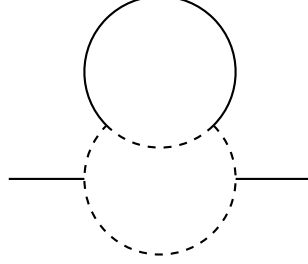


metric convention: $(+, -, -, -)$

Lagrangian:

$$\mathcal{L} = \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \frac{1}{2} M^2 \phi^2 + \partial_\mu \chi^\dagger \partial^\mu \chi - m^2 \chi^\dagger \chi - g_3 \phi \chi^\dagger \chi - g_4 \phi^2 \chi^\dagger \chi.$$

1 Diagram 1



$$\Pi_1(p^2) = g_3^4 \int \frac{d^d q}{(2\pi)^d} \frac{d^d r}{(2\pi)^d} \left(\frac{1}{q^2 - m^2} \right)^2 \frac{1}{r^2 - m^2} \frac{1}{(p - q)^2 - m^2} \frac{1}{(q - r)^2 - M^2}.$$

First loop evaluation (r):

$$\begin{aligned} \Pi_1(p^2) &= g_3^4 \int \frac{d^d q}{(2\pi)^d} \left(\frac{1}{q^2 - m^2} \right)^2 \frac{1}{(p - q)^2 - m^2} \int \frac{d^d r}{(2\pi)^d} \frac{1}{r^2 - m^2} \frac{1}{(q - r)^2 - M^2} \\ &=: g_3^4 \int \frac{d^d q}{(2\pi)^d} \left(\frac{1}{q^2 - m^2} \right)^2 \frac{1}{(p - q)^2 - m^2} P_1. \end{aligned}$$

$$\begin{aligned} P_1 &= \int dx \int \frac{d^d r}{(2\pi)^d} \left((1 - x)(r^2 - m^2) + x[(q - r)^2 - M^2] \right)^{-2} \\ &= \int dx \int \frac{d^d r}{(2\pi)^d} \left((r - xq)^2 - x^2 q^2 - (1 - x)m^2 + xq^2 - xM^2 \right)^{-2} \\ &= \int_0^1 dx \int \frac{d^d k}{(2\pi)^d} \left(k^2 - \Delta_1 \right)^{-2} \\ &= \frac{i}{(4\pi)^{2-\epsilon}} \Gamma(\epsilon) \int_0^1 dx \frac{1}{\Delta_1^\epsilon}, \end{aligned}$$

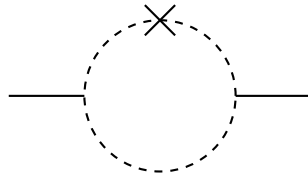
where $l = r - xq$ and $\Delta_1 = -x(1 - x)q^2 + (1 - x)m^2 + xM^2$.

The integrand can be rewritten as following:

$$\begin{aligned} &\left(\frac{1}{q^2 - m^2} \right)^2 \frac{1}{r^2 - m^2} \frac{1}{(p - q)^2 - m^2} \frac{1}{(q - r)^2 - M^2} \\ &= 24 \int dF_4 x \left(x(q^2 - m^2) + y(r^2 - m^2) + z[(p - q)^2 - m^2] + w[(q - r)^2 - M^2] \right)^{-5} \end{aligned}$$

where $\int dF_4 = \int_0^1 dx dy dz dw \delta(x + y + z + w - 1)$.

2 Diagram 2



3 Diagram 3

