



Estimating $ZZ \rightarrow \ell\ell\nu\nu$ background in the $\ell\ell + E_T^{\text{miss}}$ final state using $Z\gamma \rightarrow \ell\ell\gamma$ data

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Certificate

This is to certify that this dissertation, entitled "Estimating $ZZ \rightarrow \ell\ell\nu\nu$ background in the $\ell\ell + E_T^{\text{miss}}$ final status using $Z\gamma \rightarrow \ell\ell\gamma$ data", submitted towards the partial fulfilment of the BS-MS dual degree programme at the Indian Institute of Science Education and Research (IISER), Pune, represents the work carried out by Mangesh Sonawane at the Deutsches Elektronen-Synchrotron (DESY), Hamburg, under the supervision of Dr. Beate Heinemann, Professor of Experimental Particle Physics at the Institute of Physics, University of Freiburg, during the academic year 2017-2018.



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I dedicate this thesis to my parents, Avinash and Ranjana Sonawane, my mentors, Dr. Sourabh Dube and Dr. Seema Sharma, and to my friends and colleagues and IISER, without whose timely advice and support this thesis would not have been made possible.

Declaration

I hereby declare that the matter contained within the thesis entitled "Estimating $ZZ \rightarrow \ell\ell\nu\nu$ background in the $\ell\ell + E_T^{\text{miss}}$ final status using $Z\gamma \rightarrow \ell\ell\gamma$ data", contains the results of the work carried out by me at the Deutsches Elektronen-Synchrotron (DESY) Hamburg, under the supervision of Dr. Beate Heinemann, and the same has not been submitted elsewhere for any other degree.



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Abstract

In the search for Dark Matter (DM) at the LHC, SM particles are produced in association with DM particles, which are invisible as they don't interact with the detector. Thus events with large imbalance in transverse momentum are of interest. One such signature is $\ell\ell + E_T^{miss}$. The dominant background contributing to the search for DM in the $\ell\ell + E_T^{miss}$ is $ZZ \rightarrow \ell\ell\nu\nu$. Currently, this background is determined using Monte Carlo simulation, with an uncertainty of $\approx 10\%$. The goal of this study is to establish a data driven method to estimate this background, and reduce the uncertainty. Using $Z\gamma \rightarrow \ell\ell\gamma$, which is a process with low backgrounds and has a high $BR \times \sigma$, it is possible to estimate the $ZZ \rightarrow \ell\ell\nu\nu$ contribution. In regions where $p_T(\gamma) \gg M_Z$, the two processes are kinematically similar. They have the same production mechanisms, but differ due to the photon and Z boson couplings to the quarks being different, as well as the difference in mass (photons are massless, while Z bosons are massive). Introducing a transfer factor R as the ratio $\sigma(ZZ)/\sigma(Z\gamma)$ which is determined from simulation, the contribution of $ZZ \rightarrow \ell\ell\nu\nu$ to the background can be estimated from $Z\gamma \rightarrow \ell\ell\gamma$ data. The uncertainty on the prediction of R due to theoretical aspects is estimated in this work.

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Chapter 1

Introduction

Fundamental particle physics has a remarkable goal. It attempts to explain the interactions of matter and energy with the minimum possible number of mathematical assumptions, with everything else in the Universe being an emergent property.

Not only is it remarkably ambitious, the Standard Model of physics is one of the most successful theories developed, describing the fundamental particles and their interactions [1]. It is theoretically self-consistent, and has enjoyed tremendous success in providing accurate experimental predictions. However, the Standard Model is not a complete theory of fundamental interactions. It does not provide an explanation for several observed phenomena, such as gravity, or the accelerating expansion of the Universe, among others.

One such question that triggers burning curiosity is the apparent incongruity of galaxy rotation curves with the theory of Newtonian mechanics: stars in the arms of spiral galaxies appear to move much faster than Newtonian physics would predict. Either the current understanding of mechanics is incomplete, or there is more mass present somewhere in the galaxy that is not visible by any method that is currently employed. This invisible hunk of matter is what is termed as Dark Matter (DM).

Detailed observations of these rotation curves, along with measurements of other phenomena such as gravitational lensing by distant galaxies, galaxy clusters, and Cosmic Microwave Background (CMB) lead to the conclusion that, if the Dark Matter hypothesis is true, the amount of visible Baryonic matter in the Universe is a mere 4%. The remaining 96% of the Universe is composed of Dark Matter and Dark Energy.

Now it becomes important to address the question: what exactly is Dark Matter?

Several extensions to the Standard Model, called Beyond Standard Model (BSM) theories, attempt to provide an explanation of these observed phenomena. Dark Matter hasn't been observed to interact directly through the electromagnetic force, and are thus invisible to current detectors. Consequently candidates for Dark Matter are called Weakly Interacting Massive Particles (WIMPs). In LHC experiments, events with WIMPs in the final state show up as an imbalance in the momentum in the plane transverse to the beam (referred to as E_T^{miss} throughout this thesis).

One such BSM theory postulates that these Dark Matter candidate particles may couple to Standard Model particles in interactions mediated by the Higgs boson. Fig 1.1 illustrates some of the possible processes for the production of the Higgs boson. The Higgs boson can then decay into invisible particles.

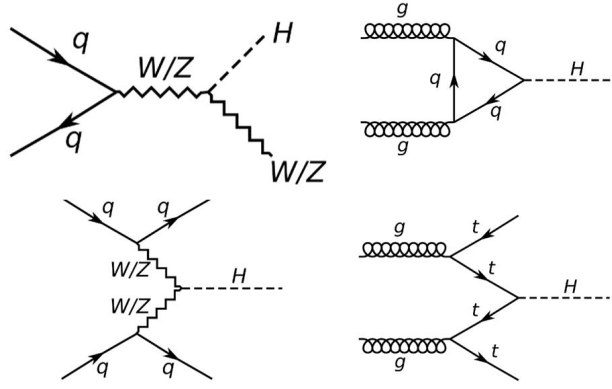


Figure 1.1: Feynman diagrams for the Standard Model production of the Higgs boson; VH: Higgs produced in association with a W/Z boson (top left), ggF: gluon-gluon fusion (top right), VBF: vector boson fusion (bottom left), ttH: (bottom right).

High energy collision experiments are a method to experimentally investigate the predictions made by particle physics in a controlled manner. Several other kinds of detector experiments, both passive and active, investigate phenomena such as neutrino flavor oscillations and direct dark matter searches. The Large Hadron Collider (LHC), built and operated by CERN, is a proton-proton (and heavy ion) collider located in Switzerland and France, is the largest such collider in the world. It has provided invaluable data since commencing operations in 2008, providing experimental confirmation for phenomena such as the Higgs boson.

In this thesis, a closer look is taken at the VH channel i.e. the production of a Higgs boson in association with a vector boson, in particular ZH , where the Higgs boson decays invisibly into DM particles, and the Z boson decays into a dilepton pair. The signature of such a process is two same flavor, oppositely charged leptons, and an imbalance in event momentum ($\ell\ell + E_T^{\text{miss}}$). A possible search in this channel would constitute stacking all known Standard Model processes that contribute to the $\ell\ell + E_T^{\text{miss}}$ signal (making up the background) and look for excesses in data which will indicate the presence of non-Standard-Model processes. In this thesis, the $ZZ \rightarrow \ell\ell\nu\nu$ process is studied, which constitutes the dominant SM background in the $\ell\ell + E_T^{\text{miss}}$ final state. However, it is difficult to discriminate between the Standard Model $ZZ \rightarrow \ell\ell\nu\nu$ and $ZH \rightarrow \ell^+\ell^- + E_T^{\text{miss}}$, the process under consideration, because of the identical final state. Thus, an attempt is made to estimate it using alternate processes with clean signals.

This chapter gives an overview of the Standard Model, its constituent matter particles, forces, and their interactions. It also delves into the shortcomings of the Standard Model, and introduces some ways in which Dark Matter is probed at the LHC. Chapter 2 describes the LHC, as well the ATLAS detector, where high energy collisions experiments are carried out. Chapter 3 discusses the theoretical aspects of investigating the $ZZ \rightarrow \ell\ell\nu\nu$ contribution, and details the approach taken, and chapter 4 presents the results obtained.

1.1 The Standard Model

The Standard Model is the name given to the theory of particles, fundamental forces, and interactions that govern the Universe. It describes three of the four forces: the electromagnetic, strong and weak forces. The Standard Model is formulated using the framework of Quantum Field Theories (QFT), which describe particles as excitations of an underlying field.

Throughout this thesis, the Lorentz-Heaviside system of units is used, such that $c = \hbar = 1$ (where c is

the speed of light, and $\hbar = h/2\pi$ is the reduced Planck's constant), and thus these units do not show up in equations. Ref [1] is the reference textbook for much of this section.

1.1.1 Matter and Forces

In the Standard Model, matter is made up of fermions and bosons. Fermions are particles with half-integer spin, and interact through the exchange of gauge bosons, which have integer spin. All fundamental Standard Model fermions have spin 1/2. The Standard Model gauge bosons which mediate the interactions between particles have spin 1. The Higgs boson is a scalar boson, and has spin 0.

Figure 1.2 shows a schematic representation of the elementary particles in the Standard Model.

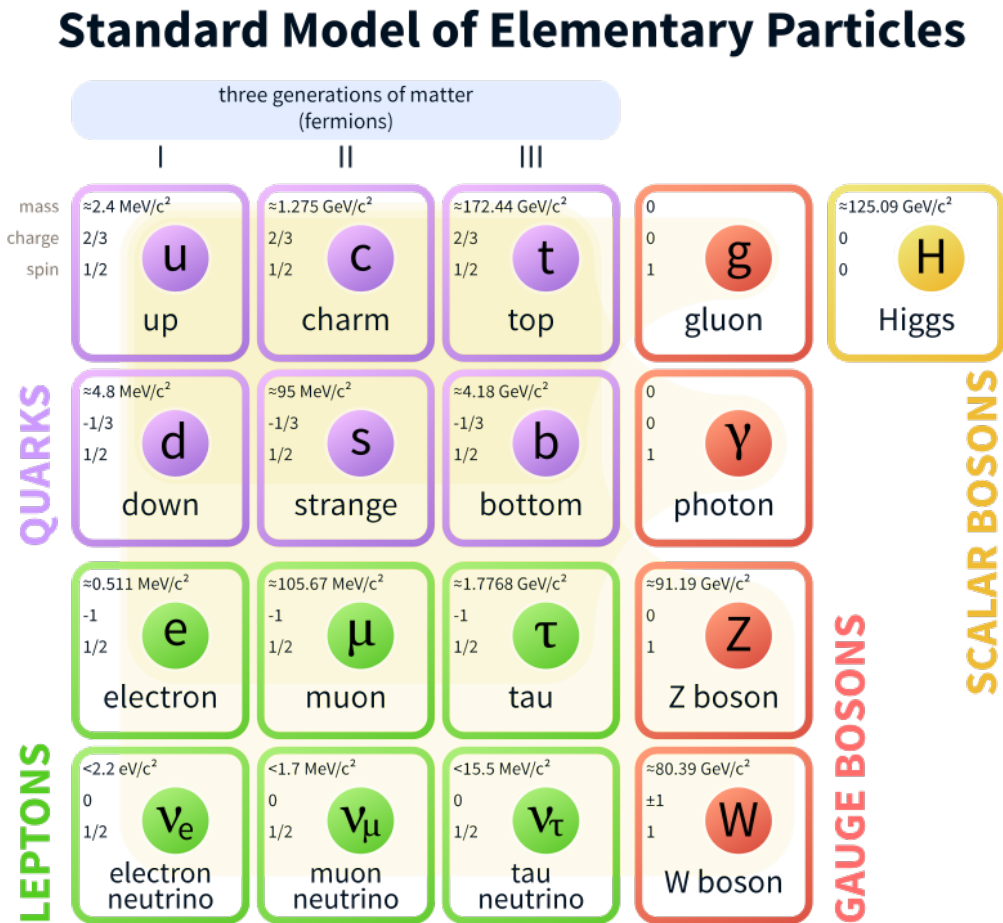


Figure 1.2: A schematic representation of the Standard Model [2] of particles. The table shows the three generations of fermions (classified as quarks and leptons) that are the building blocks of all known matter in the Universe, and bosons that mediate interactions, and are thus responsible for ‘forces’.

All particles, except the neutral bosons (with no electromagnetic charge) have a corresponding antiparticle, which has the same properties, except with an opposite electric charge.

Fermions are divided into two categories: leptons and quarks. There are six flavors of leptons and six flavors of quarks. All the quarks, and three flavors of leptons are electrically charged, and thus participate in electromagnetic interactions. Electromagnetic interactions are described by **Quantum Electrodynamics** (QED) [3], a QFT. QED describes interactions in which two electrically charged

77 particles exchange a photon. The photon is a spin-1 gauge boson, is electrically neutral, massless, and
 78 mediates electromagnetic interactions. Figure 1.3 shows the fundamental interaction vertex in QED,
 79 the interaction between two charged fermions and the photon.

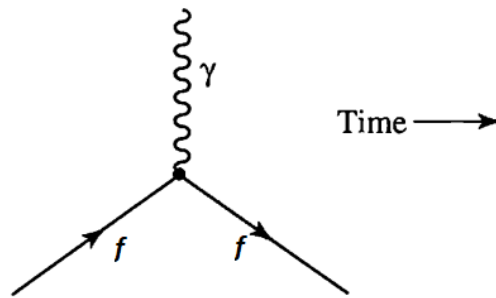


Figure 1.3: Feynman diagram showing the fundamental interaction vertex in Quantum Electrodynamics. Charged fermions (f) interact via the exchange of a photon (γ), reproduced from Ref [1].

80 Quarks come in 6 flavors, which are divided into 3 ‘generations’ having progressively higher masses;
 81 the up and down (u and d) are first generation quarks, charmed and strange (c and s) are second gener-
 82 ation quarks, top and bottom, or formerly, truth and beauty, (t and b) belong to the third generation.
 83 Up-type quarks (u , c and t) have an electric charge of $+2/3e$ (where e is the unit of electronic charge,
 84 equal to 1.6×10^{-19} Coulombs), while down-type quarks have an electric charge of $-1/3e$. Quarks are
 85 the fundamental particles that form composite particles called hadrons; bound states of $q\bar{q}'$ are called
 86 *mesons*, and $qq'q''$ bound states are called baryons. Protons (bound state of uud) and neutrons (bound
 87 state of udd) are the most familiar examples of baryons.

88 Hadrons are bound together by the strong nuclear force. The strong interaction is described by the
 89 theory of **Quantum Chromodynamics** (QCD). In QCD, the strong interaction is mediated by gluons,
 90 which, like the photon, are massless spin-1 gauge bosons. However, unlike the photon, gluons don’t
 91 carry electric charge. Instead, they carry an analogous color charge. There are three types of color
 92 charge, dubbed “red”, “green” and “blue”. These titles are arbitrary, and have been chosen under the
 93 heuristic that all naturally occurring states must be “colorless”. Thus, a baryon must have three quarks
 94 such that red, green and blue occur in equal measures, or meson must have a quark and antiquark such
 95 that the color and anticolor cancel out. This leads to the implication that a color charged object cannot
 96 exist in isolation, a phenomenon known as confinement [4].

97 Quarks are the only fermions that interact through the strong force. However, gluons also carry color
 98 charge, and thus interact with quarks, and also with themselves. Gluons have several interesting prop-
 99 erties; they are massless, have no distinct antiparticle, and are capable of self interaction, as shown in
 100 Figure 1.4. These properties lead to gluons splitting and radiating infinitely. Such interactions occur-
 101 ring in the vicinity of quarks result in the strength of the strong force changing inversely as a function
 102 of the distance between interacting quarks, i.e. quarks that are close to each other interact less strongly
 103 than quarks that are further apart. When quarks are separated, the potential energy arising from the
 104 strong force increases until it is energetically more favorable for the production of a quark-antiquark
 105 pair from the vacuum, screening the quarks, than it is to maintain the separation between them. This
 106 process, where a color-charged particle will cause other color-charged particles to be produced from
 107 the vacuum until the resulting bound state is color-neutral, is known as *hadronization*, and results
 108 in single quarks or gluons from the hard interaction point forming “jets” of several hadrons in the
 109 detector.

