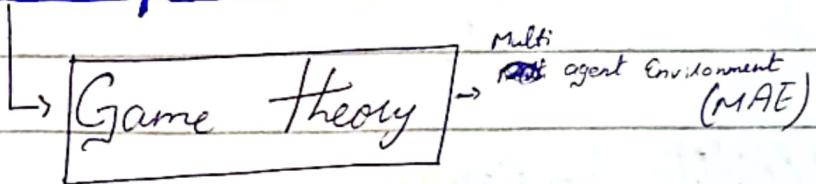


# A-I Lecture no (19-20)

- Uniformed Search }
- Informed Search → One Agent
- local Search
- hill climbing

## Adversarial Search / Minimax Search



→ It has more than one agent.



→ Always considered moves of opponent

→ Opponent always involves "randomness" or "Unpredictable".

## Zero sum games

→ One Agent gain is the "equivalent" loss of opponent.

In payoff

→ When one agent is gain and a

→ The loss of opponent is the equivalent gain of 1 Agent.

## Game Formulation

- States :-  $S \rightarrow$  (Start state)
- Player :-  $P \rightarrow$  (how many Player in a game)
- Actions :-  $A \rightarrow$  (which actions will perform) (changing state)  
(is action)
- Transition Factor :-  ~~$S \times A \rightarrow S$~~
- Terminal State test :-  $S \rightarrow \{T, F\}$
- Terminal Utility :- The gain of agent is utility. Every agent minimize its utility.

## Utility Functions

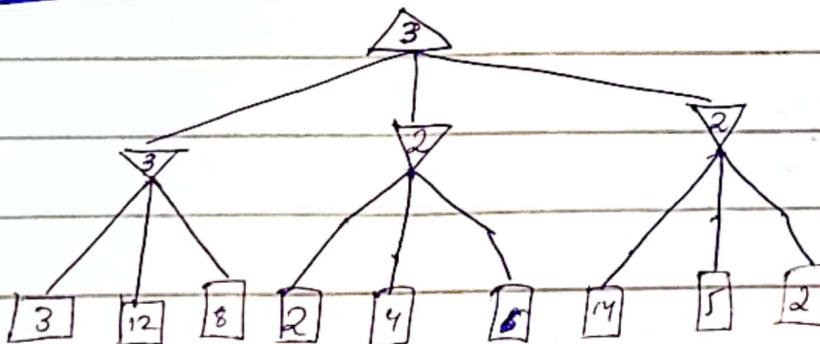
which have two agent

$$\text{Max} = \text{Me} \longrightarrow +1 / +C (+10) \xrightarrow{\substack{\text{value is +ve} \\ \text{we win}}}$$

$$\text{Min} = \text{Opponent} \longrightarrow -1 / -C (-10) \xrightarrow{\substack{\text{value is -ve} \\ \text{opponent win}}}$$

$$\text{No one} \longrightarrow 0; \xrightarrow{\substack{\text{no value match} \\ \text{draw}}}$$

