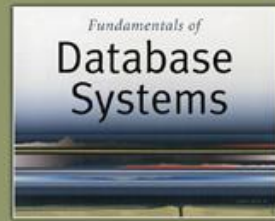


# Indexing Structures for Files



5th Edition

Elmasri / Navathe



Copyright © 2007 Ramez Elmasri and Shamkant B. Navathe

# Chapter Outline

- Types of Single-level Ordered Indexes
  - Primary Indexes
  - Clustering Indexes
  - Secondary Indexes
- Multilevel Indexes
- Dynamic Multilevel Indexes Using B-Trees and B+-Trees
- Indexes on Multiple Keys

# Indexes as Access Paths

- A single-level index is an auxiliary file that makes it more efficient to search for a record in the data file.
- The index is usually specified on one field of the file (although it could be specified on several fields)
- One form of an index is a file of entries **<field value, pointer to record>**, which is ordered by field value
- The index is called an access path on the field.

# Indexes as Access Paths (contd.)

- The index file usually occupies considerably less disk blocks than the data file because its entries are much smaller
- A binary search on the index yields a pointer to the file record
- Indexes can also be characterized as dense or sparse
  - A **dense index** has an index entry for every search key value (and hence every record) in the data file.
  - A **sparse (or nondense) index**, on the other hand, has index entries for only some of the search values

# Indexes as Access Paths (contd.)

- Example: Given the following data file EMPLOYEE(NAME, SSN, ADDRESS, JOB, SAL, ... )
- Suppose that:
  - record size  $R=150$  bytes      block size  $B=512$  bytes       $r=30000$  records
- Then, we get:
  - blocking factor  $Bfr = B \div R = 512 \div 150 = 3$  records/block
  - number of file blocks  $b = (r/Bfr) = (30000/3) = 10000$  blocks
- For an index on the SSN field, assume the field size  $V_{SSN}=9$  bytes, assume the record pointer size  $P_R=7$  bytes. Then:
  - index entry size  $R_i = (V_{SSN} + P_R) = (9+7) = 16$  bytes
  - index blocking factor  $Bfr_i = B \div R_i = 512 \div 16 = 32$  entries/block
  - number of index blocks  $b_i = (r/Bfr_i) = (30000/32) = 938$  blocks
  - binary search needs  $\log_2 b_i = \log_2 938 = 10$  block accesses
  - This is compared to an average linear search cost of:
    - $(b/2) = 30000/2 = 15000$  block accesses
  - If the file records are ordered, the binary search cost would be:
    - $\log_2 b = \log_2 30000 = 15$  block accesses

# Types of Single-Level Indexes

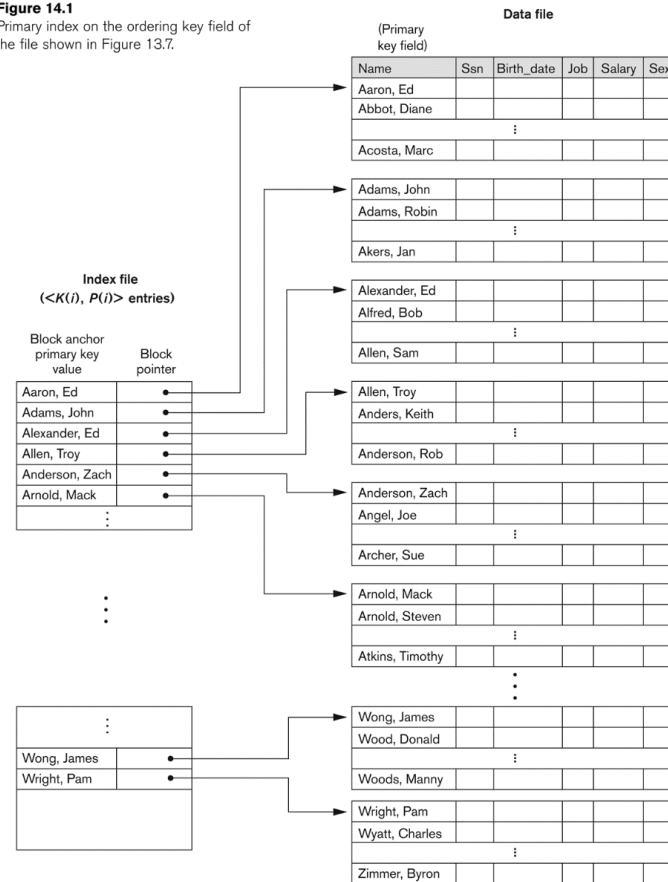
## ■ Primary Index

- Defined on an ordered data file
- The data file is ordered on a **key field**
- Includes one index entry *for each block* in the data file; the index entry has the key field value for the *first record* in the block, which is called the *block anchor*
- A similar scheme can use the *last record* in a block.
- A primary index is a nondense (sparse) index, since it includes an entry for each disk block of the data file and the keys of its anchor record rather than for every search value.

# Primary index on the ordering key field

**Figure 14.1**

Primary index on the ordering key field of the file shown in Figure 13.7.



