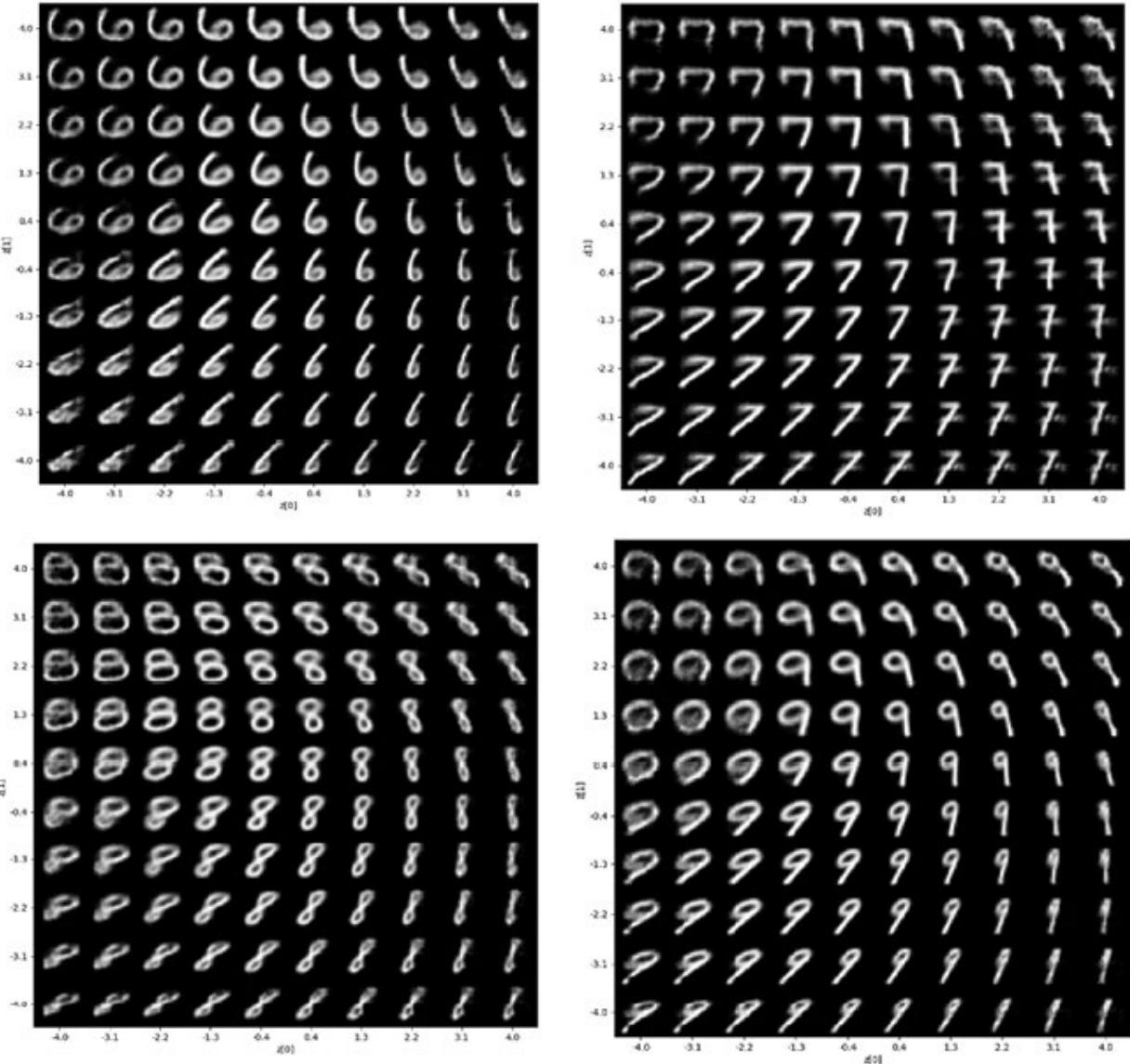
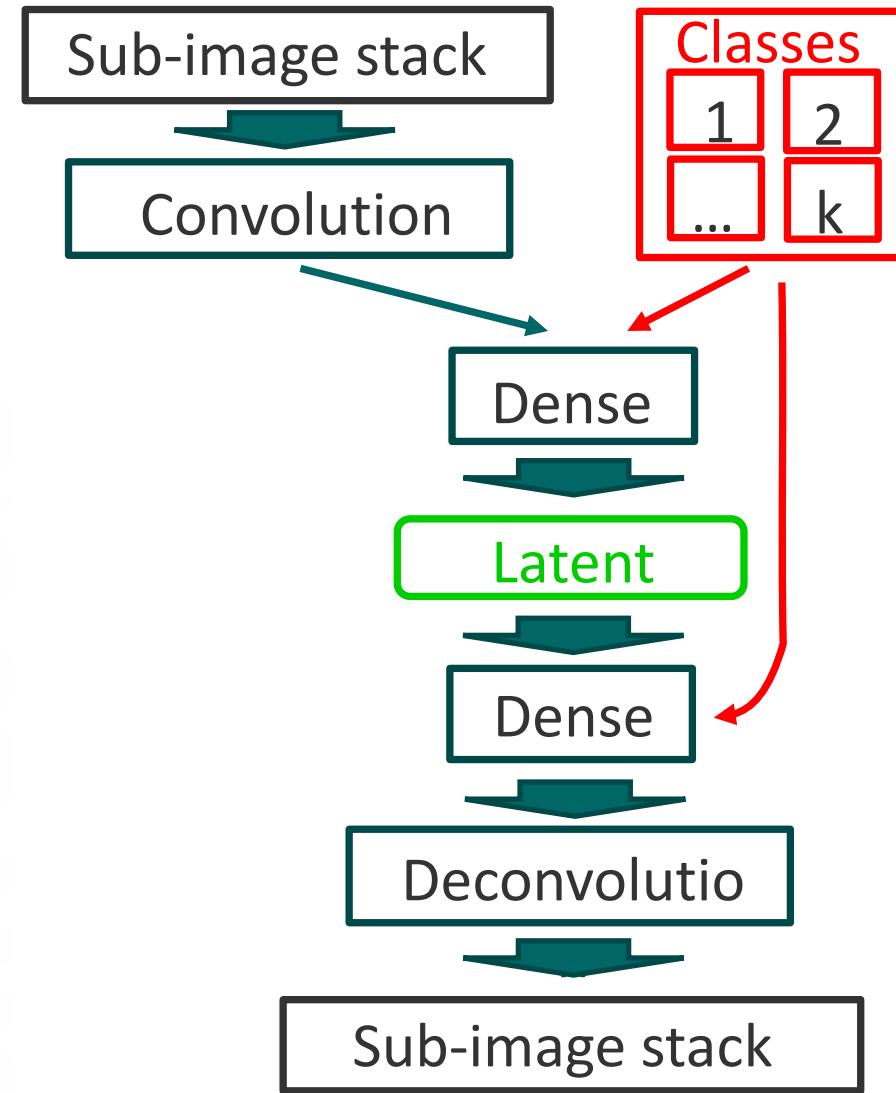


Lecture 31: Invariant Variational Autoencoders

Sergei V. Kalinin

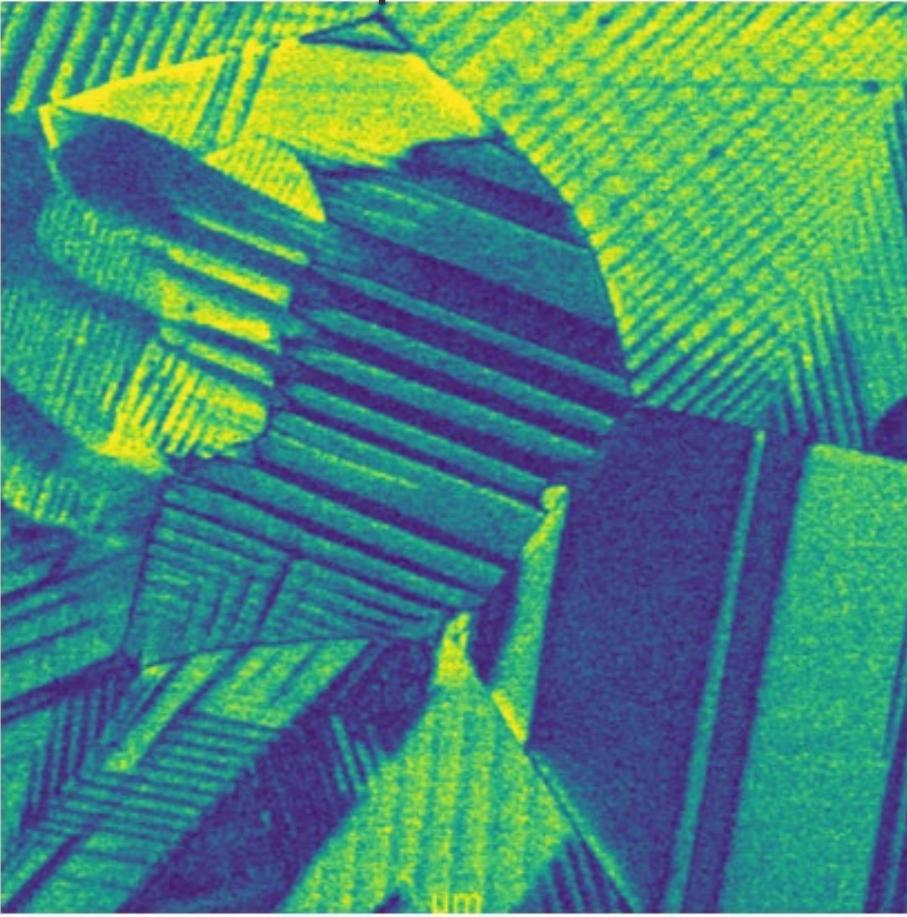
Conditional VAE



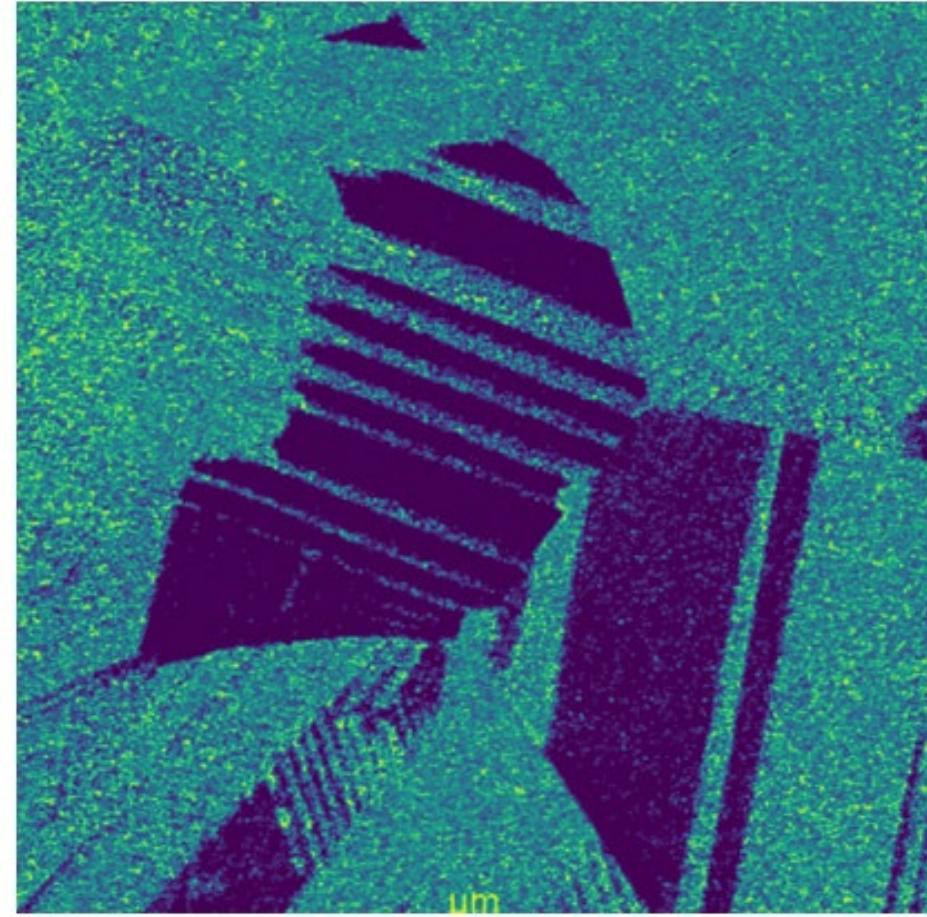
Note the trends in the latent representation for each digit: **disentanglement of the representations**

