FOORT Documentation

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Welcome to the documentation for FOORT, which will make using FOORT but a small efFOORT!

1 Installation

1.1 Libconfig library

1.1.1 Ubuntu systems

- sudo apt-get update -y to make sure apt-get is up to date.
- sudo apt-get install -y libconfig++-dev to install the package. (If this doesn't work, try the same command with libconfig-dev instead.)
- export LD_LIBRARY_PATH=/usr/local/lib If necessary, change /usr/local/lib to your actually library folder.

1.1.2 Arch systems

Thanks to Suvendu!!

• sudo pacman -Syu libconfig to install the package.

1.2 Compiling

To compile under Windows with VS, open the FOORT.sln file with VS. (VS 2022 was used to create FOORT.)

To compile under Linux, in the FOORT subfolder (where all code files are), there is a makefile, so running the command make should compile FOORT if g++ and libconfig are correctly installed. (The command make clean should remove FOORT and/or all intermediate object .o files that are created while compiling.)

Note: Under some Linux systems, it is possible that the LDFLAGS setting needs to be changed to:

LDFLAGS = -lm -lstdc++fs -L\$(LD_LIBRARY_PATH) -lconfig++ before it will compile correctly.

Once compiled, FOORT will hopefully run correctly as long as LD_LIBRARY_PATH has been set correctly (see above under installation of libconfig).

Note: the -lstdc++fs is necessary for access to the "experimental" std::filesystem in older versions of g++; in principle, the newer versions should not need the extra flag (so it can be changed to -lstdc++ instead). Note also that older versions of gcc (like 8.1 or 8.2, which is included in the current standard installation of Mingw64) will not compile at all due to issues with std::filesystem; the gcc compiler needs to be brought to a more current version first (see these steps to fix this issue).

There is also a file makefile_precompiledmode. This can be used to compile FOORT without installing libconfig, but only if configuration mode has been turned off in the FOORT source file. To do this, comment out (or remove entirely) the line

#define CONFIGURATION_MODE

at the beginning of Config.h. FOORT will then not need libconfig to compile, and will run use the precompiled settings that are set in Main.cpp in the function LoadPrecompiledOptions().

2 Configuration Options

FOORT is set up that all possible parameters that can be changed, can be changed from the configuration file only — meaning recompiling is unnecessary unless you are adding new objects (e.g. a new Metric) to the code.

Always be mindful of options that take numbers: if they take real, then the number passed must be a floating-point number — e.g. 1000.0 instead of 1000. (Of course, the reverse is true if the option must take a int.) If the incorrect format of number is passed, then this option will not be recognized (and the default value(s) will be used).

(DRM: need to figure out how longs etc are passed in libconfig)

2.1 Metric

This heading is where the metric is selected and all its options set. The first option to set is the type of metric:

- Name = "MetricName"; where MetricName is one of the following:
 - Kerr: Kerr in normal Boyer-Lindquist coordinates, with the units chosen such that M=1.
 - FlatSpace: flat space in spherical coordinates.

By default (if this setting is not specified in the configuration), the Kerr metric will be selected.

Depending on which metric has been selected, there can be additional options to be specified:

• Kerr:

- a = real;
 where real is a number between -1 and 1; FOORT will give a warning if this is not satisfied. (Default: 0.5.)
- RLogScale = bool; where bool is true or false. If true, then the Kerr metric will be evaluated in the logarithmic radial coordinate $u = \log r$; this leads to better integration around the horizon. (Default: false.)

• FlatSpace: No further options to specify.

• Rasheed-Larsen:

- m = real; a = real; p = real; q = real; These specify the parameters for the Rasheed-Larsen black hole metric. Note that the parameters must satisfy $p, q \ge 2m$, $a^2 < m^2$ and m > 0; FOORT will give a warning if this is not satisfied. The parameters (which all have dimensions of length) will always be rescaled so that the mass of the black hole is M = 1 (i.e. they are measured in units of the black hole mass); note that M = (p + q)/4. The horizon is at $r_+ = m + \sqrt{m^2 - a^2}$. (Defaults: m = 1, a = 0.5, p = q = 2.)
- RLogScale = bool;
 Same logarithmic radius as for the Kerr metric, see above.