# Types of Single-Level Indexes

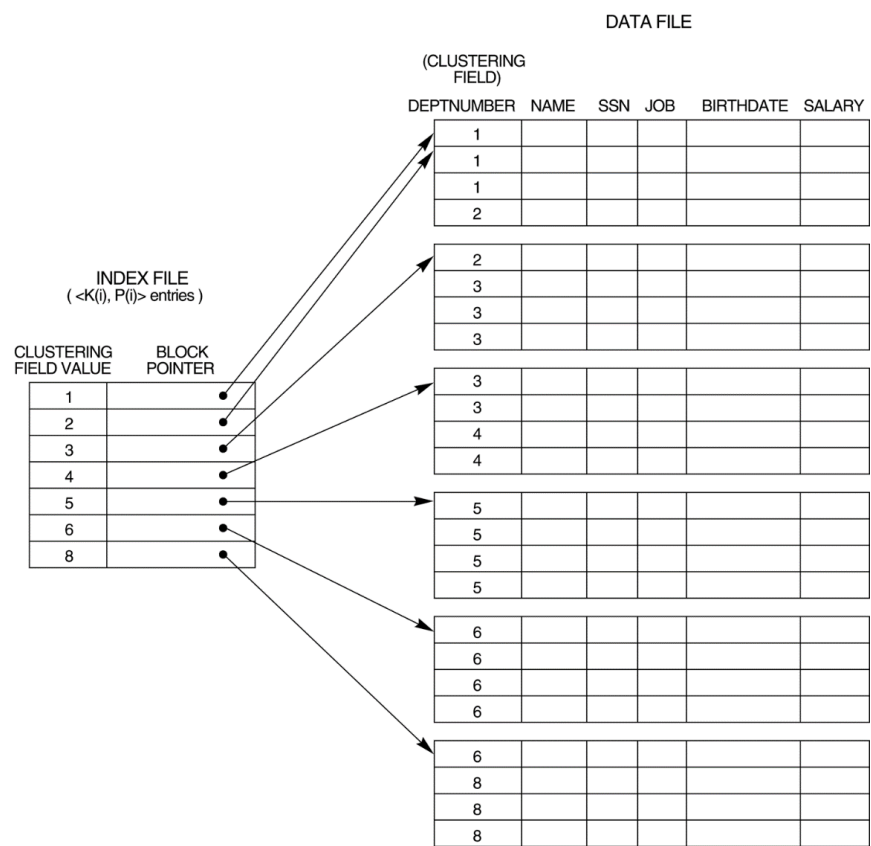
## ■ Clustering Index

- Defined on an ordered data file
- The data file is ordered on a *non-key field* unlike primary index, which requires that the ordering field of the data file have a distinct value for each record.
- Includes one index entry *for each distinct value* of the field; the index entry points to the first data block that contains records with that field value.
- It is another example of *nondense* index where Insertion and Deletion is relatively straightforward with a clustering index.

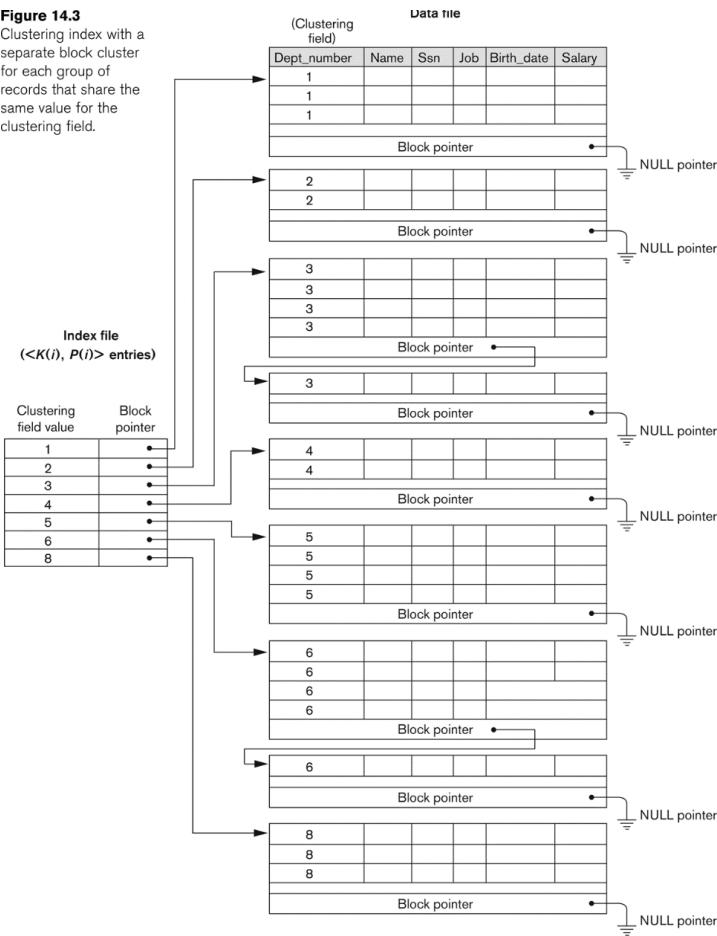


# A Clustering Index Example

- **FIGURE 14.2**  
A clustering index on the DEPTNUMBER ordering non-key field of an EMPLOYEE file.