Ferroelectric domain and domain walls

Amplitude



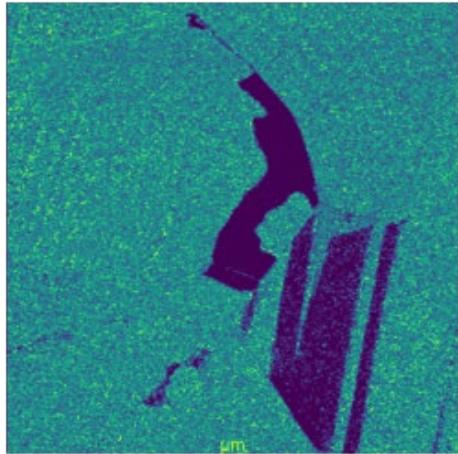
Phase



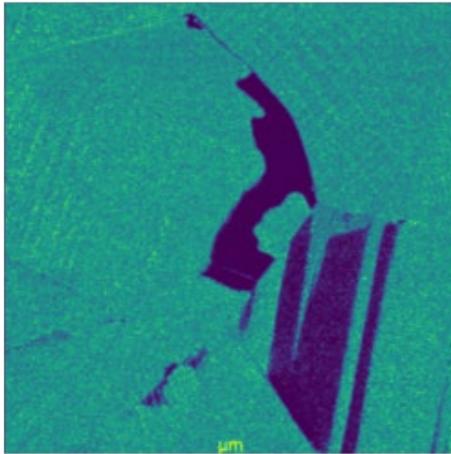
Detecting domain walls

Canny filter

Phase Image

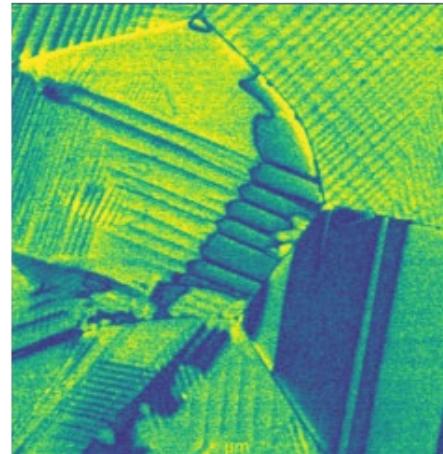


Gaussian Filter

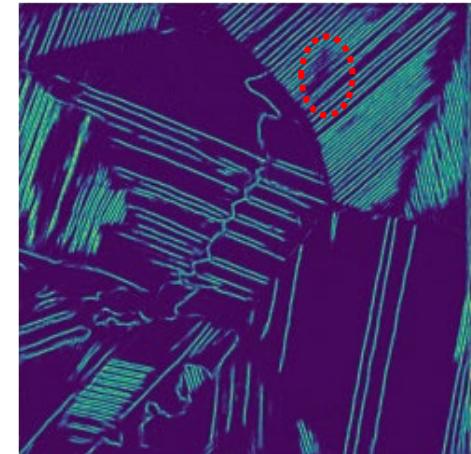


DCNN Prediction

Image



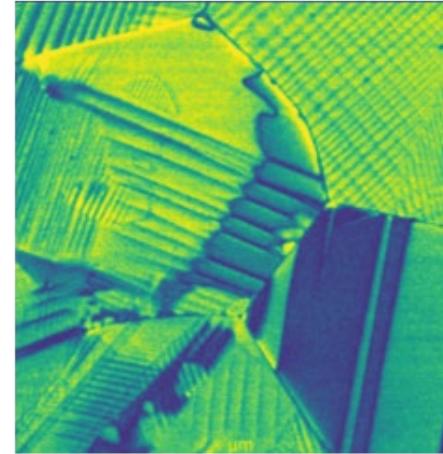
Predicted



Wall by Canny Filter



Gaussian Filter

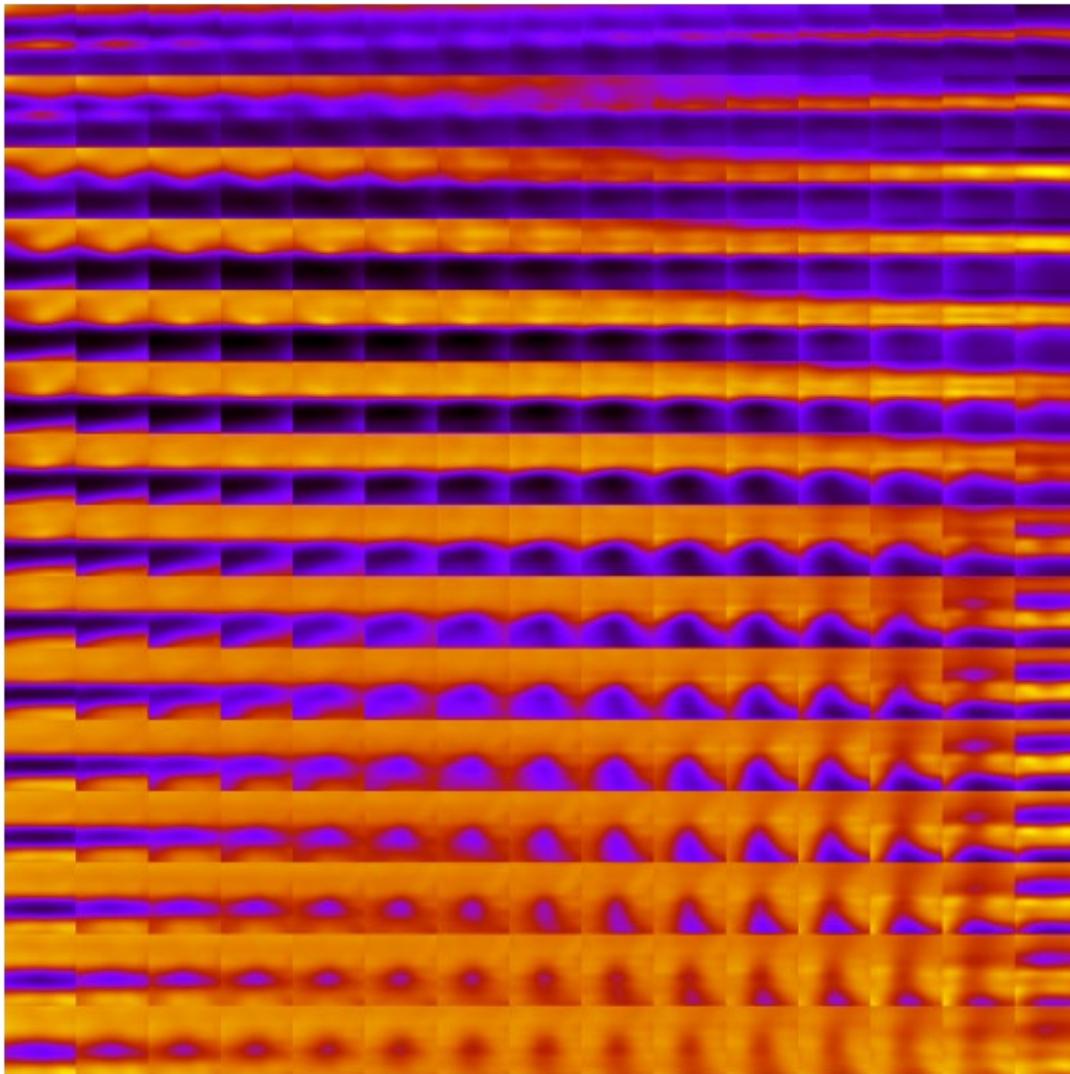


Gaussian Filter and Predicted

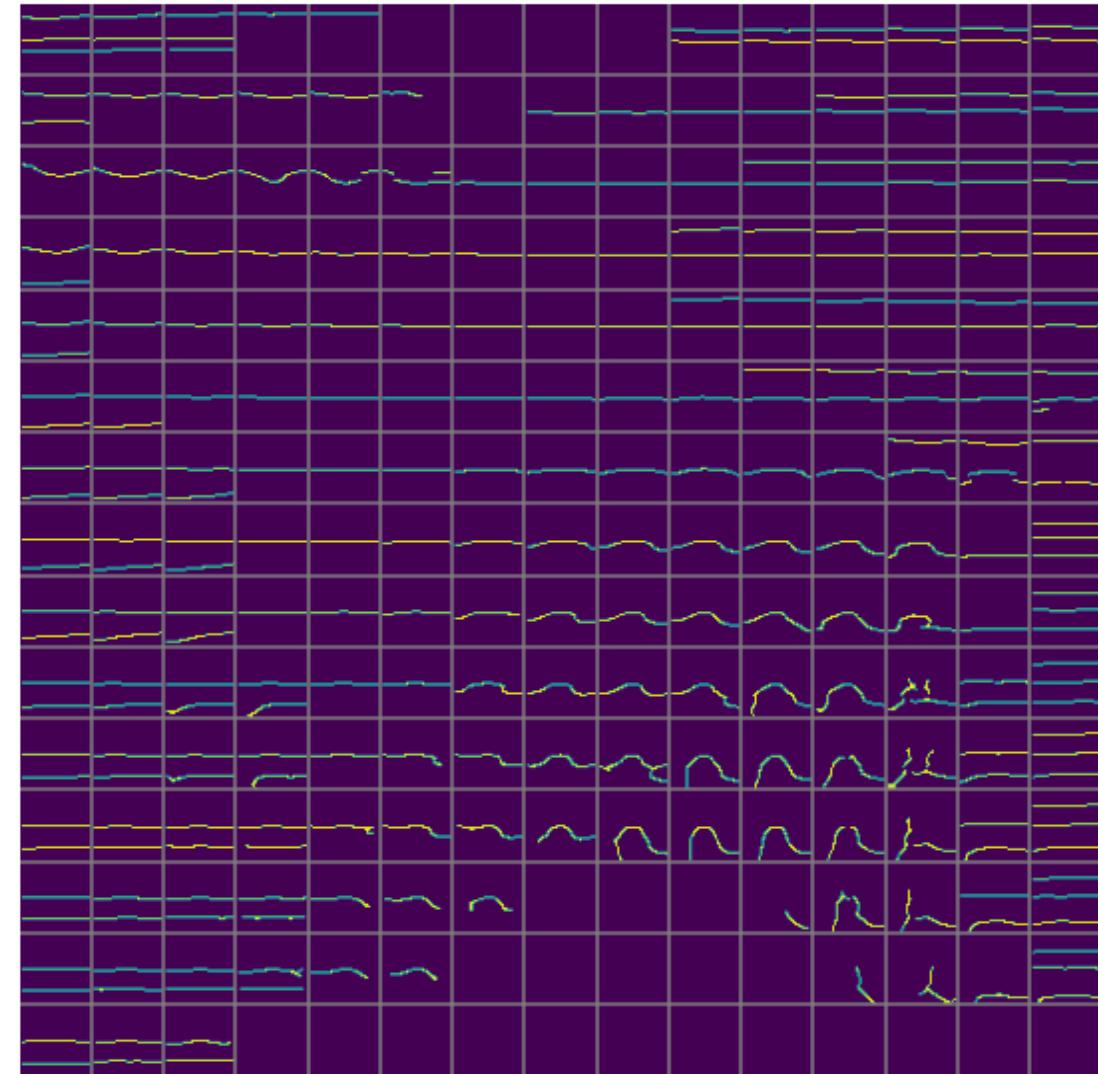


rVAE analysis

Latent Space

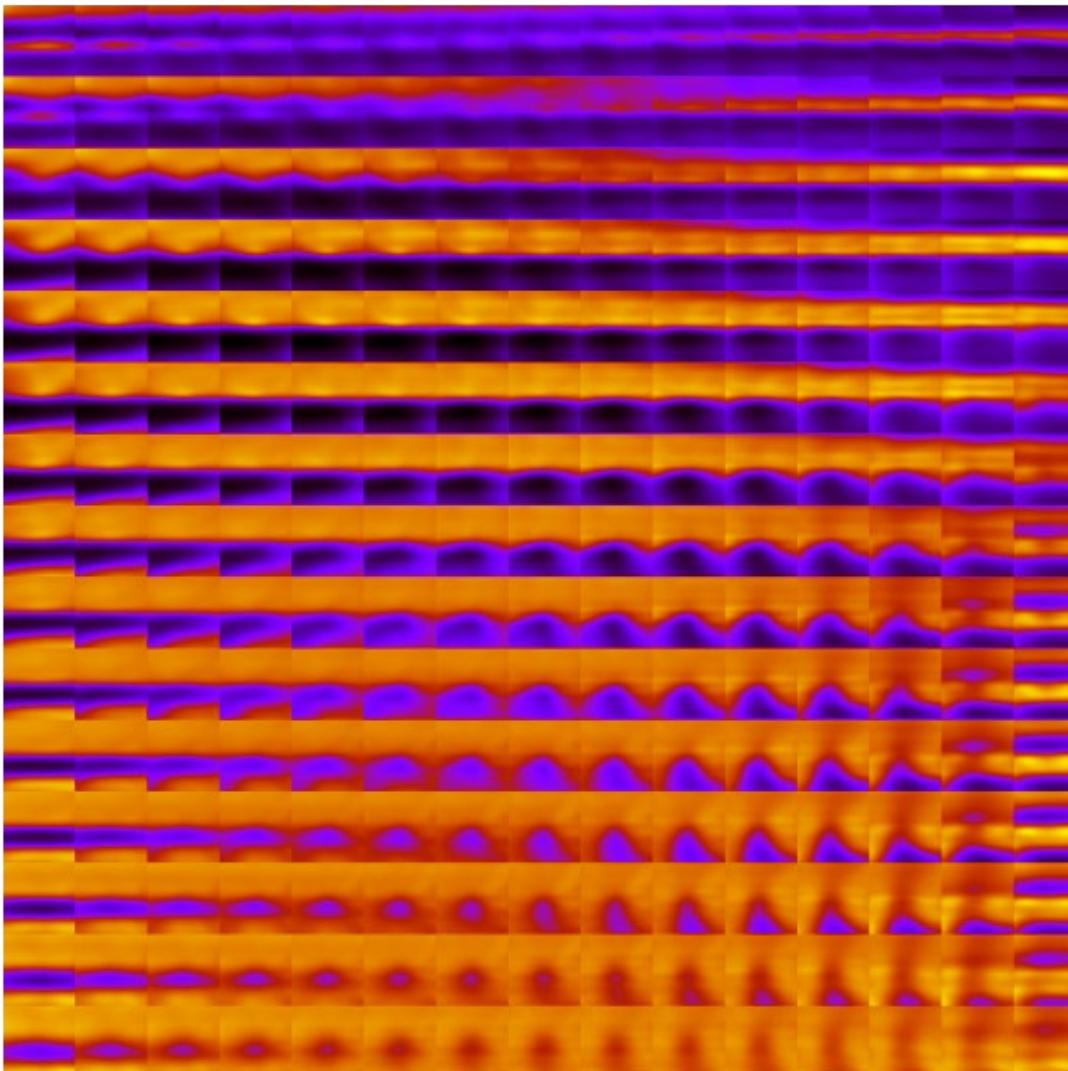


Domain Walls

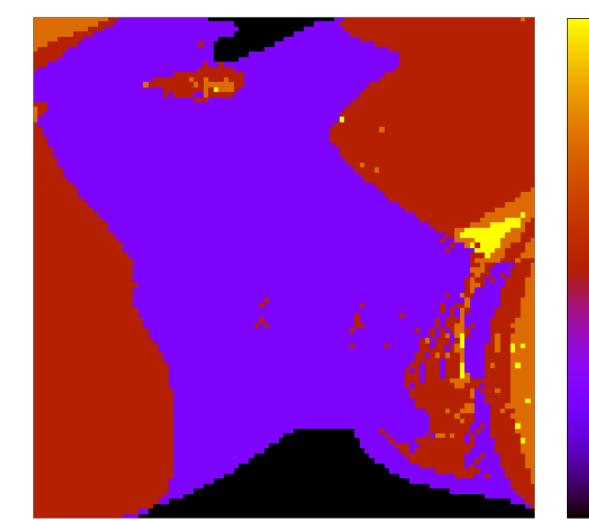


rVAE latent space

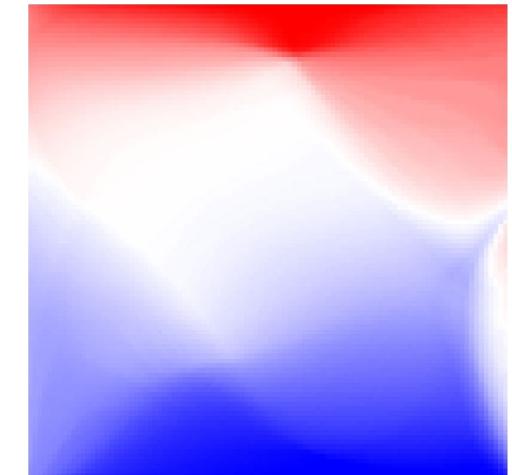
Latent Space



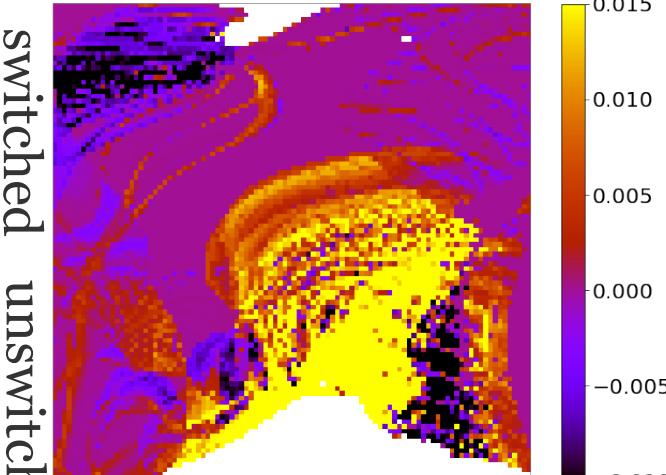
Domain wall count



Switching degree



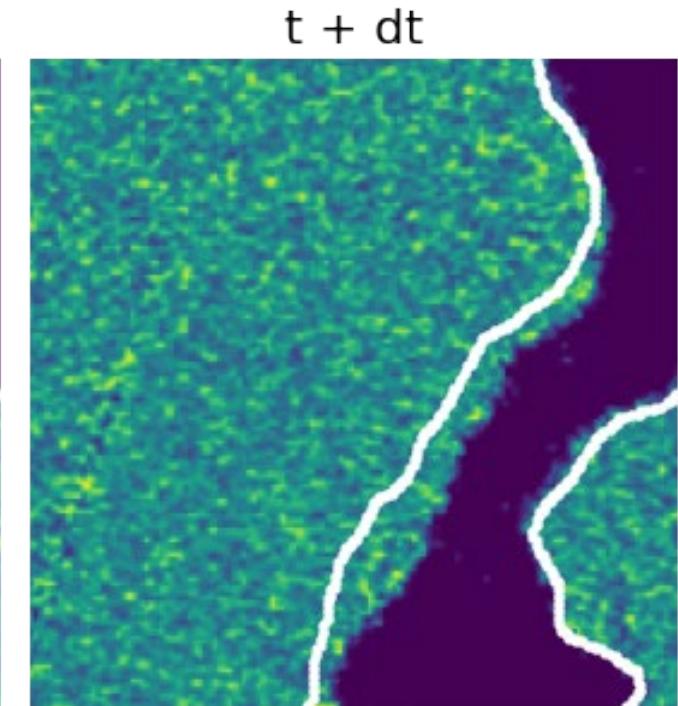
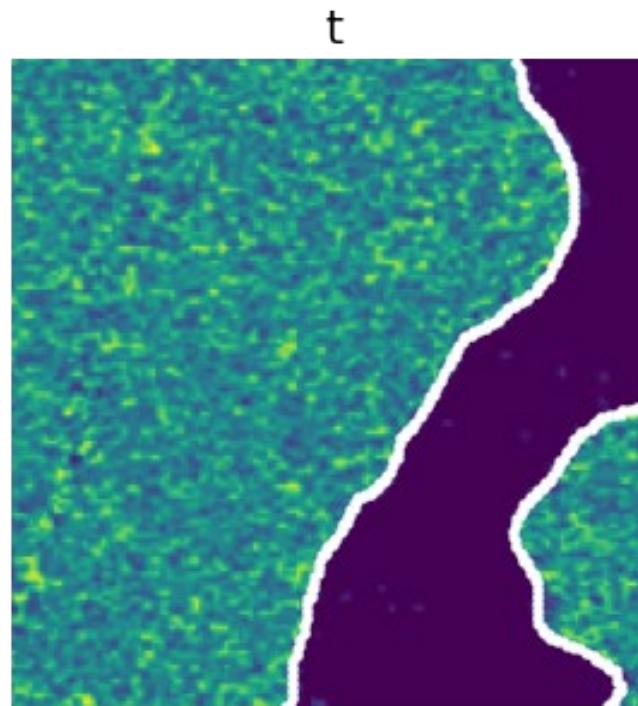
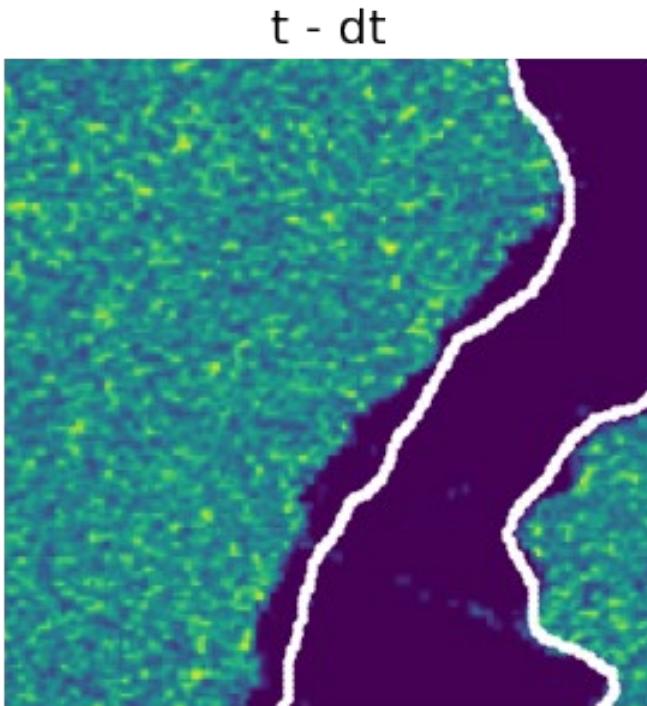
Average wall curvature