• Johanssen:

- a = real; This sets the rotation parameter; just like for Kerr, |a| < 1 since M = 1.
- alpha13 = real; alpha22 = real; alpha52 = real; epsilon3 = real; This sets the four leading order parameters that control deviations from Kerr. (When all of these are zero, the metric is exactly Kerr.) The allowed region of these variables is a complicated non-linear relation; for each parameter, FOORT only checks the relation that must hold when the other parameters vanish.
- RLogScale = bool;
 Same logarithmic radius as for the Kerr metric, see above.

• Manko-Novikov:

- a = real; This sets the rotation parameter; just like for Kerr, |a| < 1 since M = 1.
- alpha3 = real; This sets the octupolar deviation $M_3/M^4 \sim \alpha_3$ from Kerr (so $\alpha_3 = 0$ corresponds to Kerr).
- RLogScale = bool;
 Same logarithmic radius as for the Kerr metric, see above.

2.2 Source

This heading is where you determine a source for the geodesic equation (i.e. a force on the right-hand side for the geodesic equation, making the geodesic fail to be an actual geodesic). Currently, only NoSource is implemented (i.e. no rhs to the geodesic equation):

• Source = "SourceName"; where currently SourceName can only be NoSource (and there are no further options to specify).

2.3 Diagnostics

Inside the heading Diagnostics, each Diagnostic has its own subheading. Under their own subheading, the most important options to specify is:

• On = bool;

where bool is true is you want the Diagnostic to be turned on and false otherwise. Only if the Diagnostic is turned on will the other options in the Diagnostic's subheading be considered.

• UseForMesh = bool;

where bool is true if this is the Diagnostic that should be used in the Mesh to determine "values" to assign to geodesics and "distances" between neighboring geodesics, which the Mesh will use to determine where to refine. Note: only one Diagnostic can have this setting set to true!

By default, if no diagnostic sets UseForMesh to true, FourColorScreen will be used if it is turned on. If FourColorScreen is not turned on, then all Diagnostic settings revert to the default of only turning on FourColorScreen. If more than one Diagnostic has UseForMesh set to true, the first one to set it will be used (in the order of Diagnostics given below).

The different possible Diagnostic subheadings and further options therein are:

- FourColorScreen: This is the four-color screen, assigning an integer 1-4 to the geodesic according to which quadrant of the boundary sphere it has escaped to. Geodesics that do not terminate due to exiting the boundary sphere (due to e.g. timing out or falling into a horizon) will be assigned 0. There are no other settings that FourColorScreen takes.
- GeodesicPosition: This keeps track of the position of the geodesic along its integration and outputs all those positions; this can be used for e.g. plotting individual geodesic trajectories. The options to specify are:

- UpdateFrequency = int;

with int a number larger or equal to zero. The Diagnostic will only store a position every number of steps as indicated here. If this is 0, the Diagnostic does not update the position during integration, but may update at start and finish according to the following two options. (Default is 1.)

- UpdateStart = bool;

(Only relevant if UpdateFrequency = 0.) Decides whether the Diagnostic stores the position of the geodesic at the very start of integration.

- UpdateFinish = bool;

(Only relevant if UpdateFrequency = 0.) Decides whether the Diagnostic stores the position of the geodesic at the very end of integration.

- OutputSteps = int;

Here, int is the (approximate!) number of positions per geodesic that will be outputted to file. If the Diagnostic has stored more than this many positions during the integration of the geodesic, the Diagnostic will select only (approximately) this many steps to output to file, evenly selected among the stored positions. If this is set to 0, it outputs all steps. (Default is 0.)

