

Read in the following dictionary:

$x_6$	3.0	$+7.00x_1$	$+2.00x_2$	$-10.00x_3$	$-2.00x_4$	$-6.00x_5$
$x_7$	1.0	$-1.00x_1$	$+3.00x_2$	$+8.00x_3$	$+5.00x_4$	$-4.00x_5$
$x_8$	-24.0	$+1.00x_1$	$+10.00x_2$	$+8.00x_3$	$-8.00x_4$	$+9.00x_5$
$x_9$	6.0	$-4.00x_1$	$+7.00x_2$	$+7.00x_3$	$+4.00x_4$	$-6.00x_5$
$x_{10}$	43.0	$-9.00x_1$		$-3.00x_3$	$-7.00x_4$	$-4.00x_5$
$z$	0.0	$+5.00x_1$	$-1.00x_2$	$+4.00x_3$	$+4.00x_4$	$+5.00x_5$

## 0.1 Initialization Phase: Dual Problem Solving

New Objective in primal was changed to :

$$\max \sum_{j=1}^5 -x_j$$

Primal variable  $x_j$  corresponds to dual variable  $y_j$  for  $j = 1, \dots, 10$  Dual Dictionary (with objective changed is):

$y_1$	1.0	$-7.00y_6$	$+1.00y_7$	$-1.00y_8$	$+4.00y_9$	$+9.00y_{10}$
$y_2$	1.0	$-2.00y_6$	$-3.00y_7$	$-10.00y_8$	$-7.00y_9$	
$y_3$	1.0	$+10.00y_6$	$-8.00y_7$	$-8.00y_8$	$-7.00y_9$	$+3.00y_{10}$
$y_4$	1.0	$+2.00y_6$	$-5.00y_7$	$+8.00y_8$	$-4.00y_9$	$+7.00y_{10}$
$y_5$	1.0	$+6.00y_6$	$+4.00y_7$	$-9.00y_8$	$+6.00y_9$	$+4.00y_{10}$
$z$	-0	$-3.00y_6$	$-1.00y_7$	$+24.00y_8$	$-6.00y_9$	$-43.00y_{10}$

Initialization succeeded in finding final dual dictionary with 2 pivots

$y_1$	0.9	$-6.80y_6$	$+1.30y_7$	$+0.10y_2$	$+4.70y_9$	$+9.00y_{10}$
$y_8$	0.1	$-0.20y_6$	$-0.30y_7$	$-0.10y_2$	$-0.70y_9$	
$y_3$	0.2	$+11.60y_6$	$-5.60y_7$	$+0.80y_2$	$-1.40y_9$	$+3.00y_{10}$
$y_4$	1.8	$+0.40y_6$	$-7.40y_7$	$-0.80y_2$	$-9.60y_9$	$+7.00y_{10}$
$y_5$	0.1	$+7.80y_6$	$+6.70y_7$	$+0.90y_2$	$+12.30y_9$	$+4.00y_{10}$
$z$	2.4	$-7.80y_6$	$-8.20y_7$	$-2.40y_2$	$-22.80y_9$	$-43.00y_{10}$

Primal Dictionary is:

$x_6$	7.8	$+6.80x_1$	$+0.20x_8$	$-11.60x_3$	$-0.40x_4$	$-7.80x_5$
$x_7$	8.2	$-1.30x_1$	$+0.30x_8$	$+5.60x_3$	$+7.40x_4$	$-6.70x_5$
$x_2$	2.4	$-0.10x_1$	$+0.10x_8$	$-0.80x_3$	$+0.80x_4$	$-0.90x_5$
$x_9$	22.8	$-4.70x_1$	$+0.70x_8$	$+1.40x_3$	$+9.60x_4$	$-12.30x_5$
$x_{10}$	43.0	$-9.00x_1$		$-3.00x_3$	$-7.00x_4$	$-4.00x_5$
$z$	-2.4	$-0.90x_1$	$-0.10x_8$	$-0.20x_3$	$-1.80x_4$	$-0.10x_5$

Primal Dictionary with original objective is:

$x_6$	7.8	$+6.80x_1 + 0.20x_8 - 11.60x_3 - 0.40x_4 - 7.80x_5$
$x_7$	8.2	$-1.30x_1 + 0.30x_8 + 5.60x_3 + 7.40x_4 - 6.70x_5$
$x_2$	2.4	$-0.10x_1 + 0.10x_8 - 0.80x_3 + 0.80x_4 - 0.90x_5$
$x_9$	22.8	$-4.70x_1 + 0.70x_8 + 1.40x_3 + 9.60x_4 - 12.30x_5$
$x_{10}$	43.0	$-9.00x_1 - 3.00x_3 - 7.00x_4 - 4.00x_5$
$z$	-2.4	$+5.10x_1 - 0.10x_8 + 4.80x_3 + 3.20x_4 + 5.90x_5$

## 1 Optimization Phase Simplex

Starting Dictionary is:

$x_6$	7.8	$+6.80x_1 + 0.20x_8 - 11.60x_3 - 0.40x_4 - 7.80x_5$
$x_7$	8.2	$-1.30x_1 + 0.30x_8 + 5.60x_3 + 7.40x_4 - 6.70x_5$
$x_2$	2.4	$-0.10x_1 + 0.10x_8 - 0.80x_3 + 0.80x_4 - 0.90x_5$
$x_9$	22.8	$-4.70x_1 + 0.70x_8 + 1.40x_3 + 9.60x_4 - 12.30x_5$
$x_{10}$	43.0	$-9.00x_1 - 3.00x_3 - 7.00x_4 - 4.00x_5$
$z$	-2.4	$+5.10x_1 - 0.10x_8 + 4.80x_3 + 3.20x_4 + 5.90x_5$