110 Confinement explains why quarks or gluons have never been observed, and why the strong-interaction
 111 is short ranged despite being mediated by the massless gluons. The property of strongly interacting
 112 particles, that at small distances of the order of less than a femtometer they basically act as free parti-

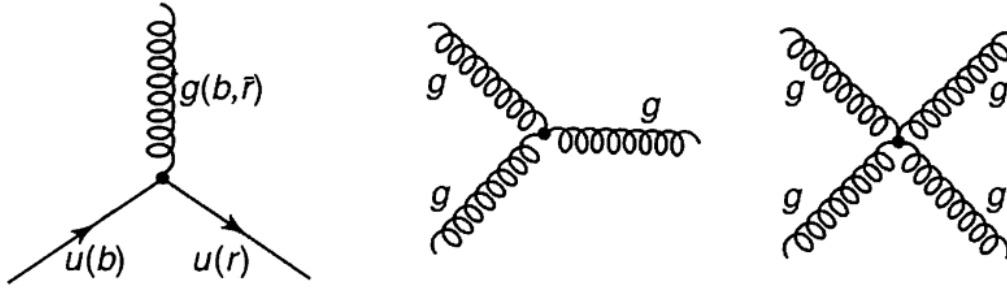


Figure 1.4: Feynman diagram showing the fundamental interaction vertex in Quantum Chromodynamics. reproduced from Ref [1]. The quark-quark-gluon vertex (left) shows the gluon mediating the interaction between two up quarks, with their color content visible, to illustrate the conservation of color charge. Gluons are also capable of self-interacting, leading to three- or four-gluon interaction vertices (center, right).

cles, is known as *asymptotic freedom*. At these scales, quarks and gluons may be treated individually rather than as a bound state.

The other family of fermions, leptons, also form three generations. Each generation consists of an electrically charged lepton, and its corresponding electrically neutral neutrino; i.e. electrons (e), muons (μ) and taus (τ) (in increasing order of mass), which have an electric charge of $-1e$, and their correspondingly flavored neutrinos (ν_e , ν_μ and ν_τ). Neutrinos, assumed by the Standard Model to be massless, have been observed to have masses [5–7] which are known to be small, but have not been measured. Tau leptons are the heaviest at 1.78 GeV, and decay rapidly, having a mean lifetime of 2.9×10^{-13} s in their rest frame. Muons have a mass of 106 MeV, about 200 times heavier than that of the electrons (0.511 MeV). Muons, however, decay with a mean lifetime of $2.2\mu\text{s}$, which is long compared to the time scales in collider experiments, and are stable enough to pass through the detectors intact.

All leptons interact through the weak nuclear force. Neutrinos especially only participate in Standard Model interactions through the weak interaction, thus making them difficult to detect. Collider experiments don't even attempt to detect neutrinos, instead inferring their presence through momentum imbalance (as they are invisible to the detectors).

There are two kinds of weak interactions; charged-current and neutral-current interactions. The Z boson, an electrically neutral, spin-1, massive gauge boson, mediate neutral-current weak interactions. Such interactions are analogous to electromagnetic interactions. However, there are notable differences. The Z boson is massive (at 91 GeV, it is one of the largest known masses in the Standard Model), whereas the photon is massless. This limits the range of the interaction, as the Z boson decays, and has a mean lifetime of the order 10^{-25} s. The fact that the Z boson is massive gives it longitudinal polarization modes [8] as well, which the photon does not possess. The Z boson also mediates interactions between neutrinos, which the photon does not as neutrinos are electrically neutral. Also, weak interactions do not respect Parity (P) symmetry. The coupling strengths of the Z boson to fermions depends on their flavor and helicity, with left-handed fermions and right-handed anti-fermions coupling more strongly than right-handed fermions and left-handed anti-fermions. In fact, the Z boson doesn't couple at all to right-handed neutrinos. However, neutral-current interactions still respect combined charge and parity (CP) symmetry.

A slight digression to define helicity is warranted at this point. Helicity is defined as the projection of a particle's spin vector onto its momentum vector. If the helicity is positive, the particle is considered to be right-handed. If it is negative, the particle is considered to be left-handed.

Charged-current interactions are mediated by the W^+ and W^- bosons, which carry an electrical

charge. Charged-current interactions do not respect parity symmetry either, and are in fact maximally parity violating; the W bosons only couple to left-handed fermions and right-handed anti-fermions. Thus, with neutrinos only interact weakly, and neither the Z nor W bosons interact with right-handed neutrinos, there doesn't appear to be a reason for right-handed neutrinos to exist within the Standard Model. Charged-interactions do not respect the combined CP symmetry either, unlike neutral-current interactions. This CP violation occurs at a small but measurable rate. The first evidence of CP violation was provided by the Fitch-Cronin experiment [9], in 1964, in the neutral kaon system, before the theory of the weak force was even completely formulated. After its formulation, it was apparent that CP violations arise from a complex phase in Cabibbo-Kobayashi-Maskawa (CKM) matrix [10], a unitary 3×3 matrix shown in Figure 1.5. Charged-current weak interactions are capable of coupling quarks from different generations, the degree of which is given by the CKM matrix. A complex phase in the elements of this matrix is what gives rise to CP violation.

$$\begin{bmatrix} d' \\ s' \\ b' \end{bmatrix} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix} \begin{bmatrix} d \\ s \\ b \end{bmatrix}$$

Figure 1.5: The Cabibbo-Kobayashi-Maskawa matrix that shows the degree of mixing among the quark flavors. Charged-current weak interactions, mediated by the W bosons, allow coupling of quarks between two generations, causing the eigenstates of the weak interaction d' , s' and b' to be superpositions of the observable mass eigenstates d , s and b .

CP violation has subsequently been confirmed in several meson decays [11–16].

Continuing the analogy between the electric charge and the color charge to the weak interaction as well, the quantum number for the weak interaction is the three-component weak isospin, T^i . It is typically defined such that T^3 is the measure component, and may be treated as the weak charge. Weak isospin is conserved in electromagnetic, strong and fermion-fermion weak interactions, however interactions involving the Higgs field change this isospin of particles. Electric charge Q , however, is always conserved, and is a combination of the weak isospin T^3 and the weak hypercharge (the quantum number corresponding to the $U(1)$ gauge symmetry) Y_W .

$$Q = T^3 + \frac{1}{2}Y_W$$

The connection between the electromagnetic and weak forces, and the similarities between weak neutral-current interactions and QED hint at unification, and indeed the Standard Model unifies them into a single *electroweak* force. The differences between electromagnetic and weak interactions, such as the mass of weak gauge bosons, arise from electroweak symmetry breaking.

The strong, weak and electromagnetic forces can be described by the $SU(3) \times SU(2) \times U(1)$ local gauge symmetry group, where the $SU(3)$ symmetry group describes the strong interaction, and the electroweak interactions are based on the $SU(2) \times U(1)$ symmetry group. There are 8+3+1 generators associated with this model, each generator corresponding to a vector boson. Thus, there exist 8 gluons for the 8 generators of the $SU(3)$ group. The interaction of the scalar Higgs field with the vector fields W^+ , W^- , W^0 and B causes the spontaneous breaking of the $SU(2) \times U(1)$ symmetry, resulting in 3 massive and one massless gauge boson. It also implies the existence of a neutral scalar boson, known as the Higgs boson, which was discovered in July 2012 [17, 18]. The 3+1 generators of $SU(2) \times U(1)$ correspond to the W^+ , W^- and Z bosons, massive vector bosons, and the massless vector boson γ (photon).

Vertices in Feynman diagrams, such as in Figures 1.3 and 1.4, correspond to a coupling between the particles, which is quantified by a coupling constant. The coupling constant in electromagnetic

interactions is called the fine structure constant α . It is a dimensionless constant, and arises from the ratio of the interaction energy between two electrically charged particles to the energy of a photon, and is approximately equal to $1/137$. In strong interactions, this coupling constant is denoted by α_S , and is very different from the electromagnetic coupling constant. The strong coupling constant α_S changes as a function of distance (or equivalently, the energy scale of the interaction), with it having a larger magnitude at larger distances (small interaction energy scales), and is small at distances smaller than a nucleon (high interaction energy scales), leading to strongly interacting particles behaving as though they are free; the origin of asymptotic freedom. This scale dependence is known as the running of the strong coupling constant. The value of the strong coupling constant at lengths scales of about the separation of nucleons ($\approx 10^{-15}$ m) is ≈ 1 . The weak interaction is extremely short range. Thus the weak coupling constant, evaluated from the lifetime of a muon, and has a coupling of strength of between $10^{-7} - 10^{-6}$. Thus, at length scales of the order of femtometers (10^{-15} m), the electromagnetic, weak and strong coupling strengths are in the ratio (up to the closest order of magnitude) $10^{-2} : 10^{-6} : 1$.

The strong coupling satisfies the following renormalization group equation (RGE):

$$\mu_R^2 \frac{d\alpha_S}{d\mu_R^2} = \beta(\alpha_S) = -(b_0\alpha_S^2 + b_1\alpha_S^3 + b_2\alpha_S^4 + \dots) \quad (1.1)$$

where the b_i are the loop-coefficients of the coupling α_S , and μ_R is the renormalization scale, of which α_S is a function. The minus sign on the right hand side of Equation 1.1 is the origin of asymptotic freedom, and dictates that the strong coupling constant becomes weak for processes involving large momentum transfers. For such processes, α_S is sufficiently small to be treated perturbatively, and this theoretical framework is called perturbative QCD (pQCD). In perturbative QCD, predictions for observables are made in terms of the renormalized coupling $\alpha_S(\mu_R^2)$, a function of an arbitrary unphysical renormalization scale μ_R . When μ_R is taken to be close to the momentum transfer scale Q of a process, the strong coupling constant $\alpha_S(\mu_R^2 \simeq Q^2)$ indicates the strength of the strong interaction in the process. Renormalization is briefly discussed in Section 3.6. Calculations for most processes occurring at high momentum transfer scales can be simplified by only calculated up to a fixed order (*fixed order calculations*).

Each interaction vertex in a Feynman diagram translates to a term featuring the corresponding coupling constant in the transition amplitude of the process from initial state to final state. The order of a coupling constant in a process is the number of times the vertex features in the transition amplitude i.e. a process having two strong vertices can be described as $O(\alpha_S^2)$. For interactions that take place at low interaction energies, the electromagnetic and weak coupling constants are much smaller than one. Thus, Feynman diagrams with more weak or electromagnetic vertices contribute less than lower order diagrams, and may be treated perturbatively. Higher order Feynman diagrams with strong vertices, however, must be at high interaction energies to be treated perturbatively. In perturbative expansions, the term with the highest contribution is known as the leading order (LO) term; the term with the next highest contribution is called the next-to-leading order (NLO) term, and so on.

Considering that the electromagnetic and weak forces have been unified into the electroweak force, it is speculated that there exists an energy scale where all the coupling constants are expected to be identical. This idea of the unifying all the forces at some scale known as the ‘‘Grand Unification’’ scale is unproven as of now, and the value of this scale is not known. In perturbative QFT, often divergences are encountered when calculating the cross section. To remove these divergences, terms dependent on the momentum scale of the interactions are introduced. The coupling constants then depend on this scale as well.

1.2 Inadequacies of the Standard Model

Despite its immense success, the Standard Model does not paint a complete picture of everything that we observe. It does not account for several phenomena that are experimentally observed, such as:

- **Dark Matter and Dark Energy:** Cosmological observations, such as galaxy rotation curves, do not match predictions based on the visible amount of mass in the Universe. A fit with the observations predicts additional invisible matter, called Dark Matter [19]. Similarly, the Universe is expanding at an accelerating rate, which hints at the existence of Dark Energy [20]. The Standard Model does not account for exotic matter such as these. In fact, the Standard Model only accounts for about 4% of the content of the Universe [21, 22].
- **Hierarchy problem [23–26]:** Quantum corrections to the Higgs boson mass are divergent, and force it to be very large. However, experiments show a surprisingly small number for the Higgs boson mass, at 125 GeV. There appear to be some extraordinary fine tuned cancellations that make this mass so small.
- **Matter-antimatter asymmetry:** Just after the Big Bang, matter and antimatter should be created in equal quantities. However, the Universe appears to have a preference for matter, indicating that in its initial state of the Universe, this symmetry was broken [27].
- **Neutrino masses:** Neutrinos are assumed to be massless in the Standard Model. However, neutrino oscillations have been observed [28], which are only possible if neutrinos have mass [29].
- **Gravity:** The Standard Model does not include gravity. If, analogous to the other forces, a ‘graviton’ is introduced into the Standard Model as an extension, it does not describe what is observed experimentally. In fact, the Standard Model is incompatible with general relativity [30].

The Standard Model is incomplete, and thus requires modifications or additions to it, which are collectively called Beyond Standard Model (BSM) theories.

1.2.1 Dark Matter

Cosmological observations of galaxies made over the decades, such as the velocity curves of galaxies (called galaxy rotation curves) indicate an anomaly; the stars in the arms of spiral galaxies appear to move faster than what would be expected from Keplerian relations, using the visible mass from the galaxies. Figure 1.6 shows the two rotation curves, expected and observed, of NGC 6503, a field¹ spiral galaxy. [31]

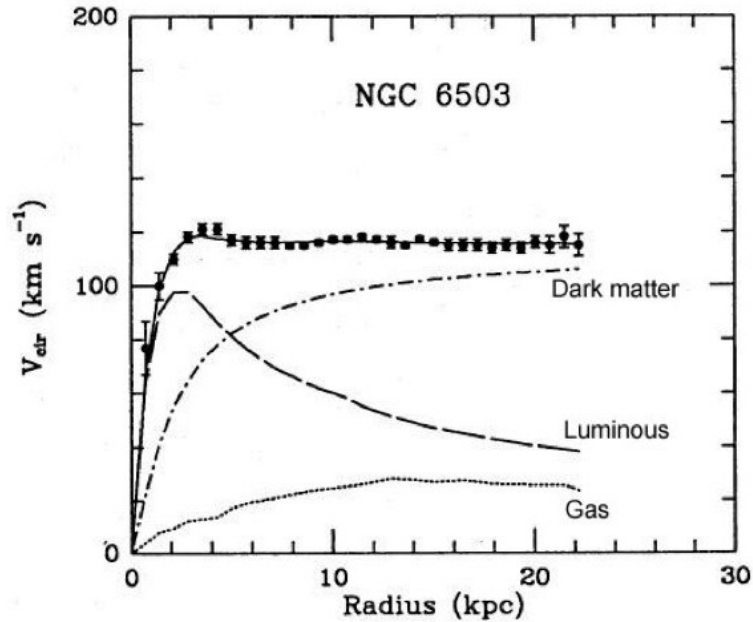


Figure 1.6: Velocity of stars in NGC 6503, a field spiral galaxy, as a function of radial distance from the center of the galaxy [31]. The 'Luminous' curve is what would be expected from the visible mass, but what is observed is much higher, indicating excess invisible matter.

Either the current understanding of Newtonian Mechanics is incomplete, or there is additional mass that is not visible which is contributing to the mass term in Newton's equation. This invisible mass is what is termed as Dark Matter. Ergo, Dark Matter appears to interact gravitationally, but not electromagnetically, with visible (Standard Model) matter. It is possible that Dark Matter is made up of an exotic and hitherto undiscovered kind of matter, and searches are underway at the LHC to look for Dark Matter via its interactions with the Standard Model.

There is additional cosmological evidence supporting Dark Matter, such as gravitational lensing of distant galaxies, structure formation in the early Universe, anisotropy in the cosmic microwave background, etc.

1.2.2 Beyond the Standard Model

Several extensions to the Standard Model have been proposed that attempt to address some of its inadequacies.

Supersymmetry (SUSY) adds another symmetry to the Standard Model, predicting the existence of *supersymmetric* partners called sparticles, to Standard Model particles. For example, sleptons are supersymmetric partners to the corresponding leptons, and differ by spin 1/2. SUSY would also

¹Field galaxies do not belong to a large cluster, and are thus gravitationally isolated

resolve the hierarchy problem by ensuring that the divergences would cancel out at all orders in the perturbation expansions, if the superpartners have mass near the electroweak scale (broadly, between 100 and 1000 GeV).

The observation of neutrino oscillations imply that neutrinos have mass, however, these observations can only reveal the mass difference between the different neutrino flavors. The absolute mass of the neutrinos has been constrained to have an upper limit of 2 eV, much smaller than the lightest SM particles, by precision measurements of tritium decays. To incorporate neutrino masses, an extension to the Standard Model, the see-saw mechanism, introduces right handed neutrinos and couples them to left-handed neutrinos with a Dirac mass term.

Both SUSY and the addition of a sterile right-handed neutrino to the SM are extensions that could provide possible candidates for Dark Matter. These candidates are known as Weakly Interacting Massive Particles (WIMPs). They do not interact electromagnetically, and are thus invisible to most detectors.

BSM theories propose experimental predictions which, if observed, could confirm that Dark Matter does exist and provide insight into its nature and properties.

Dark Matter searches at the Large Hadron Collider

As Dark Matter does not interact electromagnetically, any Dark Matter particles produced in collider experiments will be invisible to detectors at the LHC. Thus, in event reconstruction, such events are expected to be marked by a significant imbalance in transverse momentum (E_T^{miss}). Currently, Dark Matter searches are conducted at the LHC [32]. Dark Matter particles are denoted by χ .