• EquatorialPasses: This keeps track of the number of passes through the equator $\theta=\pi/2$ that the geodesic makes. It returns a positive number for geodesics that have escapes out the boundary sphere, and a negative number for geodesics that eventually fall in the horizon. This Diagnostic also takes the options UpdateFrequency, UpdateStart, UpdateFinish just as GeodesicPosition does above. In addition, it takes the option:

- Threshold = real;

- Only consider a geodesic "above" or "below" the equatorial plane if its θ coordinate is Threshold× $\pi/2$ above or below $\pi/2$. This threshold is mainly useful for (near-)equatorial camera positions, since in that case without a threshold there is often a discontinuity in equatorial passes between the top and bottom half of the screen. (Default is 0.01.)
- ClosestRadius: This keeps track of the smallest radius r that the geodesic reaches. The true r value is always reported, even if a logarithmic r scale is used in integration. Note that if a geodesic enters a horizon, it will reported to reach r=0. This Diagnostic only takes the options UpdateFrequency (Default: 1), UpdateStart, UpdateFinish (see GeodesicPosition above).
- EquatorialEmission: This keeps track of the brightness intensity of the geodesic assuming a particular model for emission from an equatorial disc. It will output both the brightness intensity and the number of equatorial passes (just as EquatorialPasses does). Note that EquatorialEmission, if turned on, automatically turns off EquatorialPasses if it is turned on, and additionally assumes the role of value mesh diagnostic if EquatorialPasses had this role. The total brightness intensity I_{tot} for the geodesic is calculated as:

$$I_{\text{tot}} = \sum_{n=1}^{N_{max}} \zeta_n I_0(p^{(n)}) g(p^{(n)})^f, \tag{1}$$

where the sum is over the n passes through the equatorial plane that the geodesic makes, $\zeta_1 = 1, \zeta_{n>1} = \zeta$ is the "geometric fudge factor" (used to mimic the effects of a geometrically thick disc), N_{max} is either the total number of passes that the geodesic makes or a pre-specified maximum allowed passes (this can be set to a finite number to avoid partially unresolved higher order rings), $I_0(p^{(n)})$ is the local emitted intensity, $g(p^{(n)})$ is the redshift factor (determined by the dot product of the velocity of the emitting fluid and the velocity of the geodesic at that point), and f is the power of the redshift factor (3 or 4). To specify all of these degrees of freedom, EquatorialEmission takes the same options as EquatorialPasses listed above, and additionally:

- GeometricFudgeFactor = real; This specifies the geometric fudge factor (ζ). (Default is 1.0.)
- EquatUpperBound = int; The maximum number of equatorial passes allowed to contribute to the intensity (N_{max}) . Setting this to 0 means unlimited passes allowed. (Default is 0.)
- RedshiftPower = int; The power of the redshift used in calculating the observed intensity (f); should be 3 or 4. (Default is 3.)
- EmissionModel = "EmissionModelName"; Model for local emitted intensity $I_0(p)$. Depending on which model used, could have additional options to set as well. Current options for EmissionModelName:
 - * GLMJohnsonSU: Johnson's SU model with three parameters as used by GLM:

$$I_0(t, r, \theta, \phi) = \left((r - \mu)^2 + \sigma^2 \right)^{-1/2} \exp\left(-\frac{1}{2} \left[\gamma + \operatorname{arcsinh}\left(\frac{r - \mu}{\sigma}\right) \right]^2 \right). \tag{2}$$

