Linear Model Assumptions

Serena Peterson

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```
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
library(stats)
library(lmtest)
## Warning: package 'lmtest' was built under R version 4.3.2
## Loading required package: zoo
## Warning: package 'zoo' was built under R version 4.3.2
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
```

Check Assumptions of Linear Models

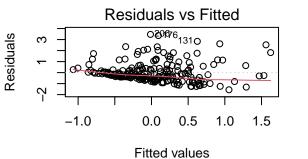
```
# Load data
alldata1 <- read.csv(file = file.choose())
alldata2 <- read.csv(file = file.choose())

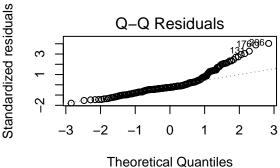
#Remove indexing columns
alldata1 <- alldata1 %>% select(-c(X, X.1))
alldata2 <- alldata2 %>% select(-c(X, X.1))

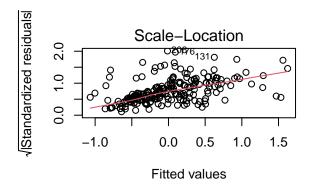
#Standardize data
alldata1 <- alldata1 %>% mutate_all(~(scale(.) %>% as.vector))
alldata2 <- alldata2 %>% mutate_all(~(scale(.) %>% as.vector))
```

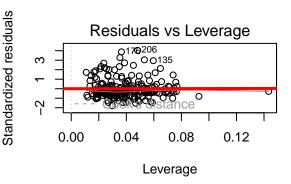
Data from Approach 1

```
#Build models
model1 <- lm(Avg.Loss ~ .,</pre>
              data = alldata1 %>% select(-c(RMSE,MAE)))
model2 \leftarrow lm(MAE \sim .,
              data = alldata1 %>% select(-c(Avg.Loss,RMSE)))
model3 <- lm(RMSE ~ .,</pre>
              data = alldata1 %>% select(-c(Avg.Loss,MAE)))
#Diagnostic Plots
par(mfrow=c(2,2))
plot(model1)
abline(model1, lwd=3, col='red')
## Warning in abline(model1, lwd = 3, col = "red"): only using the first two of 9
## regression coefficients
```



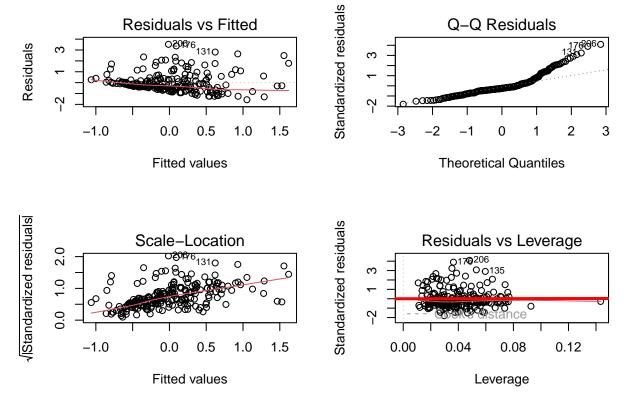






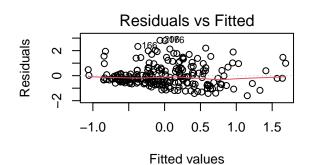
```
par(mfrow=c(2,2))
plot(model2)
abline(model2, lwd=3, col='red')
```

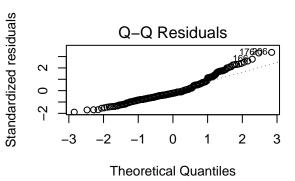
Warning in abline(model2, lwd = 3, col = "red"): only using the first two of 9 ## regression coefficients

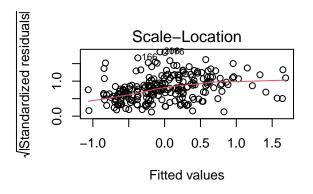


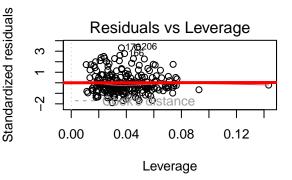
```
par(mfrow=c(2,2))
plot(model3)
abline(model3, lwd=3, col='red')
```

Warning in abline(model3, lwd = 3, col = "red"): only using the first two of 9
regression coefficients









#Normality

shapiro.test(model1\$res)

```
##
## Shapiro-Wilk normality test
##
## data: model1$res
## W = 0.87021, p-value = 6.385e-13
shapiro.test(model2$res)

##
## Shapiro-Wilk normality test
##
## data: model2$res
## W = 0.87088, p-value = 6.964e-13
shapiro.test(model3$res)
```

##
Shapiro-Wilk normality test
##
data: model3\$res
W = 0.93141, p-value = 9.522e-09
Equal Variance

##

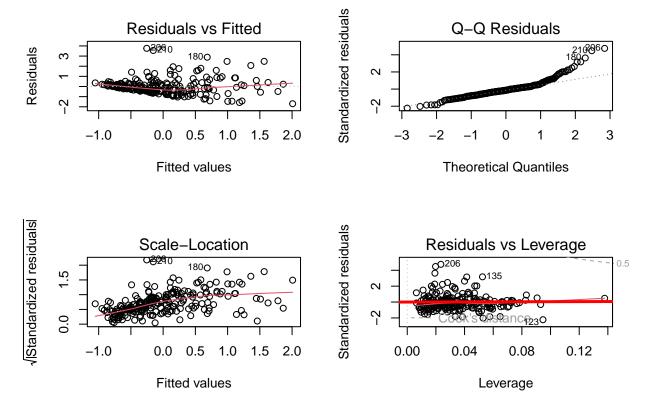
bptest(model1)