$x_1$  enters and  $x_{10}$  leaves

$x_6$	40.2888888889	$-0.76x_{10} + 0.20x_8 - 13.87x_3 - 5.69x_4 - 10.82x_5$
$x_7$	1.9888888889	$+0.14x_{10} + 0.30x_8 + 6.03x_3 + 8.41x_4 - 6.12x_5$
$x_2$	1.9222222222	$+0.01x_{10} + 0.10x_8 - 0.77x_3 + 0.88x_4 - 0.86x_5$
$x_9$	0.3444444444	$+0.52x_{10} + 0.70x_8 + 2.97x_3 + 13.26x_4 - 10.21x_5$
$x_1$	4.7777777778	$-0.11x_{10} - 0.33x_3 - 0.78x_4 - 0.44x_5$
$z$	21.9666666667	$-0.57x_{10} - 0.10x_8 + 3.10x_3 - 0.77x_4 + 3.63x_5$

$x_3$  enters and  $x_2$  leaves

$x_6$	5.52173913043	$-0.96x_{10} - 1.61x_8 + 18.09x_2 - 21.57x_4 + 4.65x_5$
$x_7$	17.115942029	$+0.23x_{10} + 1.09x_8 - 7.87x_2 + 15.32x_4 - 12.86x_5$
$x_3$	2.50724637681	$+0.01x_{10} + 0.13x_8 - 1.30x_2 + 1.14x_4 - 1.12x_5$
$x_9$	7.78260869565	$+0.57x_{10} + 1.09x_8 - 3.87x_2 + 16.65x_4 - 13.52x_5$
$x_1$	3.94202898551	$-0.12x_{10} - 0.04x_8 + 0.43x_2 - 1.16x_4 - 0.07x_5$
$z$	29.7391304348	$-0.52x_{10} + 0.30x_8 - 4.04x_2 + 2.78x_4 + 0.17x_5$

$x_4$  enters and  $x_6$  leaves

$x_4$	0.256048387097	$-0.04x_{10} - 0.07x_8 + 0.84x_2 - 0.05x_6 + 0.22x_5$
$x_7$	21.0383064516	$-0.45x_{10} - 0.06x_8 + 4.98x_2 - 0.71x_6 - 9.55x_5$
$x_3$	2.80040322581	$-0.04x_{10} + 0.05x_8 - 0.34x_2 - 0.05x_6 - 0.87x_5$
$x_9$	12.0463709677	$-0.17x_{10} - 0.16x_8 + 10.10x_2 - 0.77x_6 - 9.93x_5$
$x_1$	3.64516129032	$-0.06x_{10} + 0.04x_8 - 0.54x_2 + 0.05x_6 - 0.32x_5$
$z$	30.4516129032	$-0.65x_{10} + 0.10x_8 - 1.71x_2 - 0.13x_6 + 0.77x_5$

$x_5$  enters and  $x_9$  leaves

$x_4$	0.517766497462	$-0.05x_{10} - 0.08x_8 + 1.06x_2 - 0.06x_6 - 0.02x_9$
$x_7$	9.45177664975	$-0.28x_{10} + 0.09x_8 - 4.73x_2 + 0.03x_6 + 0.96x_9$
$x_3$	1.7461928934	$-0.02x_{10} + 0.06x_8 - 1.23x_2 + 0.01x_6 + 0.09x_9$
$x_5$	1.21319796954	$-0.02x_{10} - 0.02x_8 + 1.02x_2 - 0.08x_6 - 0.10x_9$
$x_1$	3.2538071066	$-0.06x_{10} + 0.05x_8 - 0.87x_2 + 0.08x_6 + 0.03x_9$
$z$	31.3908629442	$-0.66x_{10} + 0.08x_8 - 0.92x_2 - 0.19x_6 - 0.08x_9$

$x_8$  enters and  $x_4$  leaves

$x_8$	6.640625	$-0.62x_{10} - 12.83x_4 + 13.57x_2 - 0.81x_6 - 0.28x_9$
$x_7$	10.0729166667	$-0.34x_{10} - 1.20x_4 - 3.46x_2 - 0.04x_6 + 0.94x_9$
$x_3$	2.13541666667	$-0.06x_{10} - 0.75x_4 - 0.43x_2 - 0.03x_6 + 0.07x_9$
$x_5$	1.109375	$-0.01x_{10} + 0.20x_4 + 0.80x_2 - 0.07x_6 - 0.10x_9$
$x_1$	3.57291666667	$-0.09x_{10} - 0.62x_4 - 0.21x_2 + 0.04x_6 + 0.02x_9$
$z$	31.953125	$-0.71x_{10} - 1.09x_4 + 0.23x_2 - 0.26x_6 - 0.10x_9$

$x_2$  enters and  $x_7$  leaves

$x_8$	46.1067669173	$-1.94x_{10} - 17.53x_4 - 3.92x_7 - 0.98x_6 + 3.39x_9$
$x_2$	2.90827067669	$-0.10x_{10} - 0.35x_4 - 0.29x_7 - 0.01x_6 + 0.27x_9$
$x_3$	0.878195488722	$-0.02x_{10} - 0.60x_4 + 0.12x_7 - 0.03x_6 - 0.05x_9$
$x_5$	3.44962406015	$-0.09x_{10} - 0.08x_4 - 0.23x_7 - 0.08x_6 + 0.12x_9$
$x_1$	2.95187969925	$-0.07x_{10} - 0.54x_4 + 0.06x_7 + 0.04x_6 - 0.04x_9$
$z$	32.6120300752	$-0.73x_{10} - 1.16x_4 - 0.07x_7 - 0.26x_6 - 0.04x_9$

Final Dictionary Solution: 32.6120300752 Num Pivots: 7