This profile only depends on the radius. Additional options to specify are:

```
· mu = real;
· gamma = real;
· sigma = real;
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These specify the three parameters used in the model. (Default for μ is the horizon radius (if a black hole metric) or 1.0 otherwise; other defaults are $\gamma = 0.0$ and $\sigma = 1.0$.)

- FluidVelocityModel = "FluidVelocityModelName";

Model used to determine the local fluid four-velocity (which is used to determine the redshift factor). Depending on which model used, could have additional options to set as well. Current options for FluidVelocityModelName:

- * GeneralCircularRadial: A "mix" of (sub)Keplerian circular orbits and infalling (geodetic) orbits. Additional options to specify are:
 - xi = real;
 betar = real;
 betaphi = real;

All three parameters must lie between 0.0 and 1.0. (FOORT will check and rescale the inputted values if necessary.) ξ is the sub-Keplerian parameter; for $\xi=1.0$ the pure (geodesic) Keplerian circular orbits are used. β_r and β_ϕ determine the "mix" between the circular orbits and the radial infall orbits; for $\beta_r=\beta_\phi=1.0$ purely the circular orbits are used, and for $\beta_r=\beta_\phi=0.0$ the pure radial infall is used. (Defaults are $\xi=\beta_r=\beta_\phi=1.0$.)

2.4 Terminations

Terminations are set very similar to Diagnostics as discussed above. Each Termination has its own subheading, with most important option to specify:

• On = bool; which determines if the Termination is used or not.

By default (e.g. if no Terminations are turned on, or there is no Terminations subheading), TimeOut and BoundarySphere will be turned on with the default options set as indicated below.

The different possible Termination subheadings and further options therein are:

- Horizon: If the metric has a horizon at a constant r radius, then we want to stop integration before we get to the horizon, since usually the horizon is a coordinate singularity where geodesics spend an infinite amount of coordinate time approaching. (FOORT will check whether the Metric is a descendant class of SphericalHorizonMetric; if not, this Termination will be turned off.) Options to set are:
 - Epsilon_Horizon = real; Here, real is the percentage of the horizon radius at which to terminate the geodesic above the horizon radius. For example, if $r = r_h$ is the horizon and real = ϵ , then integration will be terminated at $r = r_h(1 + \epsilon)$. By default, this is set to 0.01.
 - UpdateFrequency = int;
 Check this condition every int steps of the geodesic integration. By default,
 this is set to 1.

- BoundarySphere: A (fictitious) boundary sphere at a constant radius far away from the object; if the geodesic escapes *outside* this sphere, we stop integration. Options to set:
 - SphereRadius = real;
 This radius real is the large radius at which to terminate integration. By default, set to 1000.
 - UpdateFrequency = int;
 This is analogous to the same setting under Horizon above. (Default is 1.)
- TimeOut: Terminate the geodesic integration if it has taken too many integration steps. This sometimes happens if a geodesic travels too close to a coordinate singularity. Options to set are:
 - MaxSteps = int;
 The maximum number of integration steps allowed before the geodesic terminates. Default is 10000.
 - UpdateFrequency = int;
 Analogous to the same setting under Horizon above. Default is 1.
 Warning: if this is not set to 1, then the effective maximum number of integration steps that the geodesic is allowed before being terminated is MaxSteps*UpdateFrequency
- ThetaSingularity: Terminate the geodesic integration if it comes too close to a polar coordinate singularity ($\theta = 0, \pi$). This can sometimes be useful to check in cases where geodesics are pushed towards the poles in extreme metrics (e.g. Manko-Novikov). Options to set:
 - Epsilon = real; How close θ is allowed near the poles. (Default is 10^{-5} .)
 - UpdateFrequency = int;
 This is analogous to the same setting under Horizon above. (Default is 1.)

2.5 ViewScreen

Under this subheading, all options are set that determine the location, size, orientation, etc. of the viewing screen. The camera is assumed to be a spherical point-sized camera with a certain aperture; the "screen size" is then determined by this aperture — the "screen" is taken to be an square in the plane going through r=0 and perpendicular to the viewing direction.

The options that can be specified are:

- Position = { t = real; r = real; theta = real; phi = real; }
 This specifies the position of the camera. (Default is (0, 1000, π/2, 0).)

 Warning: If the initial radius of the camera is *outside* of the boundary sphere radius set in the Horizon Termination, then all geodesics will terminate immediately after zero steps!
- Direction = { t = real; r = real; theta = real; phi = real; }
 This specifies the direction that the camera is pointing in.