```
## studentized Breusch-Pagan test
##
## data: model1
## BP = 26.189, df = 8, p-value = 0.0009748
bptest(model2)
##
  studentized Breusch-Pagan test
##
##
## data: model2
## BP = 25.887, df = 8, p-value = 0.001098
bptest(model3)
##
   studentized Breusch-Pagan test
##
## data: model3
## BP = 18.844, df = 8, p-value = 0.01572
#Independence
dwtest(model1)
## Durbin-Watson test
##
## data: model1
## DW = 1.3753, p-value = 8.354e-07
## alternative hypothesis: true autocorrelation is greater than 0
dwtest(model2)
##
## Durbin-Watson test
## data: model2
## DW = 1.3722, p-value = 7.443e-07
## alternative hypothesis: true autocorrelation is greater than 0
dwtest(model3)
##
## Durbin-Watson test
##
## data: model3
## DW = 1.226, p-value = 1.634e-09
\#\# alternative hypothesis: true autocorrelation is greater than 0
Data from Approach 2
```

```
#Observations
par(mfrow=c(2,2))
plot(model1)
abline(model1, lwd=3, col='red')
## Warning in abline(model1, lwd = 3, col = "red"): only using the first two of 8
## regression coefficients
                                                         Standardized residuals
                                                                             Q-Q Residuals
                   Residuals vs Fitted
Residuals
      က
                                                               ^{\circ}
      7
           -1.0
                        0.0
                            0.5
                                  1.0
                                         1.5
                                               2.0
                                                                                                   2
                                                                                                          3
                                                                          -2
                        Fitted values
                                                                            Theoretical Quantiles
/|Standardized residuals
                                                         Standardized residuals
                                                                         Residuals vs Leverage
                     Scale-Location
      2.0
                                                                                                            0.5
                                                0
      0.0 1.0
           -1.0
                                               2.0
                                                                   0.00
                                                                                                  0.12
                        0.0
                             0.5
                                   1.0
                                         1.5
                                                                             0.04
                                                                                        0.08
                        Fitted values
                                                                                  Leverage
par(mfrow=c(2,2))
```

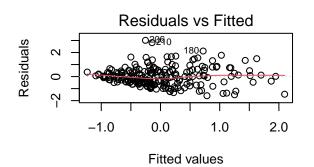
```
par(mfrow=c(2,2))
plot(model2)
abline(model2, lwd=3, col='red')
```

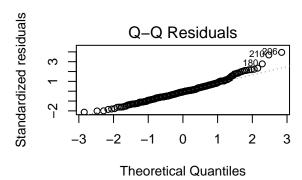
Warning in abline(model2, lwd = 3, col = "red"): only using the first two of 8
regression coefficients

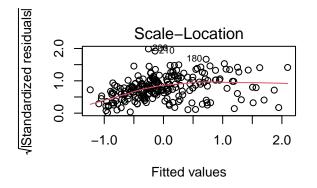


```
par(mfrow=c(2,2))
plot(model3)
abline(model3, lwd=3, col='red')
```

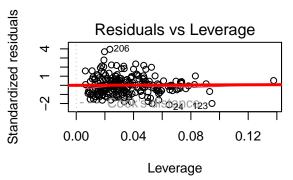
Warning in abline(model3, lwd = 3, col = "red"): only using the first two of 8
regression coefficients







Equal Variance
bptest(model1)



```
#Normality
shapiro.test(model1$res)
##
##
   Shapiro-Wilk normality test
##
## data: model1$res
## W = 0.88814, p-value = 7.257e-12
shapiro.test(model2$res)
##
   Shapiro-Wilk normality test
##
##
## data: model2$res
## W = 0.88797, p-value = 7.086e-12
shapiro.test(model3$res)
##
   Shapiro-Wilk normality test
##
##
## data: model3$res
## W = 0.96842, p-value = 6.535e-05
```

```
##
## studentized Breusch-Pagan test
## data: model1
## BP = 17.894, df = 7, p-value = 0.01246
bptest(model2)
##
## studentized Breusch-Pagan test
##
## data: model2
## BP = 17.568, df = 7, p-value = 0.01408
bptest(model3)
##
## studentized Breusch-Pagan test
##
## data: model3
## BP = 18.029, df = 7, p-value = 0.01184
#Independence
dwtest(model1)
## Durbin-Watson test
## data: model1
## DW = 1.6799, p-value = 0.006268
## alternative hypothesis: true autocorrelation is greater than 0
dwtest(model2)
## Durbin-Watson test
## data: model2
## DW = 1.6746, p-value = 0.005596
## alternative hypothesis: true autocorrelation is greater than 0
dwtest(model3)
## Durbin-Watson test
##
## data: model3
## DW = 1.4863, p-value = 3.797e-05
## alternative hypothesis: true autocorrelation is greater than 0
```