# Another Clustering Index Example



# Types of Single-Level Indexes

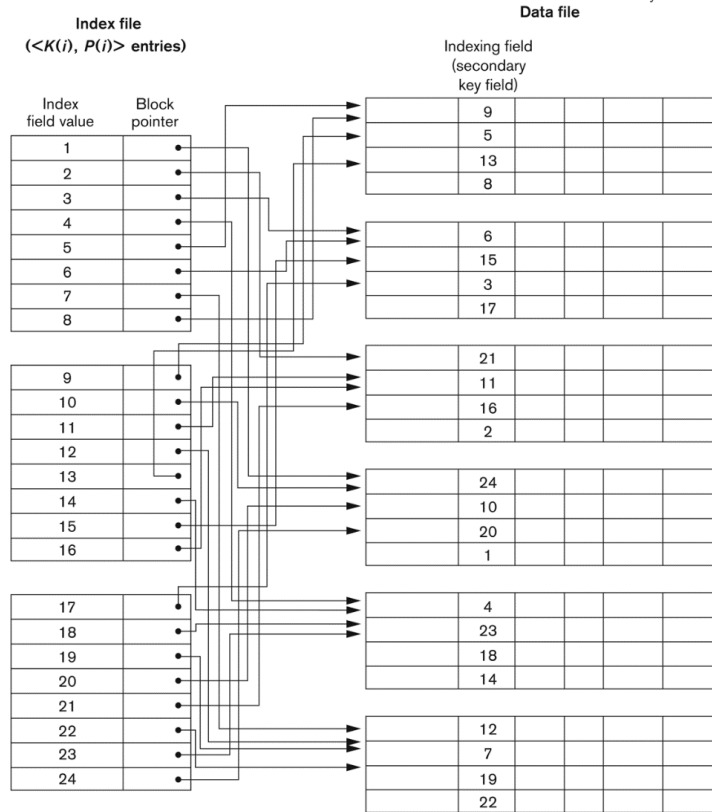
## ■ Secondary Index

- A secondary index provides a secondary means of accessing a file for which some primary access already exists.
- The secondary index may be on a field which is a candidate key and has a unique value in every record, or a non-key with duplicate values.
- The index is an ordered file with two fields.
  - The first field is of the same data type as some **non-ordering field** of the data file that is an indexing field.
  - The second field is either a **block** pointer or a record pointer.
  - There can be *many* secondary indexes (and hence, indexing fields) for the same file.
- Includes one entry *for each record* in the data file; hence, it is a *dense index*

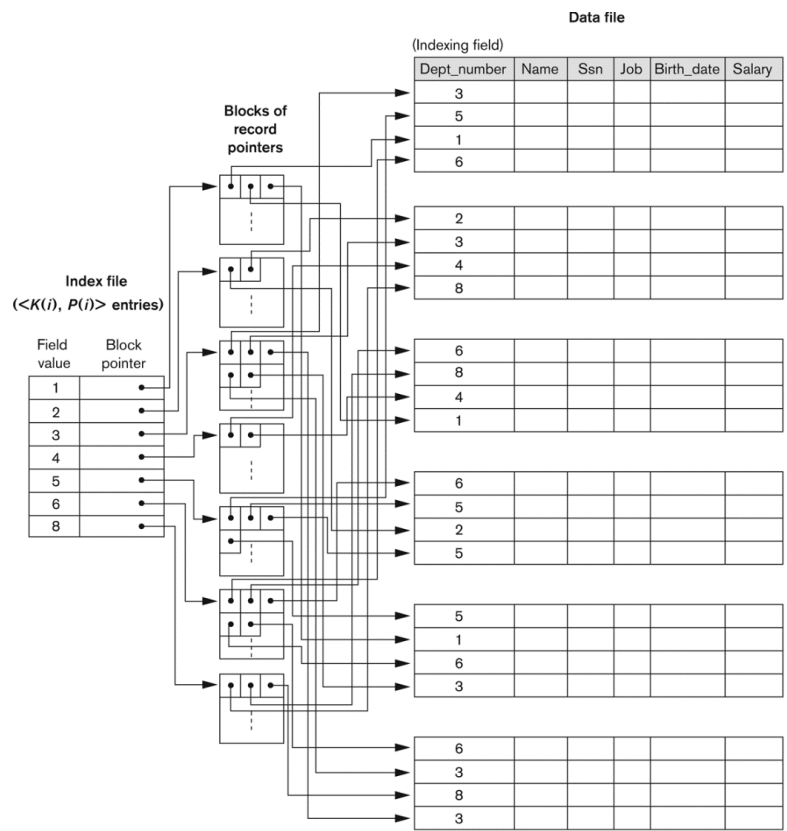
# Example of a Dense Secondary Index

**Figure 14.4**

A dense secondary index (with block pointers) on a nonordering key field of a file.



