

# New Actuators Types

## Mechatronics, Lecture 12

by Sergei Savin

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- Variable Stiffness Actuators
- Twisted Spring Actuators
- Tensegrity structures

# Variable Stiffness Actuators

# VARIABLE STIFFNESS ACTUATOR

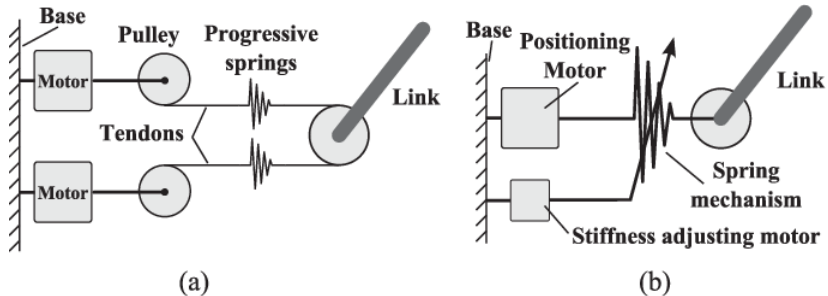


Figure 1: Wolf, Sebastian, et al. "Variable stiffness actuators: Review on design and components." IEEE/ASME transactions on mechatronics 21.5 (2015): 2418-2430.

Different types of Variable Stiffness Actuators (VSA) have different models. Qbmove actuator is described by the following one:

$$\begin{cases} L_1 \dot{I}_1 + R_1 I_1 + C_{w,1} \dot{\theta}_1 = u_1 \\ L_2 \dot{I}_2 + R_2 I_2 + C_{w,2} \dot{\theta}_2 = u_2 \\ J_1 \ddot{\theta}_1 + \mu_1 \dot{\theta}_1 = C_{\tau,1} I_1 - \tau_1 \\ J_2 \ddot{\theta}_2 + \mu_2 \dot{\theta}_2 = C_{\tau,2} I_2 - \tau_2 \\ J \ddot{\varphi} + \mu \dot{\varphi} = \tau_1 + \tau_2 \end{cases} \quad (1)$$

where  $\theta_1, \theta_2$  - orientation of the internal motor shaft, and  $\varphi$  - orientation of the output shaft,  $\tau_1, \tau_2$  - torque produced by elastic elements,  $J, J_1, J_2$  - moment of inertia,  $\mu, \mu_1, \mu_2$  - viscous friction coefficient,  $L, R, C_w, C_\tau, I, u$  are inductance, resistance, back-EMF and torque coefficients, current and input voltage.

The torque produced by elastic elements for Qbmove is given as:

$$\tau_1 = \sigma \sinh(a_1(\theta_1 - \varphi)) \quad (2)$$

$$\tau_2 = \sigma \sinh(a_2(\theta_2 - \varphi)) \quad (3)$$

where  $a_1$  and  $\sigma$  are model constants.

The non-linearity of this model allows us to control the stiffness of the VSA.

Stiffness  $\mathcal{K}$  of an actuator can be defined as a partial derivative of the output torque with respect to the output shaft orientation:

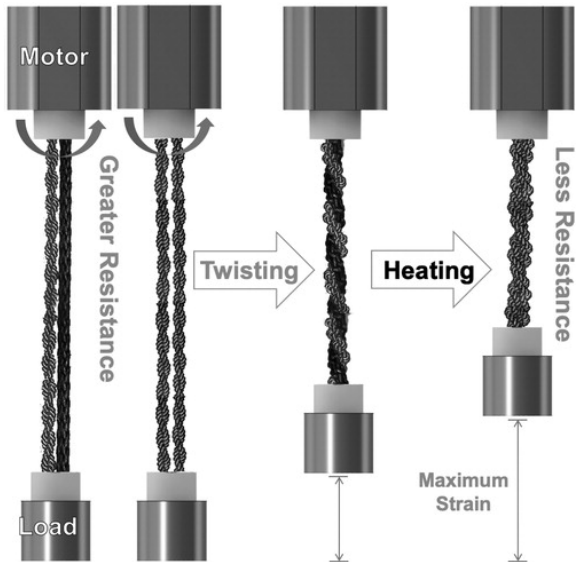
$$\mathcal{K} = \frac{\partial(\tau_1 + \tau_2)}{\partial\varphi} \quad (4)$$

Note that if the torque was linear or affine with respect to  $\varphi$ , then stiffness of such actuator could not be influenced by internal variables  $\theta_i$  or the orientation of the output shaft  $\varphi$ .