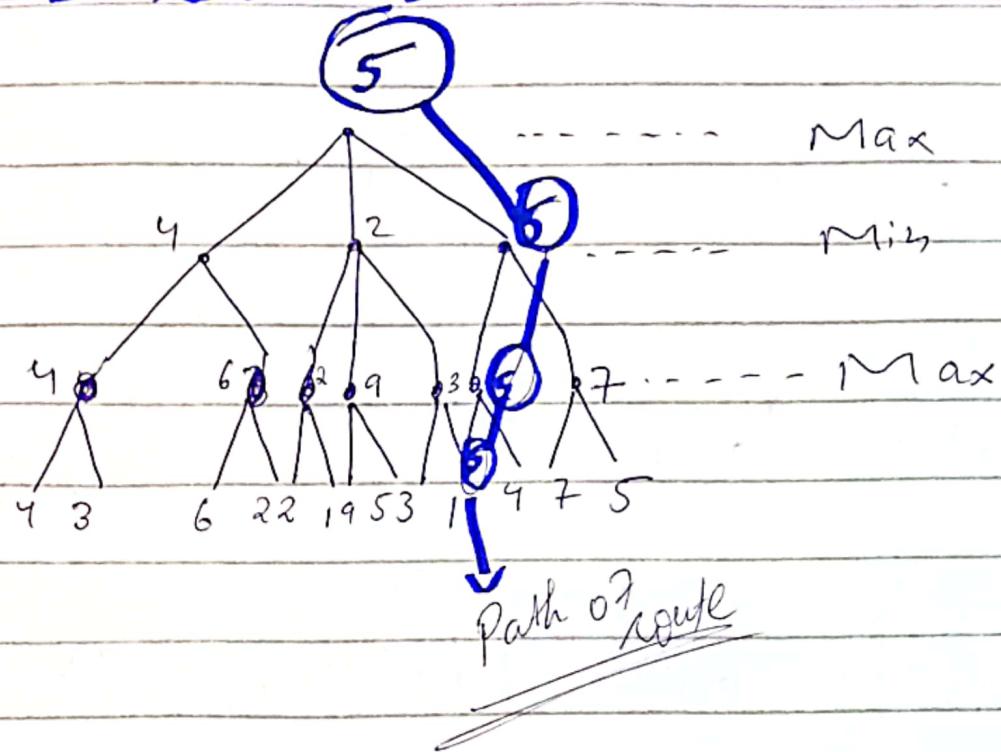
## Minimax Examples-



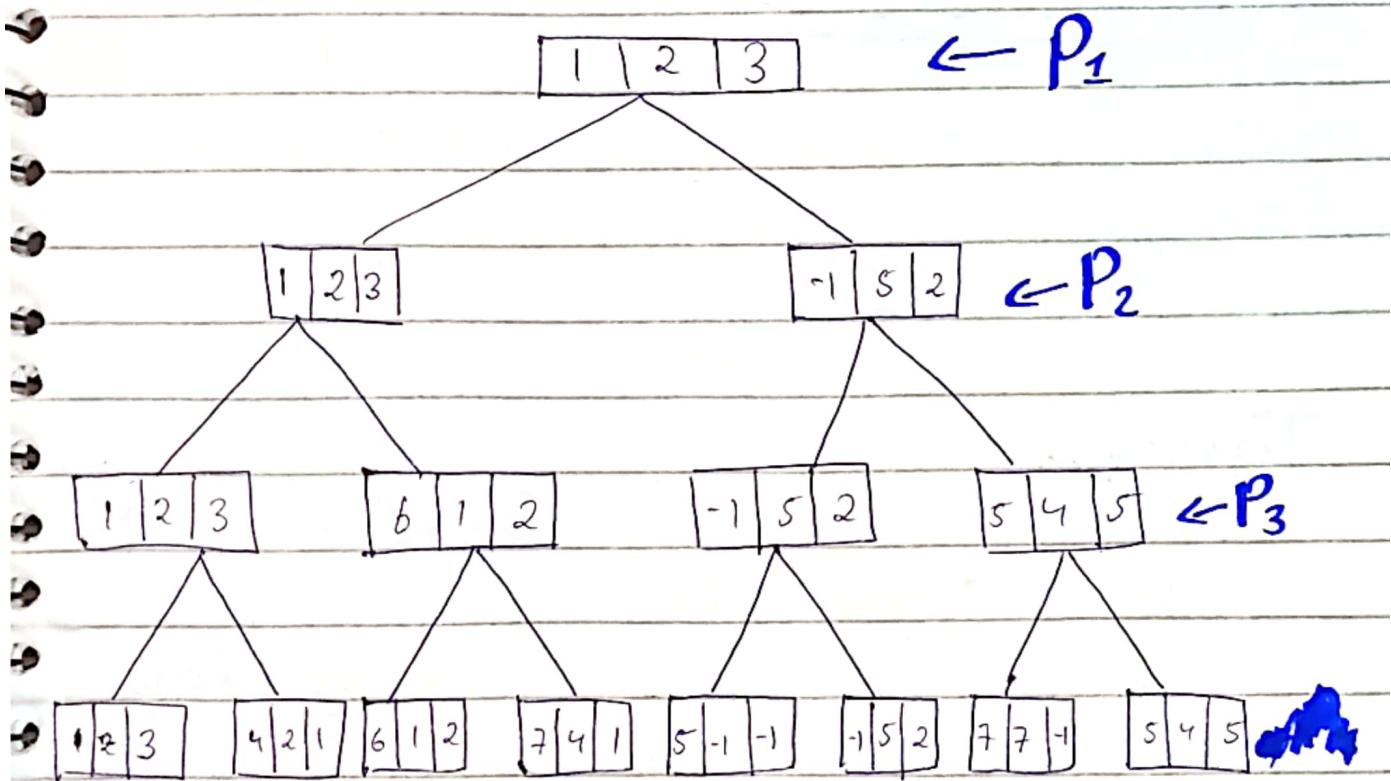
Max =  $-\infty$  ✓ Max always initialize with  $-\infty$  (Max denote with " $\alpha$ ").

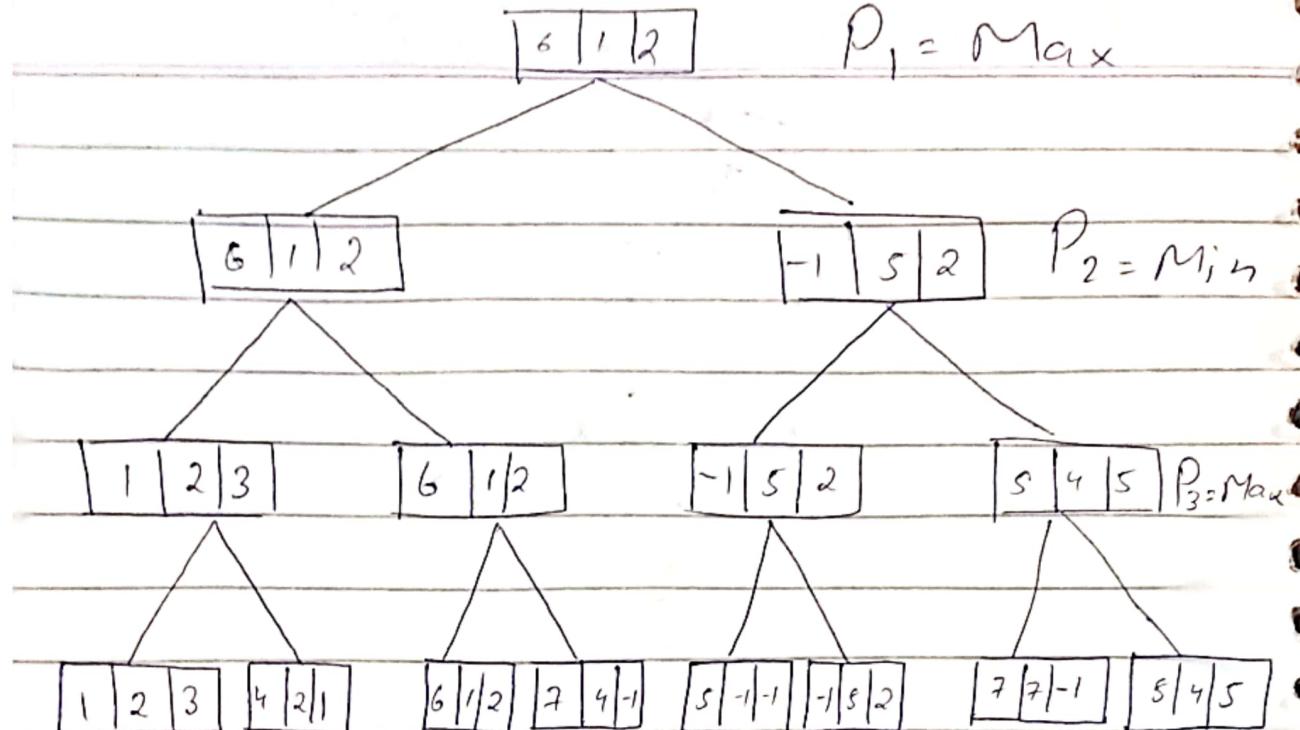
Min =  $+\infty$  ✓ Min always initialize with  $+\infty$  (Min denote with " $\beta$ ").