# An Example of a Secondary Index



**Figure 14.5**  
A secondary index (with record pointers) on a nonkey field implemented using one level of indirection so that index entries are of fixed length and have unique field values.

# Properties of Index Types

**TABLE 14.2 PROPERTIES OF INDEX TYPES**

<b>TYPE OF INDEX</b>	<b>NUMBER OF (FIRST-LEVEL) INDEX ENTRIES</b>	<b>DENSE OR NONDENSE</b>	<b>BLOCK ANCHORING ON THE DATA FILE</b>
Primary	Number of blocks in data file	Nondense	Yes
Clustering	Number of distinct index field values	Nondense	Yes/no <sup>a</sup>
Secondary (key)	Number of records in data file	Dense	No
Secondary (nonkey)	Number of records <sup>b</sup> or Number of distinct index field values <sup>c</sup>	Dense or Nondense	No

<sup>a</sup>Yes if every distinct value of the ordering field starts a new block; no otherwise.

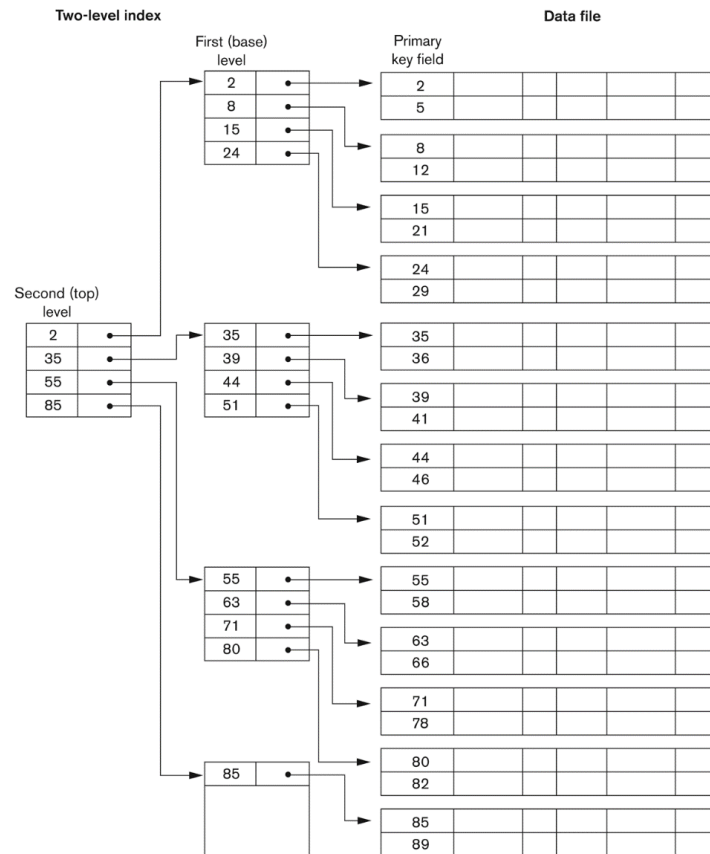
<sup>b</sup>For option 1.

<sup>c</sup>For options 2 and 3.

# Multi-Level Indexes

- Because a single-level index is an ordered file, we can create a primary index *to the index itself*;
  - In this case, the original index file is called the *first-level index* and the index to the index is called the *second-level index*.
- We can repeat the process, creating a third, fourth, ..., top level until all entries of the *top level* fit in one disk block
- A multi-level index can be created for any type of first-level index (primary, secondary, clustering) as long as the first-level index consists of *more than one* disk block

# A Two-level Primary Index



**Figure 14.6**

A two-level primary index resembling ISAM (Index Sequential Access Method) organization.

