Read in the following dictionary:

0.1 Initialization Phase: Dual Problem Solving

New Objective in primal was changed to:

$$\max \sum_{j=1}^{5} -x_{j}$$

Primal variable x_j corresponds to dual variable y_j for j = 1, ..., 14 Dual Dictionary (with objective changed is):

```
+1.00y_6 -4.00y_7 +7.00y_8 +9.00y_9 +9.00y_{10} +7.00y_{11} -3.00y_{12} -7.00y_{13} -3.00y_{14} +1.00y_{15} +1.0
y_1
                                             1.0
                                                                                                         +8.00y_6 -7.00y_7 +9.00y_8 -7.00y_9 -8.00y_{10} +8.00y_{11} -9.00y_{12} -5.00y_{13} +6.00y_{14}
y_2
                                             1.0
                                                                                                       -3.00y_6 \quad -9.00y_7 \quad -4.00y_8 \quad -5.00y_9 \quad -8.00y_{10} \quad -2.00y_{11} \quad +2.00y_{12} \quad -10.00y_{13} \quad +3.00y_{14} \quad -10.00y_{15} \quad +3.00y_{15} \quad -10.00y_{15} \quad +3.00y_{15} \quad +3.00y_{1
y_3
                                             1.0
                                                                                                       +7.00y_6 +10.00y_7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                -1.00y_{10} \ -5.00y_{11} \ -1.00y_{12}
y_4
                                                                                                                                                                                                        +4.00y_7 -6.00y_8 +1.00y_9 -8.00y_{10} +5.00y_{11} -10.00y_{12} -10.00y_{13} +10.00y_{14}
                                             1.0
y_5
                                                                                                  -17.00y_6 +3.00y_7 -31.00y_8 -5.00y_9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                -37.00y_{11} +2.00y_{12} +40.00y_{13} -10.00y_{14}
```

Initialization succeeded in finding final dual dictionary with 6 pivots

```
0.0391304347826
                                                                                                                                                                                                                     +0.26y_6 +0.04y_3 +1.37y_8 +1.34y_9 +1.90y_{10} +0.76y_{11} -0.32y_7 +0.05y_5 -0.10y_{10} +0.00y_{10} +0.00y_{10
 y_{14}
                                             0.0228260869565\\
                                                                                                                                                                                                                     +0.40y_6 +0.11y_3 +0.63y_8 +1.28y_9 +1.11y_{10} +1.03y_{11} +0.90y_7 -0.06y_5 -0.00y_7 +0.00y_7 +0.0
 y_{12}
                                                   0.447826086957
                                                                                                                                                                                                                       +6.65y_6 -0.39y_3 + 10.83y_8 - 11.29y_9 -6.54y_{10} +2.15y_{11} -12.90y_7 + 0.77y_5 + 0.10y_{10}
    y_2
                                                        0.78152173913
                                                                                                                                                                                                                     +5.29y_6 -0.33y_3 -7.50y_8 -8.00y_9 -11.63y_{10} -9.83y_{11} +10.71y_7 -0.18y_5 +0.70y_8
    y_4
                                                                                                                                                                                                                 0.116304347826
y_{13}
                                                        4.30652173913
```

Primal Dictionary is:

```
24.4565217391
                            -0.26x_{14} - 0.40x_{12} - 6.65x_2 - 5.29x_4 + 0.14x_{13}
x_6
       2.82608695652
                            -0.04x_{14} - 0.11x_{12} + 0.39x_{2} + 0.33x_{4} + 0.07x_{13}
x_3
       37.9043478261
                            -1.37x_{14} - 0.63x_{12} - 10.83x_2 + 7.50x_4 - 0.14x_{13}
x_8
                            -1.34x_{14} - 1.28x_{12} + 11.29x_2 + 8.00x_4 - 0.16x_{13}
       9.47608695652
x_9
                            -1.90x_{14} - 1.11x_{12} + 6.54x_2 + 11.63x_4 + 0.01x_{13}
x_{10}
       17.0826086957
       33.2065217391
                            -0.76x_{14} - 1.03x_{12} - 2.15x_2 + 9.83x_4 - 0.23x_{13}
x_{11}
       24.6869565217
                            +0.32x_{14} -0.90x_{12} +12.90x_2 -10.71x_4 +0.82x_{13}
x_7
                            -0.05x_{14} + 0.06x_{12} -0.77x_2 +0.18x_4 -0.00x_{13}
      0.458695652174
x_5
       1.02173913043
                            +0.13x_{14} +0.08x_{12} -0.17x_2 -0.73x_4 +0.05x_{13}
      -4.30652173913
                           -0.04x_{14} - 0.02x_{12} - 0.45x_2 - 0.78x_4 - 0.12x_{13}
```