# AI-Lecture no "21"



Minimax for 3 players -





~~M<sup>0</sup>  $\leftarrow$  Tmp<sup>final</sup>~~  
Prune condition,

$$\begin{cases} \alpha = -\infty \\ \beta = +\infty \end{cases}$$

→ Where value of  $\alpha$  is greater or equal than  $\beta$  then the node is pruned.

## Traversing :-

→ When we move up to down we always copy the value of  $\alpha$  and  $\beta$ .

→ When we move down to up we always update the value if the level is "min" then only value of " $\beta$ " is updated. And if level is "max" then only update the value of " $\alpha$ ".

$\alpha \geq \beta$

we will plane

$\alpha = -\infty$   
 $\beta = \infty$

Max  $\rightarrow$

$\alpha = -\infty$   
 $\beta = \infty$

Min  $\rightarrow$

3

3

8

$\alpha = -\infty$   
 $\beta = +\infty$

2

2

6

2

7

2

$\alpha > \beta$   
 $\alpha = -\infty$   
 $\beta = +\infty$

14  
5  
2

3

2

8

2

4

6

7

2

2

# AI-Lecture no "2-3"

## Genetic Algorithm

= heuristic means → to calculate fitness

= competition → Survival of fitness

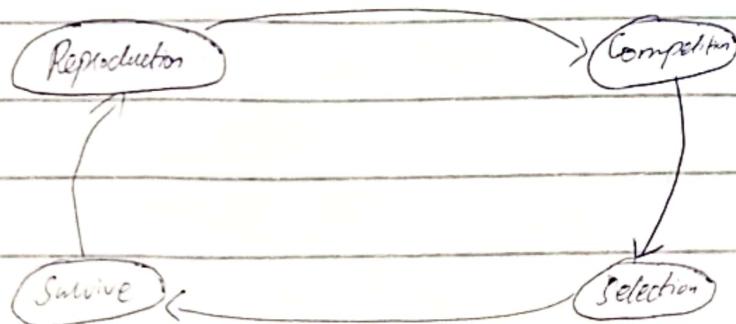
Step 1) Generate Initial Random population :-

It has no sequence and so if we require any population then we generate by random population.

Step 2) Calculate fitness of each ~~for~~ chromosomes -

when we generate population then we also calculate the fitness.

Step 3) P-Select (Parent select) :-



Step 4) Genetic Operations -

(a) Crossover ↗ 1 point crossover  
↘ multipoint cossuv.

(b) Mutation (multiple methods)

Step 5) New Generations -

Fitness

## New generation -

- Q: ① How can an individual be represented?
- Q: ② What is fitness function?
- Q: ③ How are individuals selected?
- Q: ④ How do individuals are generated?

A: ① → Every represent in number

A: ② → formula given to calculate fitness.

A: ③ → Use roulette wheel

A: ④ → Apply genetic Operations

## Reproduction -

→ States are Chromosomes

→ In the form of {0, 1}

→ No of pair of chromosomes are 23 total

$$23 \times 2 = 46$$

## One point crossover -

Ch-1	11 01		0100	Ch-N1	11 01	1111
Ch-2	00 10		1111	Ch-N2	00 10	0100

## Two point crossover

Ch-1	11   01 01 00	Ch-N1	11 000000
Ch-2	11   00 00   10	Ch-N2	11 01 01 10

31  
32 16 8 4 2 1  
1 1 1 1

## Mutation:-

→ 11 01 11001 by random mutation  
 choose any random? and change it to 1-0 or 0-1.

→ Mutation → 11 01 01001

### Problem 2

Maximize the function  $f(x) = x^2$   
 where  $x$  varies between "1-31".

Sq

Total population = 31

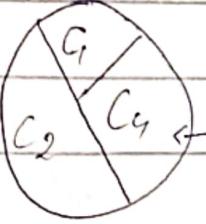
→ Generate any four (4) random numbers.

S.No	Initial popult	x-value	$f(x) = x^2$
1	01101	13	169
2	11000	24	576
3	01000	8	64
4	10011	19	361

16 8 4 2 1  
 1 1 1 1 0

Sl-no	n-value	$f(n) = n^2/f_c$	$P_{Select} = \frac{f(n)}{\sum f_i}$	Expected Count $f(n)^2/\text{Avg}$	Roulette wheel
1	13	169	<del>0.14</del> <del>0.14</del> = $\frac{169}{1170}$	$0.053 = \frac{169}{292.5}$	1
2	24	576	<del>0.49</del> <del>0.49</del> = $\frac{576}{1170}$	$1.97 = \frac{576}{292.5}$	2
3	8	64	<del>0.06</del> <del>0.06</del> = $\frac{64}{1170}$	$0.22 = \frac{64}{292.5}$	0
4	19	361	<del>0.31</del> <del>0.31</del> = $\frac{361}{1170}$	$1.33 = \frac{361}{292.5}$	1
		$\sum f_i = 1170$			

$$\text{Avg} = \frac{1170}{4} = 292.5$$

		$f(n)^2$	
		$C_2$	$C_2$
			$29 = 841$
		$C_1$	$13 = 169$
			$20 = 400$
			$25 = 625$

<u>11 00 0</u>	<u>11 000</u>	$2035 = \frac{2035}{4} = 508.75$
<u>01 1 0 1</u>	<u>10 011</u>	
$G_{\text{New}}(11001)$	$C_3 \text{New}(11011)$	So our new generation
$G_{\text{New}}(01100)$	$C_4 \text{New}(10000)$	is best.