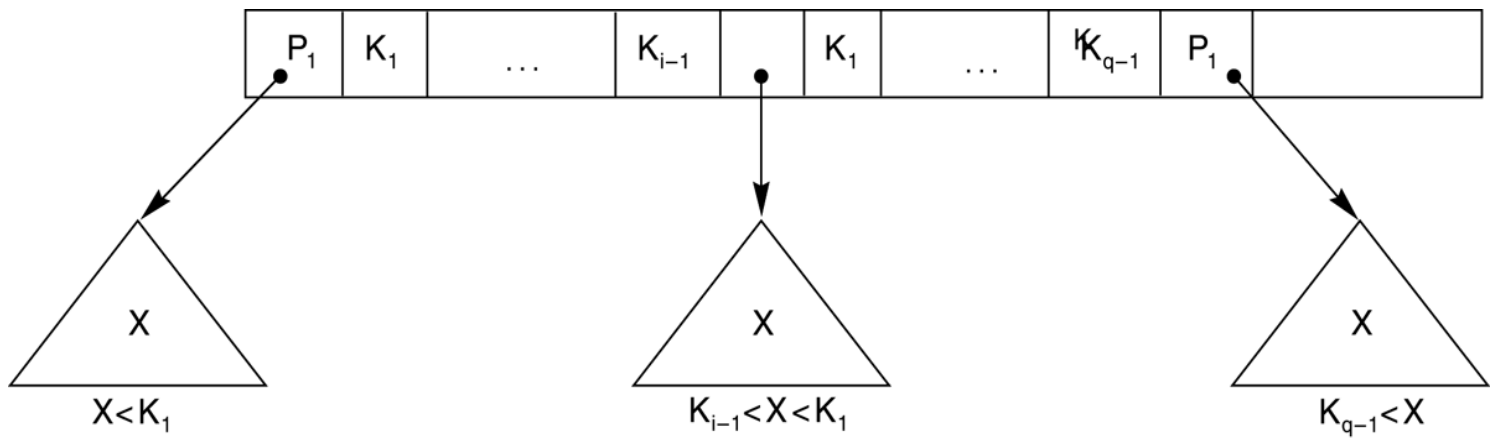


# Multi-Level Indexes

- Such a multi-level index is a form of *search tree*
  - However, insertion and deletion of new index entries is a severe problem because every level of the index is an *ordered file*.

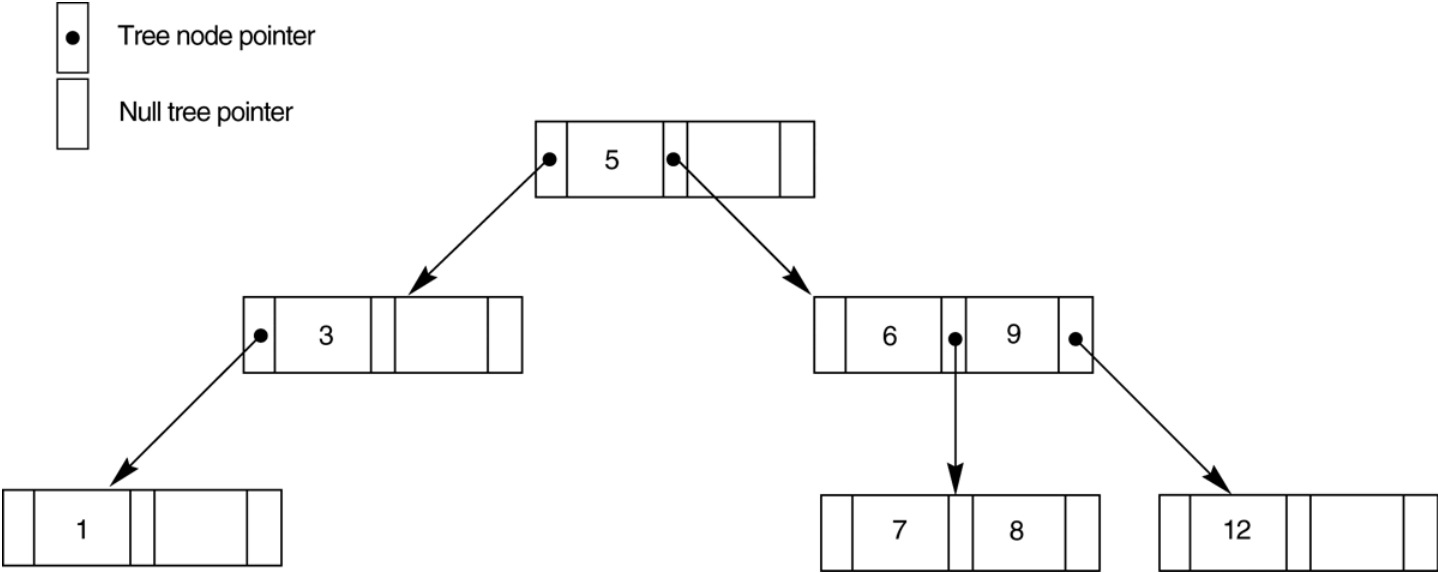
# A Node in a Search Tree with Pointers to Subtrees below It

## ■ FIGURE 14.8



# FIGURE 14.9

## A search tree of order $p = 3$ .



# Dynamic Multilevel Indexes Using B-Trees and B+-Trees

- Most multi-level indexes use B-tree or B+-tree data structures because of the insertion and deletion problem
  - This leaves space in each tree node (disk block) to allow for new index entries
- These data structures are variations of search trees that allow efficient insertion and deletion of new search values.
- In B-Tree and B+-Tree data structures, each node corresponds to a disk block
- Each node is kept between half-full and completely full

# Dynamic Multilevel Indexes Using B-Trees and B+-Trees (contd.)

- An insertion into a node that is not full is quite efficient
  - If a node is full the insertion causes a split into two nodes
- Splitting may propagate to other tree levels
- A deletion is quite efficient if a node does not become less than half full
- If a deletion causes a node to become less than half full, it must be merged with neighboring nodes