Primal Dictionary with original objective is:

```
24.4565217391
                           -0.26x_{14} - 0.40x_{12} - 6.65x_2 - 5.29x_4 + 0.14x_{13}
x_6
       2.82608695652
                           -0.04x_{14} - 0.11x_{12} + 0.39x_2 + 0.33x_4 + 0.07x_{13}
x_3
       37.9043478261
                           -1.37x_{14} - 0.63x_{12} - 10.83x_2 + 7.50x_4 - 0.14x_{13}
x_8
       9.47608695652
                           -1.34x_{14} - 1.28x_{12} + 11.29x_2 + 8.00x_4 - 0.16x_{13}
x_9
       17.0826086957
                           -1.90x_{14} - 1.11x_{12} + 6.54x_2 + 11.63x_4 + 0.01x_{13}
x_{10}
                           -0.76x_{14} - 1.03x_{12} - 2.15x_2 + 9.83x_4 - 0.23x_{13}
x_{11}
       33.2065217391
       24.6869565217
                           +0.32x_{14} -0.90x_{12} +12.90x_2 -10.71x_4 +0.82x_{13}
x_7
      0.458695652174
                           -0.05x_{14} + 0.06x_{12} -0.77x_2 +0.18x_4 -0.00x_{13}
x_5
                           +0.13x_{14} +0.08x_{12} -0.17x_2 -0.73x_4 +0.05x_{13}
       1.02173913043
x_1
       2.48260869565
                           -0.70x_{14} - 0.41x_{12} + 2.94x_2 + 0.93x_4 - 0.09x_{13}
```

1 Optimization Phase Simplex

Starting Dictionary is:

```
24.4565217391
                           -0.26x_{14} - 0.40x_{12} - 6.65x_2 - 5.29x_4 + 0.14x_{13}
x_6
x_3
       2.82608695652
                           -0.04x_{14} - 0.11x_{12} + 0.39x_{2} + 0.33x_{4} + 0.07x_{13}
       37.9043478261
                           -1.37x_{14} - 0.63x_{12} - 10.83x_2 + 7.50x_4 - 0.14x_{13}
x_8
       9.47608695652
                           -1.34x_{14} - 1.28x_{12} + 11.29x_2 + 8.00x_4 - 0.16x_{13}
x_9
       17.0826086957
                           -1.90x_{14} - 1.11x_{12} + 6.54x_2 + 11.63x_4 + 0.01x_{13}
x_{10}
       33.2065217391
                           -0.76x_{14} - 1.03x_{12} - 2.15x_2 + 9.83x_4 - 0.23x_{13}
x_{11}
       24.6869565217
                           +0.32x_{14} -0.90x_{12} +12.90x_2 -10.71x_4 +0.82x_{13}
x_7
                           -0.05x_{14} + 0.06x_{12} -0.77x_2 +0.18x_4 -0.00x_{13}
x_5
      0.458695652174
       1.02173913043
                           +0.13x_{14} +0.08x_{12} -0.17x_2 -0.73x_4 +0.05x_{13}
x_1
       2.48260869565
                           -0.70x_{14} - 0.41x_{12} + 2.94x_2 + 0.93x_4 - 0.09x_{13}
```