Applying Mutation	New Population
11 00 1	11 10 1 $\Rightarrow 29$
01 1 0 0	01 1 0 1 $\Rightarrow 13$
11 0 1 1	10 1 0 0 $\Rightarrow 20$
10 0 0 0	11 0 0 1 $\Rightarrow 25$

$$f(x) = -x^2 + 15x$$

## Practice questions

			(Chromosomes 10) # of frags	Ratio %	Percent prob
1)	12	$\Rightarrow 1100 \Rightarrow$	36	$\frac{36}{218} = 0.16$	16.5%
2)	4	$\Rightarrow 0100 \Rightarrow$	44	$\frac{44}{218} = 0.20$	20.2%
3)	1	$\Rightarrow 0001 \Rightarrow$	14	$\frac{14}{218} = 0.06$	6.4%
4)	14	$\Rightarrow 1110 \Rightarrow$	14	$\frac{14}{218} = 0.06$	6.4%
5)	7	$\Rightarrow 0111 \Rightarrow$	56	$\frac{56}{218} = 0.25$	25.7%
6)	9	$\Rightarrow 1001 \Rightarrow$	57	$\frac{57}{218} = 0.24$	21.8%
			E9: = avg	$\frac{218}{6} = 36.3$	
					R.W

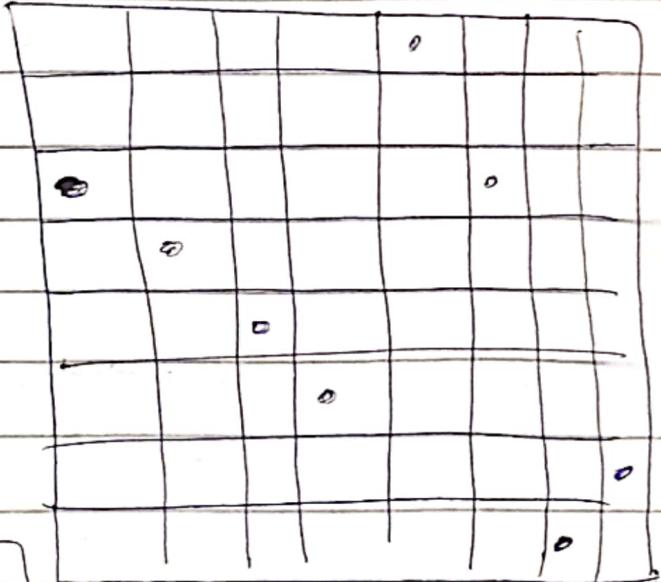
fi/avg	Round wheel	5	$-(5)^2 + 15(5) = 50$	$50/48 = 1.0$	1
$36/36.3 = 0.99$	1	11	$-(11)^2 + 15(11) = 44$	$44/48 = 0.9$	1
$44/36.3 = 1.21$	1	5	$-(5)^2 + 15(5) = 50$	$50/48 = 1.0$	1
$14/36.3 = 0.38$	0	4	$-(4)^2 + 15(4) = 44$	$44/48 = 0.9$	1
$14/36.3 = 0.38$	0	5	$-(5)^2 + 15(5) = 50$	$50/48 = 1.0$	1
$86/36.3 = 1.54$	2	10	$-(10)^2 + 15(10) = 50$	$50/48 = 1.0$	1
$54/36.3 = 1.48$	1		$288 = \frac{288}{6} = 48$		

				mutant	mutation
				2 <sup>nd</sup> bit from left	
	0 11 1	1 1 0 0	0 0 0 1		
	0 0 0 1	0 1 0 0	1 1 1 0	extreme change	
	0001	1100	0111		
	0111	0100	1000		
	0101	0101	0101	5 5 5	
	1011	0100	1010	1 9 10	

## 8-queens Problem

6, 5, 4, 3, 8, 6, 1, 2

→ Always start with  
left-bottom if not  
given.



8 queen ~~No. of~~ fitness = 28

$Q_1 = 5$

(To see attacking always looks forward)

$Q_2 = 5$

$Q_3 = 5$

$Q_4 = 3$

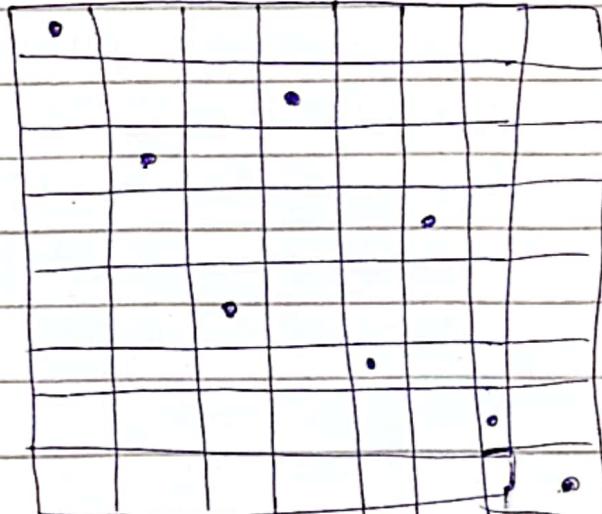
$Q_5 = 3$

$Q_6 = 2$

$Q_7 = 0$

$Q_8 = 0$

23



fitness

~~Good One~~

2	6	1	4	4	7	1	3
4	1	8	8	5	1	2	2

~~New chromosomes~~

2 6 1 8 5 1 2 3  
4 1 8 4 4 7 1 2

~~Mutation~~

↓ Swap any 2 in new chromosomes

3 6 1 8 5 1 2 2  
2 1 8 4 4 7 1 4

# A-I-Lecture no "4"

## Genetic Algo-

(1) IRPG

(2) Fitness

(3) P-selection

To calculate fitness:

24748552 → Total number of 0's & 1's to 51007  
8x8



24748552 → 24748552 → 24742411 → 24742411

32752411 → 32752411 → 32758352 → 32758352

Change by Random

again calculate  
by 8x8 table

→ In 8-queens problem it might possible to generate more than one number.

45 [2] 1 [2] 5 6 7

→ In TSP (Traveling Salesman problem) we cannot visit more than one city.

(A B C D E)

1 1 R 1 A R 1 S 1 C M P E

0 1 2 3 4 } → Randomness number

Always use two  
point crossover

P1 :-	7	4	(1 5 3 9)	6	{ 8 2
P2 :-	3	2	{ 9 4 7 1	8	{ 5 6

① Always write children of the parent. Parent-children called "Offspring" → "O".

② Cut values in parent "1" and cancel them in Parent "2".

③ Always start reading from 2<sup>nd</sup> cut point in sequence.