switched unswitched

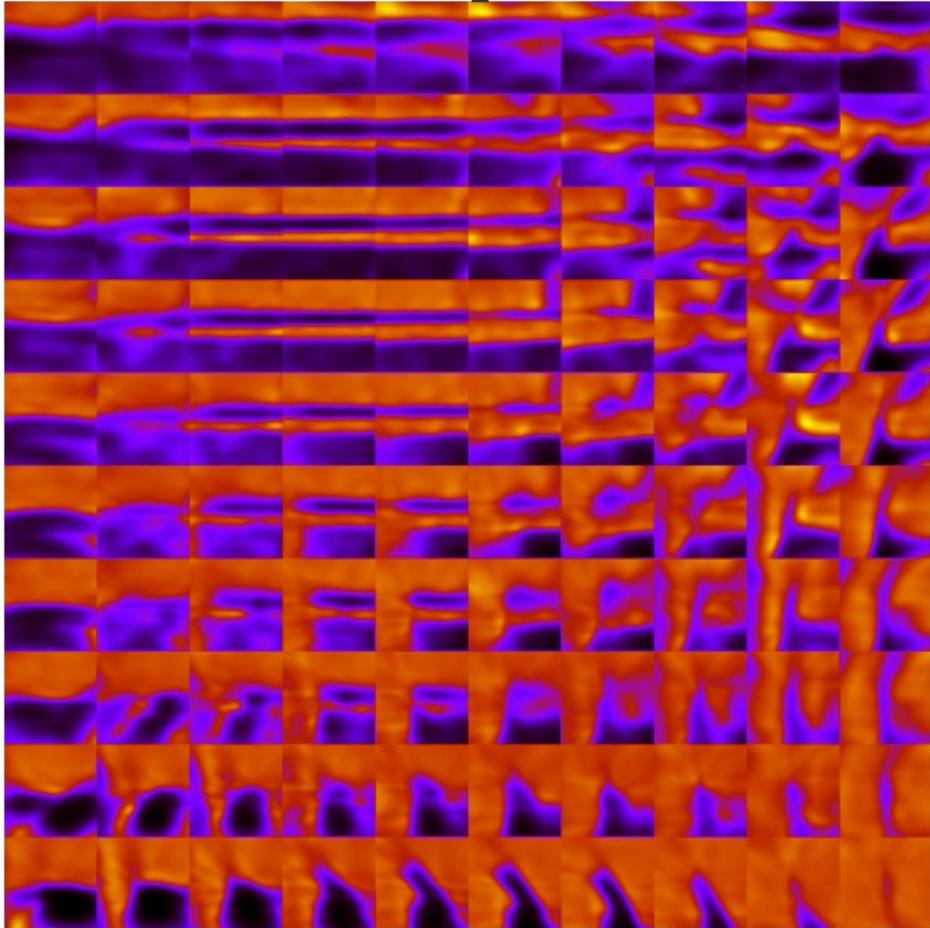
rVAE with time delay

Training dataset



rVAE with time delay

Latent space

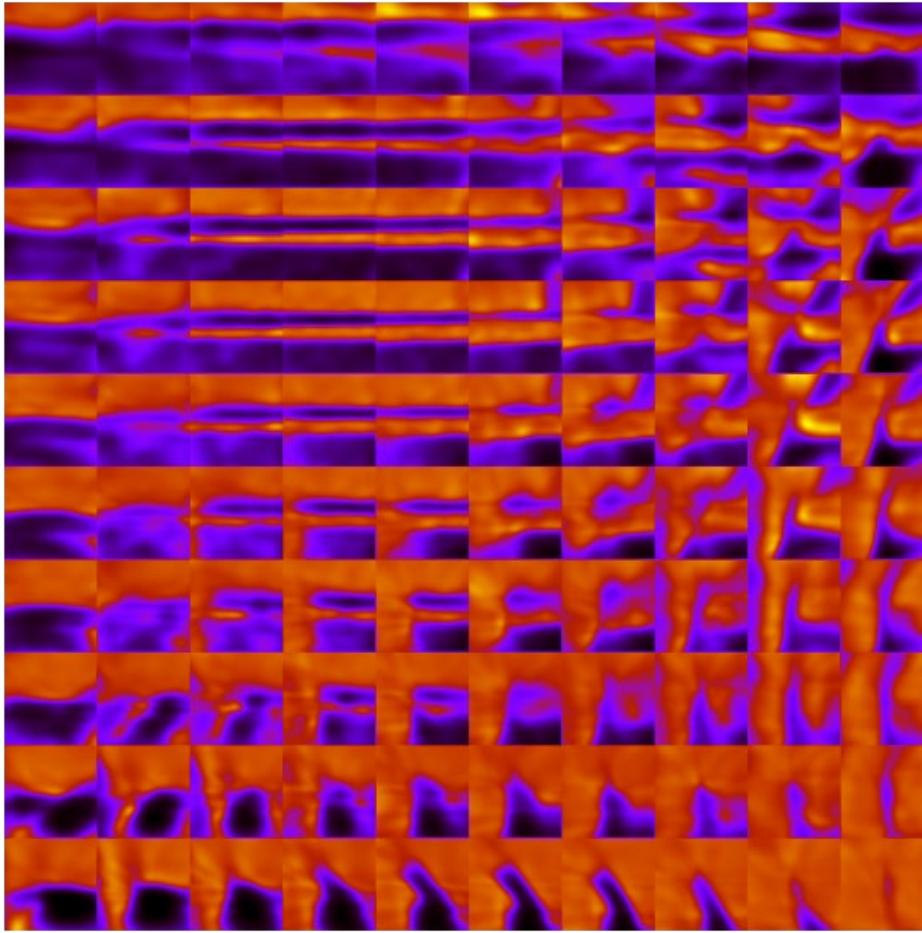


Domain wall

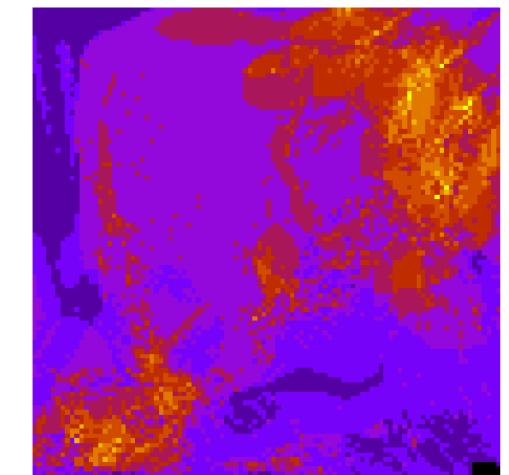


rVAE with time delay

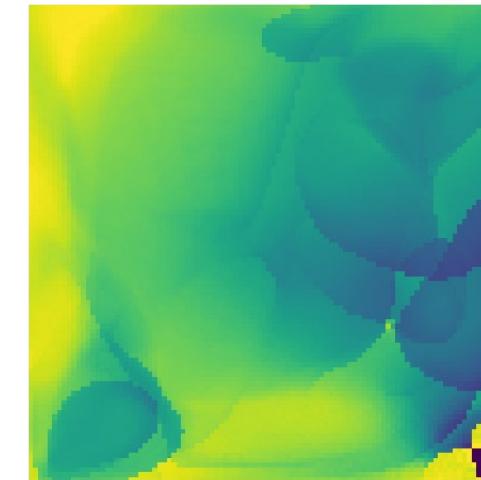
Latent space



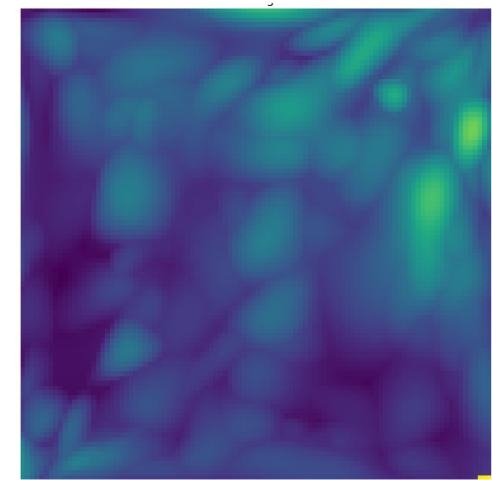
Wall count



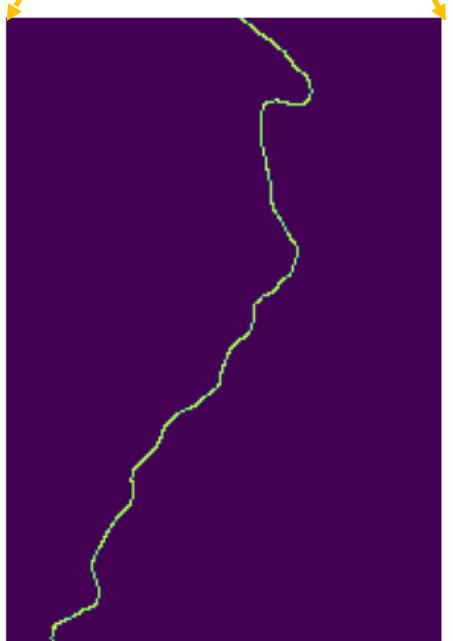
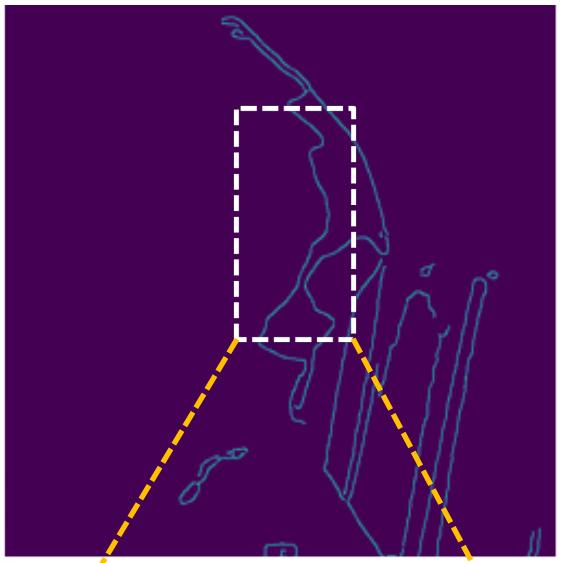
Domain convex



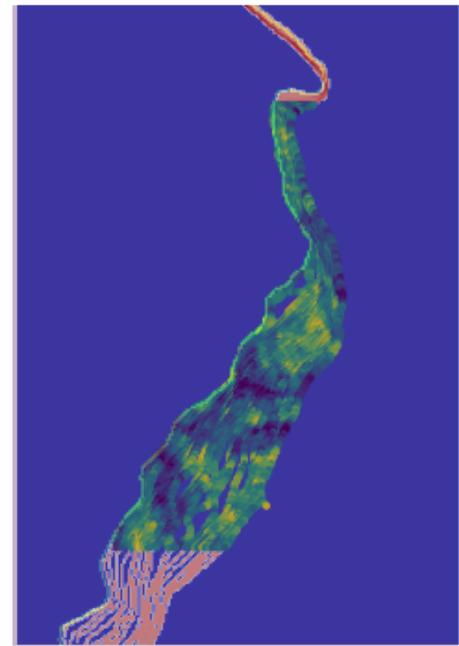
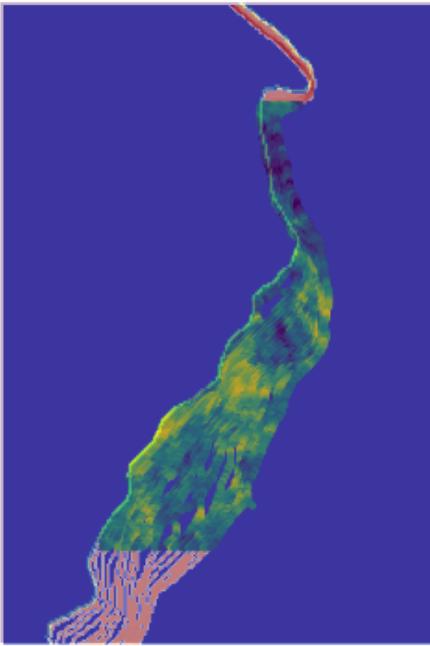
Switch significance



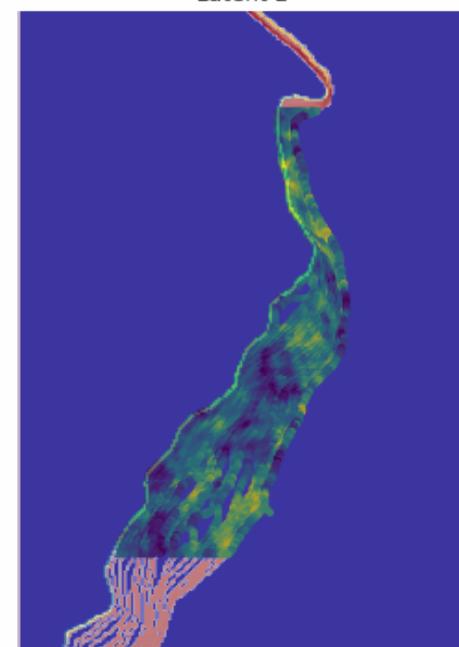
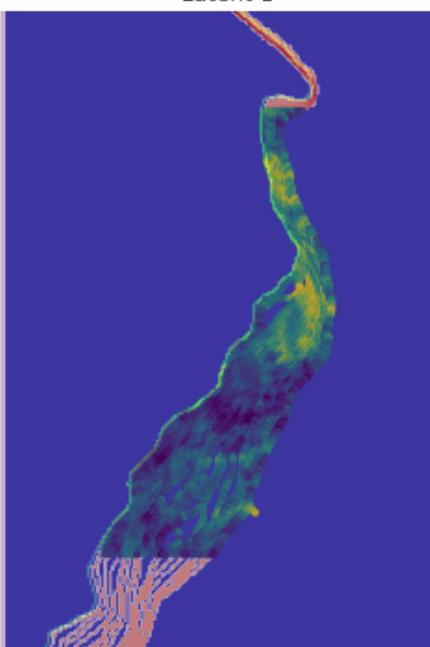
Domain wall evolution