Among the Dark Matter signature searched for at the LHC, $E_T^{\text{miss}} + X$ is an important signature. These searches look for the production of a Standard Model particle in association with E_T^{miss} . Figure 1.7 shows the Feynman diagrams for the $E_T^{\text{miss}} + X$ processes. The requirement of DM to be produced in association with another particle is imposed so that the event signature is identifiable, and allows the events to be triggered upon.

- $E_T^{\text{miss}} + \text{jet}$: In theory, it is possible to produce Dark Matter particles in association with one or more QCD jets from initial state radiation. Thus $E_T^{\text{miss}} + \text{jet}$ searches look for one or more jets in events with large E_T^{miss} .
- $E_T^{\text{miss}} + V$: In a similar manner to $E_T^{\text{miss}} + \text{jet}$ searches, a $E_T^{\text{miss}} + V$ search looks for a single vector (γ, W or Z) boson. If DM particles couple directly to a pair of gauge bosons, this may be the dominant mode of DM production.
- $E_T^{\text{miss}} + \text{Higgs}$: It may also be that a single Higgs boson is produced in association with E_T^{miss} . Such events would be characterised by a $H \rightarrow \gamma\gamma$ or $H \rightarrow b\bar{b}$ final state.

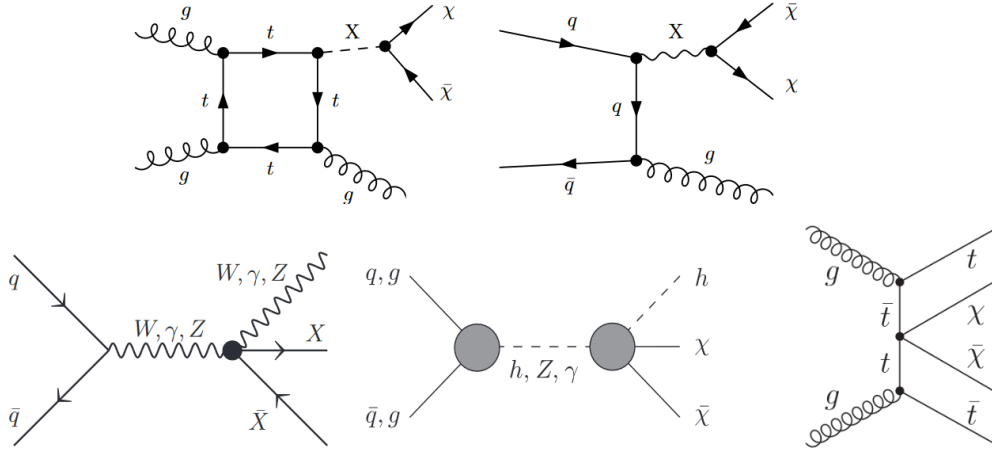


Figure 1.7: Feynman diagrams for mono X processes, showing E_T^{miss} +jet production (top) induced by gluons (top left) and quarks (top right) [33] where the mediator X can be a scalar, pseudo-scalar, vector or axial-vector particle; E_T^{miss} +V (bottom left) [34]; and E_T^{miss} +higgs (bottom center) [35], where h is the Standard Model Higgs boson with mass 125 GeV; gluon-induced $t\bar{t} + E_T^{\text{miss}}$ (bottom right)

- E_T^{miss} +top : If DM particles couple predominantly to heavy quark flavors, a search for a top quark pair is a promising direction to head in.
- E_T^{miss} +VBF : In such events, DM particles are produced from a vector boson fusion.

Several models propose mediators that couple Dark Matter particles to Standard Model particles. These mediators can be vector, pseudo-vectors, scalars, pseudo-scalars or axions. The Higgs boson is an example of a scalar mediator, and is what this thesis focuses on.

Models using the Higgs as a mediator result in events with the Invisible Higgs signature; if the mass of the DM particles is less than half the mass of the Higgs boson, it may be possible that the DM particles couple to the Standard Model via the Higgs boson, i.e $H \rightarrow \chi\chi$ processes. The main methods of Standard Model Higgs production are shown in Figure 1.1.

- Vector boson fusion (VBF): In VBF processes, the Higgs is produced from the interaction of two vector bosons.
- Production of Higgs in association with a massive vector boson (VH) : This mechanism, together with VBF are the most important methods of Higgs production in invisible Higgs searches. Such events can be recognised with a large imbalance in transverse momentum, as well as the decay products of the vector boson.
- Gluon gluon fusion (ggF) : It is also possible for the Higgs to be produced from the interaction of gluons. This is similar to a E_T^{miss} +jet like search.

Chapter 2

Experimental Apparatus

2.1 The Large Hadron Collider

The Large Hadron Collider (LHC) is a circular particle collider located in France and Switzerland. It was built by the European Council for Nuclear Research (CERN) in collaboration with over 10000 scientists from all over the world, between 1998 to 2008, when it began its operation and started collecting data. It is the world's largest, most powerful particle collider, focusing primarily on proton-proton collisions, but also conducts heavy ion collision experiments.

The goal of the LHC is to experimentally test predictions made by theories of particle physics, and look for evidence of new physics. It has enjoyed remarkable successes, such as the discovery of the Higgs Boson in 2012 [17, 18].

The LHC houses seven experiments: ATLAS and CMS are the largest, general-purpose detectors that research a number of Standard Model predictions, such searches for new physics and measurements of Standard Model parameters, among other tasks. ALICE is a heavy ion collider experiment that studies lead-lead collision, while LHCb studies mesons and baryons containing b - or c - quarks. In addition, three smaller experiments, TOTEM, MoEDAL and LHCf, are used for highly specialized research.

2.2 History

The concept of the LHC was officially recognized during a workshop held by CERN and the European Committee for Future Accelerators (ECFA) during 21-27 March 1984. The tunnel that would later house the LHC, was constructed between 1983-1988 for the Large Electron-Positron Collider experiment. The tunnel is 27 km in circumference, and located underground, underneath the border between Switzerland and France.

The construction of the LHC was completed in 2008, and on the 10th of September 2008, a beam of protons was successfully steered around the 26.7 kilometer ring of the LHC for the first time. After initial lower energy collision runs in 2009, the first 7 TeV center of mass energy collisions were recorded in 2010.

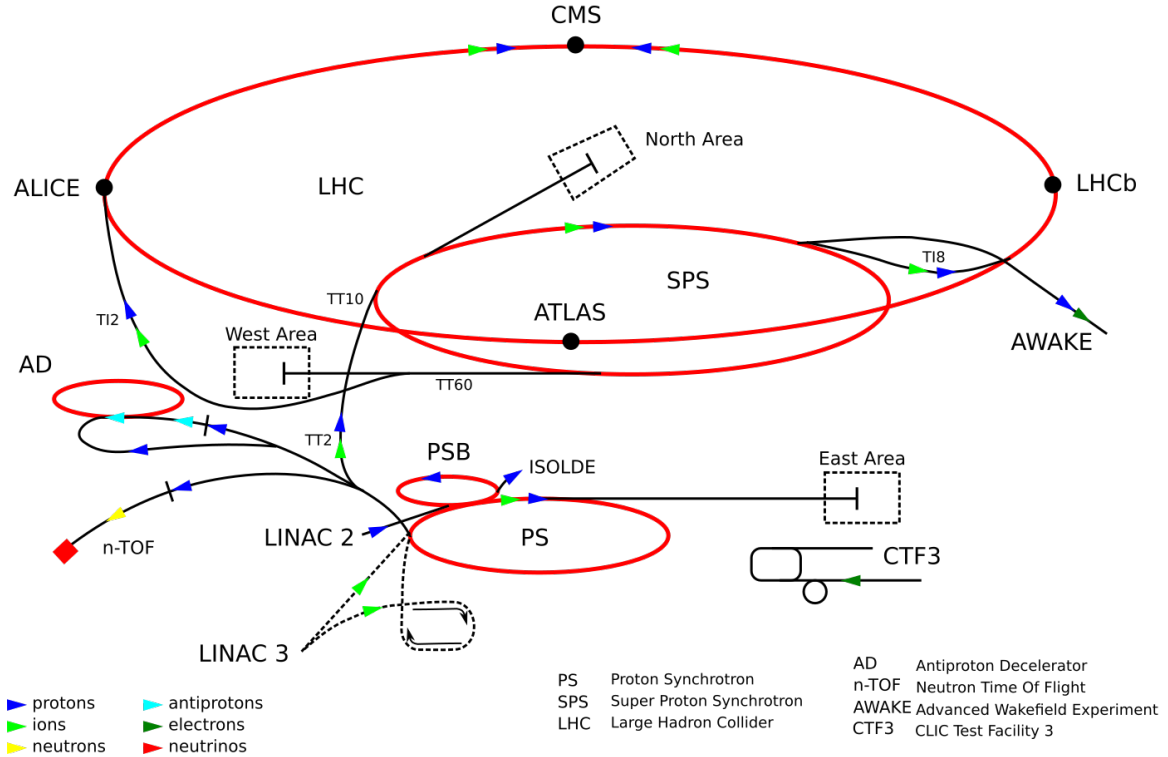


Figure 2.1: The CERN accelerator complex showing the various components of the Large Hadron Collider experiment, such as the linear accelerators, the accelerating synchrotrons, the main ring, and the four detectors, where the protons or heavy ions are collided.

344 The LHC is contained in a circular tunnel 26.7 km in circumference, located at a depth ranging
 345 between 50 and 175 meters underneath the border between Switzerland and France. The tunnel
 346 contains two parallel beam pipes. Each of the two beam pipes house a beam of protons (or heavy ions),
 347 composed of several bunches of particles, which travel in opposite directions, until they are made to
 348 collide at 4 points where the beam pipes intersect. The beams are kept on their path by an array of 1232 superconducting dipole magnets. An additional 392 superconducting quadrupole magnets
 349 focus the beams to maximize the chance of interaction. Magnets of higher multipole orders are used
 350 to correct deviations in the field geometry. In total, the LHC uses about 10000 superconducting
 351 magnets. In order to keep these magnets at superconducting temperatures (-271.25°C), about 96
 352 tonnes of helium-4 coolant is required, thus making the LHC the world's largest cryogenic facility at
 353 liquid helium temperature.
 354

355 The colliding protons are prepared for collisions by a sequence of systems that progressively increase
 356 their energy. The linear particle accelerator, LINAC 2 generates 50 MeV protons, which are fed into
 357 the Proton Synchrotron Booster (PSB). The PSB accelerates the protons to 1.4 GeV, and from there
 358 the protons are injected into the Proton Synchrotron (PS), where they are accelerated to 26 GeV. The
 359 Super Proton Synchrotron (SPS) then increases their energy further to 450 GeV, before the protons
 360 are injected into the LHC ring.

361 Instead of a continuous beam, the protons are accumulated into bunches and accelerated to their peak
 362 energy at 6.5 TeV over a period of 20 minutes, during which the magnetic field of the superconducting
 363 dipole magnets is increased from 0.54 to 7.7 Teslas, and circulated for up to 24 hours while collisions
 364 occur at the four intersection points. Each proton bunch consists of approximate 1.15×10^{11} protons
 365 in each bunch, with 2,556 bunches [36] at a time. The interactions happen at intervals 25 nanoseconds

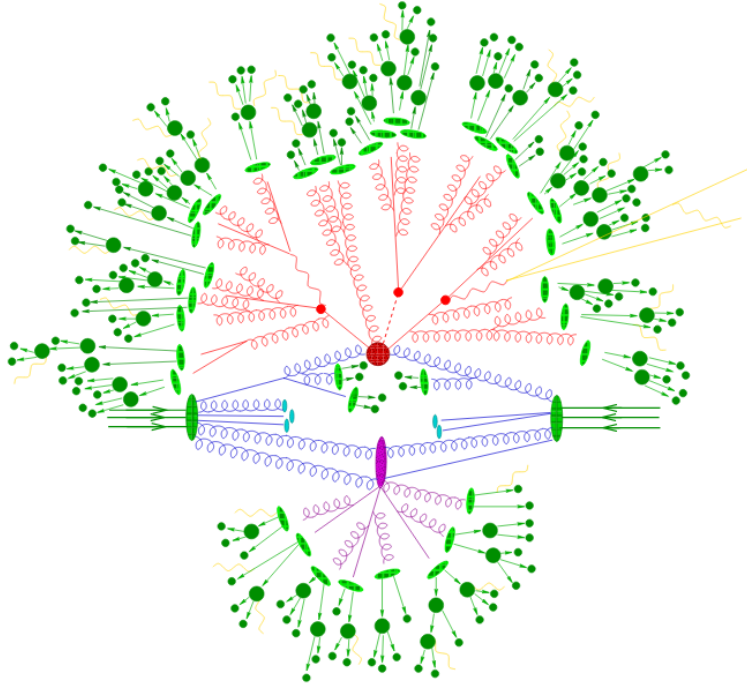


Figure 2.2: Illustration of a pp collision. The initial proton proton collision (the green ellipses) undergo initial state radiation, and interact in the hard process (red circle). The emergent parton shower (red) from the hard interaction results in partons that hadronise into color neutral states (light green circles). The proton remnants then participate in a secondary interaction (purple ellipse) creating a parton shower (purple) again, which hadronises and further decays into stable particles. This, along with the beam remnants (light blue ellipses), is part of the underlying event. Electromagnetic radiation (yellow) can be emitted by charged particles at any stage.

apart. Figure 2.1 shows the layout of the LHC main ring, LINAC2, PSB, PS and SPS.

2.4 Proton-Proton Collisions

Theory and experiment go hand in hand. It is necessary to have experimental confirmation of theoretical predictions, while at the same time, new or unexpected experimental observations prod theories along in the right direction. There are a number of parameters in theory that are unknown, and thus, experiments provide measurements of such parameters.

The work in thesis was conducted with the ATLAS Collaboration. ATLAS, being one of the detector experiments at the LHC, probes proton-proton collisions. Figure 2.2 shows a proton proton collision in detail. This section gives an overview of the physics of proton-proton collisions, which are one of several ways to probe particle interactions at high energy scales.

Protons are baryons, bound states of three quarks (uud), known as the valence quarks. However, the mass of the quarks put together is only about 1% of the mass of the proton (938 MeV). The remainder of the proton mass originates from the QCD binding energy, which is the exchange of virtual gluons. The constituents of the proton, namely the quarks and gluons, are collectively known as partons. Roughly half the total momentum of the proton is carried by the gluons [8]. Now, the number of gluons is not conserved, and they are capable of self interaction, the gluon structure within a proton is not constant. Gluons produce virtual $q\bar{q}$ pairs that again annihilate on timescales of the order $t_{virt} = 1/\Delta E$ [37]. A color-charged particle with sufficient energy to probe the particle structure of the proton is capable of interacting with a color-charged parton (quark or gluon). Interesting physics in

pp collisions are initiated by qq , $q\bar{q}$, qg and gg scattering.

The fraction of proton momentum carried by a parton is not deterministic, because of the unpredictable gluon structure. It is, however, possible to model the parton momenta as a probability distribution. For proton with momentum P , a parton of a given type carrying a momentum xP is given by the **Parton Distribution Function** (PDF) $f(x, Q^2)$, where x is the fraction of momentum carried by the parton, and Q is the momentum transfer of the interaction [37], and sets the scale at which the incoming particle is able to resolve the partons. QCD predicts quantitatively the rate of change of parton distributions when the energy scale Q^2 varies, governed by the DGLAP equations (names after the authors; Dokshitzer, Gribov, Lipatov, Altarelli, Parisi) [38], in the region where perturbative calculations can be applied. While the DGLAP differential equations give the energy scale Q^2 dependence, they cannot predict the x dependence of the parton distributions at a given Q^2 . The PDFs sets must be obtained from fits on experimental data from $e^\pm p$ deep inelastic scattering (DIS), and hadron collider data. Fits are carried out on a large number of cross section data points, on a grid of Q^2 and x values from several experiments. This work is carried out by groups such as MSTW [39–41], MMHT [42], NNPDF [43], etc. Figure 2.3 shows an example of parton distribution functions.