 x_2 enters and x_5 leaves

```
x_6
       20.4915254237
                           +0.15x_{14} - 0.88x_{12} + 8.64x_5 - 6.88x_4 + 0.17x_{13}
       3.0593220339
                           -0.07x_{14} - 0.08x_{12} - 0.51x_5 + 0.42x_4 + 0.06x_{13}
x_3
       31.4463276836
                           -0.70x_{14} - 1.42x_{12} + 14.08x_5 + 4.92x_4 - 0.09x_{13}
x_8
       16.2062146893
                           -2.05x_{14} - 0.47x_{12} - 14.67x_5 + 10.70x_4 - 0.21x_{13}
x_9
       20.9802259887
                           -2.31x_{14} - 0.64x_{12} - 8.50x_5 + 13.19x_4 - 0.02x_{13}
x_{10}
       31.9237288136
                           -0.63x_{14} - 1.18x_{12} + 2.80x_5 + 9.32x_4 - 0.22x_{13}
x_{11}
                           -0.48x_{14} + 0.03x_{12} - 16.77x_5 - 7.63x_4 + 0.76x_{13}
       32.3785310734
x_7
                           -0.06x_{14} + 0.07x_{12} -1.30x_5 +0.24x_4 -0.00x_{13}
x_2
       0.59604519774
      0.918079096045
                           +0.14x_{14} +0.06x_{12} +0.23x_5 -0.77x_4 +0.06x_{13}
x_1
       4.23446327684
                           -0.89x_{14} - 0.20x_{12} - 3.82x_5 + 1.63x_4 - 0.11x_{13}
```

 x_4 enters and x_1 leaves

```
12.2844036697
                           -1.11x_{14} - 1.45x_{12} + 6.62x_5 + 8.94x_1 - 0.32x_{13}
x_6
       3.55963302752
                           +0.01x_{14} - 0.05x_{12} - 0.39x_5 - 0.54x_1 + 0.09x_{13}
x_3
                           +0.20x_{14} -1.01x_{12} +15.52x_5 -6.39x_1 +0.26x_{13}
x_8
       37.3119266055
x_9
       28.9633027523
                           -0.08x_{14} + 0.41x_{12} - 11.53x_5 - 13.90x_1 + 0.56x_{13}
      36.7155963303
                           +0.11x_{14} +0.45x_{12} -4.62x_5 -17.14x_1 +0.92x_{13}
x_{10}
                           +1.08x_{14} - 0.41x_{12} + 5.53x_5 - 12.10x_1 + 0.44x_{13}
       43.0366972477
x_{11}
      23.2752293578
                           -1.88x_{14} - 0.60x_{12} - 19.01x_5 + 9.92x_1 + 0.22x_{13}
x_7
      0.880733944954
                           -0.02x_{14} + 0.09x_{12} -1.23x_5 -0.31x_1 +0.01x_{13}
x_2
                           +0.18x_{14} + 0.08x_{12} + 0.29x_5 -1.30x_1 +0.07x_{13}
      1.19266055046
x_4
      6.18348623853
                           -0.59x_{14} - 0.06x_{12} - 3.34x_5 - 2.12x_1 + 0.01x_{13}
```

 x_{13} enters and x_6 leaves

```
-3.44x_{14} - 4.49x_{12} + 20.51x_5 + 27.68x_1 - 3.10x_6
      38.0397727273
x_{13}
      7.11931818182
                         -0.31x_{14} - 0.47x_{12} + 1.53x_5 + 2.05x_1 - 0.29x_6
x_3
                         -0.69x_{14} - 2.17x_{12} + 20.83x_5 + 0.77x_1 - 0.80x_6
x_8
      47.1534090909
      50.1818181818
                         -2.00x_{14} - 2.09x_{12} - 0.09x_5 + 1.55x_1 - 1.73x_6
x_9
                         -3.06x_{14} - 3.69x_{12} + 14.31x_5 + 8.41x_1 - 2.86x_6
      71.8238636364
x_{10}
                         -0.44x_{14} - 2.40x_{12} + 14.60x_5 + 0.14x_1 - 1.37x_6
      59.8579545455
x_{11}
                         -2.63x_{14} - 1.57x_{12} - 14.57x_5 + 15.91x_1 - 0.67x_6
      31.5113636364
x_7
      1.36931818182
                         -0.06x_{14} + 0.03x_{12} -0.97x_5 +0.05x_1 -0.04x_6
x_2
                         -0.06x_{14} - 0.24x_{12} + 1.76x_5 + 0.68x_1 - 0.22x_6
x_4
      3.91477272727
      6.60227272727
                         -0.62x_{14} - 0.11x_{12} - 3.11x_5 - 1.82x_1 - 0.03x_6
```

Final Dictionary Solution: 6.60227272727 Num Pivots: 4