Forward:
 t vs $t+1$

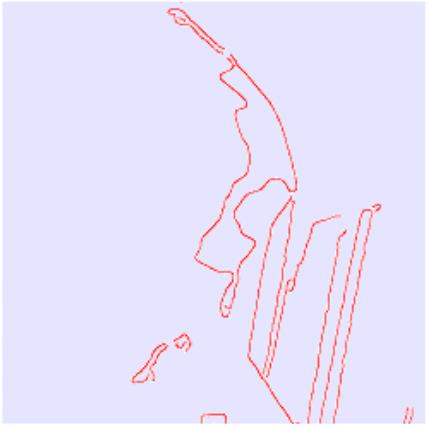


Reverse:
 t vs $t+1$

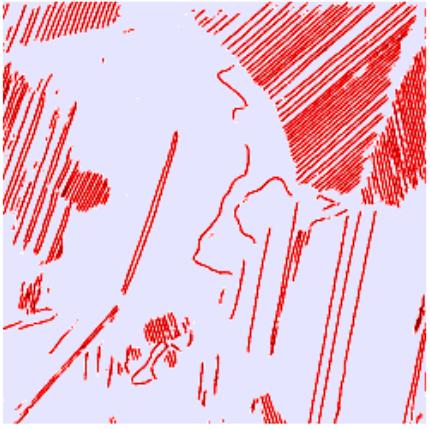


Multilayer rVAE

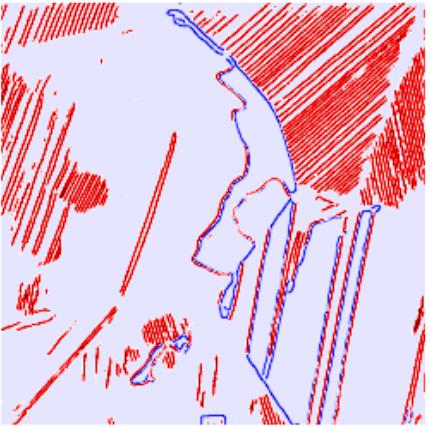
180° Walls



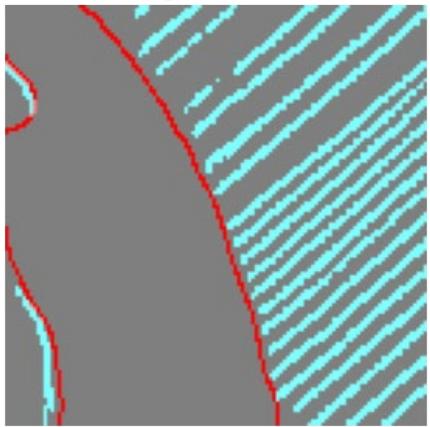
180°+Non180° Walls



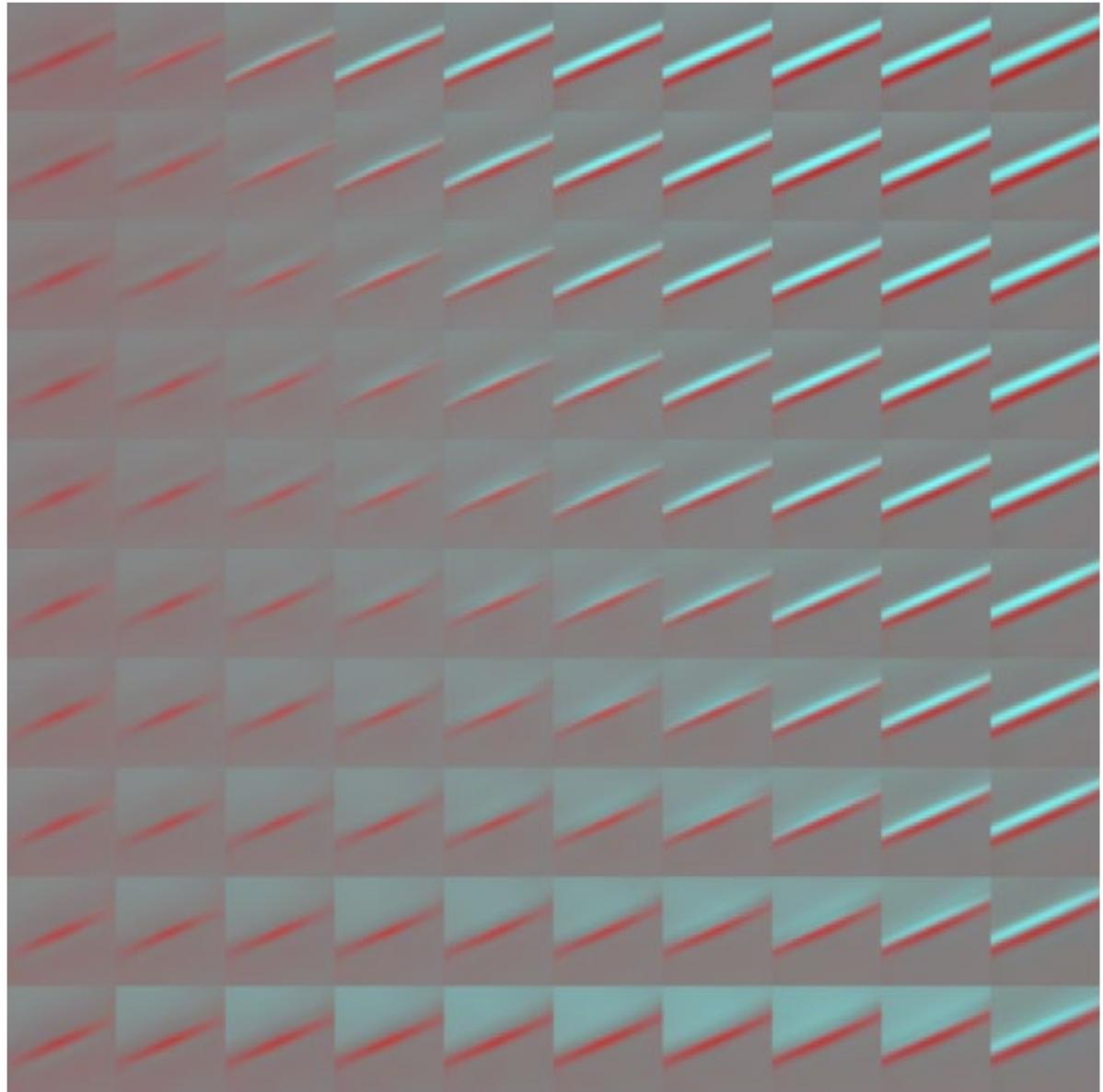
Subtraction = Non180° Walls



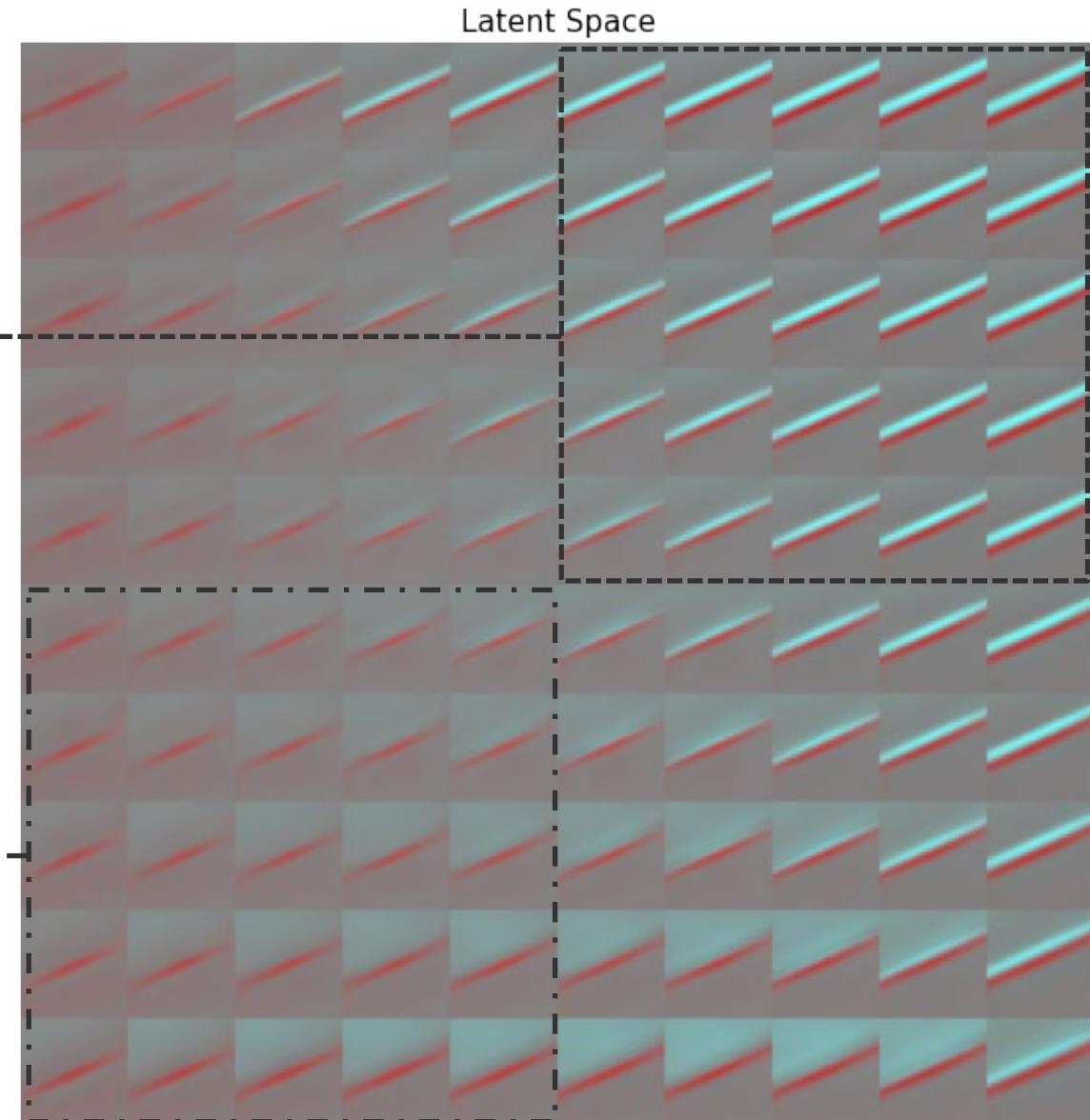
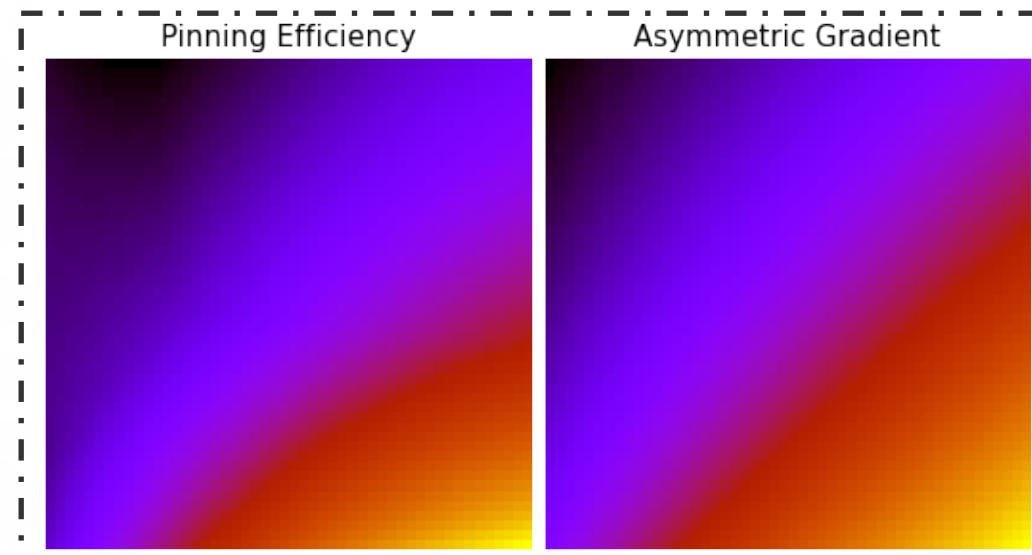
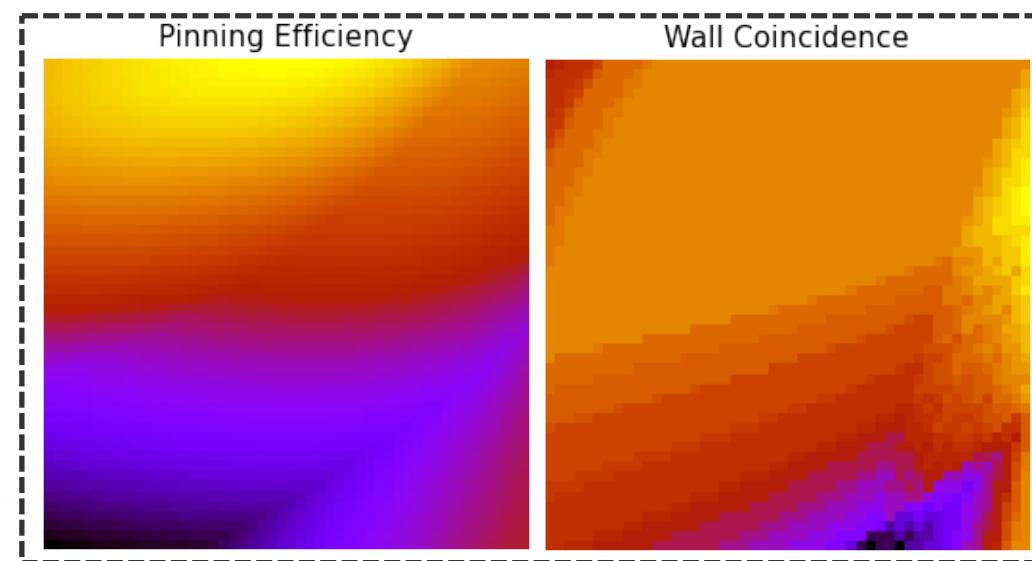
subimage of stack walls



Latent Space



Pinning mechanism

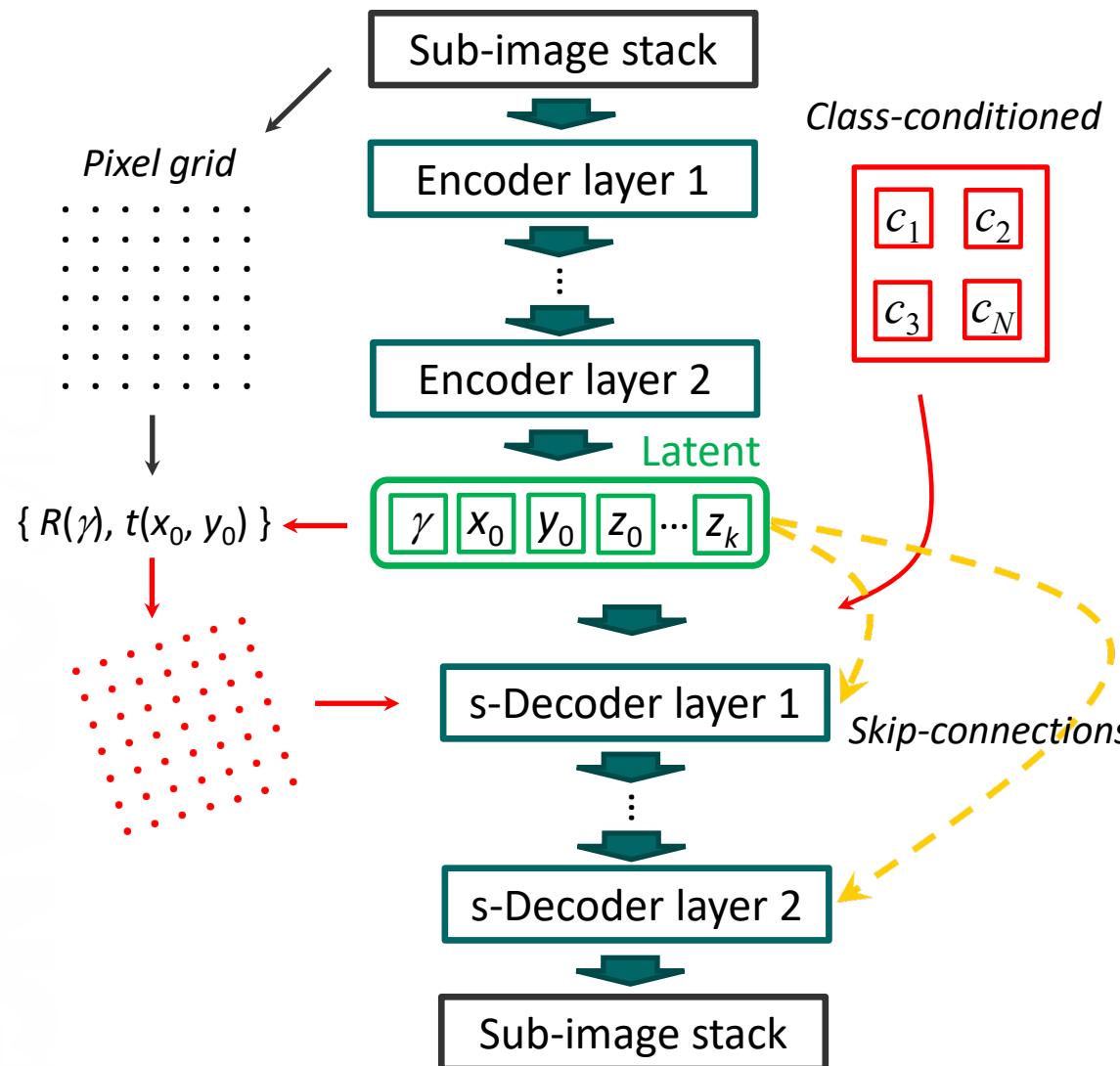


color scale

What if we have multiple classes?

1. Classes are known: conditional (discrete) VAE
2. Factors of variability are known: conditional (continuous) VAE
3. Some classes are known: semi-supervised VAE
4. Number of classes are known: joint VAE

Conditional VAE



- Generative model is a function of spatial coordinate
- 3 additional latent variables to absorb rotations and shifts
- Disentangles rotations and translations from image content
- Ideal for analyzing microscopy sub-images on atomic level

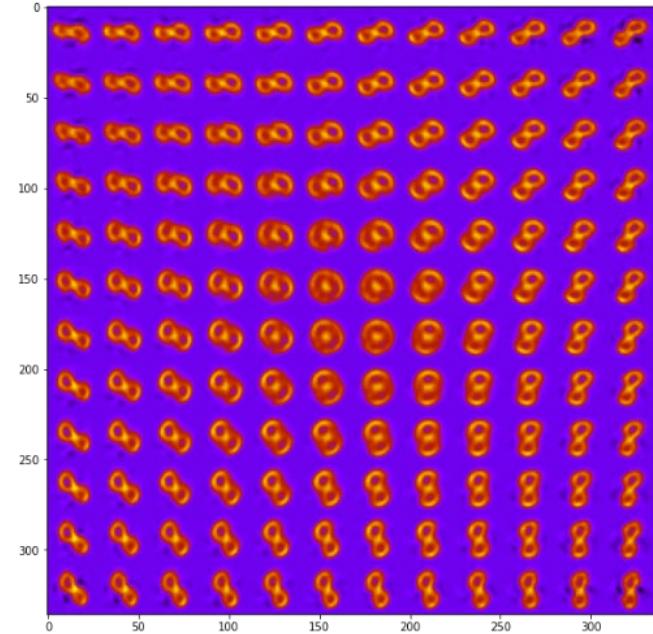
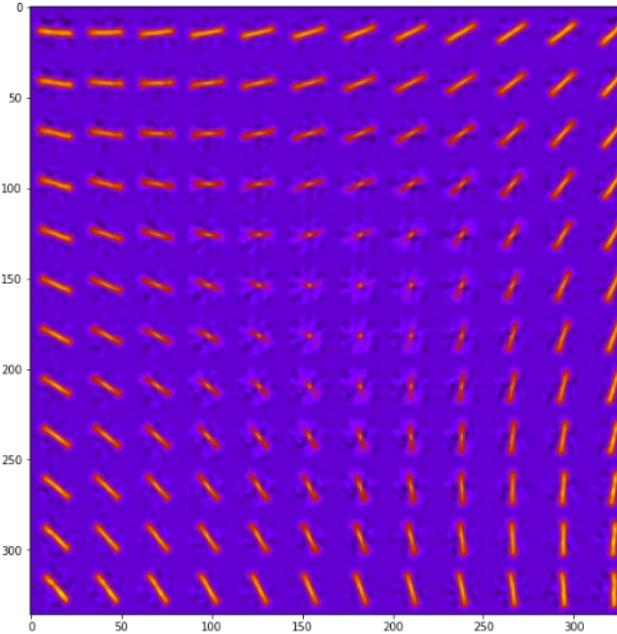
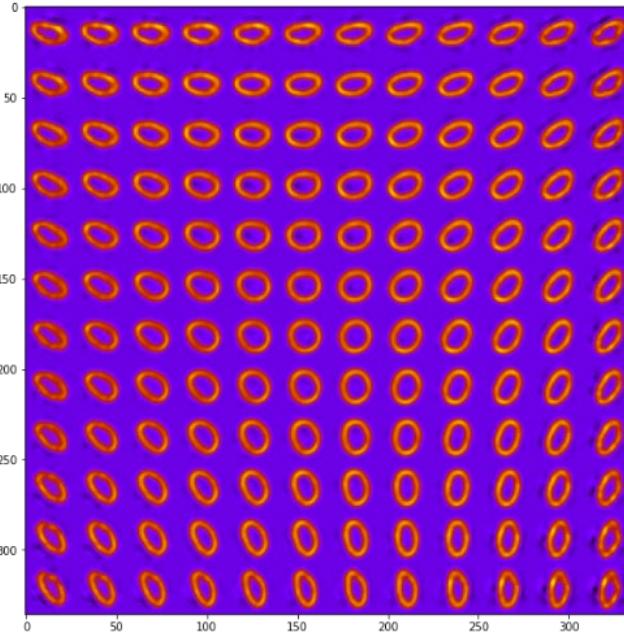
ELBO

$$\begin{aligned} &= \text{Reconstruction Loss} \\ &- D_{KL}(q(z|x)\|\mathcal{N}(0,I)) \\ &- D_{KL}(q(\gamma|x)\|\mathcal{N}(0,s_\gamma^2)) \\ &- D_{KL}(q(\Delta r|x)\|\mathcal{N}(0,s_{\Delta r}^2)) \quad \text{Regular VAE} \\ &+ D_{KL}(\text{physics-based "priors"}) ? \\ &+ D \quad (\text{physics}) ? \end{aligned}$$

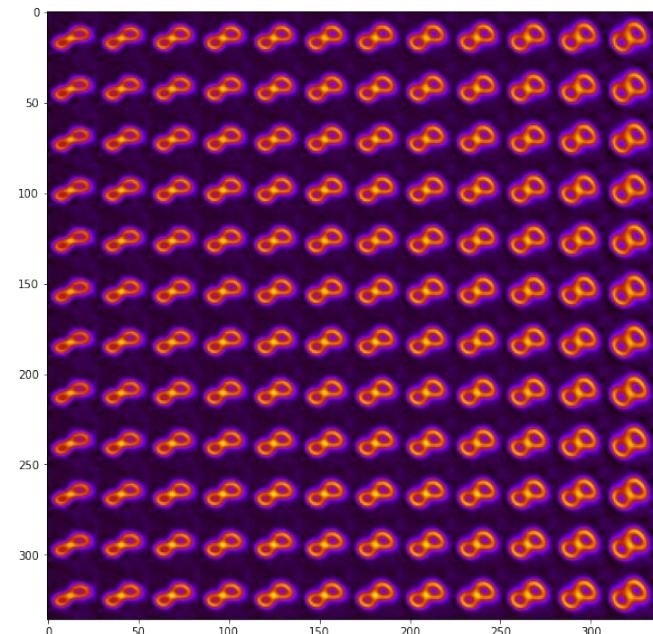
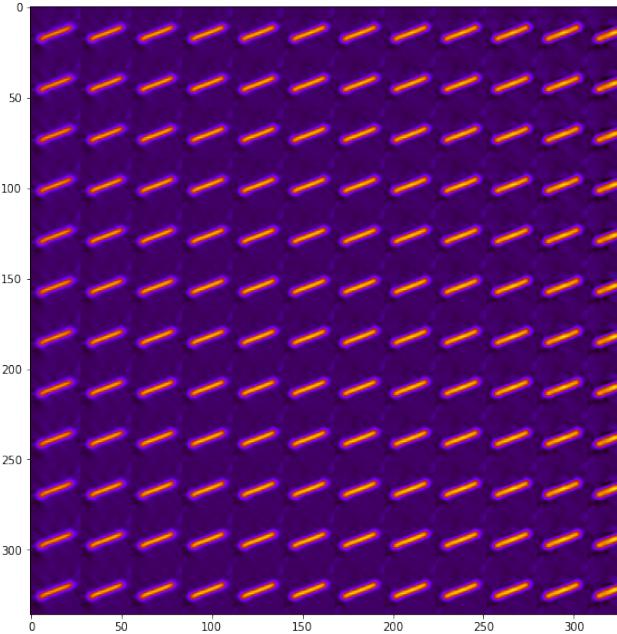
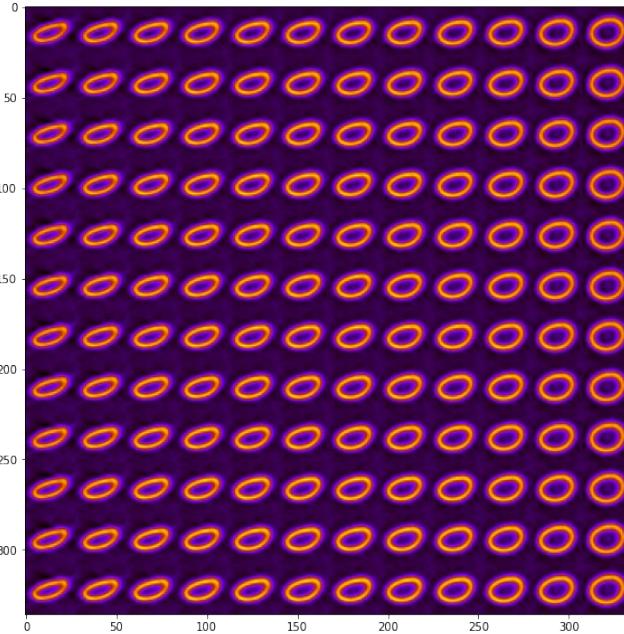
Rotation
Translation