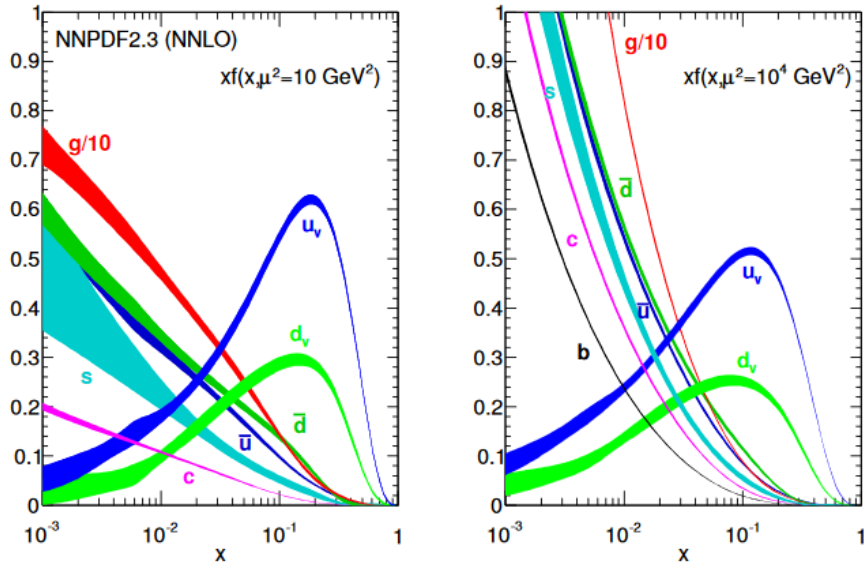


Figure 2.3: Parton Distribution Functions from NNPDF3.1, reproduced from [43]. The y-axis displays the probability of the given parton as a function of the proton momentum fraction, given on the x -axis. As seen here, the u quark has about 66% probability, and the d -quark has about 33% probability of possessing 10% of a proton's momentum. Thus the proton's quark content is uud . Here, μ^2 is used in place of Q^2 to denote the momentum transfer.

The rate at which a scattering process occurs is called the cross section σ of the process, having the unit given in barns. Barn is a unit of area, $b = 10^{-24} \text{ cm}^2$. The number of collisions is characterised by the luminosity \mathcal{L} . The luminosity gives a measure of the performance of a particle accelerator, and is defined as the ratio of the rate of event detection to the cross section (Equation 2.1):

$$\mathcal{L} = \frac{1}{\sigma} \frac{dN}{dt} \quad (2.1)$$

The rate of events having a final state X will then be given by Equation 2.2.

$$\frac{dN_X}{dt} = \sigma(pp \rightarrow X) \mathcal{L} \quad (2.2)$$

For head-on colliding protons, each with momentum P , such that their center-of-mass energy is $\sqrt{s} = 2P$, the interacting partons will have a total energy $\sqrt{\hat{s}} = \sqrt{2x_1x_2}P$, where x_1 and x_2 give the fraction of its proton momentum carried by each parton. Thus, the cross section of the interaction is given by Equation 2.3.

$$\sigma(pp \rightarrow X) = \sum_{p_1, p_2 \in q, \bar{q}, g} C_{p_1, p_2} \int dx_1 dx_2 f_{p_1}(x_1, Q^2) f_{p_2}(x_2, Q^2) \sigma_{ME}(p_1 + p_2 \rightarrow X) \quad (2.3)$$

where σ_{ME} is the matrix element level cross section for the scattering of the individual partons to the final state X , and C_{p_1, p_2} is a combinatorial factor based on the number of possible color combinations, varying based on the initial state partons p_1 and p_2 . Separation of the calculation into the perturbative hard scattering physics and non perturbative PDFs simplifies calculations.

2.5 The ATLAS experiment

The ATLAS (A large Toroidal Apparatus detector) is located at one of the four beam intersection points. It is a multipurpose experiment which, after the discovery of the Higgs boson in 2012, focuses on a wide range of topics, including searches for new physics, such as supersymmetry or dark matter, and measurements of Standard Model parameters. The experiment is a collaboration between around 4000 physicists from over 175 institutions in 38 countries.

The ATLAS detector is a large apparatus with a cylindrical geometry, forward-backward symmetry, and nearly 4π solid angle coverage. It is 46 meters long, 25 meters in diameter and weight 7000 tonnes. The detector consists of concentric cylindrical layers around the interaction point, where the proton beams collide. Broadly, it consists of the Inner Detector, the electromagnetic (EM) and hadronic calorimeters, the muon spectrometers and the magnetic systems, each composed of multiple layers. These layers complement each other's functionality: the inner detector accurately tracks charged particles passing through it, the calorimeters measure the energy deposited by the particles passing through or stopped by it, the magnet systems employ the Lorentz force law to bend charged particles and measure their momenta, and the muon systems measure the momenta of muons that pass through all other layers to reach it. Figure 2.4 displays the ATLAS detector and its components.

The ATLAS detector cannot detect neutrinos or other invisible particles; their existence is inferred from the momentum imbalance from the detected stable particles that register in the detector components. Thus, the detector must be “hermetic”, and must have no blind spots. The momentum imbalance can be accurately calculated in the transverse plane, and is called missing transverse momentum, denoted by E_T^{miss} .

2.5.1 Coordinate system

ATLAS uses a right-handed Cartesian coordinate system, with the interaction point as the origin. The z -axis is along the beam direction, the x -axis points towards the center of the LHC ring, and the y -axis is directed vertically. The xy -plane defines the transverse plane, and is represented by polar coordinates (r, ϕ) with $\phi = 0$ on the x -axis. The pseudorapidity replaces the polar angle θ as given in Equation 2.4. Some values of the pseudorapidity are shown in Figure 2.5.

$$\eta = -\ln \left(\tan \left(\frac{\theta}{2} \right) \right) \quad (2.4)$$

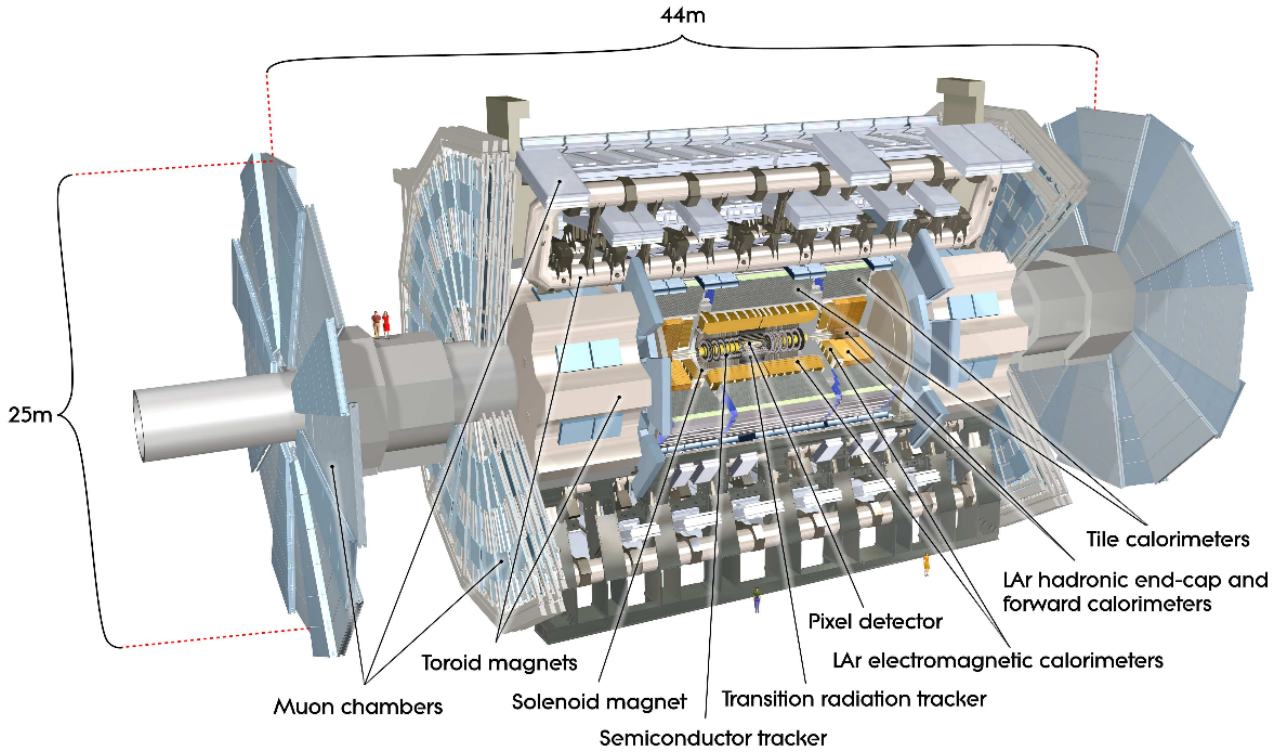


Figure 2.4: Cut away view of the ATLAS detector, displaying its dimensions and components, reproduced from Ref [44]

In the limit where the mass of particles is much less than their momentum, it is approximately equal to the rapidity (y) of the particle. The rapidity,

$$y = \frac{1}{2} \ln \left(\frac{E + p_z}{E - p_z} \right), \quad (2.5)$$

in turn, is an effective coordinate as it is Lorentz invariant under boosts in the z -direction.

The separation between two physical objects in the detector is described by

$$\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2} \quad (2.6)$$

where ϕ is the angular coordinate in the transverse plane.

2.5.2 Inner Detector

The Inner Detector (ID) [45] is a tracking detector located at the center of the ATLAS detector. It extends from a few centimeters away from the proton beam axis to a radius of 1.2 meters, and is 6.2 meters in length along the beam pipe.

The three main components of the ID are the pixel detector consisting of 140 million silicon pixels, the SemiConductor Tracker(SCT) made of layers of silicon strips, and the Transition Radiation Tracker(TRT) which is composed of $\approx 300,000$ straw drift tubes. Together, the ID has a solid angle coverage of $|\eta| < 2.5$, and occupies a cylindrical volume between $33.25 \text{ mm} < r < 1082 \text{ mm}$. The purpose of the ID is to accurately detect the path of charged particles as they pass through it, bending in the magnetic field of the solenoid. This allows the measurement of their momenta.

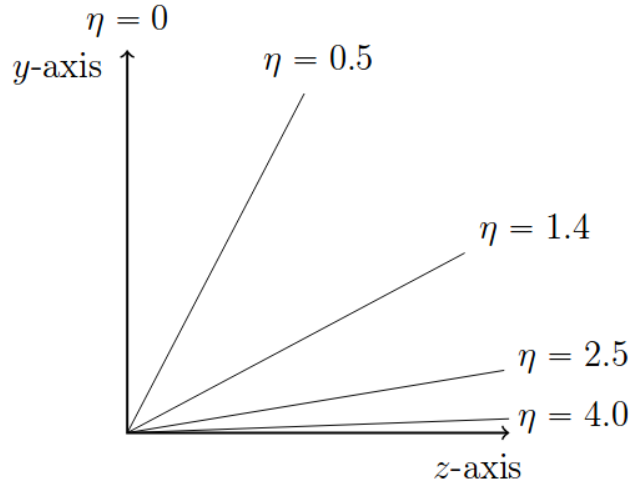


Figure 2.5: Some important and often mentioned values of pseudorapidity η .

2.5.3 Calorimeters

The calorimeter system is used to measure the energy of hadrons, electron and photons that leave energy deposits in it. ATLAS has an electromagnetic calorimeter, located just outside the ID and based on Liquid Argon (LAr), and a hadronic calorimeter, located outside the EM calorimeter that is based on iron-scintillator “tiles” (Tile). The two detectors employ different methods owing to the different interactions of electrons or photons, and hadrons. Overall, the calorimeters cover a solid angle up to $|\eta| < 4.9$. The electromagnetic calorimeter provides finer grained resolution for electron and photon measurements. The hadronic calorimeter has coarser resolution, but is adequate for jet-reconstruction and E_T^{miss} measurement.

2.5.4 Muon Spectrometer

Muons are stable particles, and unlike electrons, photons or hadrons, do not deposit all their energy in the calorimeters. Thus, muons are able to reach the outermost region of the detector. The Muon Spectrometers are constructed on the outer layers of the detector, and consist of three toroidal magnets that provide the magnetic field, a set of 1200 chambers measuring the outgoing muon tracks with high precision, and a set of triggering chambers with accurate time-resolution. They measure the position of muons as they traverse the detector, and the deflection in the muon tracks in the magnetic field allow the measurement of their momentum. The muon systems are thus used as triggers to select events with high energy muons and cover a range of $|\eta| < 2.7$.

2.5.5 Magnet Systems

The ATLAS detector uses two large superconducting solenoid magnet systems to bend charged particles such that their momenta can be measured, due to the Lorentz force. The inner solenoid produces a field of 2T that surrounds the Inner Detector. The outer toroidal magnetic field is produced by eight large air-core superconducting barrel loops and two end-caps air toroidal magnets located within the muon system. The magnetic field generated extends 26 meters long and 20 meters in diameter. The field is not uniform inside the detector.

2.5.6 ATLAS Triggers and Data Collection

The ATLAS detector employs a multi-level trigger to reduce the bandwidth from the LHC proton bunch crossing rate of 40MHz to 1kHz that is written to disk [46, 47]. The first tier, called Level 1 (L1), is implemented in real time, and makes an early event selection containing objects of interest, and reduces the data flow to 100kHz. The second tier, known as the High Level Trigger (HLT) [48] is implemented on a computing cluster with custom triggering software. The HLT uses information from the L1 system to retrieve information from the Readout System (ROS) [49].

2.6 Event Simulation

It is essential to have some reference to compare with when interpreting LHC data. The observations must be compared to expected outcomes predicted by physical models, such as the Standard Model or SUSY. Thus, ATLAS uses event simulation, beginning from the initial proton proton collisions, leading up to the process(es) of interest, up to the expected detector response.

Event generation employs the $pp \rightarrow X$ process of interest using random sampling from Monte Carlo (MC) techniques. These randomly drawn samples represent possible outcomes of a given process. The processes are generated using software packages such as MadGraph [50], that calculate the matrix element for each process to some order in QCD. These generators use parton distribution functions (PDFs) to model the interaction between partons up to a given order in QCD, with higher order corrections being accounted for in a “k-factor” (details in Chapter 4). The radiating partons after the hard interaction result in a shower are modelled by a parton showering software, such as Pythia [51]. The output of these steps is input into the next step of the simulation, and are also used for generator-level studies, called “truth-level”.

The next step is detector simulation, where the propagation of particles through the different layers of the detector is simulated using software such as Geant4 [52]. This is a slow process, and often a faster but more approximate detector simulation is used. The detector simulation digitizes the interaction of particles by emulating the response of the electronics in the detector. The output of this step is identical to the response of the actual physical detector.

At this point, both simulated and actual recorded events are used to identify the objects associated with fundamental particles, such as electrons, muons, photons and jets. If not matched to physics objects, the energy deposits are collected into a “soft terms” category, which is then used in the calculation of missing transverse momentum E_T^{miss} .

2.6.1 Missing Transverse Momentum

The missing transverse momentum is an important quantity in looking for new physics, where stable non-electromagnetically and non-hadronically interacting particle is expected. Such particles do not interact with any of the various layers, and thus result in an imbalance in the total momentum. Since the momentum of the protons is only along the beam axis (x -axis), the total momentum in the transverse plane is zero before the collision. Thus, it is possible to measure the imbalance in the total transverse momentum and establish the presence of such particles by their absence. For predicted particles with high mass, or particles that carry high momentum away from the hard interaction vertex, a large imbalance is expected.

The missing transverse momentum of an event is defined as the negative vector sum of the transverse

526 momenta of all visible reconstructed objects in the event:

$$\vec{p}_T^{\text{miss}} = - \sum_{\text{visible}} \vec{p}_T \quad (2.7)$$

527

528 where the visible objects include electrons, muons, jets, photons, taus, and a soft term.

529 The magnitude of \vec{p}_T^{miss} is denoted by E_T^{miss} .

Chapter 3

Analysis Strategy

3.1 Invisible Higgs in association with a Z boson - ZH

In the search for Dark Matter candidates, some Beyond Standard Model theories postulate that the Higgs boson mediates the interaction between Dark Matter particles and Standard Model particles, as shown in Figure 3.1. In this thesis, the production of the Higgs boson, in association with a Z boson is considered. The Higgs boson decays into Dark Matter candidates (Weakly Interacting Massive Particles, or WIMPS), and the Z boson decays into a lepton-antilepton pair. As Dark Matter is invisible to current detectors, this process results in the $\ell\ell + E_T^{\text{miss}}$ signature.

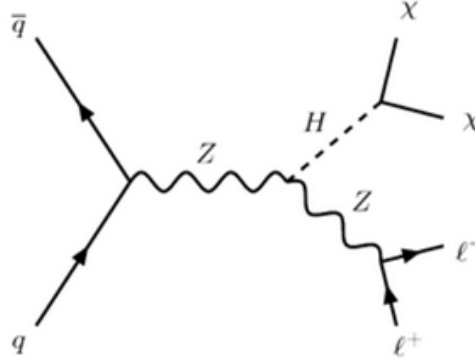


Figure 3.1: Feynman diagram showing the associated production of a Higgs boson with a Z boson. The Higgs boson decays to two invisible DM particles and the Z boson decays leptonically, resulting in the $\ell\ell + E_T^{\text{miss}}$ signature.

The main Standard Model background processes for the $\ell\ell + E_T^{\text{miss}}$ final state are $ZZ \rightarrow \ell\ell\nu\nu$, $WZ \rightarrow \ell\ell\nu$, $WW \rightarrow \ell\nu\ell\nu$, $Z + \text{jets}$ and $W + \text{jets}$.