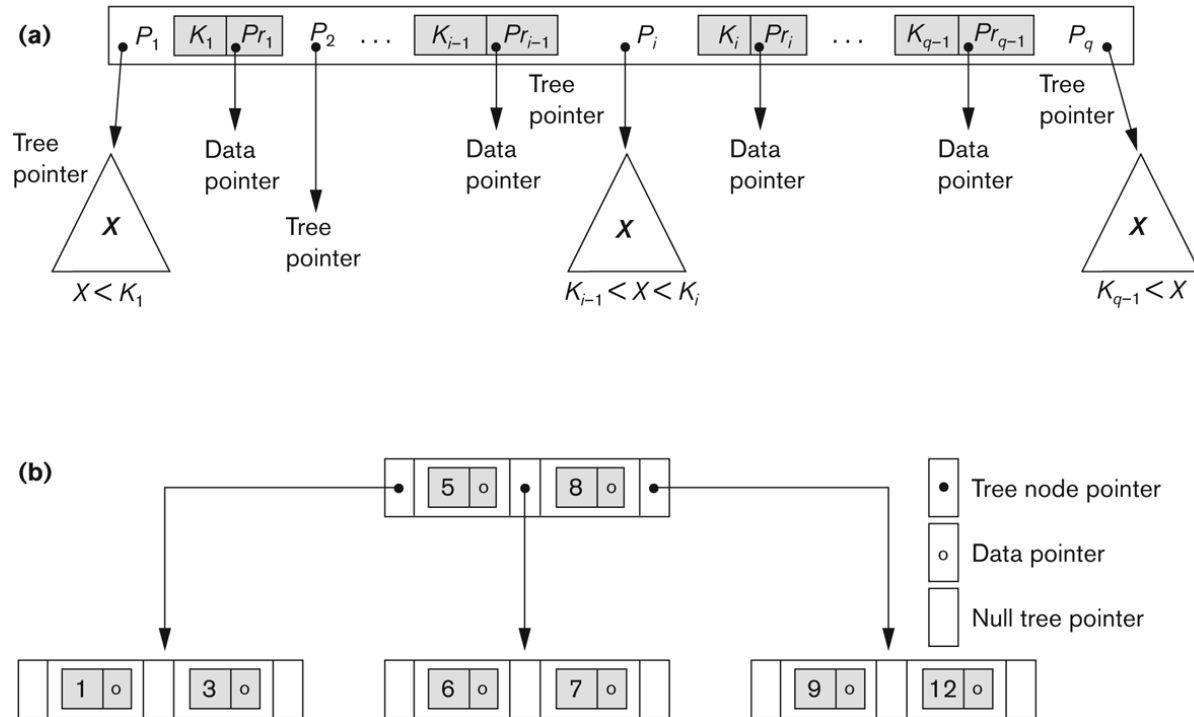
# Difference between B-tree and B+-tree

- In a B-tree, pointers to data records exist at all levels of the tree
- In a B+-tree, all pointers to data records exists at the leaf-level nodes
- A B+-tree can have less levels (or higher capacity of search values) than the corresponding B-tree

# B-tree Structures

**Figure 14.10**

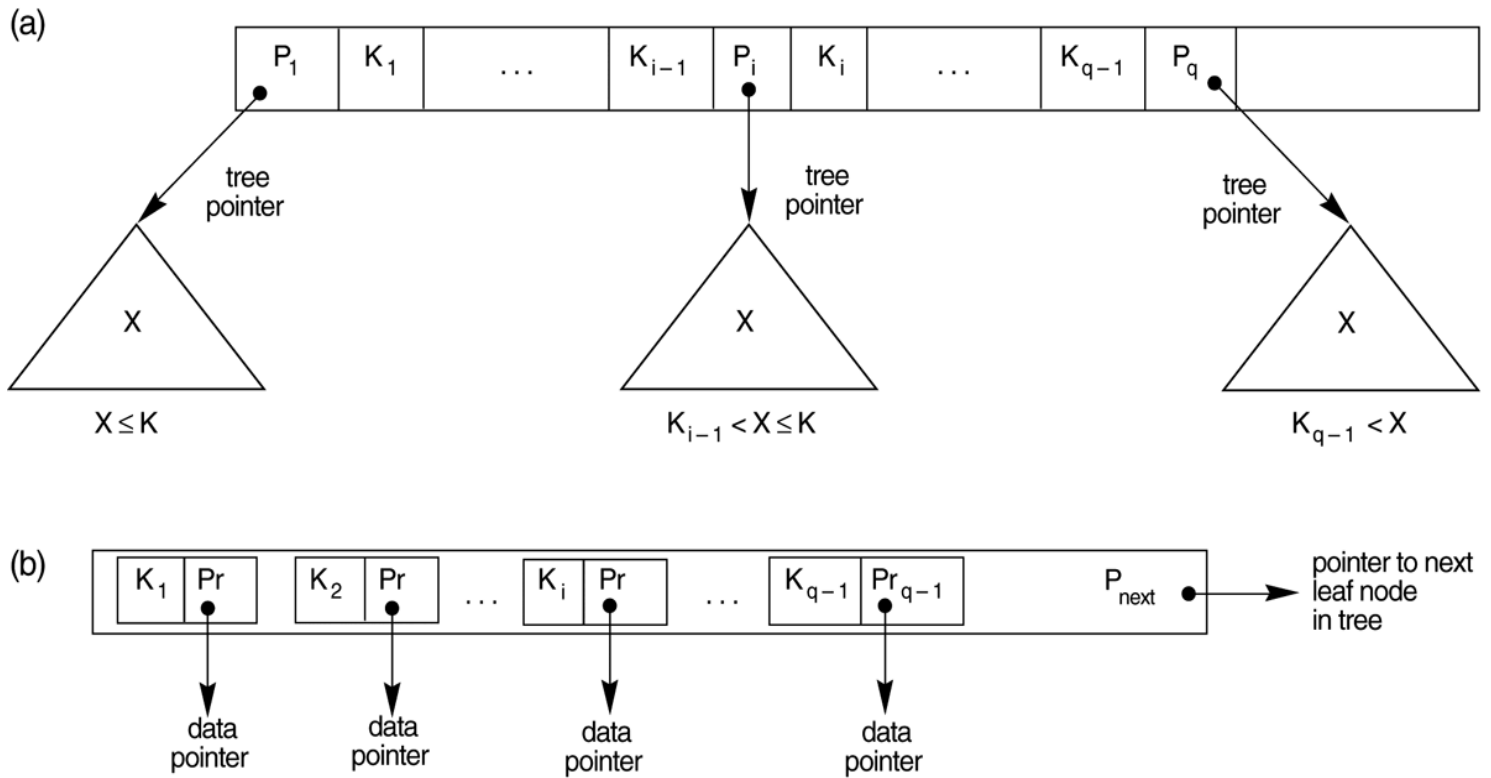
B-Tree structures. (a) A node in a B-tree with  $q - 1$  search values. (b) A B-tree of order  $p = 3$ . The values were inserted in the order 8, 5, 1, 7, 3, 12, 9, 6.