④ To perform mutation swap the numbers.

O<sub>1</sub>: - - 1 5 3 9 - - -

O<sub>2</sub>: - - 9 4 7 1 - - -

Mut

P<sub>1</sub>: 1 2 3 | 4 5 6 7 8 9

P<sub>2</sub>: 4 8 2 | 1 8 7 6 9 3

O<sub>1</sub>: x x x 4 5 6 7 x x => 2 1 8 4 5 6 7 9 3

O<sub>2</sub>: x x x 1 8 7 6 x x => 3 4 5 1 8 7 6 9 2

P<sub>1</sub>: 7 4 1 5 3 9 | 6 8 2

P<sub>2</sub>: 3 2 9 4 7 1 | 8 5 6

Crossover

O<sub>1</sub>: 4 7 | 1 5 3 9 | 8 6 2

O<sub>2</sub>: 5 3 | 9 4 7 1 | 6 8 2

4 2 9 3 8 1 6 2

mutation swap bit from 2<sup>nd</sup> cell to 2<sup>nd</sup> last

O<sub>1</sub>: 4 6 1 5 3 9 8 7 2

O<sub>2</sub>:

O<sub>1</sub>: 4 7 | 5 3 9 8 6 7

O<sub>2</sub>: 5 3 | 2 4 7 1 6 8 3

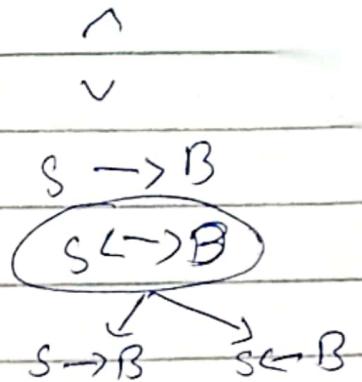
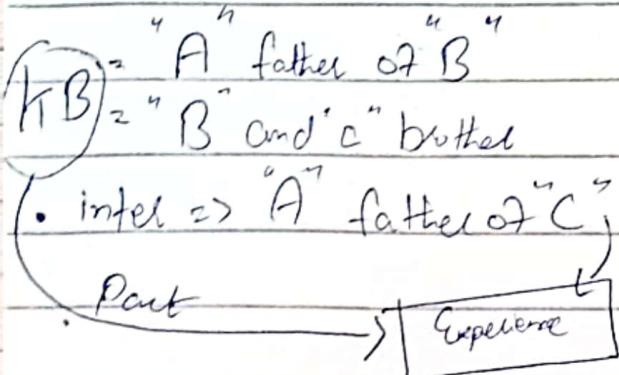
O<sub>1</sub>: 4 7 8 9 3 5 1 6 2

O<sub>2</sub>: 5 3 6 | 7 4 9 8 2

## Knowledge Representation (KR) :-

- ① KB Knowledge base
- ② Resolving OR Reasoning
- ③ Inference (dive)

$S_1 \Rightarrow$  It is raining  
 $S_2 \Rightarrow$



AI - "Lecture no 5 - 6"

Genetic Algo

Knapsack

~~try~~ do it by yourself



(Inv)

### Wumpus World 3-

4				
3				
2				
1	A			

1 2 3 4

→ 16 rooms in 4-by-4

→ There's only one monster in any of the one room.

→ In the room where is monster is static. It can't change.

→ No diagonal movement. Only up, down.

→ Strong smell smells available in room and agent has to identify the next room is monster.

→ The room in which Gold available has gliter. Agent find the gold and escape freely.

→ There is Pit available in multiple rows if goes then die.

→ There will be breeze available in directly connected to pit room.

→ Backtrack allows

→ Right side movement breeze found.

→ If agent move right side breeze found and

agent didn't know where is pit so it backtrack.

→ when agent moves up in room there is sting and one of the following have monster

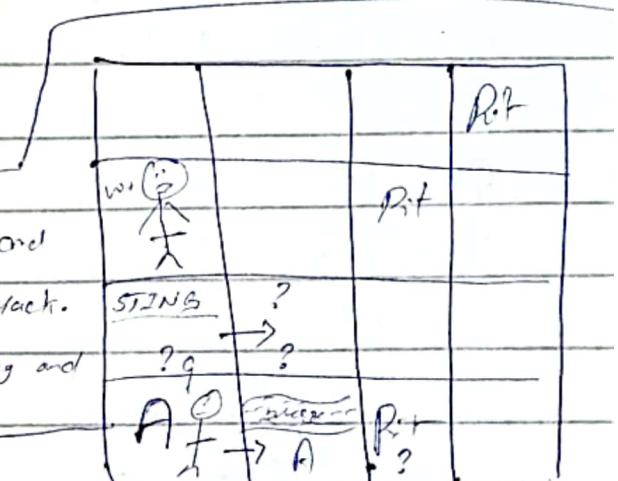
Fully Observable 3 - No

Deterministic 3 - Yes

Static 3 - Yes

Episodic 3 - No

Distinct 3 - Yes



### Modus Ponens

$$R_1 = \text{Clow} \rightarrow \text{Dog}$$

$$R_2 = \text{Clow}$$

Dog

$$R_1 = S_1 \rightarrow S_2, S_1$$

$$R_2 = S_2$$

$$R_1 (A \vee B) \rightarrow (C \wedge D)$$

$$R_2 (A \vee B)$$

(C  $\wedge$  D)

### And-Elimination

$$R_1 = A_1 \wedge A_2 \wedge A_3 \wedge A_4$$

$$R_2 = A_1$$

$$R_3 = A_2$$

$$R_4 = A_3$$

B<sub>2</sub>

$$\exists R_1 = \text{Cat} \wedge \text{Clow} \wedge \text{doll} \wedge \text{duck}$$

$$R_2 = \text{Cat}$$

$$R_3 = \text{Clow}$$

$$R_4 = \text{doll}$$

B<sub>2</sub> duck

### And-Introduction

$$R_1 = \text{cat}$$

$$R_2 = \text{doll}'$$

$$R_3 = \text{cat} \wedge \text{doll}'$$

### Or-Introduction

$$R_1 = \text{Clow}$$

$$R_2 \text{ Clow} \vee \text{ duck}$$

double negation elimination

$$\neg\neg S_1 = S_1$$

### Unit resolution

$$R_1 = \alpha \vee \beta \cancel{\alpha \beta} \rightarrow \beta$$

$$R_2 = \alpha$$

### Supervised Learning-

In supervised learning our data is labeled.

