

1. Worst case asymptotic running time analysis:

	isEmpty	size	Insert	findMin	deleteMin
BinaryHeap	$O(1)$	$O(1)$	$O(\log(n))$	$O(1)$	$O(\log(n))$
ThreeHeap	$O(1)$	$O(1)$	$O(\log(n))$	$O(1)$	$O(\log(n))$
MyPQ	$O(1)$	$O(1)$	$O(\log(n))$	$O(1)$	$O(\log(n))$

2. Run-time values

Timing for Binary Heap (in nanoseconds)

	Insert	delete
10	923	2256
100	935	3056
500	648	3245
1000	824	2408
10,000	654	3062

Timing for Three Heap (in nanoseconds)

	Insert	delete
10	956	4023
100	623	3408
500	453	4520
1000	635	4301
10,000	635	3652

Timing for MyPQ (in nanoseconds)

	Insert	delete
10	853	4268
100	346	4654
500	836	3200
1000	990	4620
10,000	982	4561

3.
 - a. The asymptotic analysis wasn't very useful in predicting the run time for my implementations.
 - b. I think the way java compiles and runs programs cause serious variations in timing when the run time is on the order of a few thousand nanoseconds. Also, increase in size of n isn't very significant due to the speed at which the computer is capable of navigating the array.
 - c. In theory, however, the binary tree should be the fastest. Operations of multiplication by 2 (simple bit shifting operation) makes array navigation the fastest in the binary tree. I think in all cases, the binary tree would out-perform the other two implementations.

4. To test my implementations, I built a tester program that would test sizes of 1 – 10. Inputting random values into my Priority Queue, and printing them back out, making sure they are in sorted order.

5. a.

	Child nodes at:
Binary	$i*2$ and $i*2+1$
3-Heap	$i*3-1$ and $i*3$ and $i*3+1$
4-Heap	$i*4-2$ and $i*4-1$ and $i*4$ and $i*4+1$
5-Heap	$i*5-3$ and $i*5-2$ and $i*5-1$ and $i*5$ and $i*5+1$

b.

The left-most child for any heap of order-d would be:

$i*d - d + 2 = \text{child index}$, for parent index: “i”, and number of children “d”