3.1.1 Selection Criteria

The selection criteria used in Ref [53] is applied for the analysis reported in this thesis as well. The search is conducted on events with a $\ell\ell + E_T^{\text{miss}}$ final state, having a pair of high p_T electrons (ee) or muons ($\mu\mu$), and large missing transverse momentum. Events with extra leptons or b -jets are removed to reduce backgrounds, and the requirement of a boosted Z boson back to back with the missing transverse momentum vector is imposed. Electron candidates are selected based on the

ATLAS tracker and EM calorimeter dimensions, with $p_T > 7$ GeV and pseudorapidity $|\eta| < 2.47$. Similarly, muon candidates are required to have $p_T > 7$ GeV and pseudorapidity $|\eta| < 2.5$.

The leading and subleading leptons in the event are required to have sufficiently high transverse momentum, with the leading lepton required to have $p_T > 30$ GeV, and the subleading lepton required to have $p_T > 20$ GeV. The veto on additional leptons serves to remove background from processes such as $WZ \rightarrow \ell\ell\nu$. The reconstructed mass of the leading and subleading leptons is required to be within a 15 GeV window around the mass of the Z boson, i.e. $76 < m_{\ell\ell} < 106$ GeV, to suppress backgrounds where the final state leptons do not originate from a Z boson (non-resonant $\ell\ell$ processes). The E_T^{miss} is expected to be back to back to a Z boson with high p_T , and originates from an invisibly decaying Higgs boson, thus is expected to be high as well; a cut requiring $E_T^{\text{miss}} > 90$ GeV reduces the number of events with low E_T^{miss} . As the leading and subleading leptons are expected to come from the decay of a highly boosted Z boson, their separation is expected to be small. Thus, the leading and subleading leptons in selected events are required to be separated by $\Delta R_{\ell\ell} < 1.8$. The requirement of back to back Z boson and E_T^{miss} is enforced by requiring the angular separation of the E_T^{miss} vector from the vector reconstructed from the leading and subleading leptons in the transverse plane, $\Delta\phi(\vec{p}_T^{\ell\ell}, \vec{E}_T^{\text{miss}})$ to be greater than 2.7 radians. The remaining Z+jets background events have large E_T^{miss} because of significant soft-term contribution. To remove this Z+jets background, the magnitude of the difference between the dilepton transverse momentum $p_T(\ell\ell)$ and the sum of the jet p_T and E_T^{miss} must be less than 20% of the dilepton p_T . To suppress $t\bar{t}$ and Wt backgrounds, events with one or more b -jets (jets that originate from a b -quark, such as from the decay of a top quark) are vetoed.

Table 3.1 summarises the event selection criteria in the $\ell\ell + E_T^{\text{miss}}$ search, as shown in [53].

Selection criteria	
Two leptons	Two opposite-sign leptons, leading (subleading) $p_T > 30$ (20) GeV
Third lepton veto	Veto events if any additional lepton with $p_T > 7$ GeV
$m_{\ell\ell}$	$76 < m_{\ell\ell} < 106$ GeV
E_T^{miss} and E_T^{miss}/H_T	$E_T^{\text{miss}} > 90$ GeV and $E_T^{\text{miss}}/H_T > 0.6$
$\Delta\phi(\vec{p}_T^{\ell\ell}, \vec{p}_T^{\text{miss}})$	$\Delta\phi(\vec{p}_T^{\ell\ell}, \vec{p}_T^{\text{miss}}) > 2.7$ radians
$\Delta R_{\ell\ell}$	$\Delta R_{\ell\ell} < 1.8$
Fractional p_T difference	$ p_T^{\ell\ell} - p_T^{\text{miss,jets}} /p_T^{\ell\ell} < 0.2$
b -jet veto	$N(b\text{-jets}) = 0$ with b -jet $p_T > 20$ GeV and $ \eta < 2.5$

Table 3.1: Event selection criteria in the $\ell\ell + E_T^{\text{miss}}$ search as shown in Ref [53]

3.1.2 Results of the ZH search

Using the selections in Table 3.1, background predictions are made in the $\ell\ell + E_T^{\text{miss}}$ channel. Figure 3.2 shows the observed E_T^{miss} distribution in the ee and $\mu\mu$ channels, compared to the signal and background predictions. As discussed in Ref [53], the dominant source of background is the $ZZ \rightarrow \ell\ell\nu\nu$ process, contributing $\approx 60\%$ of the background. $WZ \rightarrow ll\nu$ events, where the W boson decays into a electron or muon that escapes detection, account for 25% of the total background. $Z(\rightarrow ll)$ +jets process with misreconstructed E_T^{miss} contributes to about 8% of the total background, and non-resonant- ll processes, consisting of $t\bar{t}$, Wt , WW and $Z \rightarrow \tau\tau$ production contribute similarly. W +jets, VVV , and

577 $t\bar{t}V(V)$ backgrounds contribute to a minor extent ($< 1\%$).

An upper limit of 67% is placed on the Higgs \rightarrow DM branching ratio at the 95% confidence level.

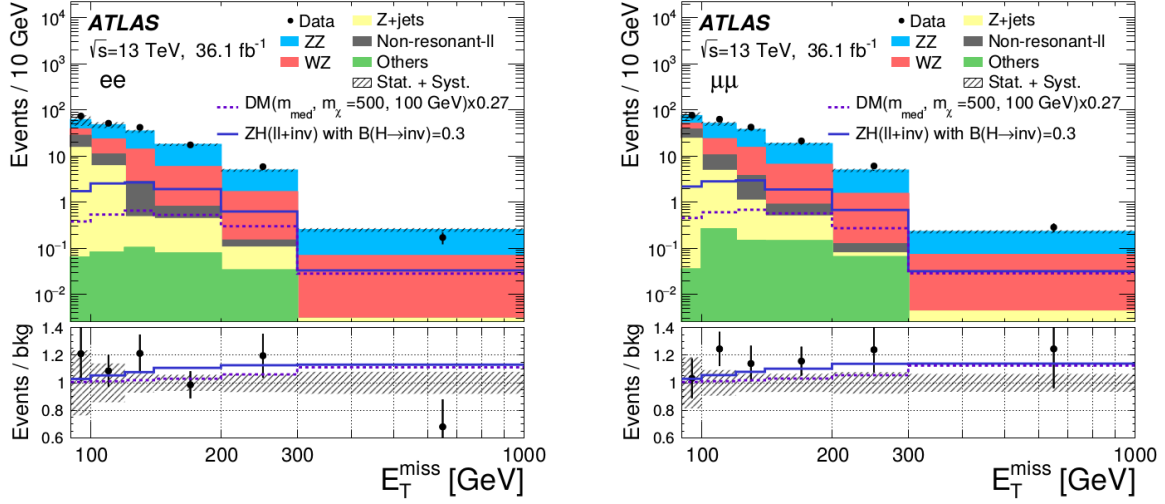


Figure 3.2: The observed E_T^{miss} distributions in the ee (left) and $\mu\mu$ channels, compared to the signal and background predictions, reproduced from Ref [53]. The total statistical and systematic uncertainty on the background predictions are shown by the error bands. The Standard Model background predictions are stacked. The $ZH \rightarrow ll + \text{invisible}$ signal distribution is shown with $B_{H \rightarrow \text{inv}} = 0.3$. The dotted line shows an alternative model for DM production that is not discussed in this work.

578

579 This thesis focuses on the ZZ background; its estimation and the uncertainty associated with it. In
580 Ref [53], the ZZ background is estimated from simulation with a total uncertainty of 10%.

581 3.2 Background estimation: ZZ

582 It is difficult to distinguish the irreducible $ZZ \rightarrow \ell\ell\nu\nu$ background events from the signal process, as
583 the final state is identical to that of $ZH \rightarrow \ell\ell + E_T^{\text{miss}}$. The contribution of $ZZ \rightarrow \ell\ell\nu\nu$ is currently
584 estimated using simulation. Figure 3.3 shows the Standard Model production of $q\bar{q} \rightarrow ZZ$ and $gg \rightarrow$
585 ZZ . One of the Z bosons decays leptonically (into e^+e^- or $\mu^+\mu^-$), while the other Z boson decays
586 into neutrinos ($\nu\bar{\nu}$). Neutrinos are very weakly interacting, and thus are invisible to the detectors at
587 the LHC, and thus result in events with missing transverse momentum.

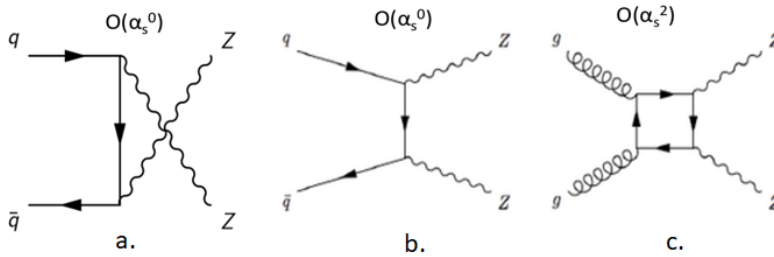


Figure 3.3: Feynman diagram showing ZZ production, in the s-channel (a) and t-channel (b) induced by $q\bar{q}$ at LO QCD, and induced by gluons (c) at NNLO QCD.

It is possible to estimate the $ZZ \rightarrow \ell\ell\nu\nu$ using $ZZ \rightarrow \ell\ell\ell\ell$ data. However, the precision of this process is statistically limited. The branching fraction $Z \rightarrow \ell\ell$ for one flavor of lepton (e/μ) is $\approx 3.4\%$, and

$Z \rightarrow \nu\nu$ is 20%.

$$BR(ZZ \rightarrow \ell\ell\ell\ell) = (2 \times 0.034) \times (2 \times 0.034) = 0.00462 \quad (3.1)$$

$$BR(ZZ \rightarrow \ell\ell\nu\nu) = (2 \times 0.034) \times (0.2) \times 2 = 0.0272 \quad (3.2)$$

588

589 Thus, branching fraction of $ZZ \rightarrow \ell\ell\ell\ell$ ($\approx 0.46\%$) compared to $ZZ \rightarrow \ell\ell\nu\nu$ (2.7%), which is about 6
590 times higher. The low branching fraction of $ZZ \rightarrow \ell\ell\ell\ell$ limits the statistics.

591 Motivated by an analysis using γ +jets to estimate Z +jets [54], an alternative method to estimate
592 $ZZ \rightarrow \ell\ell\nu\nu$ is to look at the $Z\gamma \rightarrow \ell\ell\gamma$ process. Figure 3.4 shows the leading order diagrams for the
593 production of $Z\gamma$, where the Z boson further decays leptonically. Figures 3.4.a, b and c are similar
594 to the production of ZZ , with a photon instead of one of the Z bosons. The main differences in the
595 two processes are the couplings of the photon and Z boson to the quarks, and the fact that photons are
596 massless, whereas the Z boson is massive.

597 Figure 3.4.d gives the $\ell\ell\gamma$ final state, however, the photon is radiated off of a final state lepton, i.e.
598 Final State Radiation (FSR). This process must be suppressed as it does not correspond to a similar
599 $ZZ \rightarrow \ell\ell\nu\nu$ process. The imposition of the mass window on the reconstructed mass of the lepton pair
600 to be within 15 GeV of the Z boson mass automatically does this.

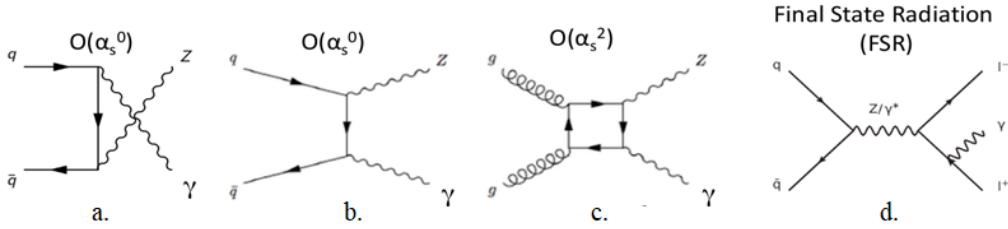


Figure 3.4: Feynman diagram showing $Z\gamma$ production, in the s-channel (a) and t-channel (b) induced by $q\bar{q}$ at LO QCD, and induced by gluons (c) at NNLO QCD. Diagram (d) shows a similar final state, but the photon is radiated off of a final state lepton (Final State Radiation), which does not have a corresponding diagram in the $ZZ \rightarrow \ell\ell\nu\nu$ process, and hence has to be suppressed.

601 At high Z boson transverse momentum, the $Z\gamma \rightarrow \ell\ell\gamma$ process should be similar to $ZZ \rightarrow \ell\ell\nu\nu$, as
602 the mass of the Z boson will be negligibly small compared to its p_T . The $Z\gamma \rightarrow \ell\ell\gamma$ signal is also
603 pure, and has a $BR \times \sigma$ as compared to $ZZ \rightarrow \ell\ell\nu\nu$. Thus, it should be possible to use $Z\gamma \rightarrow \ell\ell\gamma$ data
604 to estimate the contribution of $ZZ \rightarrow \ell\ell\nu\nu$ in regions of high Z boson p_T .

605 3.3 Approach

606 Thus far, it has been established that a method to estimate the ZZ background contribution to the
607 $ll + E_T^{\text{miss}}$ final state is to use $Z(\rightarrow ll)\gamma$ data, where the photon models the Standard Model invisible Z
608 boson. A transfer factor R is introduced as the ratio of the cross sections of $ZZ \rightarrow \ell\ell\nu\nu$ to $Z\gamma \rightarrow \ell\ell\gamma$
609. In the high Z boson p_T region, the two processes are kinematically similar, therefore the curve of
610 the transfer factor R as a function of p_T is expected to approach a constant value. This transfer can be
611 used to estimate to the contribution of $ZZ \rightarrow \ell\ell\nu\nu$ from $Z\gamma \rightarrow \ell\ell\gamma$ data.

612 A ratio of the cross sections of $ZZ \rightarrow \ell\ell\nu\nu$ and $Z\gamma \rightarrow \ell\ell\gamma$ processes is taken to obtain the R distribution
613 as a function of $E_T^{\text{miss}}/p_T(\gamma)$. The uncertainty on R is calculated by varying several parameters at
614 the generator level, such as the renormalization and factorization scales, the PDF sets used, photon
615 fragmentation, etc. The contributions of the $q\bar{q}$ and gg processes are estimated separately.

This thesis estimates value of the transfer factor, and the theoretical uncertainties associated with it. The $ZZ \rightarrow \ell\ell\nu\nu$ and $Z\gamma \rightarrow \ell\ell\gamma$ cross sections are obtained from MCFM, a femtobarn level matrix element generator. Varying the input parameters provided in the MCFM input file, the theoretical uncertainties are estimated.

3.4 Transfer factor R

To estimate the background, a transfer factor $R(p_T)$ is introduced, defined to be the ratio of the cross sections of $ZZ \rightarrow \ell\ell\nu\nu$ to $Z\gamma \rightarrow \ell\ell\gamma$ as a function of the p_T .

$$R(p_T) = \frac{\sigma_{ZZ}(p_T)}{\sigma_{Z\gamma}(p_T)} \quad (3.3)$$

With the two processes being kinematically similar at high p_T , R depends on the coupling of the Z and γ to quarks. It would be expected to reach a constant value at high p_T that can be determined theoretically. In the following paragraph, an attempt is made to obtain a simple approximate calculation of R from the contribution of qq process.

The photon - quark and Z boson - quark couplings in the Standard Model are given by,

$$-ieQ_q\gamma^\mu \quad \text{and} \quad \frac{-ie}{2\sin\theta_W\cos\theta_W}\gamma^\mu(v_q - a_q\gamma_5) \quad (3.4)$$

respectively, where Q_q, v_q and a_q are respectively the electric, vector and axial neutral weak couplings of the quarks, and θ_W is the weak mixing angle. There is a contribution due to the Z mass which appears in the internal propagators and phase space integration. This contribution becomes less important in the $p_T(\gamma) \gg M_Z$ region.

Thus, the leading order contributions from $q\bar{q} \rightarrow ZZ$ and $q\bar{q} \rightarrow Z\gamma$ are shown in Equation 3.5.

$$\begin{aligned} \sigma(q\bar{q} \rightarrow ZZ) &\propto \frac{1}{2} \frac{e^4 \{(v_q^2 + a_q^2)^2 + 4v_q^2 a_q^2\}}{16\sin^4\theta_W\cos^4\theta_W} \\ \sigma(q\bar{q} \rightarrow Z\gamma) &\propto \frac{e^2 Q_q^2 (v_q^2 + a_q^2)}{4\sin^2\theta_W\cos\theta_W} \end{aligned} \quad (3.5)$$

The u and d quarks present in a pp collision have different coupling strengths to the Z boson as stated in Ref [55], their relative contributions are accounted for using Equation 3.6

$$R = \frac{\sigma(u\bar{u} \rightarrow ZZ)\langle u \rangle + \sigma(d\bar{d} \rightarrow ZZ)\langle d \rangle}{\sigma(u\bar{u} \rightarrow Z\gamma)\langle u \rangle + \sigma(d\bar{d} \rightarrow Z\gamma)\langle d \rangle} \quad (3.6)$$

Using the vector and axial couplings of the Z boson to u and d quarks¹, assuming $\langle d \rangle / \langle u \rangle = 0.5$ and setting $\sin^2\theta_W = 0.2315$, $R \approx 1.28$ for the dominant $q\bar{q}$ interaction. This approximate calculation has not been performed for gluon induced channels, as they involve loops and require a more involved calculation. It will also give a significantly different value as the contributions of the gluon induced channels are different for the ZZ and $Z\gamma$ processes.