If class table is given it is called Classification-

### Unsupervised Learning -

In unsupervised learning our data isn't labeled.

If we give some images to the Machine and  
it arrange in group but didn't knew the table  
it is called clustering-

8-June-2023

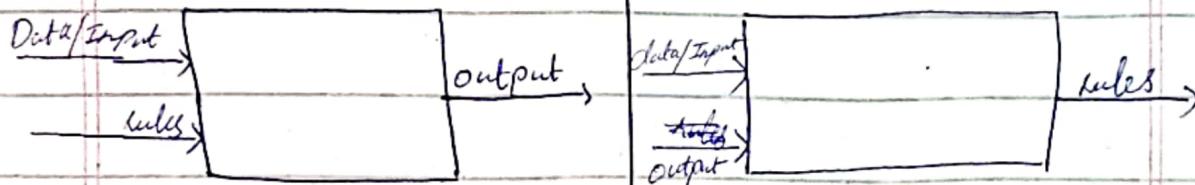
# "AI- Lecture no 19-20" Thursday

## \* Machine Learning

- Enabling machine to learn from experience without being programmed.

→ Traditional way of developing programs -

ML Program



## \* Types of Machine learning(ML)-

Classification  
Regression

- Supervised learning
- Unsupervised learning
- Semisupervised learning
- Reinforcement learning

- Deep learning
- Transfer learning

Def

In supervised learning our data is labeled dataset

Terms -

Supervised learning

Unsupervised learning

Def

Problem in which tells the class label e.g. Class A

Classification (Already existing label)

Regression → in which we predict the value.

Clustering → Label didn't know but it belongs to it in group.

Def

In unsupervised learning our data is unlabeled dataset.

## \* Semi-Supervised Learning:

Small data → ~~labeled~~ labeled

Large data → Unlabeled

## \* Reinforcement Learning:

It's contain "No Data". It learning depend on "Reward" & "Penalty".

## \* Deep Learning Insp

It is also include learning but "to copy mimic the human brain?"

## \* Transfer Learning:

To train our model and learn and transfer from one information to other information.

$\alpha$  = learning rate

$t$  = target variable

$x_1, x_2, \dots$  = Features

$w$  = weight

$B$  = Bias

$\text{---}$  = channel

$y_{in}$  = Input

$y$  = output

## \* Perception Learning -

input  $\Rightarrow$  features

$x_1$  0

$w_1$

$x_2$  0

$w_2$

$x_3$  0

$w_3$

$x_n$  0

$w_n$

Perception

Perceptrons

Activation Function (Perceptron)

Symbol =  $\int$   
Sigmoid  
Tanh  
Relu

Predict  
Cal  
Dojo

$y_{in}$  = Output

$y_{in} = f(y_{in})$

$y_{in}$  = Sum of scalar product of input feature and their respective weight and some uncertainty Bias.

$$y_{in} = x_1 w_1 + x_2 w_2 + \dots + x_n w_n + B$$

$$y_{in} = \sum_{i=1}^n x_i w_i + b$$

(if value is  
-25000 or any (neg)  
we always write  
"-1")

$$y = \begin{cases} -1 & y_{in} < 0 \\ 0 & y_{in} = 0 \\ 1 & y_{in} > 0 \end{cases}$$

(when when error then then update weights and biases)

$$w_{new} = w_{old} + \alpha t x_1$$

$$b_{new} = b_{old} + \alpha t$$

$$w_1 = w_{old} + \alpha t x_1$$

$$w_2 = 0 + 1(1)(1)$$

$$w_2 = 1$$

And Gate		
A	B	t
0	0	0
0	1	0
1	0	0
1	1	1



Assumption/Initialization -

$$w_1 = w_2 = b = 0$$

1st Iteration

1 1 1

$$b_{new} = b_{old} + \alpha t$$

$$= 0 + (1)(1)$$

$$b_{new} = 1$$

Replace w with "-1"

$x_1$	$x_2$	t
-1	-1	-1
-1	1	-1
1	-1	-1
1	1	1

$$y_{in} = x_1 w_1 + x_2 w_2 + b$$

$$= 0 + 0 + 0$$

$$y_{in} = 0$$

Error occurs so update

$$w_1_{new} = w_{old} + \alpha t x_1$$

$$= 0 + 1$$

$$w_1_{new} = 1$$

$$y_{in} = x_2 w_2 + x_1 w_1 + b$$

$$= (-1)(1) + (-1)(1) + 0(-1)$$

$$y_{in} = -2$$

Error so update

$$w_2_{new} = w_{old} + \alpha t x_2$$

$$= 0 + 1(-1)$$

$$w_2_{new} = -1$$

$$w_2_{new} = w_{old} + \alpha t x_2$$

$$= 0 + 1(-1)$$

$$w_2_{new} = -2$$

$$B_{new} = B_{old} + \alpha t$$

$$= 1 + (2)(-1) = 1 - 2 = -1$$

$$B_{new} = 0$$

# A-I • Lecture no "21-23"

## Naive Bayesian Classification-

### TYPES

• Joint probability-

$$P(A \text{ and } B) = P(A \text{ given } B) * P(B)$$

$$P(A \wedge B) = P(A/B) * P(B)$$

Int.