MNIST cVAE

No rotations

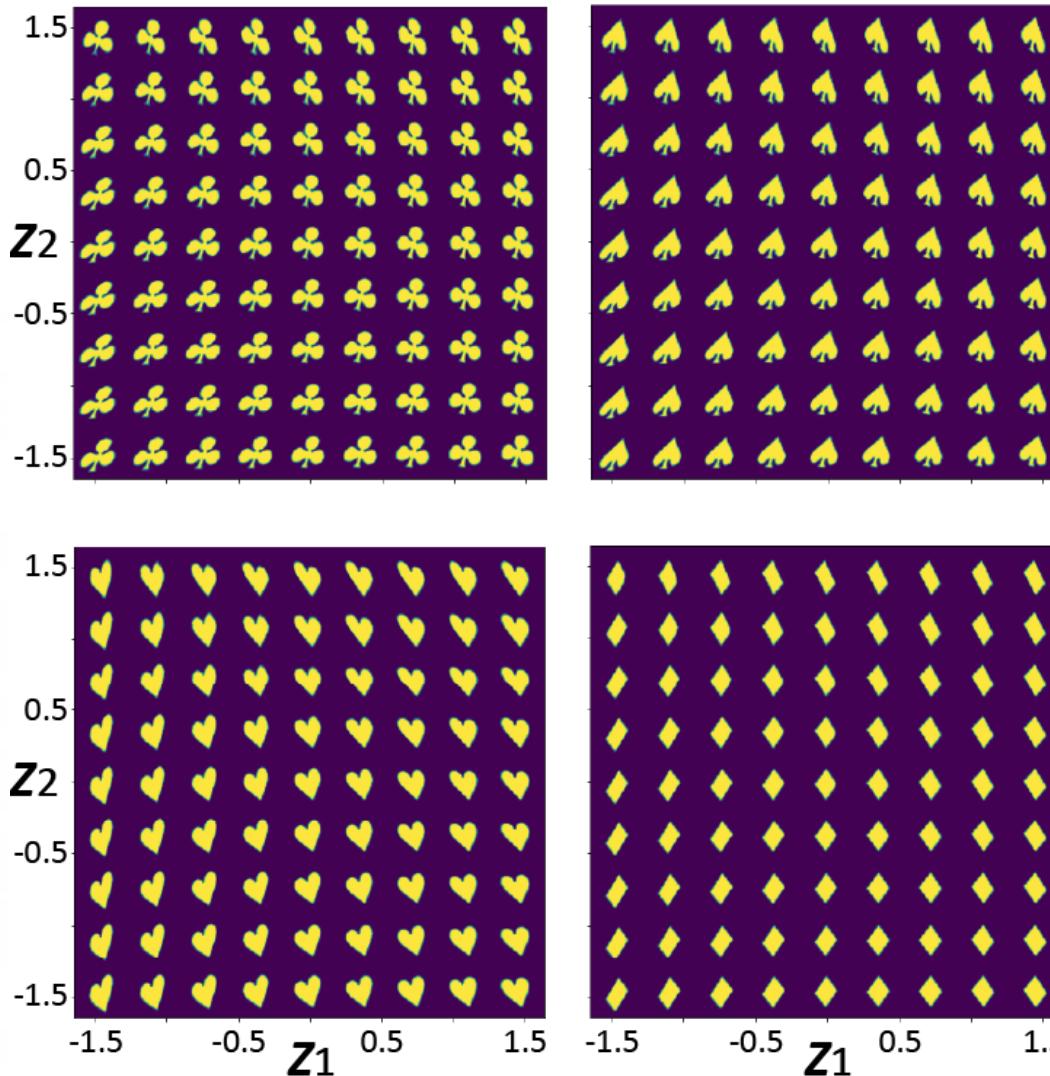


With rotations

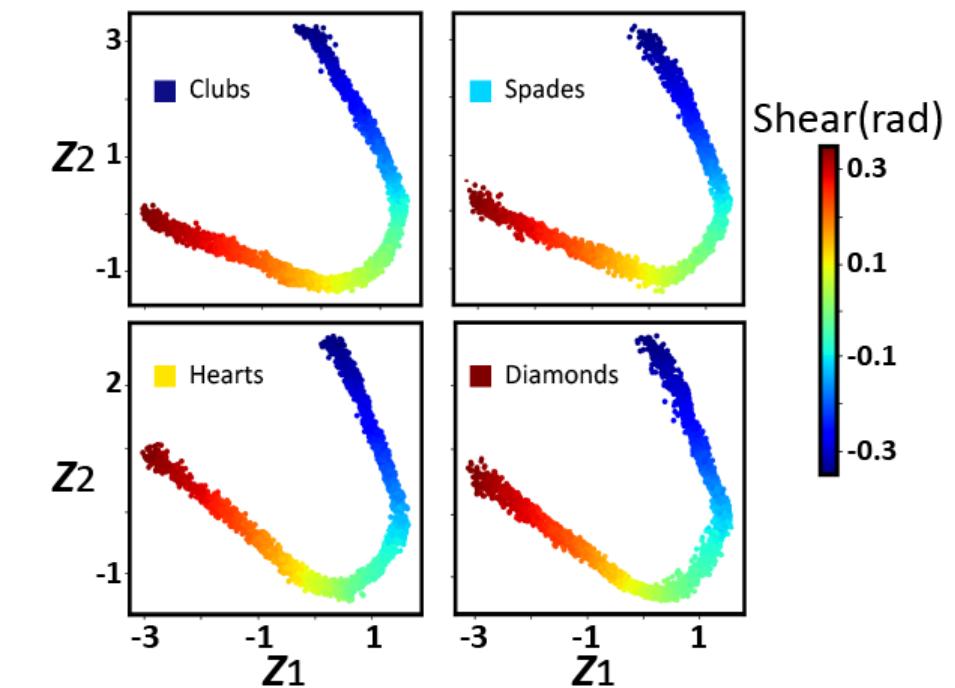


cVAE on cards data set

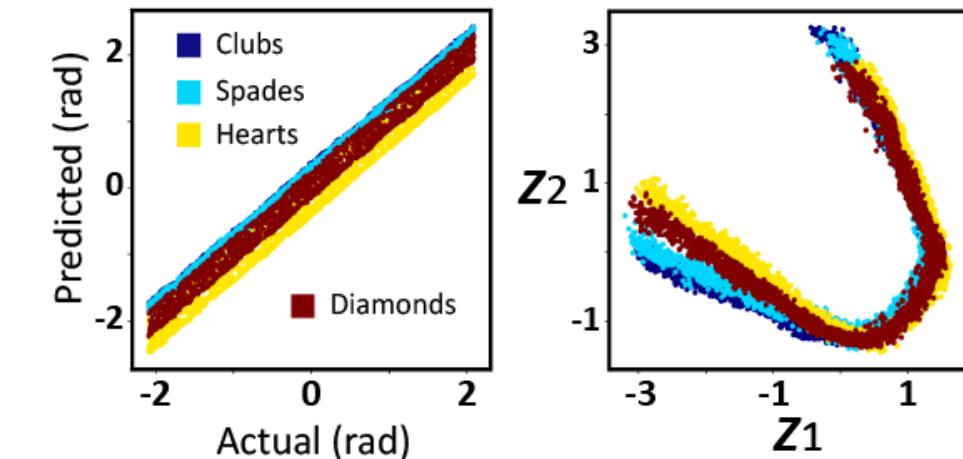
One independent latent space per class



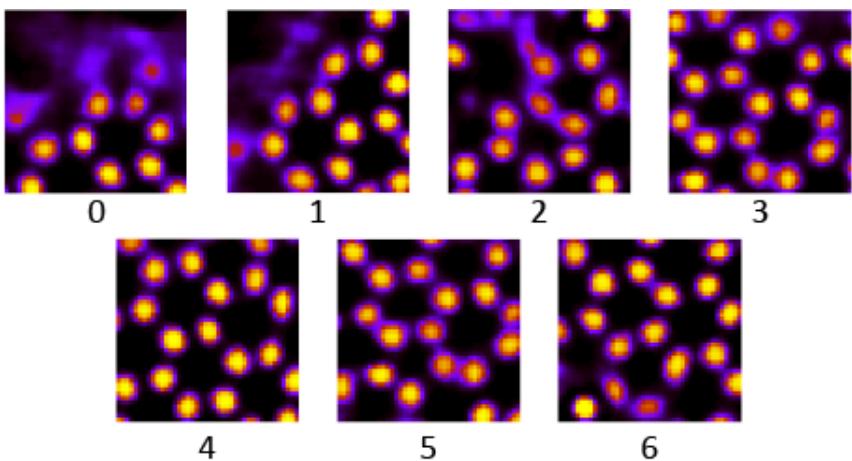
Shear distribution in latent space



All four plotted jointly



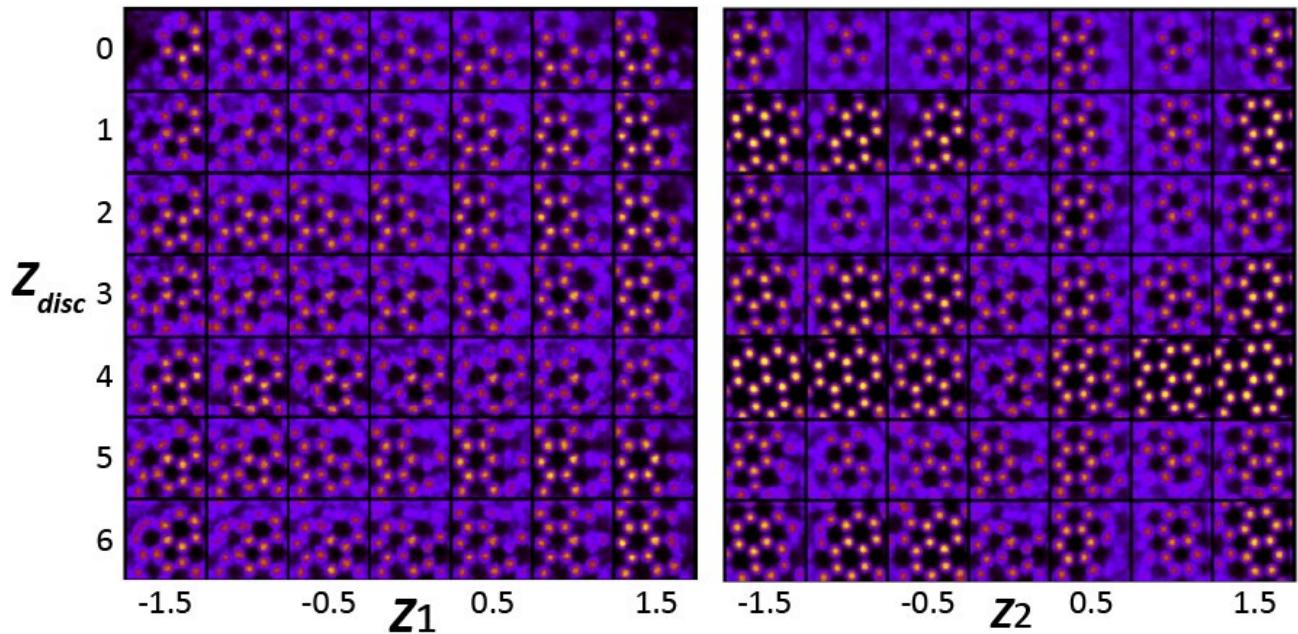
cVAE on Graphene



Autonomous sub-image labeling

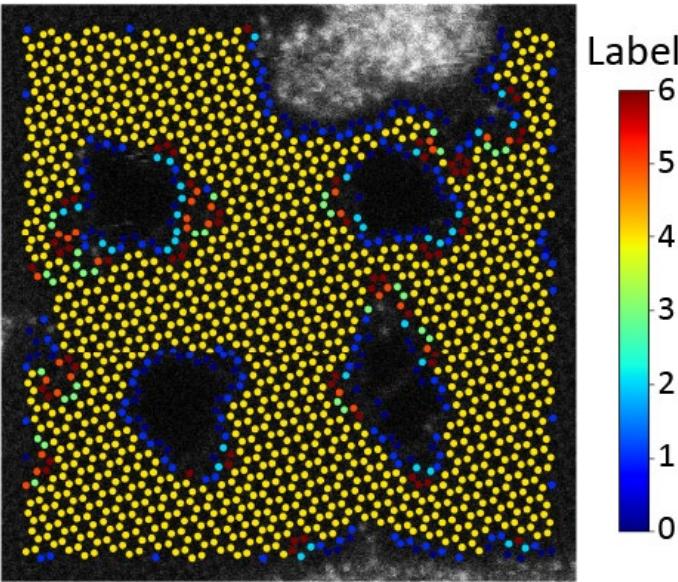
- 0: Fewer than 2 rings
- 1: two rings of size [6, 6]
- 2: three rings of size [5, 6]
- 3: three rings of size [6, 6, 7]
- 4: three rings of size [6, 6, 6]
- 5: three rings of size [5, 6, 7]
- 6: three rings of size [5, 6, 6]

Traversal manifolds

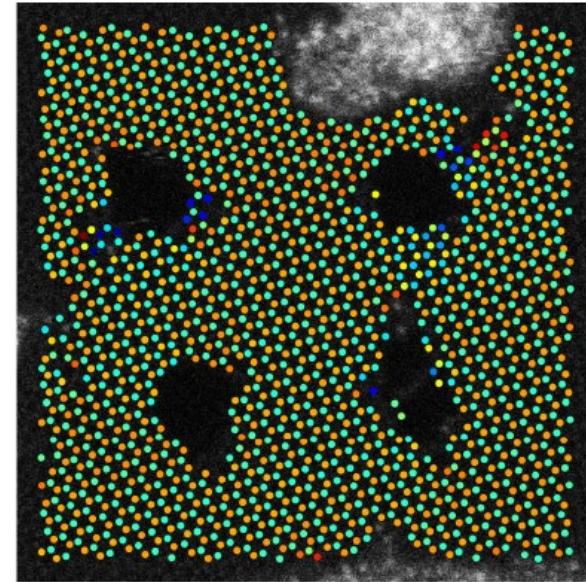
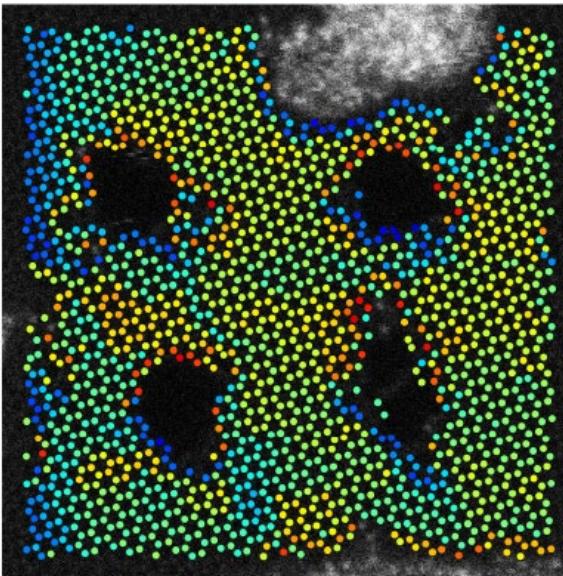