 Warning: Currently, the camera is always pointing straight towards r = 0 (i.e. the direction vector is (0, -1, 0, 0)); this option is effectively ignored.

- ScreenSize = { x = real; y = real; }
 - This sets the screen size. The screen is centered around r = 0. For example, when the Kerr metric is selected, units are such that M = 1; when a = 0, the shadow of the Schwarzschild black hole is a circle with radius $\sqrt{27}$ on the viewing screen. (Default: (10, 10).)
- ScreenCenter = { x = real; y = real; }

This sets the center of the screen. If this is the origin (0,0), then the center of the screen is determined by following the camera direction given in Direction as taken from the camera position given in Position; any non-zero ScreenCenter simply offsets the center of the screen from this point. (Default: (0,0).)

Finally, there is a subheading Mesh, under which the Mesh settings should be set. The Mesh is what determines which pixels on the viewing screen are integrated. The options under the Mesh subheading are:

• Type = "MeshName";

This indicates the type of Mesh to be used. The possibilities for MeshName are:

- SimpleSquareMesh: This is a square mesh with equal number of pixels in length and width, and pixels evenly distributed over the viewing screen.
- InputCertainPixelsMesh: On a square mesh (such as defined in SimpleSquareMesh), have the user input some pixels to be integrated. This can be useful for e.g. integrating only a few geodesics with the Diagnostic GeodesicPosition turned on, to be able to follow and plot these few geodesics along their trajectories.
- SquareSubdivisionMesh: This Mesh starts in a first integration iteration with a simple square mesh (such as in SimpleSquareMesh), and then further subdivides certain squares into smaller squares in following iterations. It uses the Diagnostic that has UseForMesh turned on (see above) to determine "values" and "distances" between geodesics/pixels, which is used to determine which pixel squares to subdivide.

When no Mesh is set with the Type option, the default is a SimpleSquareMesh (with additional default options as listed below).

Depending on which Mesh is selected with the Type option, there are different additional options to set:

- SimpleSquareMesh:
 - TotalPixels = int;

This specifies the total number of pixels in the entire grid. If this is not a perfect square, it will be rounded downwards to the nearest perfect square (because each row and column must have an integer number of pixels). (Default: 10000.)

- InputCertainPixelsMesh:
 - TotalPixels = int; This is the same option as for SimpleSquareMesh, since the user will be inputting pixels to integrate which live on such a square grid. (Default: 10000.)
- SquareSubdivisionMesh:

- InitialPixels = int:

This is similar to the option TotalPixels for SimpleSquareMesh: the option InitialPixels determines the initial square (equally spaced) pixels to be integrated in the first integration loop. (Again, if it is not a perfect square, it will be rounded down to the nearest perfect square.) (Default: 100.)

- MaxPixels = int;

This is the maximum number of pixels that can be integrated *in total*, i.e. over *all* integration loops combined. If this is set to 0, then there is no maximum number (integration will continue until the maximum subdivision has been reached or every pixel's weight is zero). (Default: 100.)

- MaxSubdivide = int;

This sets the maximum number of times a square of pixels can be subdivided. Note that the initial grid has subdivision level 1. (Default: 1, which is also what will be used if an invalid number smaller than 1 is given.)

Note that, when InitialPixels = n^2 and MaxSubdivide = d, the total square grid size of pixels will then be given by $((n-1) \cdot 2^{d-1} + 1)^2$.

- IterationPixels = int;

At each new integration loop, the Mesh is allowed to select IterationPixels squares that it wishes to subdivide; this means that at most 5×IterationPixels new geodesics will be integrated in each integration loop (except the first iteration); there could be less geodesics integrated if some of the pixels necessary to subdivide a square already existed previously. (Default: 100.)

- InitialSubdivisionToFinal = bool;

Normally, the Mesh selects only squares to subdivide with non-zero "weight", that is, squares where the "distance" (as determined by the value Diagnostic) is non-zero. However, if this option is set to true, then the Mesh will want to continue subdividing *any* square once it has been subdivided at least once (after the initial grid). (Default: false.)

2.6 Integrator

Under this subheading, the integration scheme is chosen that is used to integrate the geodesic equation, and other options set. The integration scheme is set by the option:

- Type = "IntegratorName"; Options for IntegratorName are:
 - RK4 (fourth-order Runge-Kutta integration scheme)
 - Verlet (velocity Verlet integration scheme)