This transfer factor R may be used with $Z\gamma$ data to estimate the contribution of ZZ with reasonable accuracy at high p_T . To improve precision, it is necessary to estimate the theoretical uncertainties on the transfer factor R .

¹Vector and Axial couplings of Z to u and d quarks: $v_u = 0.18, a_u = 0.50, v_d = -0.35, a_d = -0.514$

3.5 Theoretical Uncertainties

In this study, the following sources of theoretical uncertainties are studied.

- **Missing higher order corrections:** Contributions due to higher order QCD corrections cannot be calculated to arbitrarily high order, as it gets progressively more computationally expensive. Thus, this study is limited to next to leading order (NLO), and further corrections are accounted for by varying the factorization and renormalization scales. The next section 3.6 discusses the approach taken to evaluate uncertainties associated with missing higher order corrections.
- **Uncertainties associated with Parton Distribution Functions:** According to the Parton model [56], a proton is composed of three valence quarks, and several gluons and virtual quarks. These quarks and gluons are called ‘partons’. Proton-proton collisions, such as in the experiments conducted at the LHC, involve the interaction of these quarks and gluons at very high energies. These partons carry a fraction of the proton momentum. Parton Distribution Functions (PDFs) represent this fraction of proton momentum carried by partons as probability distributions. Owing to the non-deterministic nature of this fact, this study attempts to account for these uncertainties as PDF uncertainties. Chapter 2 has introduced proton-proton collisions and Parton Distribution Functions in fair depth.
- **Photon Fragmentation Uncertainties:** In the $Z\gamma \rightarrow \ell\ell\gamma$ process, the signal includes a photon. However, while reconstructing the event, soft photons, or photons resulting from other fragmentation processes may be encountered. To ensure that the photon is indeed prompt, it is required to be isolated from hadronic activity (such as pion decays). This isolation is implemented experimentally in different ways. The uncertainty associated with the implementation of this isolation is estimated as photon fragmentation uncertainties.

3.6 Renormalization

In Feynman diagrams beyond tree level, the introduction of self interaction loops, such as in Figure 3.5, lead to divergent integrals that are progressively more difficult to calculate at higher orders. A perfect calculation, carried out up to infinite orders, would give the exact cross section. However current technological capabilities limit the order to which calculations can be carried out.

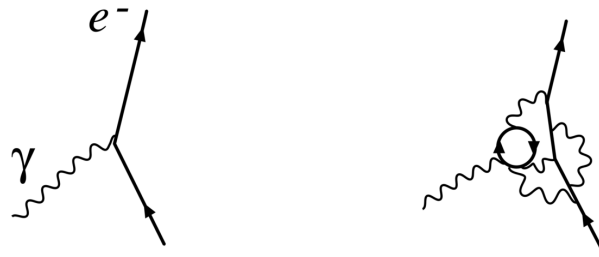


Figure 3.5: Loop corrections to the propagator and vertex illustrated using a Feynman diagram showing $\gamma \rightarrow e^+e^-$, for example. These loops represent interactions that happen at very small distance scales (and corresponding, very high energy scales), and are calculated perturbatively in QCD.

While calculating loop corrections, two kinds of divergences are encountered: infrared divergences, and ultraviolet divergences. Infrared divergences occur when the integral diverges due to the contributions of particles with very low energies (or equivalently, interactions at large distances), and

typically involve terms featuring $1/k$, thus diverging as $k \rightarrow 0$. Ultraviolet divergences are logarithmic divergences involving the term $\int d^4k \, 1/k^4$. Integrals of this form simplify as terms involving $\int \ln(k)dk$ that diverge as the integration variable approaches ∞ , occurring at very high energy scales, or equivalently, interactions at extremely short distances. They correspond to physics at long and short distances. Here, long distances are those where soft interactions take place, away from the hard parton-parton interaction. Short distances are those where the hard parton parton interactions occur.

Thus, it is necessary to regularize such integrals, i.e. render the divergences finite, or have them cancel out somehow. One method of addressing these divergences is to introduce a cutoff scale Λ as the (upper or lower) limit in the momentum integrals, such as through the Pauli-Villars regularization [57]. The divergences will then be proportional to $\log(\Lambda/\mu^2)$, where μ^2 is some arbitrary scale, an artifact of the regularization.

Dimensional regularization is another method of regularization, where the power of the momentum integration is shifted by an infinitesimally small amount 2ϵ , i.e. $\int d^4q/(2\pi)^4 q \dots \rightarrow \mu^{2\epsilon} \int d^{4-2\epsilon}q/(2\pi)^4 q \dots$. A prefactor $\mu^{2\epsilon}$ is introduced, where μ is an arbitrary scale, to ensure that all observables have the dimension of mass. Thus, regularization envelops the effect of these divergences into the arbitrary scale μ . Upon renormalizing these regularized integrals, the $1/\epsilon$ divergent terms cancel out, leaving only the scale μ to be addressed. In QCD calculations, this scale appears as part of a scale dependent parameter, namely the running strong coupling constant ($\alpha_s(\mu)$). However, this scale μ is arbitrary. It does not represent a physical quantity at all, and is a tool to get the divergent integrals to behave.

The infrared divergences are addressed by the inclusion of the factorization scale μ_F , while the ultraviolet divergences are addressed by the inclusion of the renormalization scale μ_R . These parameters are arbitrary, and are set by hand. These are then varied between $\frac{1}{2}\mu < \mu < 2\mu$ to obtain an indication of the dependence of the matrix element on the scales, and thus, the uncertainty around the chosen scale.

A perfect calculation would include an infinite number of terms in α_s , and would result in μ dependent terms cancelling out perfectly, resulting in an answer that is independent of the choice of μ . However, perturbative QCD calculations get progressively more computationally expensive as the order of the perturbative theory increases. Thus, perturbative QCD calculations are only carried out up to a fixed order. There is a difference in the cross sections obtained from one order to the next, and thus, a contribution from the uncalculated higher perturbative orders is expected. To account for the missing higher order corrections, K -factors are introduced to quantify the difference between higher orders and leading order where, at NLO, the K -factor is defined as the ratio between the cross section at NLO to the cross section at LO.

3.7 Photon Isolation

The $Z\gamma \rightarrow \ell\ell\gamma$ process may contain photons that arise from the hadron showers. It is therefore important to isolate the prompt photon from hadronic activity. This reduces unwanted background from pion decays, or fragmentation processes.

Experimentally, photon isolation is implemented with the following selection:

$$\sum_{\in R_0} E_T(\text{had}) < \epsilon_h p_T^\gamma \quad \text{or} \quad \sum_{\in R_0} E_T(\text{had}) < E_T^{\max} \quad (3.7)$$

715

limiting the transverse hadronic energy $E_T(\text{had})$ in a cone of size $R_0 = \sqrt{\Delta\eta^2 + \Delta\phi^2}$ around the photon, to some fraction of the photon p_T , or some fixed small cut-off.

717

The smooth cone isolation method of Frixione [58] is an alternative isolation procedure, which simplifies calculations by avoiding fragmentation contributions. The following isolation prescription is applied to the photon:

$$\sum_{R_{j\gamma} \in R_0} E_T(\text{had}) < \varepsilon_h p_T^\gamma \left(\frac{1 - \cos R_{j\gamma}}{1 - \cos R_0} \right)^n. \quad (3.8)$$

where $R_{j\gamma}$ is the separation of the photon and the j^{th} parton. This requirement constrains the sum of hadronic energy inside a cone of radius $R_{j\gamma}$, for all separations $R_{j\gamma}$ less than a chosen cone size R_0 . This prescription allows soft radiation inside the photon cone, but collinear singularities are removed. The smooth cone isolation is infrared finite, thus fragmentation contributions do not need to be included. The two prescriptions are significantly different. The Frixione method has its advantages, namely that it is infrared finite, removes collinear singularities and avoids fragmentation effects. However, Frixione isolation is difficult to implement experimentally, while the relative isolation, given by Equation 3.7 is used in current experimental analyses.

Chapter 4

Transfer factor R and the uncertainties associated to it

4.1 MCFM

Monte Carlo for Femtobarn processes (MCFM) is a program that calculates cross sections for femtobarn-level processes at leading order (LO) or next to leading order (NLO) QCD. In this study, MCFM v8.0 [59–62] is used to generate cross sections of $ZZ \rightarrow \ell\ell\nu\nu$ and $Z\gamma \rightarrow \ell\ell\gamma$ processes at NLO, with a selection of generator level cuts. The generation parameters in MCFM allow fine control over the sample, such as PDF sets, photon isolation, lepton and photon p_T and η , renormalization and factorization scales, etc. The samples are generated with cuts on $E_T^{miss} = p_T(Z \rightarrow \nu\nu)$ for the ZZ process and $p_T(\gamma)$ for the $Z + \gamma$ process. Table 4.1 lists the generator level settings used for the ZZ and $Z + \gamma$ processes. All lepton cuts are consistent with the ones used in the ATLAS $Z+E_T^{miss}$ analysis [53], as shown in Table 3.1.

Cuts	
M_{ee}	$76 < M_{ee} < 106 \text{ GeV}$
Order	NLO
PDF set	PDF4LHC15_nlo
$p_T^{\text{lead}}(e)$	$> 30 \text{ GeV}$
$ \eta^{\text{lead}}(e) $	< 2.47
$p_T^{\text{sublead}}(e)$	$> 20 \text{ GeV}$
$ \eta^{\text{sublead}}(e) $	< 2.47
$p_T(V)^1$	$> 90 \text{ GeV}$
Renormalization scale μ_R	$H_T = \sum_i p_{T,i}$
Factorization scale μ_F	$H_T = \sum_i p_{T,i}$

Table 4.1: Settings in input.DAT for MCFM. These parameters are common between the $ZZ \rightarrow \ell\ell\nu\nu$ (process 82) and $Z\gamma \rightarrow \ell\ell\gamma$ (process 300) processes. Here, V is a vector boson: $Z(\rightarrow \nu\nu)$ for the ZZ process and γ for the $Z\gamma$ process.

The constraint on M_{ee} in the case of $Z + \gamma$ suppresses backgrounds from non resonant $\ell\ell$ processes by ensuring that the lepton pair are from a Z boson decay only. Additionally, photon isolation is implemented using the Frixione [58] method, with $R_0 = 0.4$, $\varepsilon = 0.075$ and $n = 1$.

In MCFM generated events, leptonically decaying Z boson are constrained to an electron-positron pair only, i.e. $Z \rightarrow ee$. As electrons and muons have similar properties with the exception of mass, simply the branching fraction of $Z \rightarrow ee$ must be accounted for to obtain the inclusive value of R .

$$R_{inc} = R * \frac{BR(Z \rightarrow ee)}{BR(Z \rightarrow ee) * BR(Z \rightarrow \nu\nu) * 2} \quad (4.1)$$

4.2 Results

Using the settings listed in Table 4.1, the cross sections for $ZZ \rightarrow ee\nu\nu$ and $Z\gamma \rightarrow ee\gamma$ are generated at LO and NLO, shown in Figure 4.1. Throughout this analysis, these samples are used as the reference from which the transfer factor R is constructed, and provide the central value around which the uncertainties are calculated.

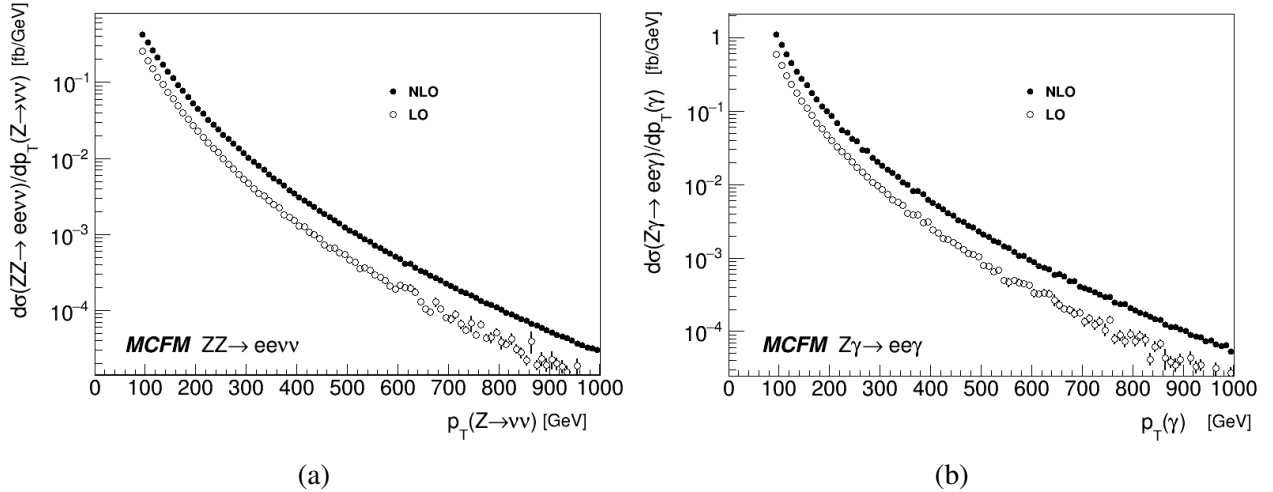


Figure 4.1: NLO and LO cross sections of $ZZ \rightarrow ee\nu\nu$ (left) and $Z\gamma \rightarrow ee\gamma$ (right) processes with the cuts as in Table 1. The leptonically decaying Z boson decays to an e^+e^- pair. The behaviour of the ratio of the NLO cross sections to the LO cross sections can be seen in Figure 4.9. There is no flavor constraint on the neutrinos.

There is a significant difference between the LO cross section and NLO cross section in both of these processes. The difference is greater at high p_T than at low p_T . However, the ratio of NLO to LO is similar between the two processes. Thus, the behavior of the transfer factor R at LO and NLO is expected to be similar at high p_T as well. This behavior is shown in Figure 4.9. The ratio $R = \sigma(ZZ \rightarrow ee\nu\nu)/\sigma(Z\gamma \rightarrow ee\gamma)$ at LO and NLO is shown in Figure 4.2a, taken as the ratio of the cross sections in Figures 4.1a and 4.1b.

The Z boson has a mass of 91 GeV, while the photon is massless. The coupling of the Z boson to quarks depends upon its mass. At low p_T , the mass dependence makes it significantly different than the coupling of the photon to quarks. At $p_T(Z \rightarrow \nu\nu) \gg M_Z$, the mass of the Z boson is negligible, and its kinematics are similar to those of the photon. The difference between the two process is largely dictated by the coupling strength of the respective bosons to the quarks.

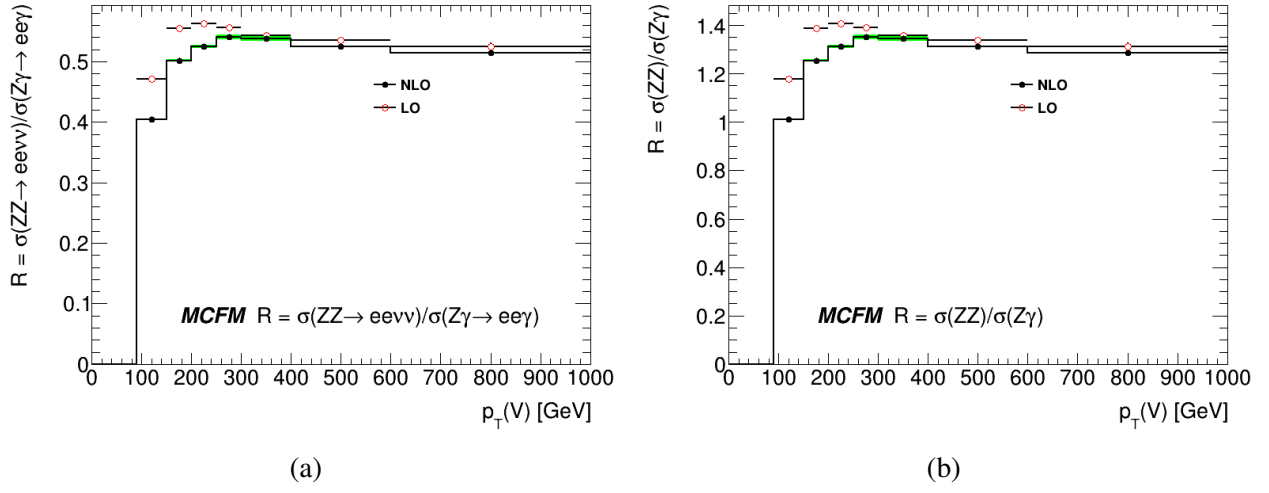


Figure 4.2: The transfer factor R as a function of p_T , taken as a ratio of the $ZZ \rightarrow ee\nu\nu$ and $Z\gamma \rightarrow ee\gamma$ cross sections at both LO and NLO. The figure on the left shows R calculated from cross sections as given by MCFM, where the leptonically decaying Z boson decays into an e^+e^- pair. The figure on the right adjusts for the branching fractions of $Z \rightarrow ee$ and $Z \rightarrow \nu\nu$, thus showing $R = \sigma(ZZ)/\sigma(Z\gamma)$, where the Z bosons do not decay.