cVAE on graphene

Class labels

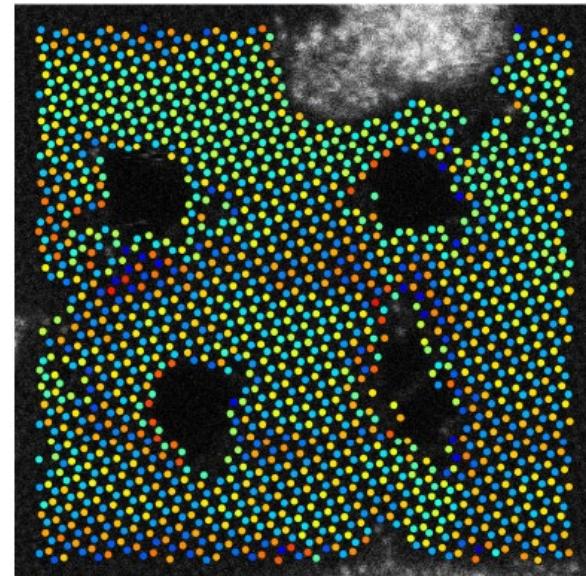


z_1



Encoded Angle

z_2



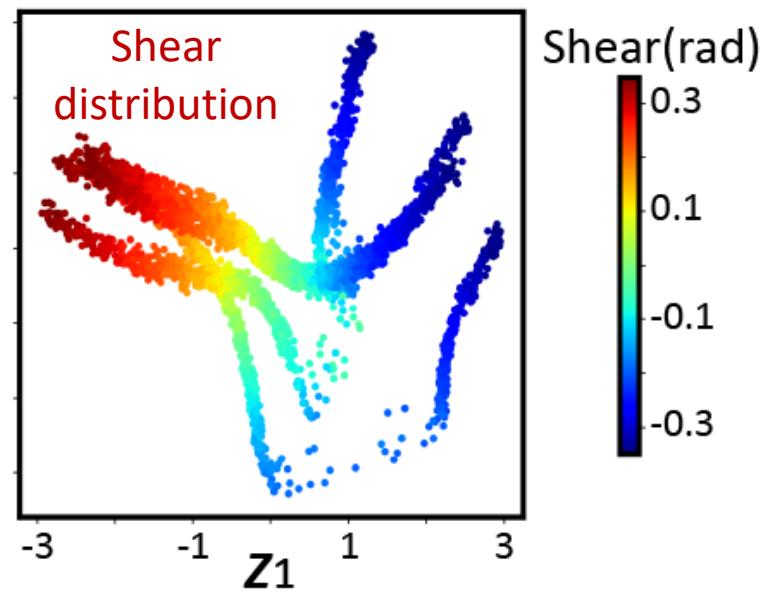
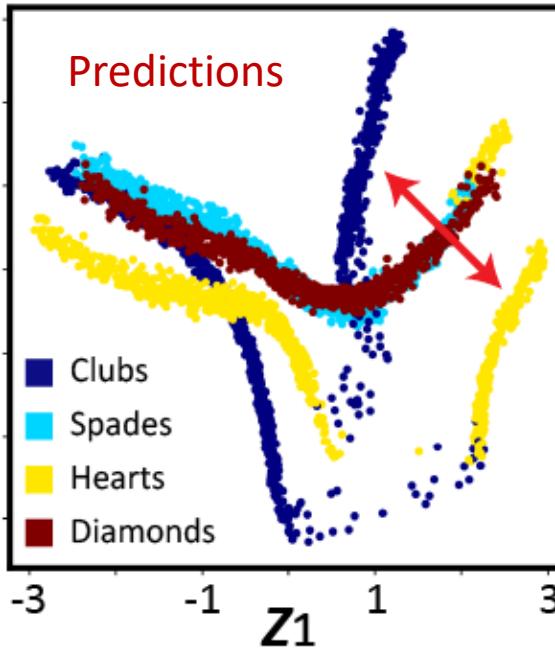
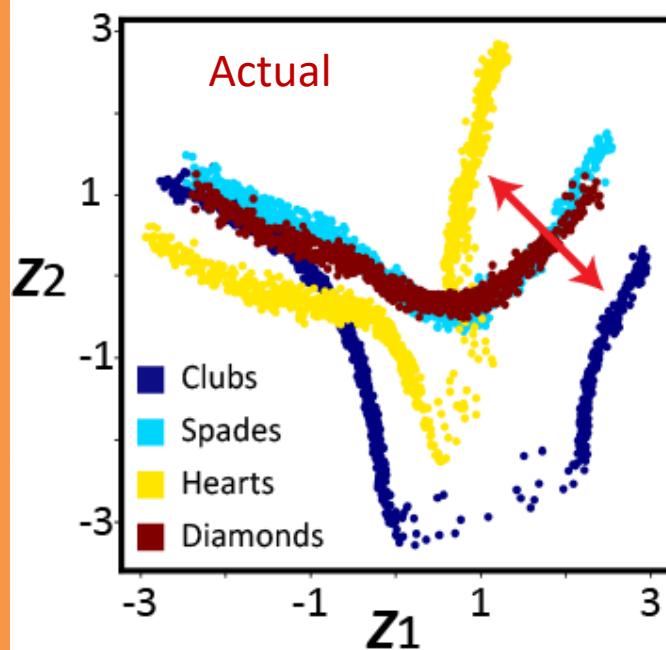
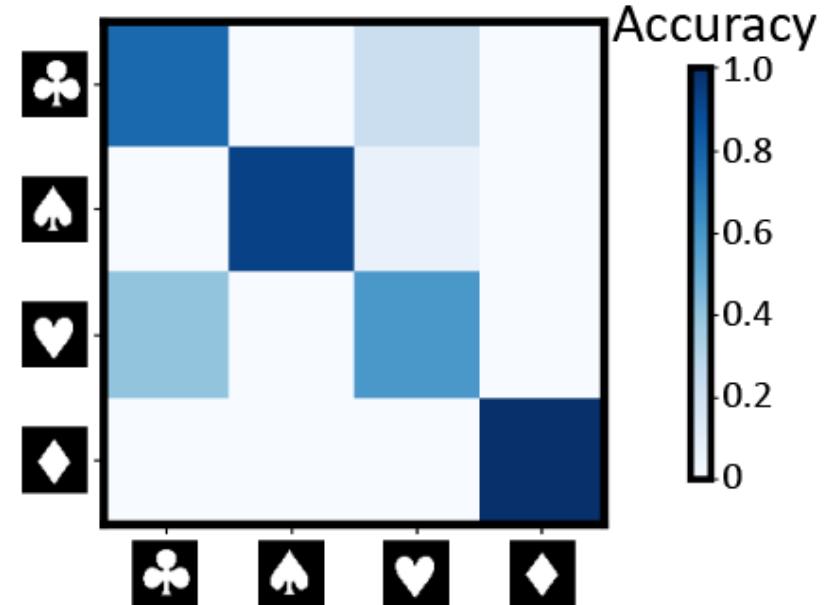
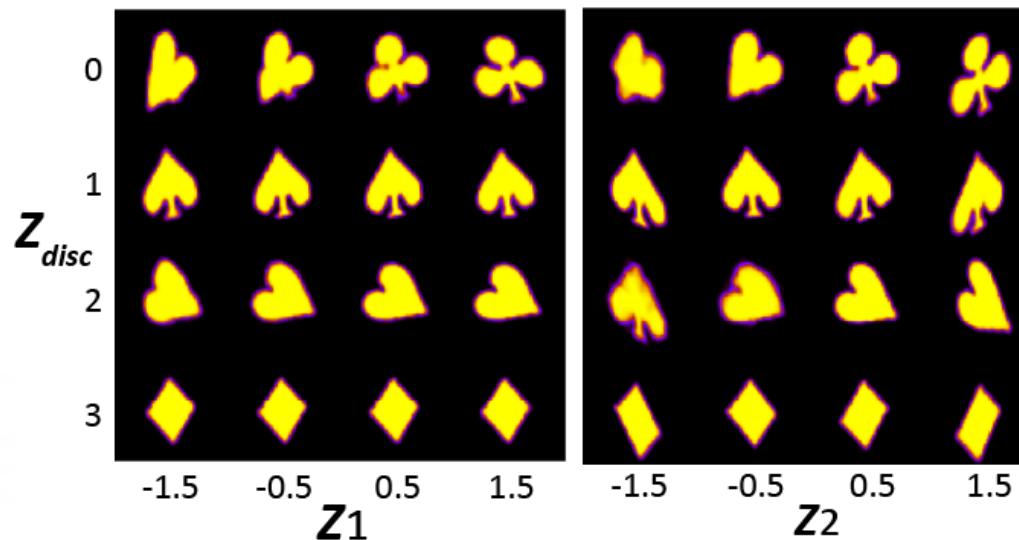
Correlation

Hypothesis: Abundance
of latent variables



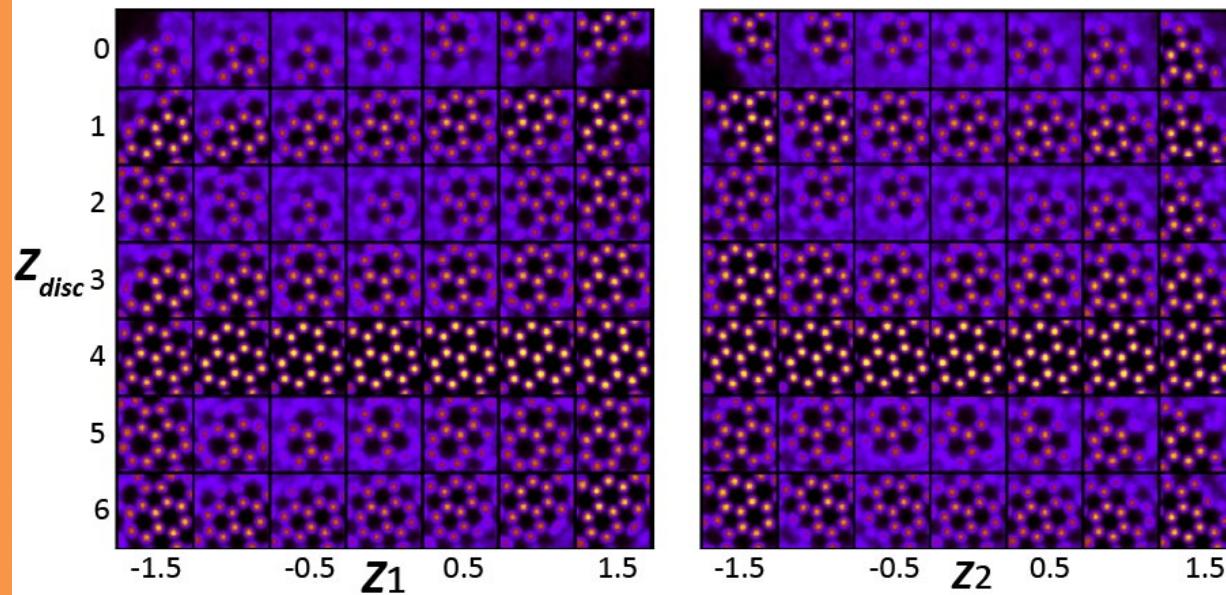
Semi-supervised VAE

Traversal Manifold

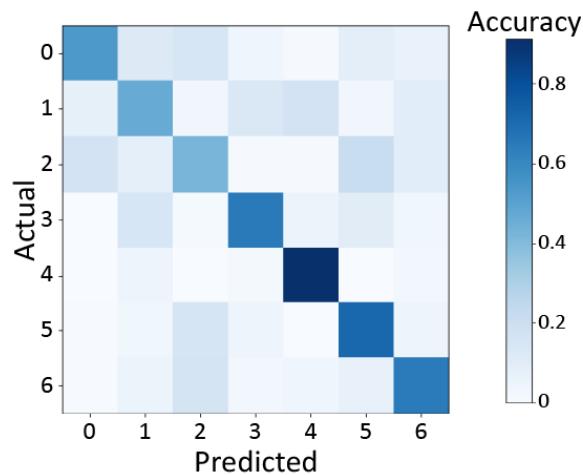


Semi-supervised VAE (graphene)

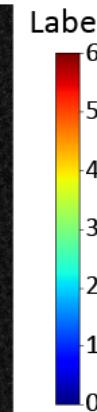
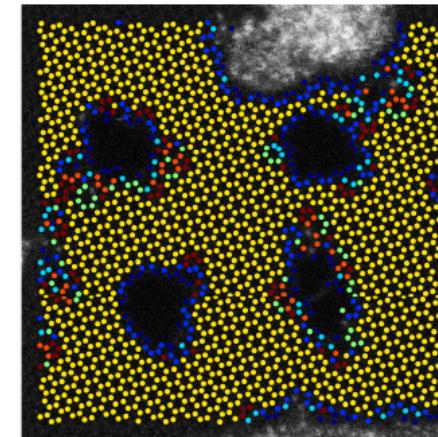
Traverse manifolds