RK4 is fourth-order while Verlet is second order, so RK4 is generally about twice as slow (since it needs to calculate twice as many Christoffel symbols). (Default: RK4.)

There are other options to set here:

VerletVelocityTolerance = real;

(Only relevant is IntegratorName is specified to Verlet.) In the velocity Verlet algorithm, the velocity is updated in two steps — this setting sets how much the intermediate step velocity can differ from the final step velocity, fractionally (calculated using the Euclidean flat norm of the four-vector). If the intermediate step

differs more than this tolerance level, then the last integration step to update the velocity is repeated until the tolerance is met. (Typically, this is only necessary one or two times, maximum.) See Dolence et al. (2009) eq. (14) and the discussion thereafter. (Default: 0.001.)

• StepSize = real;

This sets the *basic* step size (i.e. change in affine parameter) for a single integration step. This is adjusted dynamically according to the current position and velocity of the geodesic. (Default: 0.03.)

• SmallestPossibleStepsize = real;

The smallest possible step size that can be taken in one single step (after adapting StepSize). (Default: 10^{-12} .)

• DerivativeH = real;

This is the value to use in numerical derivatives, i.e. the value h for which f'(x) is approximated by f'(x) = (f(x+h) - f(x-h))/(2h). (Default: 10^{-7} .)

2.7 Output

Under this heading, you can configure how the geodesics' will be written to file. You can also set the level of detail outputted to the screen (console) during the running of the program:

• ScreenOutputLevel = int;

Here, int must be an integer between 0 and 4 (inclusive). 0 means no output to the screen at all except important warnings; 4 is all possible messages including any debug messages. (Default is 4.)

• LoopMessageFrequency = int;

During every integration loop, every (approx.) int geodesics there will be a message outputted to the console to indicate the (approx.) current number of geodesics integrated, the (approx.) speed of integration (in geodesics per second), and the estimated time left in this integration loop. Note that all the numbers outputted are approximate, as they are extrapolations from the progress of one thread of the parallel integration loop to all of the threads. (Default is essentially infinite, so no intermediate output will be shown.)

The options that are available to set that determine the format of the file name(s) to which the output is written are:

• FilePrefix = "prefix";

All output files will start with "prefix". If this is not specified, FOORT will do all output to the console.

• FileExtension = "extension";

All output files will end with "extension". If this is not specified or given as an empty string, the output files will have no extension.

• TimeStamp = bool;

bool is true if every output file contains a time stamp (with the local system time and date of when FOORT starts).

The files created will then have names such as "prefix_TIME_DiagName.extension" or "prefix_TIME_DiagName_n.extension" for n > 1, where "DiagName" is a short (spaceless) name of the Diagnostic whose data is outputted in this file. There will be a different file for each Diagnostic turned on. n is the number of file written, which is only part of the file name for n > 1. The "TIME" timestamp is of the form "yymmdd-hhmmss" (year - month - day, hour - minute - second). Note that FOORT will create any directory structures necessary to create the file.

The options that further specify details of the actual output written to files are:

• GeodesicsToCache = int;

Indicates how many geodesics should be cached (stored in memory) before writing everything in memory to file. By default, this is essentially infinite. (It is actually the maximum number storeable in a unsigned long, which is $\sim 10^{10}$).

• GeodesicsPerFile = int;

Indicates how many geodesics should be written per file. If more than this number of geodesics are integrated, additional files with filenames ending in _n (before the specified file extension) will be created. By default, is essentially infinite (just as GeodesicsToCache above). (If 0 is specified, the default will be used.)

• FirstLineInfo = bool;

If set to true, will output on the first line of every output file a string that gives descriptive data of all the objects used in integration (Metric, Source, ViewScreen, etc.)

3 Processing Output

(what is outputted in the files etc)

4 Procedures to Add New Objects

For every object to add, there are a certain number of tasks to be done. Per object, these are enumerated below. Within the source files, these add points are also indicated and sample source code is given. These steps below and the add points in the code make adding a new object not a big efFOORT at all!

