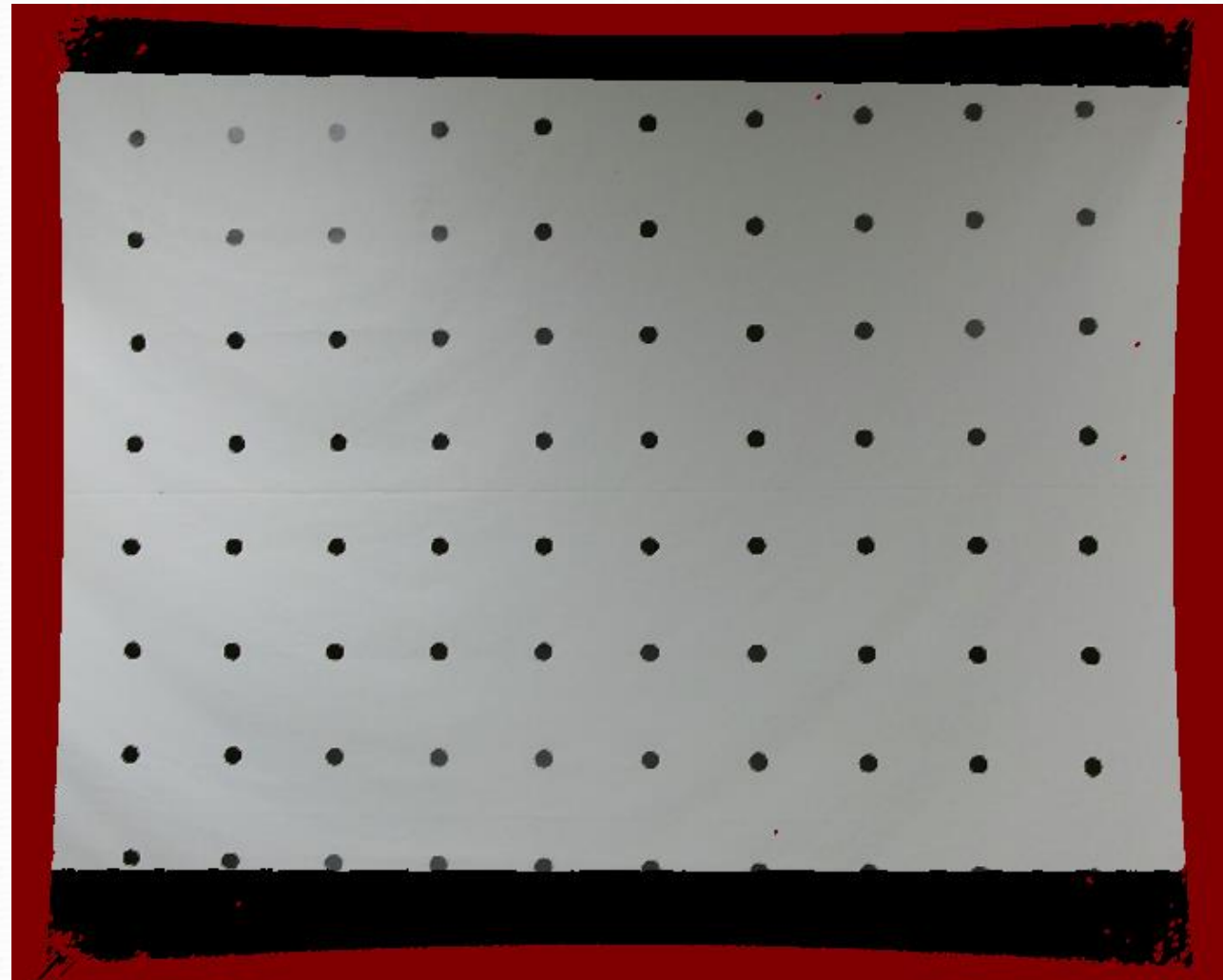


Calibrated

# Lens Distortion Correction



Before Calibration



Calibrated

# Conclusion

- Rail System

Infinite frames of data, dense calibration points, per-pixel  $D$  to  $Z^W$  mapping

- Data Collection (Per-Frame)

- Get  $Z^W$  from laser distance measurer ;

- Robust calibration points' extraction ;

Histogram Equalization, Adaptive Thresholding, Round Dots' Tracking

- Assign world space coordinates to calibration points ;

- Determine two-dimensional fourth order polynomial mapping ;

- Generate dense undistorted  $X^W Y^W$  .

- Pre-Process

- Unify staggered frames

- Throw away 10% noise pixels

- Generate LUT: *Width - Height - 6* (512\*424\*6)

- 3D Reconstruction: Undistorted 3D Reconstruction

# Future Works

- Hard Ware
  - Longer rail: singular  $D$  to  $Z^W$  linear mapping to segmented mapping ;
  - Pattern Size and Distribution: based on resolution ;
  - 2D pattern to 3D pattern: in case NIR streams cannot be used, 3D pattern for depth streams analysis ;
  - Tracking module on rail: to substitute laser distance measure, such that it is possible to input  $Z^W$  record frames automatically.
- Software
  - Better DIP techniques ;
  - Higher order polynomial  $Z^W$  to  $X^W Y^W$  mapping.





# Questions?