• Conditional Probability-

$$P(A/B) = \frac{P(B/A) * P(A)}{P(B)}$$

" $C$  = class  
 $x$  = feature

Example 1 → play

$$P(C/x) = \frac{P(x/C) * P(C)}{P(x)}$$

$$P(\text{Play}/\text{weather}) = \frac{P(\text{weather}/\text{play}) * P(\text{play})}{P(\text{weather})}$$

$$P(\text{Yes}/\text{sunny}) = \frac{P(\text{sunny}/\text{yes}) * P(\text{yes})}{P(\text{sunny})}$$

~~Prob in slides~~

$$P(\text{Yes}/\text{sunny}) = P(\text{sunny}/\text{Yes})$$

$$P(\text{Yes}/\text{sunny}) = \frac{(3/9) * (9/14)}{(5/14)}$$

$$= \frac{(0.334) * (0.642)}{(0.357)}$$

$$\boxed{P(\text{Yes}/\text{sunny}) = 0.6}$$

$$P(\text{No}/\text{sunny}) = \frac{P(\text{sunny}/\text{No}) * P(\text{No})}{P(\text{sunny})}$$

$$= \frac{P(2/5) * P(5/14)}{P(3/14)}$$

$$\boxed{P(\text{No}/\text{sunny}) = 0.4}$$

Table 15  
Solve

Example 2

$$P(\text{Gender} / \text{Name}) = P(\text{male} / \text{Gender}) * P(\text{Name})$$

$$\bullet P(\text{Male} / \text{Drew}) = \frac{P(\text{Drew} / \text{male}) * P(\text{male})}{P(\text{Drew})}$$

$$\bullet P(\text{Female} / \text{Drew}) = \frac{P(\text{Drew} / \text{female}) * P(\text{female})}{P(\text{Drew})}$$

for male

$$P(\text{Male} / \text{Drew}) = \frac{P(3/3) * P(3/8)}{3}$$

$$= \frac{P(1/3) * P(3/8)}{P(3/8)}$$

$$= P(1/3)$$

$$P(\text{Male} / \text{Drew}) = 0.333$$

for female

$$P(\text{Female} / \text{Drew}) = \frac{P(2/5) * P(5/8)}{P(3/8)}$$

$$= \frac{(0.4) * (0.625)}{(0.375)}$$

$$P(\text{Female} / \text{Drew}) = 0.667$$

## ★ Assumption

In Machine Learning, All the features are considered "to be independent to each other."

## Multi Input Attribute

One value which's increase called prior Probability

$$P(C/x_1, x_2, x_3, x_4) = P(C) * P(x_1/C) * P(x_2/C) * P(x_3/C) * P(x_4/C)$$

How to calculate probability having multiple input attribute

$x_2 = (\text{sunny, cool, High, Strong})$

$$\begin{aligned} P(\text{yes}/\text{feature}) &= P(\text{yes}) * P(\text{sunny}/\text{yes}) * P(\text{cool}/\text{yes}) * P(\text{High}/\text{yes}) * P(\text{Strong}/\text{yes}) \\ &= \left(\frac{1}{4}\right) * \left(\frac{2}{9}\right) * \left(\frac{3}{9}\right) * \left(\frac{3}{9}\right) * \left(\frac{3}{9}\right) \end{aligned}$$

$$P(\text{yes}/\text{feature}) = 0.005$$

$$P(\text{No}/\text{feature}) = P(\text{No}) * P(\text{sunny}/\text{No}) * P(\text{cool}/\text{No}) * P(\text{High}/\text{No}) * P(\text{Strong}/\text{No})$$

$$P(\text{No}/\text{feature}) = P(\text{No}) * P(\text{3}/\text{5}) * P(\text{4}/\text{5}) * P(\text{4}/\text{5}) * P(\text{3}/\text{5})$$

$$P(\text{No}/\text{feature}) = 0.02$$

$\omega = (\text{Red}, \text{Domestic}, \text{SUV})$

$P(\text{yes})$

$$P(\text{Yes/Fecture}) = P(\text{Red}/\text{yes}) * P(\text{SUV}/\text{yes}) * P(\text{Domestic}/\text{yes})$$

$$= P(1/10) * P(1/10) * P(1/10) * P(1/10)$$

$$= P(5/10) * P(3/5) * P(1/5) * P(2/5)$$

$$P(\text{Yes/Fecture}) = 0.0214$$

$$\begin{aligned} P(\text{No/Fecture}) &= P(\text{No}) + P(\text{Red/No}) * P(\text{SUV/No}) * P(\text{Domestic/No}) \\ &= P(5/10) * P(2/5) * P(3/5) * P(3/5) \end{aligned}$$

$$P(\text{No/Fecture}) = 0.072$$

Example 3

Instance =  $2, 3, 4$

$$\begin{aligned} P(\text{Fecture}) &= P(A) * P(2/A) * P(3/A) * P(4/A) \\ &= P(8/15) * P(5/8) * P(2/8) * P(4/8) \\ &= 0.0916 \end{aligned}$$

$$\begin{aligned} P(\text{Fecture}) &= P(C) * P(2/C) * P(3/C) * P(4/C) \\ &= P(3/15) * P(2/3) * P(2/3) * P(4/3) \end{aligned}$$

$$= 0.0148$$

$$P(B_{\text{feature}}) = P(B) + P(\frac{1}{B}) + P(\frac{3}{B}) + P(\frac{4}{B})$$

$$= \left(\frac{4}{15}\right) + P\left(\frac{2}{4}\right) + P\left(\frac{3}{4}\right) + P\left(\frac{2}{4}\right)$$

$\boxed{= 0.0083}$

(Yellow, Sweet, ~~Banana~~<sup>long</sup>)

$$\rightarrow P\left(\frac{\text{Mango}}{\text{Yellow}}, S, B\right) = P(\text{Mango}) * P\left(\frac{Y}{M}\right) + P(S/M) + P(L/M)$$

$$= \left(\frac{650}{1100}\right) + P\left(\frac{350}{650}\right) * P\left(\frac{450}{650}\right) + P\left(\frac{0}{650}\right)$$

$\boxed{P\left(\frac{\text{Mango}}{\text{Y}}, S, B\right) = 0}$

$$\rightarrow P\left(\frac{\text{Banana}}{\text{Y}, S, L}\right) = P(B) + P(Y/B) + P(S/B) + P(L/M)$$

$$= P\left(\frac{4}{1100}\right) + P\left(\frac{4}{1100}\right) * P\left(\frac{300}{400}\right) + P\left(\frac{350}{400}\right)$$