# The Nodes of a B+-tree

- FIGURE 14.11 The nodes of a B+-tree

- (a) Internal node of a B+-tree with  $q - 1$  search values.
- (b) Leaf node of a B+-tree with  $q - 1$  search values and  $q - 1$  data pointers.



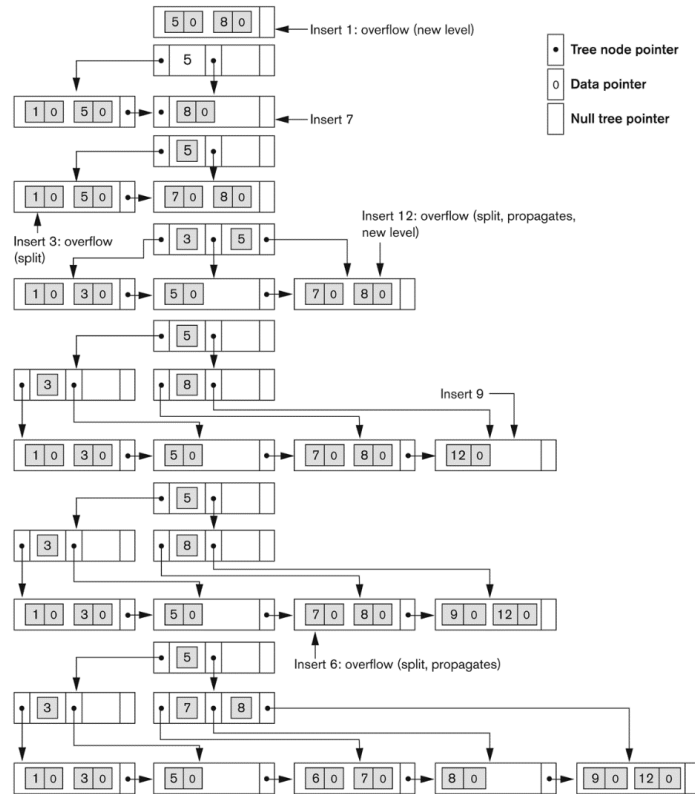


# An Example of an Insertion in a B+-tree

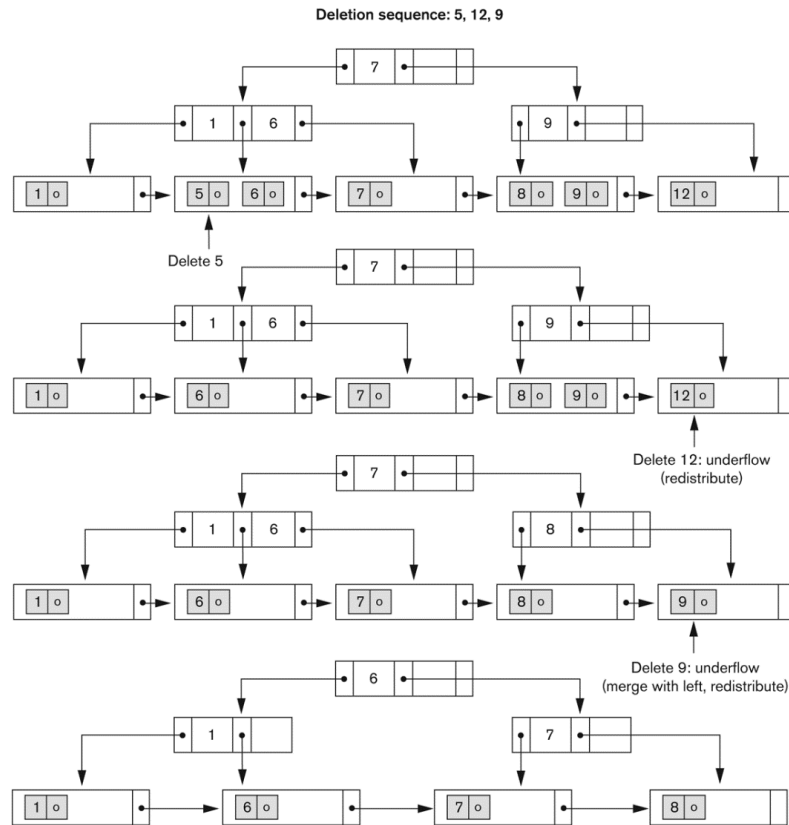
**Figure 14.12**

An example of insertion in a B+-tree with  $p = 3$  and  $p_{leaf} = 2$ .

Insertion sequence: 8, 5, 1, 7, 3, 12, 9, 6



# An Example of a Deletion in a B+-tree



**Figure 14.13**

An example of deletion from a B+-tree.

# Example

## Indexes as Access Paths (contd.)

- Example: Given the following data file EMPLOYEE(NAME, SSN, ADDRESS, JOB, SAL, ... )
- Suppose that:
  - record size  $R=150$  bytes      block size  $B=512$  bytes       $r=30000$  records
- Then, we get:
  - blocking factor  $Bfr = B \div R = 512 \div 150 = 3$  records/block
  - number of file blocks  $b = (r/Bfr) = (30000/3) = 10000$  blocks
- For an index on the SSN field, assume the field size  $V_{SSN}=9$  bytes, assume the record pointer size  $P_R=7$  bytes. Then:
  - index entry size  $R_i = (V_{SSN} + P_R) = (9+7) = 16$  bytes
  - index blocking factor  $Bfr_i = B \div R_i = 512 \div 16 = 32$  entries/block
  - number of index blocks  $b_i = (r/Bfr_i) = (30000/32) = 938$  blocks
  - binary search needs  $\log_2 b_i = \log_2 938 = 10$  block accesses
  - This is compared to an average linear search cost of:
    - $(b/2) = 30000/2 = 15000$  block accesses
  - If the file records are ordered, the binary search cost would be:
    - $\log_2 b = \log_2 30000 = 15$  block accesses

# B Tree example

- Suppose the search field is  $V = 9$  bytes long, the disk block size is  $B = 512$  bytes, a record (data) pointer is  $P_r = 7$  bytes, and a block pointer is  $P_b = 6$  bytes.