A general note about variable names and settings: the name that a particular property has in the configuration file will be the same as the name that features in the first argument (in quotation marks) in the libconfig argument lookupValue. So, for example, the line: TheSetting.lookupValue("ConfigurationFilePropertyName", LocalVariableName); looks at the ConfigSetting object TheSetting, which will be some branch within the configuration file, and within (that branch in) the configuration file reads in the line:

ConfigurationFilePropertyName = "mysetting";

and puts "mysetting" into LocalVariableName (which should in this case be a std::string!). Note that if the setting ConfigurationFilePropertyName does not exist under the branch ConfigSetting, then LocalVariableName will be unaltered (no exceptions are thrown). This is why, before using lookupValue, LocalVariableName should have been set to whatever the setting's default value should be. Note that LocalVariableName,

ConfigurationFilePropertyName, and whatever the class (private) member variable is called that eventually stores this property or value, can all be completely different names.

4.1 Adding a new Metric

A. At the end of Metric.h: Add the declaration for your new Metric class here, inheriting publically from the base Metric class (or from SphericalHorizonMetric, if your metric has a horizon at a constant radius). It is good practice to make the class (and all overriding virtual functions) final, unless further descendant Metric classes are possible. It is also good practice to make the member variables (metric parameters) private and const (and initialized in a constructor) since the metric should not change after initialization.

It is necessary to override the basic metric getter functions getMetric_dd and getMetric_uu, which return the metric with indices down or up. It is also recommended to overload GetDescriptionString(), although this has been already implemented in the base class Metric.

The implementations (definitions) of these functions can then go in Metric.cpp (or a different source code file).

Note: if your metric enjoys any Killing vectors, make sure to remember to set $m_Symmetries$ accordingly in the class constructor; e.g. a Metric that is stationary and axisymmetric should include the line $m_Symmetries = \{ 0,3 \}$; in the constructor.

B. In Config.cpp, in function Config::GetMetric(): You must add a new else if clause checking for if your new metric type has been specified. If it has, then proceed to look up any other parameters necessary for the metric before creating a new instance of it in the variable TheMetric.

4.2 Adding a new Diagnostic

- A.1. In the middle of Diagnostics.h, after all other Diagnostic class declarations: Declare your new Diagnostic class here, inheriting publically from Diagnostic. As with Metric, it is good practice to make this new Diagnostic and all its overriding functions final. The definitions of the member functions of your class can then be given in Diagnostics.cpp (or a different source code file). The necessary functions to override are:
 - A constructor that passes along the const pointer to the (owner) Geodesic to the base class constructor.
 - UpdateData(): here your Diagnostic updates itself according to the current state of its owner Geodesic.
 - getFullDataStr(): this is the full output string of the Diagnostic for its owner
 Geodesic, as should be written to a file.
 - getFinalDataVal(): this returns a vector of real numbers that indicates the final "value" that should be associated to its owner Geodesic.
 - FinalDataValDistance(...): this returns a "distance" between two geodesics based on their two final "values" (as given by getFinalDataVal(). This distance is used by adaptive mesh(es) to decide where to refine the mesh.
 - Reset() (optional): If your Diagnostic has member variables that change during the trajectory of the Geodesic, then Reset() must reset all these variables to their initial values, ready to be used for a new Geodesic. If there are no such member variables in your Diagnostic, then this function does not

need an override. Note: if you do override Reset(), make sure to add a call Diagnostic::Reset()) in your implementation of Reset(), so that the base class also resets its internal variable!

- getNameStr(): This returns a short string without spaces that will be appended to the file name, typically just a short name identifying the Diagnostic.
- getFullDescriptionStr(): This returns a longer, descriptive string (with spaces allowed) of the Diagnostic and any relevant options that are selected.
 This will e.g. be outputted to the screen at runtime to indicate which Diagnostics are turned on.

Finally, if the Diagnostic needs to specify options, a declaration of its DiagnosticOptions should be given here. Note that this is a std::unique_ptr and is static: the reason is that these options get set once (at the start of the program), and then remain the same — i.e. for all instances of the Diagnostic that belong to different instances of Geodesics.