$\boxed{= 0.021875}$

$$\rightarrow P\left(\frac{\text{Orange}}{\text{Y}, S, L}\right) = P(O) + P(Y/O) + P(S/O) + P(L/O)$$

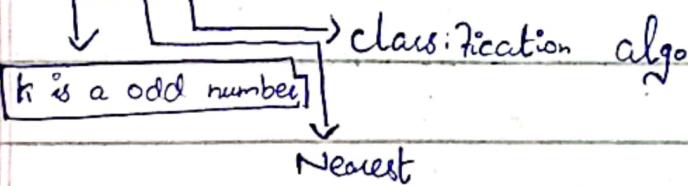
$$= P\left(\frac{150}{1100}\right) + P\left(\frac{50}{150}\right) + P\left(\frac{100}{150}\right) + P\left(\frac{50}{150}\right)$$

$\boxed{= 0.09}$

# A-I Lecture no "22"

## KNN - Algorithm

KNN:-



Height(cm)	Weight(kg)	Class	Distance
167	51	Underweight	6.7
182	62	Normal	13
176	69	Normal	13.41
173	64	Normal	7.61
172	65	Normal	8.24
174	56	Underweight	4.12
169	58	Normal	10.41
173	57	Normal	3
170	55	Normal	2
Given → 170	57	?	.

$$\textcircled{1} \quad x = 170 \quad 57 ; \quad y = 167 \quad 51$$

Using distance formula

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$d = \sqrt{(170 - 167)^2 + (57 - 51)^2}$$

$$d = \sqrt{45} = 6.7$$

$$\textcircled{2} \quad 170; 57, 182; 62$$

$$d = \sqrt{(170 - 182)^2 + (57 - 62)^2}$$

$$d = \sqrt{(12)^2 + (5)^2}$$

$$d = \sqrt{144 + 25}$$

$$d = \sqrt{169}$$

$$\textcircled{3}$$

Height(cm)	Weight	Class	Distance	Rank
169	58	Normal	10.41	1
170	55	Normal	2	2
173	57	Normal	3	3
174	56	Underweight	4.012	4
167	51	Underweight	6.07	5
173	64	Normal	7.061	6
172	65	Normal	8.024	7
182	62	Normal	13	8
176	69	Normal	13.041	9

Brightness	Saturation	Class	Distance
40	20	Red	25
50	50	Blue	33.054
60	90	Blue	68
10	25	Red	14.014
70	70	Blue	61.03
60	10	Red	47.0
25	80	Blue	45.027
20	35	?	

Brightness	Saturation	Class	Distance	Rank
10	25	Red	14014	1
40	20	Red	25	2
50	50	Blue	33054	3
25	80	Blue	45027	4
60	10	Red	4701	5
70	70	Blue	61003	6
60	90	Blue	68	7

→ For k=1 class Red

→ For k=2 class Red

→ For k=3 class Red

→ For k=4

→ For k=5 class Red

→ For k=7 class Blue



→ In case of non-numeric data we apply probability model.

→ When data is numeric we apply kNN-model

A-I

## k-mean clustering Algo:-

→ unsupervised Learning

↳ Dataset

↳ Unlabelled

Centroid :-

Mean value of each cluster.

→ Example:-

	P <sub>1</sub> (P <sub>2</sub> )	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>6</sub>	(P <sub>2</sub> ) P <sub>8</sub>	k=2
Size:-	2	3	4	84	2	5	7
Price:-	10	9	8	9	8	6	5

1:- Pick two any Random point and name as cluster

2:- Given in question 1<sup>st</sup> point.

	C <sub>1</sub> (3,9)	C <sub>2</sub> (7,5)	Cluster
(2,10)	1.041	7.07	C <sub>1</sub>
(3,9)	0	8.65	C <sub>1</sub>
(4,8)	1.041	4.24	C <sub>1</sub>
(8,9)	1.41	5	C <sub>1</sub>
(2,8)	1.041	5.83	C <sub>1</sub>
(5,6)	3.60	2.2	C <sub>2</sub>
(7,5)	5.65	0	C <sub>2</sub>
(7,6)	5	1	C <sub>2</sub>

$$C_1 = \{P_1, P_2, P_3, P_4, P_5\}$$

$$C_2 = \{P_6, P_7, P_8\}$$

\* Centroid values are updated after each iteration.

$$C_1 = \{P_1, P_2, P_3, P_4, P_5\}$$

$$C_2 = \{P_6, P_7, P_8\}$$

\* For next iteration take the mean of C1

$$C_1 = (3, 8, 88)$$

\* For next iteration take the mean of C2

$$C_2 = (6.33, 5.66)$$

Example [Centroids:  $C_1 = \{5, 5\}, C_2 = \{9, 7\}, C_3 = \{2, 3\}$ ]

x	2	3	5	8	1	7	10	9	4	8	6	4
y	2	1	7	4	6	7	2	3	4	1	3	9

	$C_1(5, 5)$	$C_2(9, 7)$	$C_3(2, 3)$	Cluster	
$P_1$ (2, 2)	4.2	8.60	1	$C_3$	$C_1 = \{P_3, P_4, P_6, P_7, P_8\}$
$P_2$ (3, 1)	4.47	8.48	2.23	$C_3$	$C_2 = \{P_6, P_7, P_8\}$
$P_3$ (5, 7)	2	4	5	$C_1$	$C_3 = \{P_1, P_2, P_5\}$
$P_4$ (8, 4)	3.06	3.06	6.08	$C_1$	
$P_5$ (1, 6)	4.12	8.06	3.06	$C_3$	$UC_1 = (5.83, 7.6)$
$P_6$ (7, 7)	8.28	2	6.40	$C_2$	$UC_2 = ($
$P_7$ (10, 2)	5.83	5.09	8.06	$C_2$	
$P_8$ (9, 3)	4.47	4	7	$C_2$	
$P_9$ (4, 4)	1.01	5.83	2.23	$C_1$	
$P_{10}$ (8, 1)	5	6.08	6.32	$C_1$	
$P_{11}$ (6, 3)	2.23	5	4	$C_1$	
$P_{12}$ (4, 9)	4.12	5.38	6.32	$C_1$	