- Each B-treenode can have *at most*  $p$  tree pointers,  $p - 1$  data pointers, and  $p - 1$  search key field values (see Figure 14.10a). These must fit into a single disk block if each B-tree node is to correspond to a disk block. Hence, we must have:
$$(p * P_b) + ((p - 1) * (P_r + V)) \leq B$$
$$(p * 6) + ((p - 1) * (7 + 9)) \leq 512$$
$$(22 * p) \leq 528$$
- We can choose  $p$  to be a large value that satisfies the above inequality, which gives  $p = 23$
- ( $p = 24$  is not chosen because of the reasons given next).

# B+ Tree Example

- To calculate the order  $p$  of a B-tree, suppose that the search key field is  $V = 9$  bytes long, the block size is  $B = 512$  bytes, a record pointer is  $P_r = 7$  bytes, and a block pointer is  $P_b = 6$  bytes, as in Example 4. An internal node of the B-tree can have up to  $p$  tree pointers and  $p - 1$  search field values; these must fit into a single block. Hence,
- we have:
$$(p * P) + ((p - 1) * V) \leq B$$
$$(p * 6) + ((p - 1) * 9) \leq 512$$
$$(15 * p) \leq 521$$
- We can choose  $p$  to be the largest value satisfying the above inequality, which gives  $p = 34$ . This is larger than the value of 23 for the B-tree, resulting in a larger fan-out and more entries in each internal node of a B+-tree than in the corresponding B-tree.
- The leaf nodes of the B+-tree will have the same number of values and pointers, except that the pointers are data pointers and a next pointer.
- Hence, the order  $P_{leaf}$  for the leaf nodes can be calculated as follows:
$$(P_{leaf} * (P_r + V)) + P_b \leq B$$
$$(P_{leaf} * (7 + 9)) + 6 \leq 512$$
$$(16 * P_{leaf}) \leq 506$$
- It follows that each leaf node can hold up to  $P_{leaf} = 31$  key value/data pointer combinations,
- assuming that the data pointers are record pointers.

# Summary

- Types of Single-level Ordered Indexes
  - Primary Indexes
  - Clustering Indexes
  - Secondary Indexes
- Multilevel Indexes
- Dynamic Multilevel Indexes Using B-Trees and B+-Trees
- Indexes on Multiple Keys