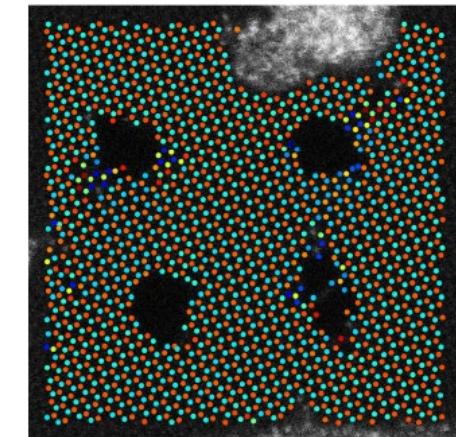
Confusion matrix



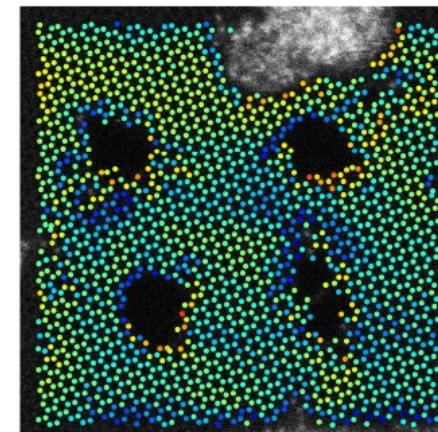
Class labels



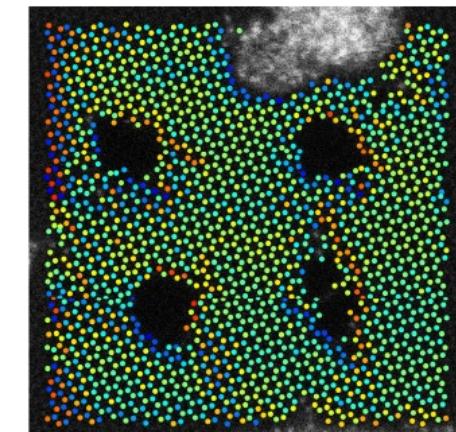
Angle Encoding



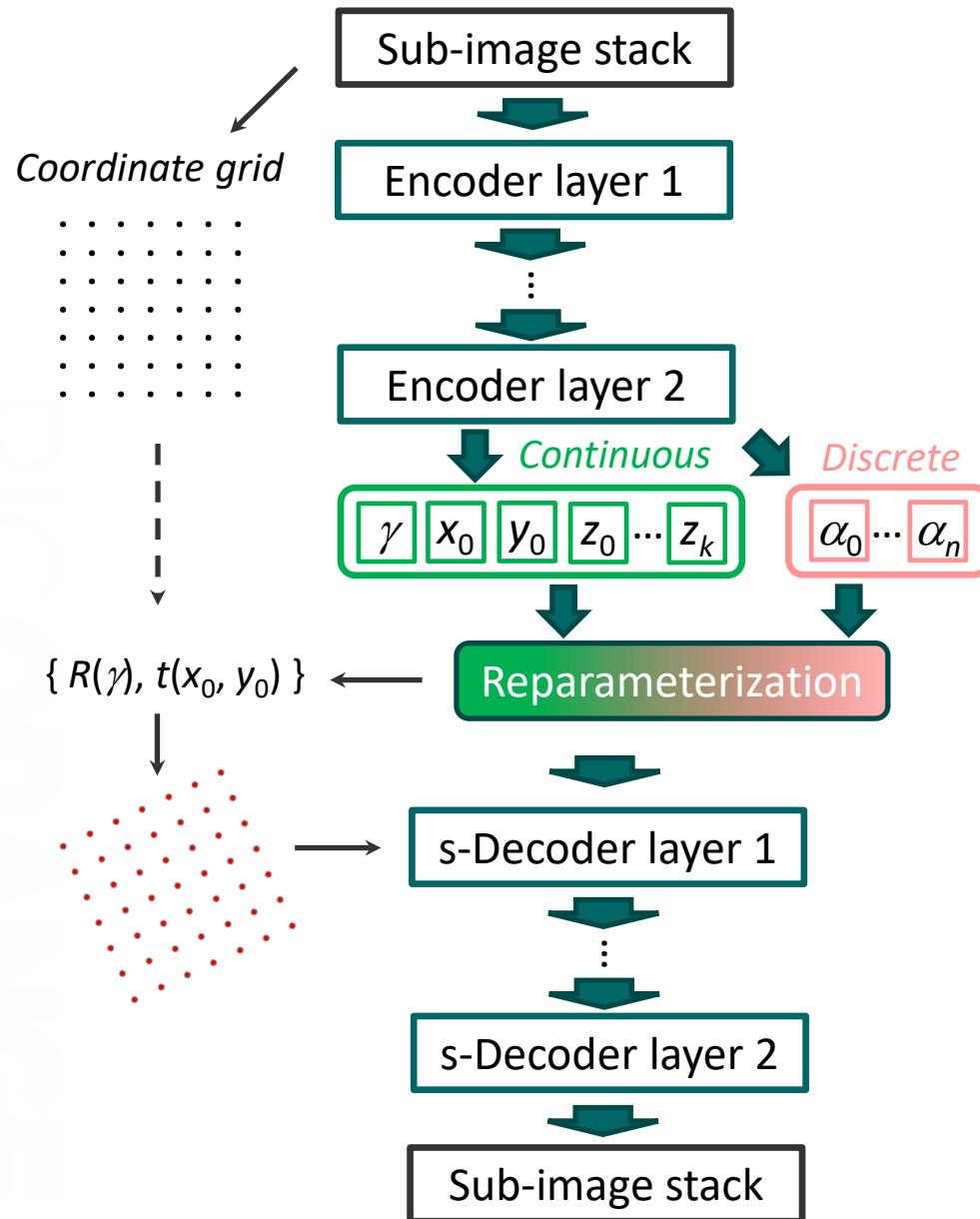
Z_1



Z_2



Joint VAE

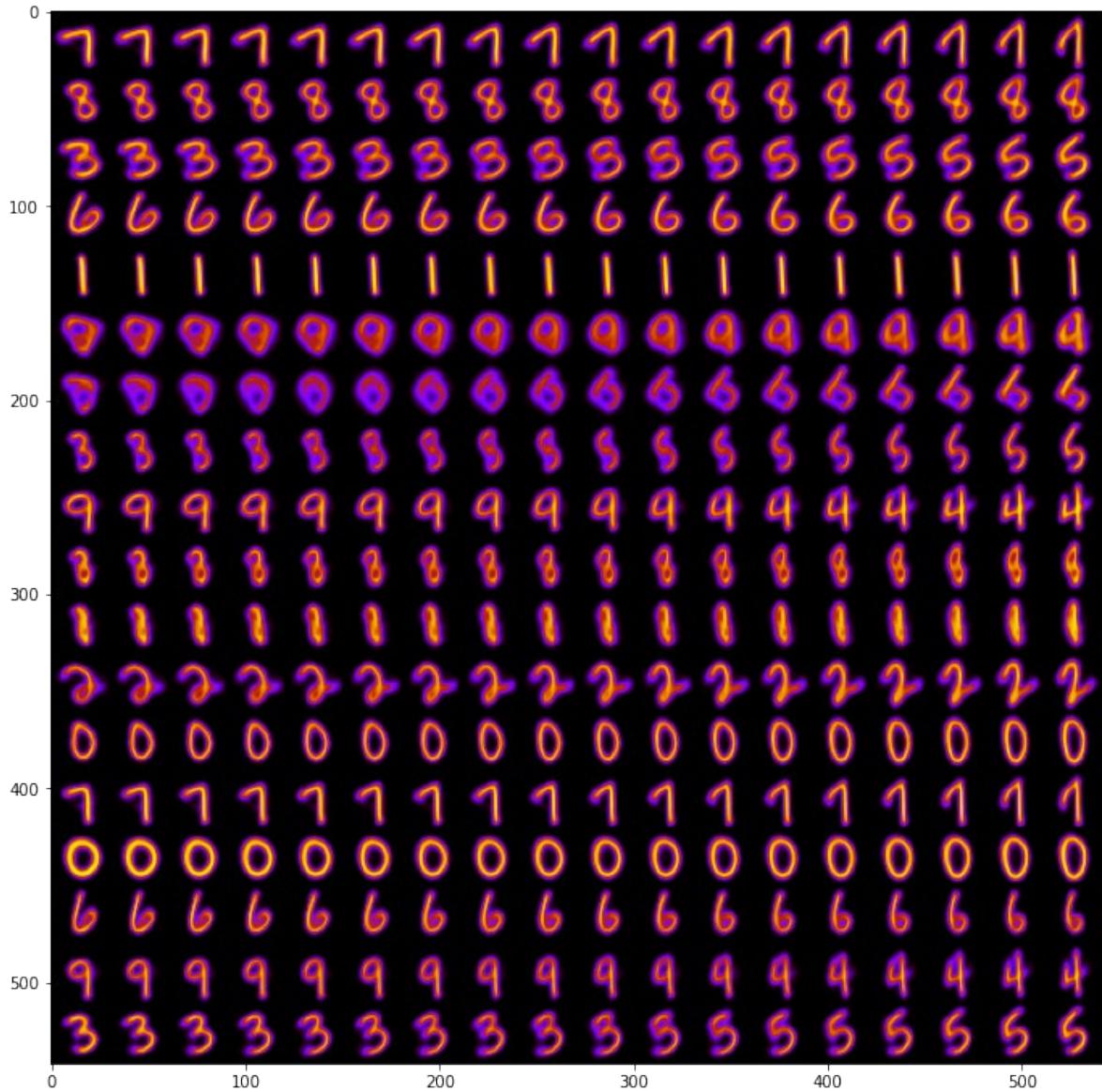
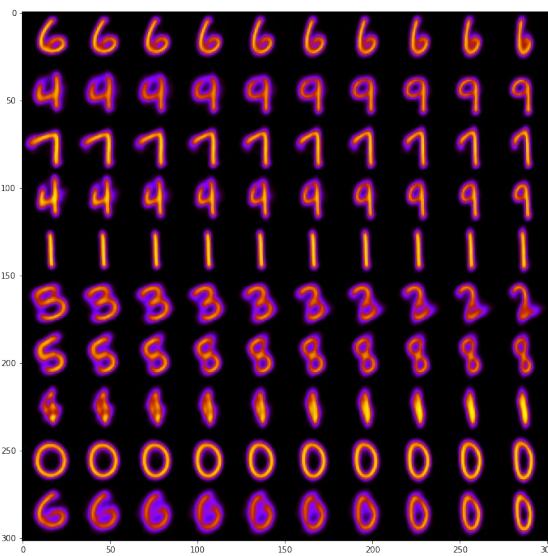
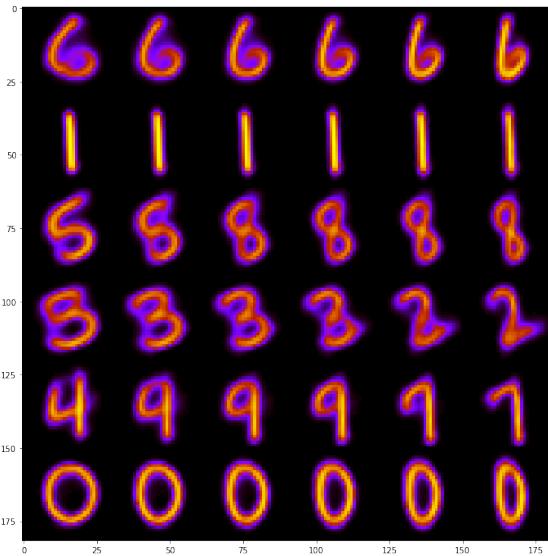


- Generative model is a function of spatial coordinate (e.g., via spatial broadcasting)
- 3 additional latent variables to absorb rotations and shifts
- Disentangles rotations and translations from image content
- Learns discrete classes in unsupervised fashion
- Well-suited for analyzing microscopy (sub-)images on atomic and molecular levels

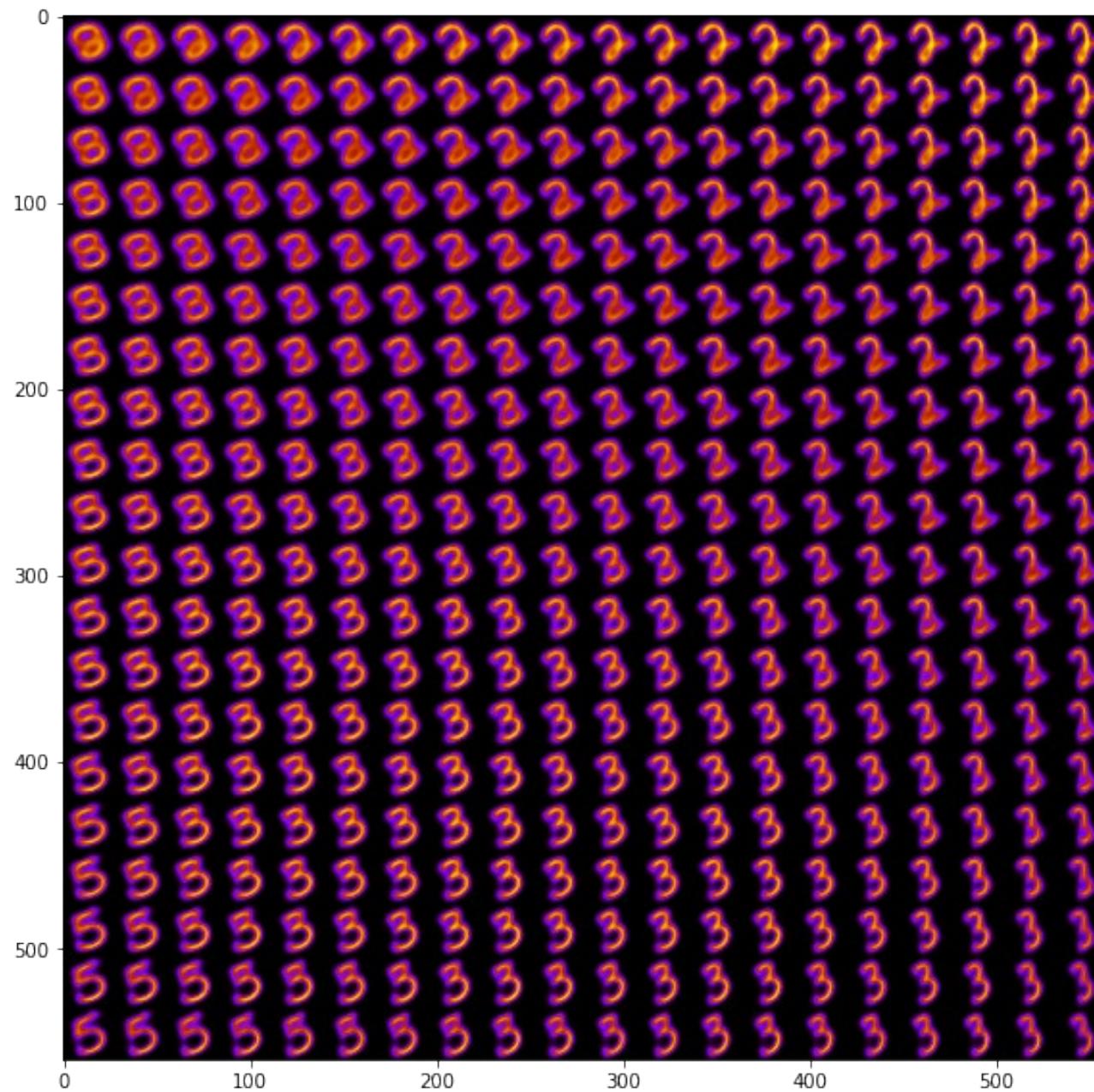
ELBO =

$$\begin{aligned} & - \text{Reconstruction Loss} \\ & - \beta_c(t) |(D_{KL}(q(z|x) \parallel p(z)) + D_{KL}(q(\gamma|x) \parallel p(\gamma)) - C_z| \quad \text{Continuous} \\ & - \beta_d(t) |D_{KL}(q(\alpha|x) \parallel p(\alpha)) - C_\alpha| \quad \text{Discrete} \\ & + \text{physics-based "loss" ?} \end{aligned}$$

jVAE on MNIST

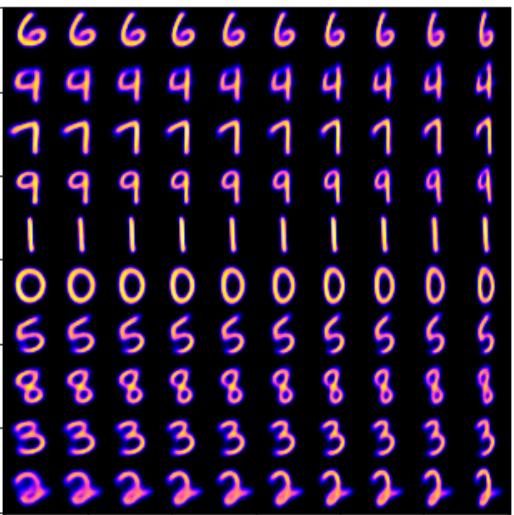


Latent representations



Ensemble jVAE

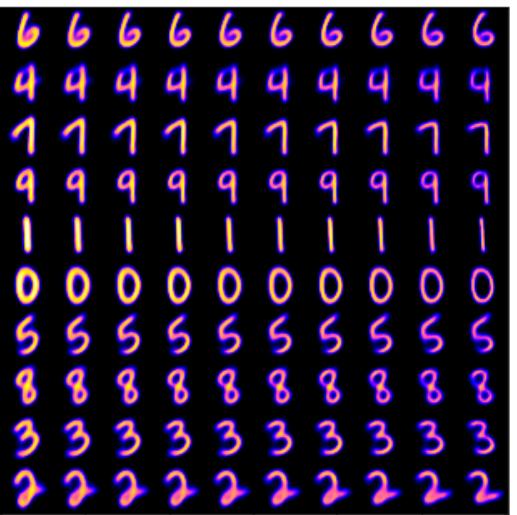
Predictions from different ensemble models



Baseline: 10 epochs
Ensemble models: 8

- The unstable classes show the largest “uncertainty”
- Indication of the quality of separation and/or a guide for selection of the number of classes

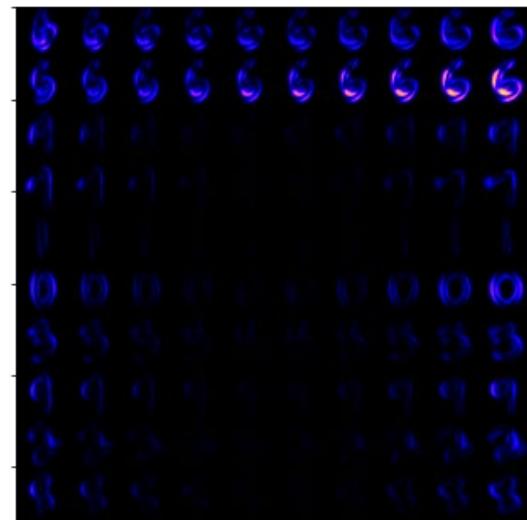
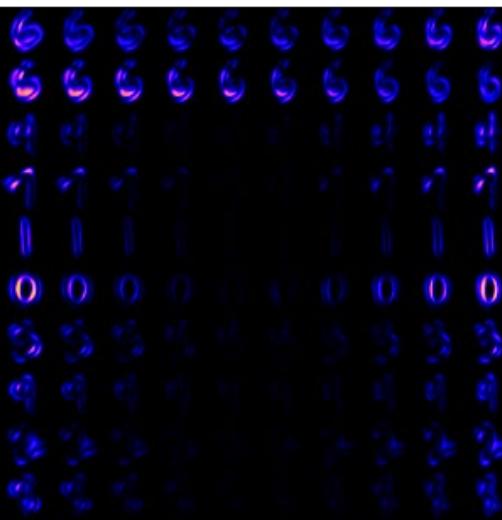
Uncertainty



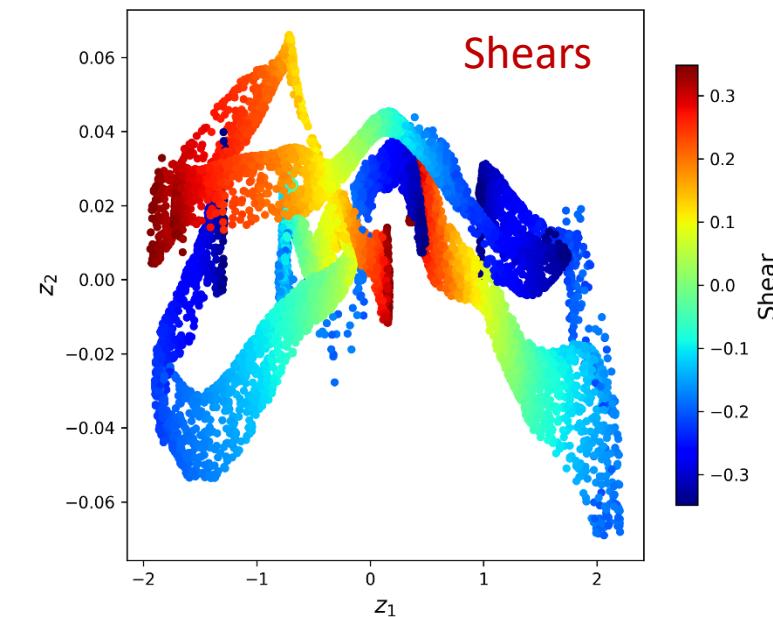
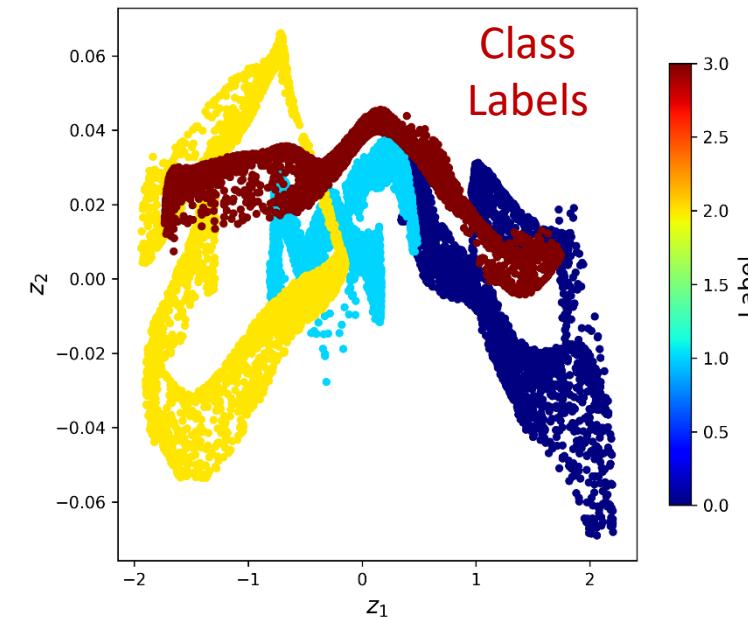
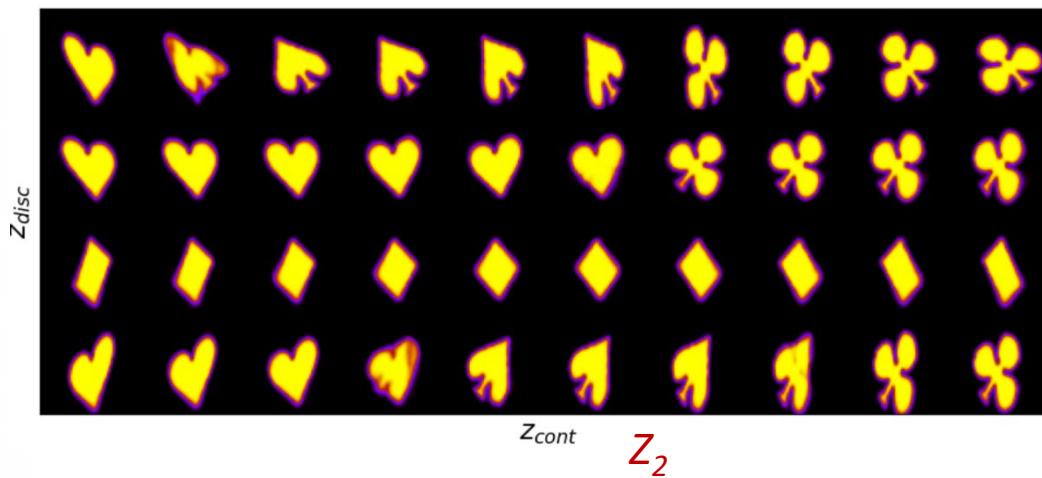
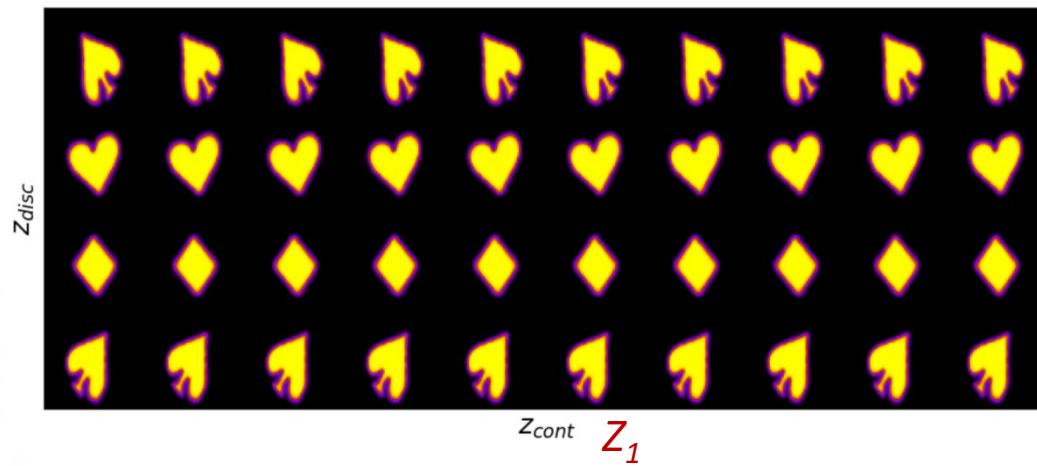
Mean prediction