Thus the R value is observed to increase from ≈ 0.43 at 100 GeV to ≈ 0.52 at high p_T , where it reaches a plateau. When the branching ratio of Z boson decaying selectively to e^+e^- , or to $\nu\nu$, is accounted for as shown in Equation 4.1, the resulting ratio $R(p_T)$ is shown in Figure 4.2b. Here, the ratio of $\sigma(ZZ)$ to $\sigma(Z\gamma)$ is shown, i.e. the Z bosons do not decay further. The value of R is observed to increase from ≈ 1.08 at 100 GeV to ≈ 1.3 at high p_T . This agrees with the simple approximate calculation presented in Section 3.4 of $R \approx 1.28$.

Figures 4.3 and 4.4 further illustrate the topology of the events by showing normalized distributions for the leading and subleading lepton p_T and rapidity.

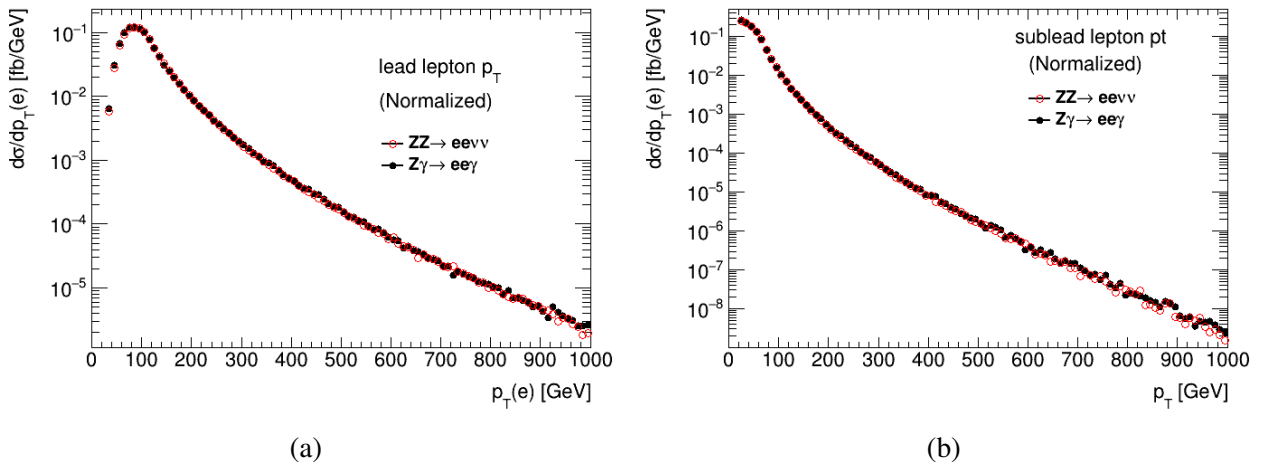


Figure 4.3: Normalized distributions showing the differential cross section as a function of the transverse momentum of the leading (left) and subleading (right) leptons for the two processes.

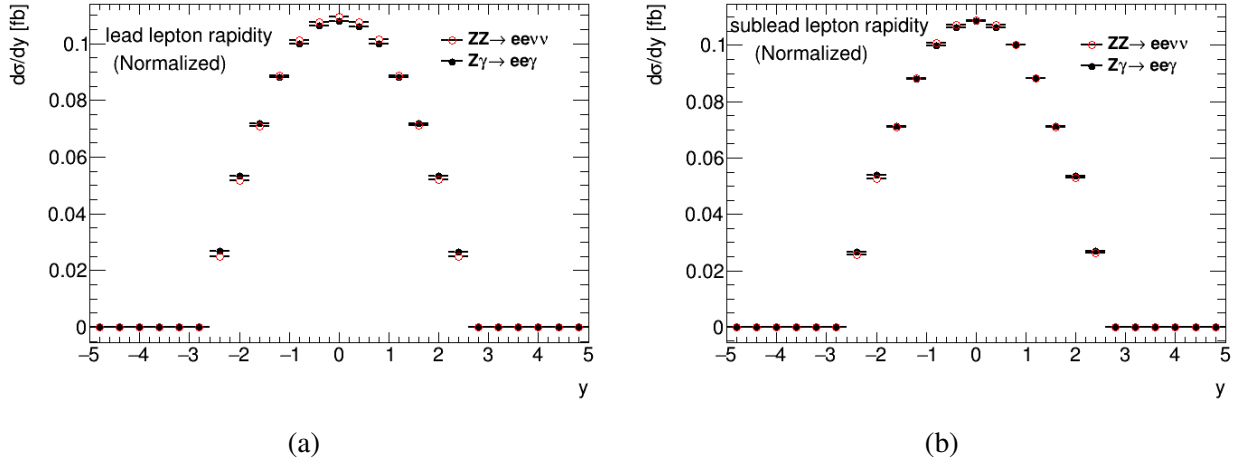


Figure 4.4: Normalized distributions showing the differential cross section as a function of the rapidity of the leading (left) and subleading (right) leptons for the two processes.

Figures 4.3 and 4.4 show that the leptons from a Z boson decay have very similar kinematic behavior between the two processes.

Gluon-gluon processes contribute to 8.6% of the total cross section for the ZZ process and 2.5% of the $Z + \gamma$ process. Figure 4.5 shows the $q\bar{q} + q\bar{q}$ and gg contributions to the ZZ and $Z\gamma$ cross section. Gluon-gluon processes contribute more at low p_T than at high p_T . This is due to asymptotic freedom; at higher energies, gluons do not interact as strongly as they do at low energies, and the cross section is dominated by the $q\bar{q}$ and qg induced processes.

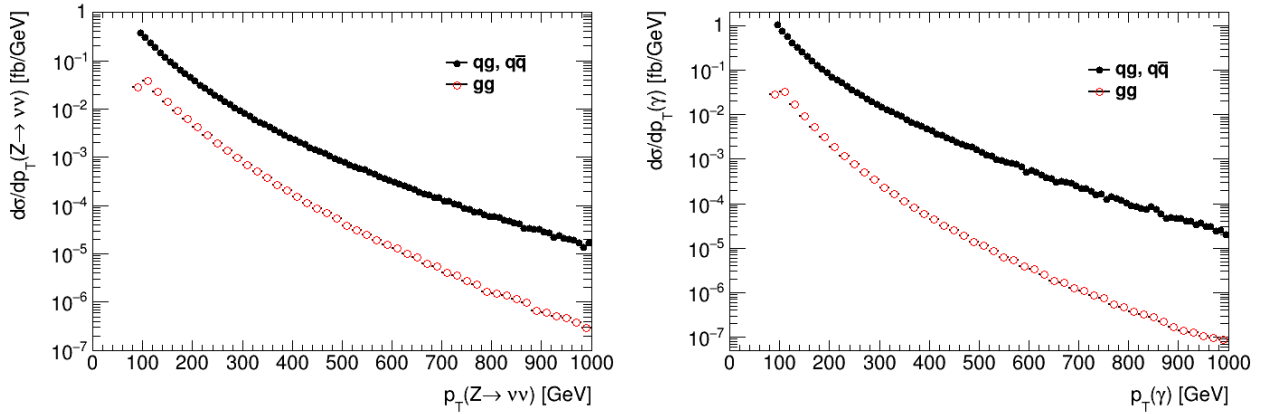


Figure 4.5: The cross sections of $ZZ \rightarrow ee\nu\nu$ (left) and $Z\gamma \rightarrow ee\gamma$ (right) as a function of p_T , from the contributing $q\bar{q}$, qg and gg processes. The leptonically decaying Z boson decays to an electron-positron pair

The R_{gg} distribution, shown in Figure 4.6 is observed to approach an asymptotic value at a much higher $p_T = 2$ TeV. The shape and value of the transfer factor for the gluon-gluon induced processes is due to the fact that the gg contribution is lower at high p_T .

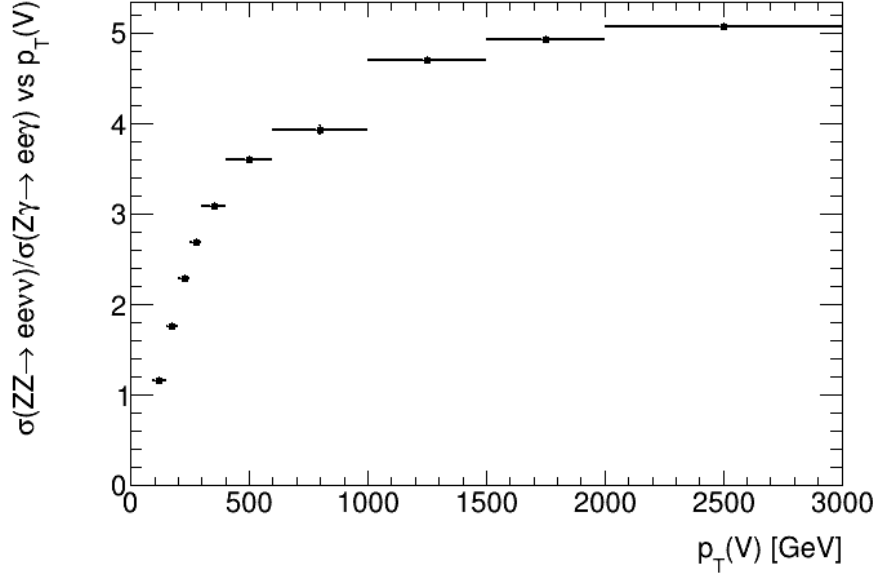


Figure 4.6: $R_{gg}(p_T)$, computed from the contributions of the gg subprocess to the cross sections of ZZ and $Z\gamma$. The curve reaches a plateau at a much higher p_T than for contributions from the $q\bar{q}$ process only. The leptonic Z bosons decay to an ee pair.

4.3 Theoretical Uncertainties

4.3.1 Uncertainty from Missing Higher Order Corrections

To address uncertainties associated with the scale in this study, a similar prescription as the one used in Ref [63] is followed. The central scale, μ_0 is chosen to be H_T for both $ZZ \rightarrow \ell\ell\nu\nu$ and $Z\gamma \rightarrow \ell\ell\gamma$ samples (where H_T is the scalar sum of the transverse momentum of all particles after collision, $\sum_i p_{T,i}$), and seven-point variations are applied, i.e.

$$\frac{\mu_i}{\mu_0} = (1, 1), (1, 2), (2, 1), (2, 2), (0.5, 1), (1, 0.5), (0.5, 0.5) \quad (4.2)$$

where $i = 0, \dots, 6$. The central cross section value is taken to be the mean of the maximum and minimum cross sections resulting from this variation, and the uncertainty to be the half the difference between the same.

$$\sigma_{NLO}^{(V)} = \frac{1}{2} \left[\sigma_{NLO}^{(V,max)} + \sigma_{NLO}^{(V,min)} \right] \quad (4.3)$$

$$\delta\sigma_{NLO}^{(V)} = \frac{1}{2} \left[\sigma_{NLO}^{(V,max)} - \sigma_{NLO}^{(V,min)} \right] \quad (4.4)$$

where

$$\sigma_{NLO}^{(V,max)} = \max \left\{ \sigma_{NLO}^{(V)}(p_T(V), \mu_i) | 0 \leq i \leq 6 \right\} \quad (4.5)$$

$$\sigma_{NLO}^{(V,min)} = \min \left\{ \sigma_{NLO}^{(V)}(p_T(V), \mu_i) | 0 \leq i \leq 6 \right\} \quad (4.6)$$

and $V = Z \rightarrow \nu\nu$ for $ZZ \rightarrow \ell\ell\nu\nu$, or $V = \gamma$ for $Z\gamma \rightarrow \ell\ell\gamma$. The value of R is calculated from the events generated with the above 7-point prescription in a correlated manner.

The variation of scales for cross sections of $ZZ \rightarrow ee\nu\nu$ and $Z\gamma \rightarrow ee\gamma$ are shown in Figure 4.7.

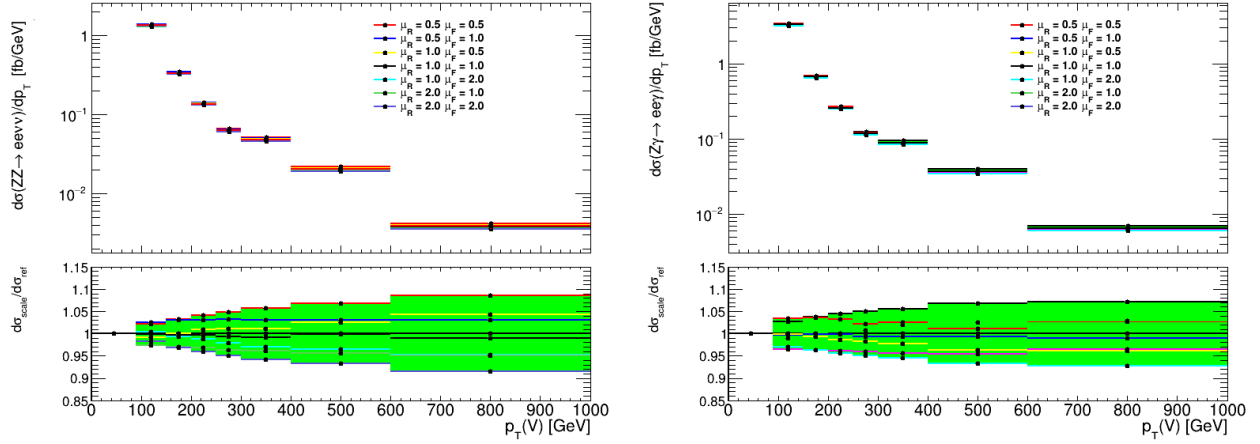


Figure 4.7: The scale variations around the cross sections of $ZZ \rightarrow ee\nu\nu$ (left) and $Z\gamma \rightarrow ee\gamma$ (right).

The uncertainty for $ZZ \rightarrow \ell\ell\nu\nu$ process is 2.5% at 100 GeV, which increases to 8.4% at high p_T . For the $Z\gamma \rightarrow \ell\ell\gamma$ process, the uncertainty increases from 3.5% at 100 GeV to 7.2% at high p_T . Here, the prescription in Equations 4.3 and 4.4 is used to compute the central value and uncertainty.

Treating the scales as correlated between the processes, the scale variation for the transfer factor R is shown in Figure 4.8. The central value of R and the uncertainty band around it is taken according to Equations 4.3 and 4.4 applied to R .

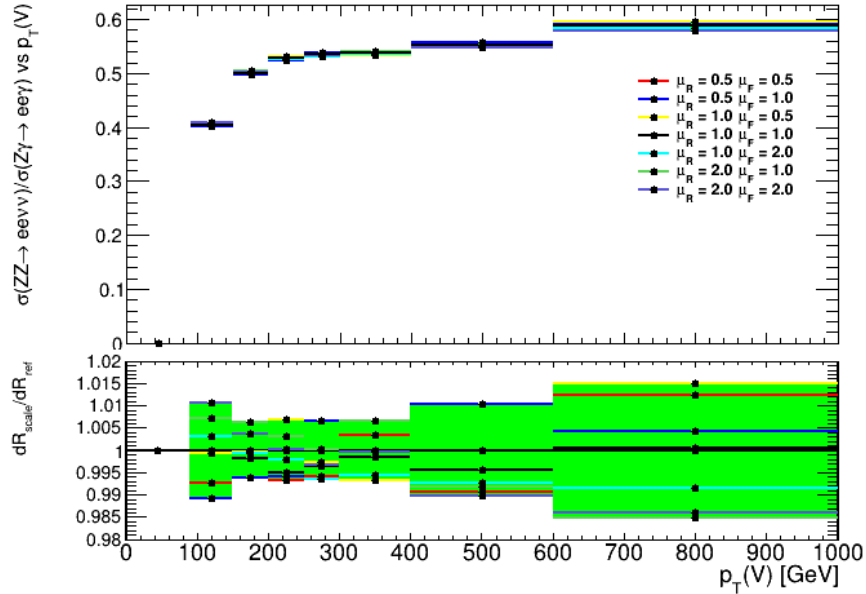


Figure 4.8: The transfer factor $R = \sigma(ZZ \rightarrow ee\nu\nu)/\sigma(Z\gamma \rightarrow ee\gamma)$ (top), with the scales varied in a correlated manner for both ZZ and $Z\gamma$ processes. The bottom plot shows the relative ratio R_i/R_0 of the varied transfer factors to the central value.