A.2. (Optional) At the end of Diagnostics.h, after all other DiagnosticOptions struct declarations: Declare and define your new DiagnosticOptions struct here, if your Diagnostic needs additional options over the standard UpdateFrequency ones provided by the base struct DiagnosticOptions. As indicated in the code, all member variables should be const but public, and initialized in the constructor. Make sure your constructor passes along the UpdateFrequency struct information to the base struct constructor.

As mentioned above, the DiagnosticOptions are static members of their owning Diagnostic class; they get set at the beginning of the program and are afterwards immutable.

- B. At the beginning of Diagnostics.h (at the definitions of the bitflags): Define a new DiagBitflag for your new Diagnostic. Make sure to use a bitflag that has not been used before! (All defined bitflags are here, so it should be clear what has been used already.)
- C. At the beginning of Diagnostics.cpp, in the definition of CreateDiagnosticVector: add an appropriate if clause checking to see if diagflags contains the newly defined DiagBitflag (which was defined in point B. above), and if so adds an instance of the Diagnostic to the Diagnostic vector being created. If it is additionally the value Diagnostic (in valdiag), then rotate the resulting vector such that it is at the front of the vector.
- D.1. At the beginning of Config.cpp: If your Diagnostic carries a static DiagnosticOptions struct (whether it is a new descendant of DiagnosticOptions or not), then it must be declared here!
- D.2. In Config.cpp, in function Config::InitializeDiagnostics(): Add an if clause here checking if your Diagnostic is turned on in the configuration file. If it is, intialize the relevant options and set the bitflags appropriately.

4.3 Adding a new Termination

A.1. At the end of the declarations of the Termination classes in Terminations.h: Declare your new Termination class here, inheriting publically from Termination. The

definitions of the member functions of your class can then be given in Terminations.cpp (or a different source code file). The necessary functions to override are:

- A constructor that passes along the const pointer to the (owner) Geodesic to the base class constructor.
- CheckTermination(): which checks if the termination condition has been reached; if not, returns Term::Continue, if so, returns the new termination condition (see below in B.2.).
- Reset() (optional): If your Termination has member variables that change during the trajectory of the Geodesic, then Reset() must reset all these variables to their initial values, ready to be used for a new Geodesic. If there are no such member variables in your Termination, then this function does not need an override. Note: if you do override Reset(), make sure to add a call Termination::Reset()) in your implementation of Reset(), so that the base class also resets its internal variable!
- getFullDescriptionStr(): This returns a descriptive string (with spaces allowed) of the Termination and any relevant options that are selected. This will e.g. be outputted to the screen at runtime to indicate which Terminations are turned on.

Finally, most likely the Terminations needs to specify options, so a declaration of its TerminationOptions should be given here. Note that this is a std::unique_ptr and is static: as for DiagnosticOptions, these options get set once (at the start of the program), and then remain the same — i.e. for all instances of the Termination that belong to different instances of Geodesics.

- A.2. (Optional) At the end of Terminations.h: Declare and define your new TerminationOptions struct here, if necessary, inheriting publically from TerminationOptions. Just as for DiagnosticOptions, all member variables should be const but public, and initialized in the constructor. Make sure your constructor passes along the UpdateFrequency struct information to the base struct constructor.
- B.1. At the beginning of Terminations.h (at the definitions of the bitflags): Define a new TermBitflag for your new Termination.
- B.2. In the definition of enum class Term in Terminations.h: Add a new termination condition in this class that can be set by your new Termination.
 - C. At the beginning of Terminations.cpp, in the definition of CreateTerminationVector: add an appropriate if clause checking to see if termflags contains the newly defined TermBitflag (which was defined in point B.1 above), and if so adds an instance of the Termination to the Termination vector being created.
- D.1. At the beginning of Config.cpp: If your Termination carries a static TerminationOptions struct (whether it is a new descendant of TerminationOptions or not), then it must be declared here!
- D.2. In Config.cpp, in function Config::InitializeTerminations(): Add an if clause here checking if your Termination is turned on in the configuration file. If it is, intialize the relevant options and set the bitflags appropriately.