# Twisted Spring Actuators



# TWISTED SPRING ACTUATOR, 1



# TWISTED SPRING ACTUATOR, 2

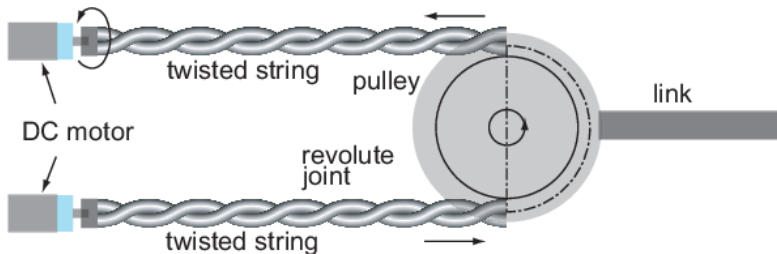
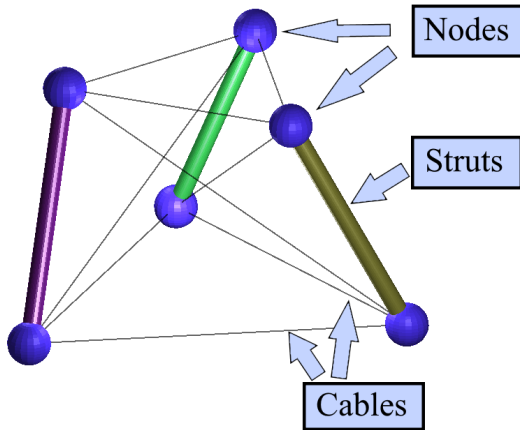


Figure 2: Inoue, T., Miyata, R. and Hirai, S., 2016, October. Force control on antagonistic twist-drive actuator robot. In 2016 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS) (pp. 3830-3835). IEEE.

# Tensegrity structures

# TENSEGRITY STRUCTURES



Note that cables are usually elastic and pre-stressed.

Elastic force acting between nodes  $\mathbf{r}_i$  and  $\mathbf{r}_j$  can be modelled as follows:

$$\mathbf{f}_{ij} = \mu_{ij}(\|\mathbf{r}_i - \mathbf{r}_j\| - \rho_{ij}) \frac{\mathbf{r}_i - \mathbf{r}_j}{\|\mathbf{r}_i - \mathbf{r}_j\|} \quad (5)$$

where  $\mu_{ij}$  - cable stiffness,  $\rho_{ij}$  - undeformed cable length

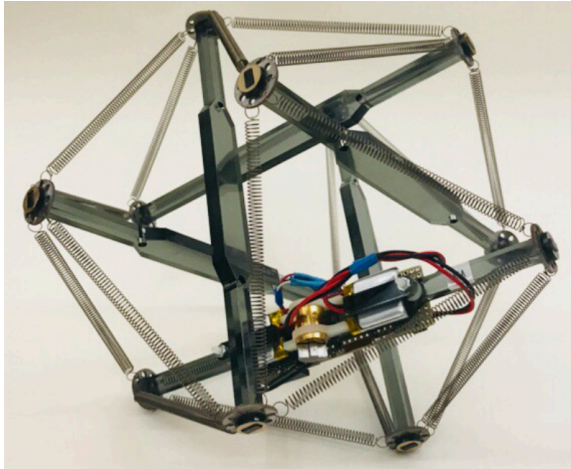


Figure 3: Rieffel, J. and Mouret, J.B., 2018. Adaptive and resilient soft tensegrity robots. *Soft robotics*, 5(3), pp.318-329.

Lecture slides are available via Github, links are on Moodle

You can help improve these slides at:  
[github.com/SergeiSa/Mechatronics-2023](https://github.com/SergeiSa/Mechatronics-2023)