The correlated scale uncertainty around R is lower compared to that of the individual cross sections. At 100 GeV, $R \approx 0.4 \pm 0.043$, or an uncertainty of 1%. At $p_T = 500$ GeV, $R \approx 0.55 \pm 0.01$, the uncertainty is 1%, significantly lower than the large uncertainties ($\approx 8\%$) obtained for the individual cross sections at high p_T .

There is no good motivation for treating the scale uncertainties of two separate processes as correlated. To account for the effects of process dependent correlations, the fact that the two processes are kinematically similar at high p_T is taken into consideration. Naively, a cancellation of the contribution due to missing higher order corrections would be expected between the two processes due to this correlation. To estimate the degree of correlation between the processes, the process dependent part of the cross sections is used. Since the study is undertaken at NLO, the K -factor is defined as in Equation 4.7.

$$K_{NLO}^{(V)} = \sigma_{NLO}^{(V)}(p_T) / \sigma_{LO}^{(V)}(p_T) \quad (4.7)$$

Assuming that the corrections to the fixed order cross section form a convergent series, and that the NLO K -factor is larger than the K -factor at higher orders,

$$\frac{\sigma_{NLO}^{(V)}}{\sigma_{LO}^{(V)}} > \frac{\sigma_{N^{\infty}LO}^{(V)}}{\sigma_{NLO}^{(V)}} \quad (4.8)$$

it is possible to use the NLO K -factor to quantify the scale uncertainties that are correlated between the two processes. Figure 4.1 illustrates that the behavior of the higher order corrections is similar between the two processes at high p_T . Thus to estimate the unknown process dependent correlation effects, the difference between the K -factors of the $ZZ \rightarrow \ell\ell\nu\nu$ and $Z\gamma \rightarrow \ell\ell\gamma$ processes is taken as the K -factor uncertainty δK_{NLO} .

$$\delta K_{NLO} = K_{NLO}^{(\gamma)}(p_T) - K_{NLO}^{(Z)}(p_T) \quad (4.9)$$

It is assumed that process dependence of the K -factor at higher orders is larger than the

$$\left(\frac{\sigma_{NLO}^{(\gamma)}}{\sigma_{LO}^{(\gamma)}} - \frac{\sigma_{NLO}^{(Z)}}{\sigma_{LO}^{(Z)}} \right) < \left(\frac{\sigma_{N^{\infty}LO}^{(\gamma)}}{\sigma_{NLO}^{(\gamma)}} - \frac{\sigma_{N^{\infty}LO}^{(Z)}}{\sigma_{NLO}^{(Z)}} \right) \quad (4.10)$$

Figure 4.9 shows the K -factor distributions for both processes, as well as the K -factor uncertainty δK_{NLO} .

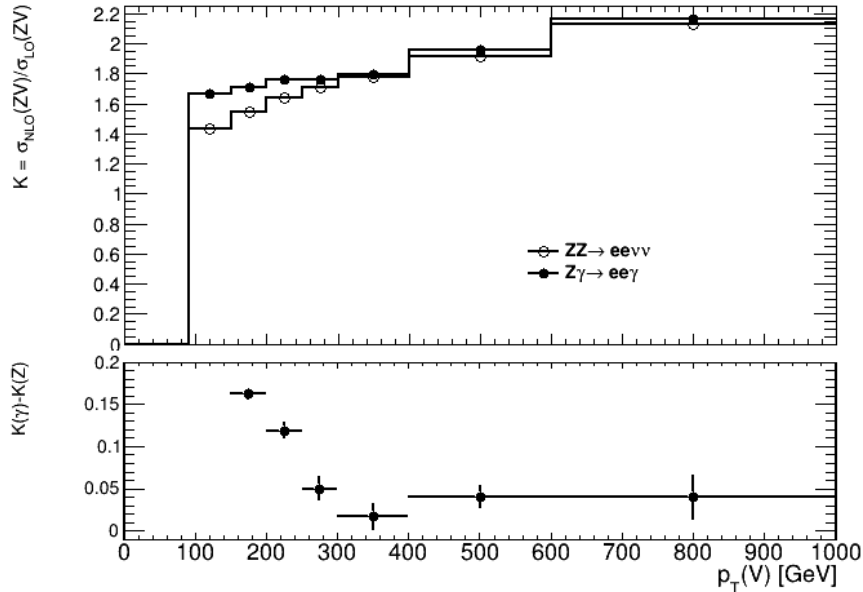


Figure 4.9: The K factor to estimate the unknown process dependent correlations, defined as $\sigma_{NLO}(V)/\sigma_{LO}(V)$. The bottom plot shows the K -factor difference relative to $K(Z)$.

The K -factor grows larger as a function of $p_T(V)$ for both processes. However, the difference between the two K -factors shrinks, due to the two processes being similar at high p_T . Thus, the K -factor uncertainty δK_{NLO} , is 4% at $p_T(V) = 500$ GeV.

4.3.2 Uncertainty associated with Parton Distribution Functions

The PDF set used for reference is the PDF4LHC15 [64] PDF set. The uncertainty on the PDFs is studied by using the 30 variations provided by the PDF4LHC15 set [64], constructed from the combination of CT14, MMHT14 and NNPDF3.0 PDF sets. These sets are provided by LHAPDF6 [65]. PDF4LHC15 provides a set of variations that include those determined by different groups (MSTW, CTEQ and NNPDF). The set used here is PDF4LHC15_nlo_30, consisting of 30 members.

Fig.4.10 shows the comparison of the ratio $R(p_T)$ from the 30 member sets of PDF4LHC15_nlo_30. To measure the uncertainty due to these 30 variations, analogous to Equation 20 in Ref [64], Equation 4.11 is used:

$$\delta^{PDF} R = \sqrt{\sum_{k=1}^{N_{mem}} (R^{(k)} - R^{(0)})^2} \quad (4.11)$$

where N_{mem} is the number of member sets in the group, in this case, 30.

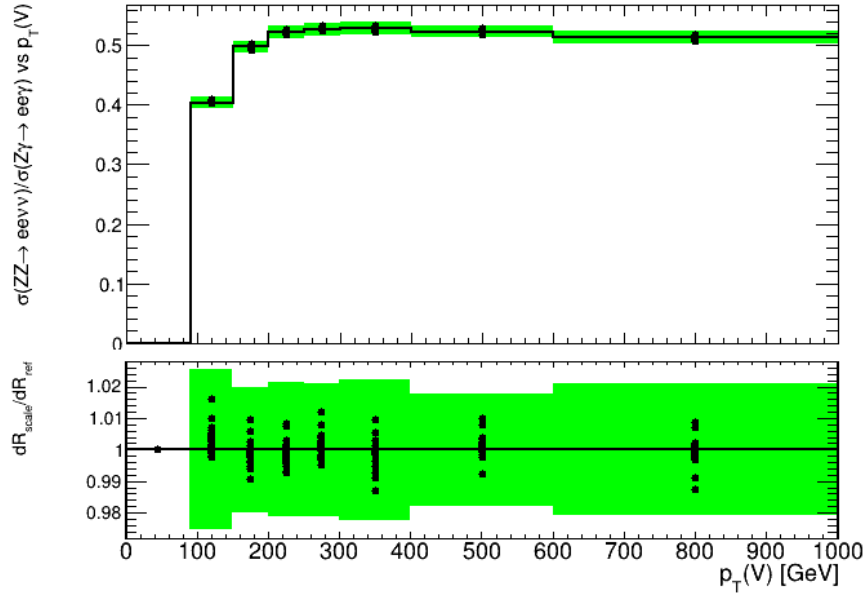


Figure 4.10: The transfer factor $R = \sigma(ZZ \rightarrow \ell\ell\nu\nu) / \sigma(Z\gamma \rightarrow \ell\ell\gamma)$ (top), and the relative ratio R_i/R_0 of the transfer factor calculated using PDF sets 1-30, with respect to set 0 which is taken as the central value.

The combined uncertainty around $R \approx 0.40$ is ± 0.01 , or about 2.3%, at 100 GeV. The uncertainty is about 1.8% at high p_T values, with $R \approx 0.51 \pm 0.01$ at $p_T(V) = 500$ GeV.

4.3.3 Photon Fragmentation Uncertainty

To identify prompt photons, and separate them from photons that arise from showers or hadronic decay, it is necessary to isolate the photons from hadronic activity. Experimentally, photon isolation is implemented by limiting the hadronic energy in a cone around the photon to some fraction of the photon momentum. An alternative method is the smooth cone isolation, or the Frixione method which avoids fragmentation contributions and removes collinear singularities. Section 3.7 details these methods.

In this analysis, R_0 is chosen to be 0.4 to agree with the experimental definition. The central value is chosen to be from the sample using smooth cone isolation (Frixione) with $\epsilon_h = 0.075$ and $n = 1$. These parameters are varied within a reasonable range to assess the uncertainty as shown in Figure 4.11. The parameters ϵ and n are varied to get a handle on the uncertainty associated with the Frixione isolation method. The experimental isolation method is also considered, and the difference between the two methods is accounted for as part of the uncertainty.

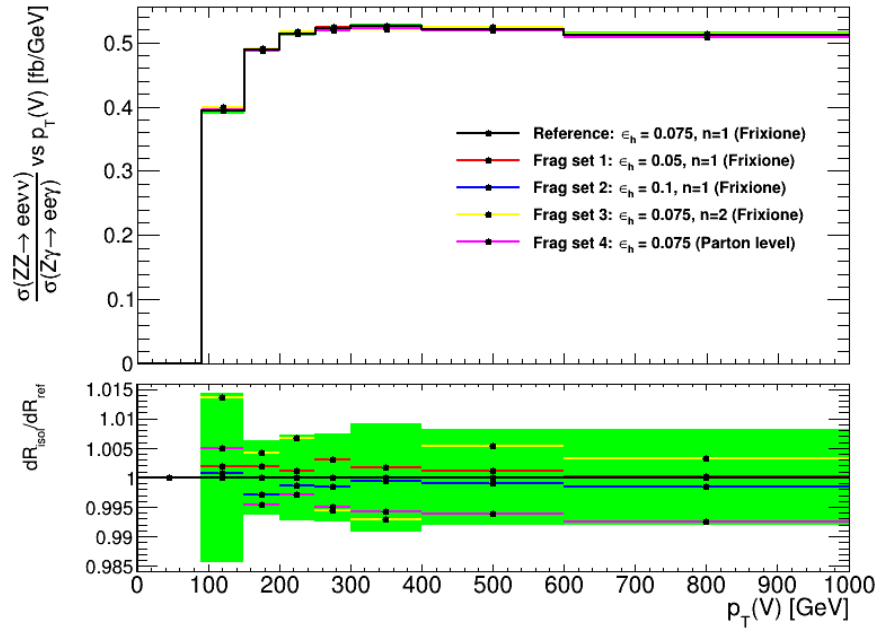


Figure 4.11: R distribution as a function of p_T , showing the uncertainty due to variation of photon isolation parameters ϵ_h and n in the smooth cone isolation procedure (Frixione), and ϵ_h in the photon isolation procedure. The lower panel shows the relative deviation of the varied sets from the central value, as well as the uncertainty band.

The uncertainty is calculated from the four sets listed in Figure 4.11:

$$\begin{aligned} \delta R_i &= |R_i - R_{ref}| \quad i \in (1, 2, 3, 4) \\ \delta R &= \sqrt{\max_{i=1,2,3} (\delta R_i)^2 + (\delta R_4)^2} \end{aligned} \quad (4.12)$$

as the effects assessed by changing the isolation definition in set 4, and varying the parameters in sets 1-3 are different.

The uncertainty is $< 1.5\%$ over the whole p_T range, and is 0.8% at $p_T(V) = 500$ GeV.

4.4 Combined Uncertainties

Combining the theoretical uncertainties due to missing higher order corrections, parton distribution functions, and photon fragmentation effects, Figure 4.12 shows the transfer factor R and its uncertainty.

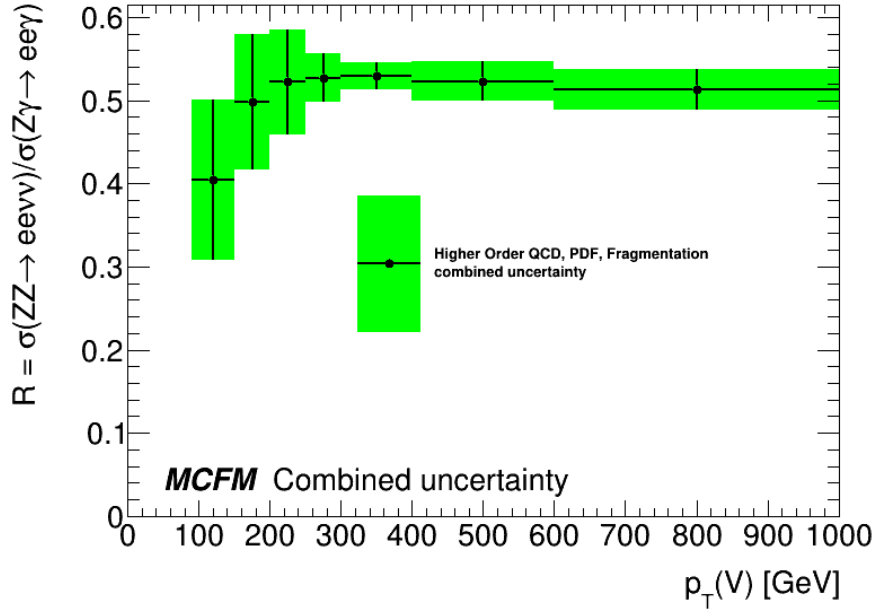


Figure 4.12: The transfer factor R with the combined theoretical uncertainties from missing higher order QCD corrections, parton distribution functions, and photon fragmentation effects.

The combined uncertainties are large at low p_T , with $R = 0.4 \pm 0.096$ (23.8%) at 100 GeV. However, the similarities in the $ZZ \rightarrow \ell\ell\nu\nu$ and $Z\gamma \rightarrow \ell\ell\gamma$ processes are apparent at high p_T , with $R = 0.52 \pm 0.024$ (4.6%) at 500 GeV.

Chapter 5

Conclusion

This thesis presents a method to estimate the Standard Model background to the $\ell\ell + E_T^{\text{miss}}$ final state in a Higgs to Dark Matter search.

The Dark Matter model proposes the Higgs boson as a mediator between Dark Matter and Standard Model particles. The Higgs boson is produced in association with a leptonically decaying Z boson, whereupon the Higgs boson decays into the invisible Dark Matter particles, resulting in a $\ell\ell + E_T^{\text{miss}}$ final state. This thesis estimates contribution of the $ZZ \rightarrow \ell\ell\nu\nu$ process to the Standard Model background in $\ell\ell + E_T^{\text{miss}}$ final state.

Estimated using Monte Carlo methods in Ref [53], an uncertainty of 10% was provided. This thesis reports a data driven method using the $Z\gamma \rightarrow \ell\ell\gamma$ process to estimate the $ZZ \rightarrow \ell\ell\nu\nu$ contribution, as the two processes behave similarly at $p_T(V) \gg M_Z$; $V = Z \rightarrow \nu\nu$ or γ , i.e. the mass of the Z boson is negligible compared to its transverse momentum.

A transfer factor R is introduced as the ratio of the $ZZ \rightarrow \ell\ell\nu\nu$ cross section to the $Z\gamma \rightarrow \ell\ell\gamma$ cross section, and the theoretical uncertainties upon R are estimated. The uncertainties due to missing higher order corrections are 23.6% at $p_T(V) = 100$ GeV and 4.1% at $p_T(V) = 500$ GeV. Uncertainties due to parton distribution functions are 2.3% at 100 GeV, and 1.8% at 500 GeV. The uncertainties due to photon fragmentation effects are $< 1.5\%$ in the full p_T range considered, and 0.8% at 500 GeV.

The combined uncertainties are large at low p_T , 23.8%, at 100 GeV, but are small at high p_T , 4.6% at 500 GeV. Thus, the transfer factor R can be used on $Z\gamma \rightarrow \ell\ell\gamma$ data to estimate the contribution of $ZZ \rightarrow \ell\ell\nu\nu$.

5.1 Outlook

This study was conducted at NLO using MCFM, a matrix element generator. Further studies are being conducted to reproduce these results and obtain similar results at NNLO using MATRIX [66]. It is also necessary to account for detector effects and estimate experimental uncertainties, which will be conducted with Monte Carlo techniques with the ATLAS framework. These studies are in progress, and are not within the scope of this thesis.

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