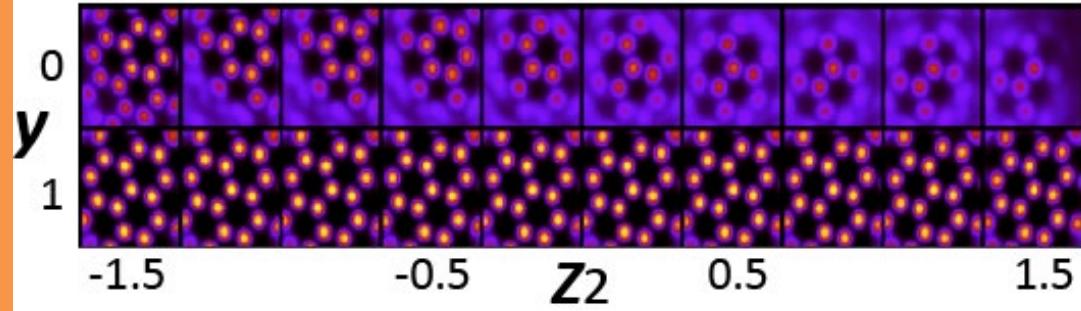
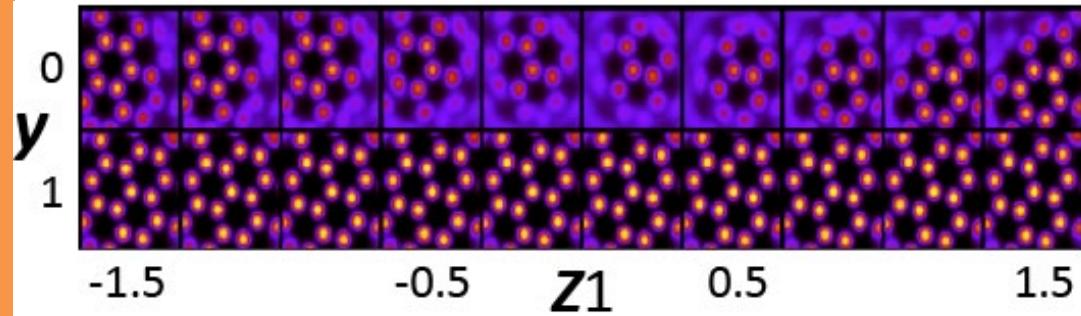
Dispersion in predictions ('uncertainty')



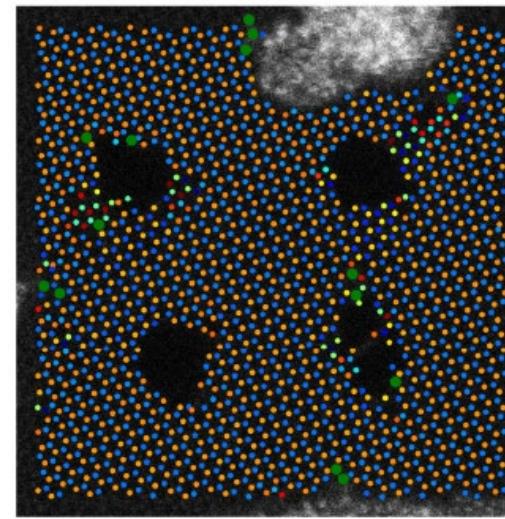
jVAE on cards



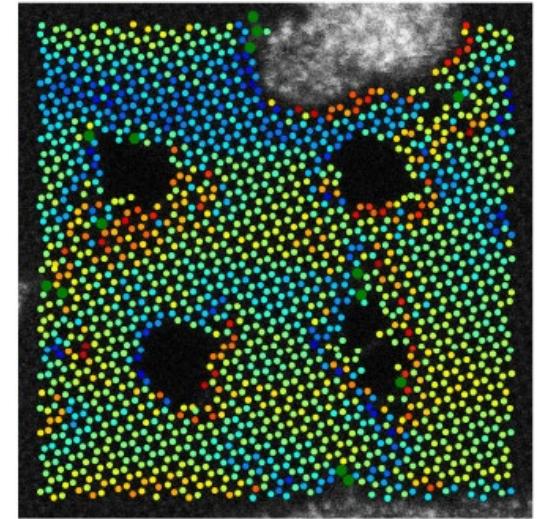
jVAE on graphene



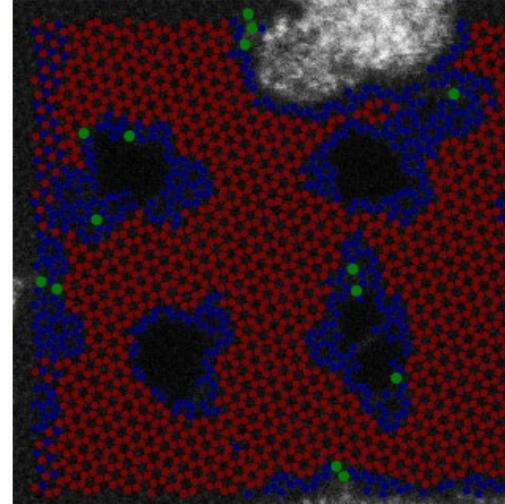
Angle encoding



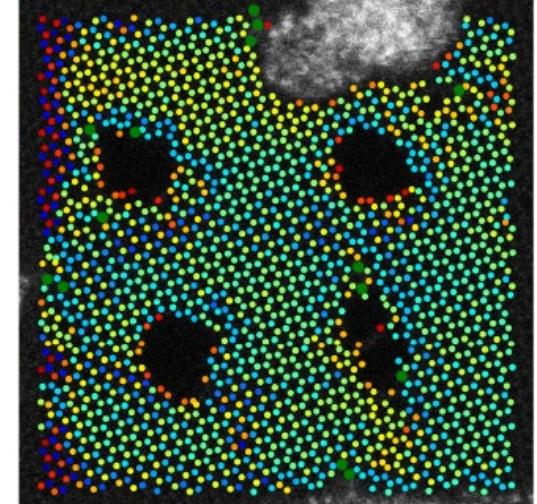
z_1



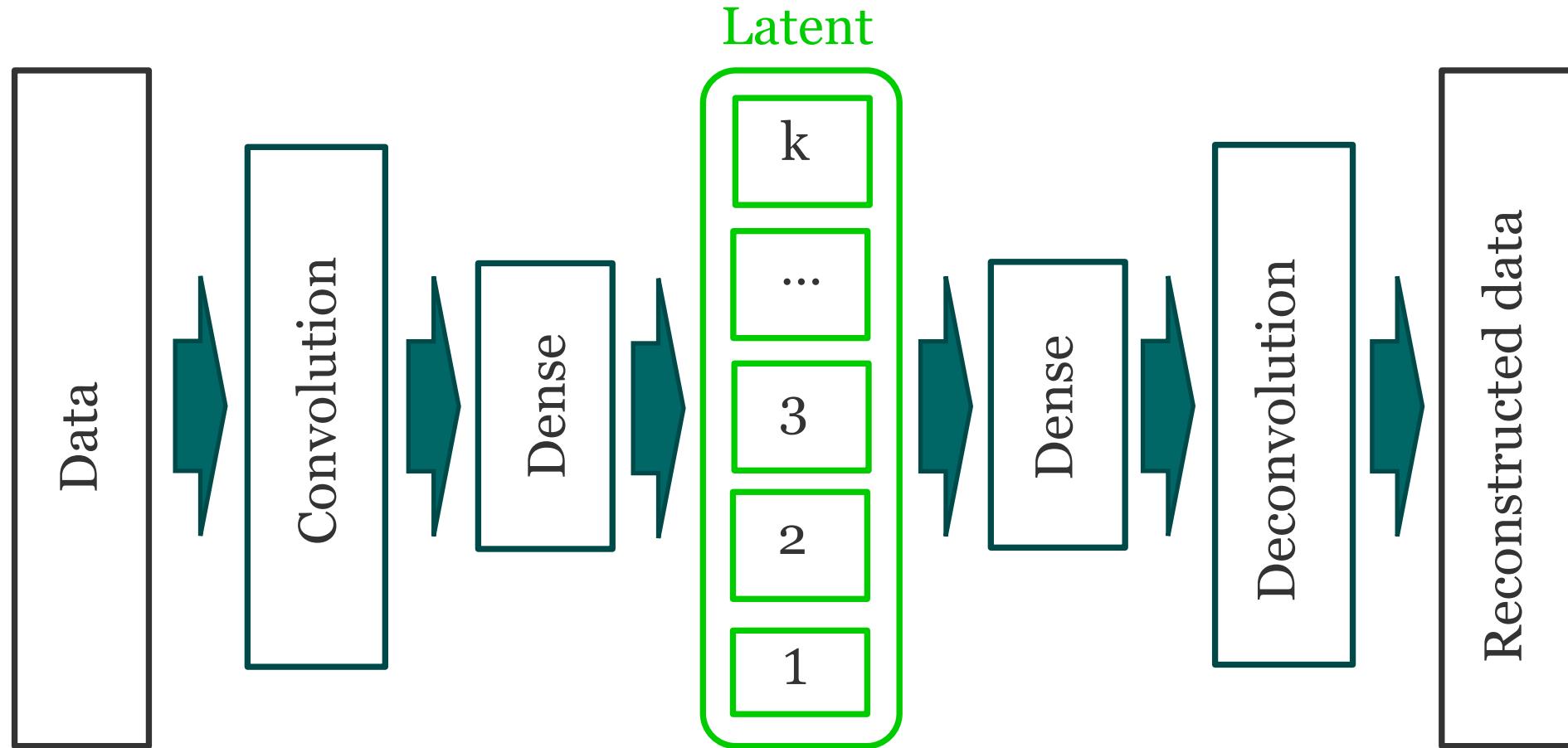
Class labels



z_2



Autoencoders



Loss: (some form of) reconstruction loss

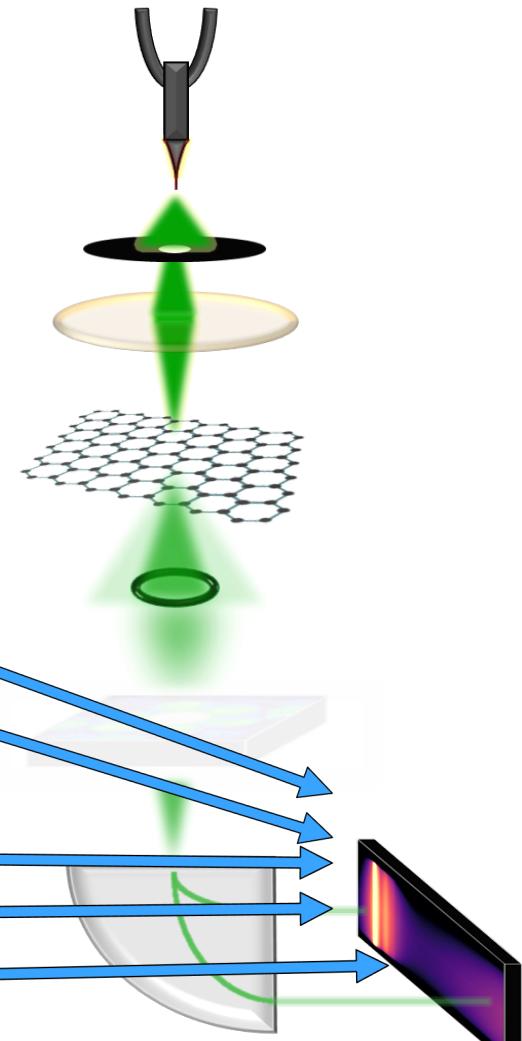
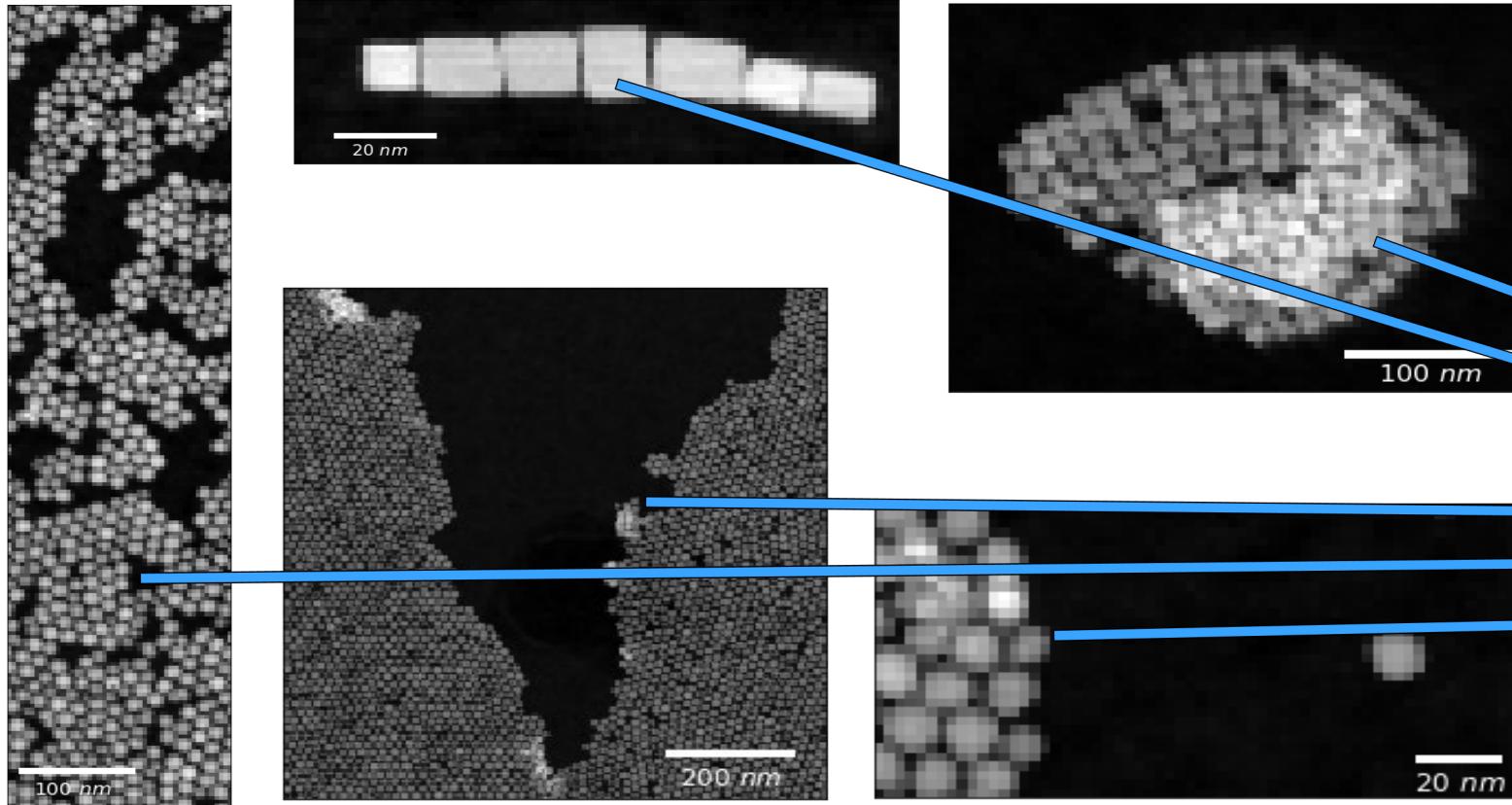
Do we have to encode and decode the same type of objects?

Examples of structure property relationships

- Molecular structure – optical spectroscopy
- Atomic configurations in catalysts – catalytic activity
- Protein sequence – geometry
- Photonic structure – optical adsorption
- Materials microstructure – dielectric/conductive properties
- Composite structure – electrochemical properties
- Antenna shape – emission characteristics
- ... and many more

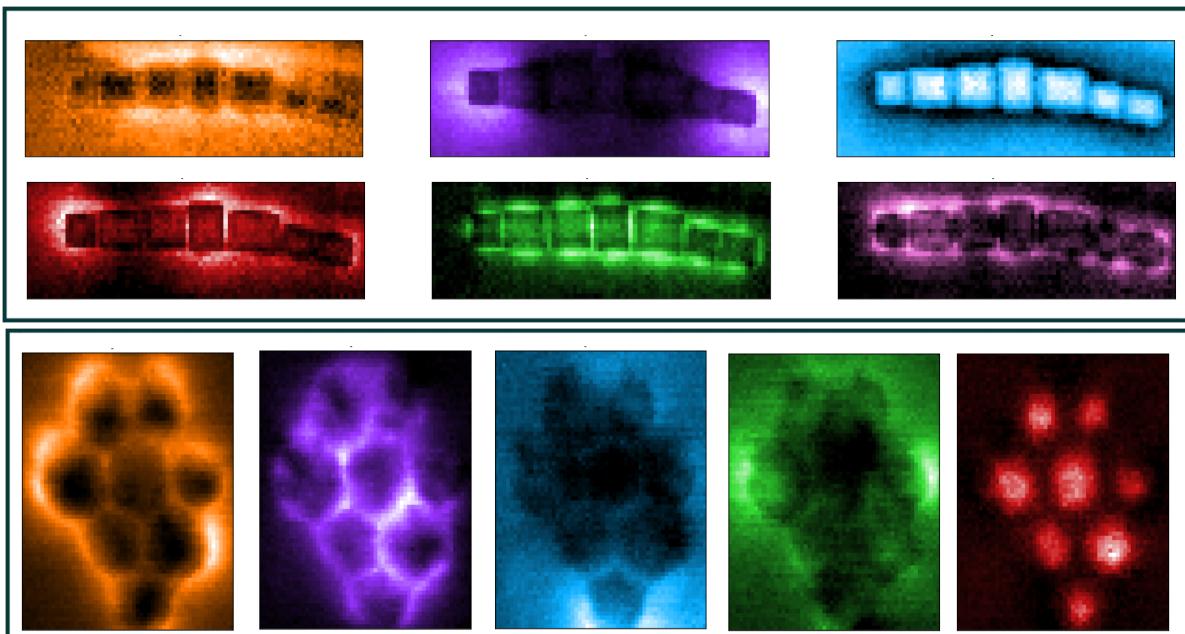
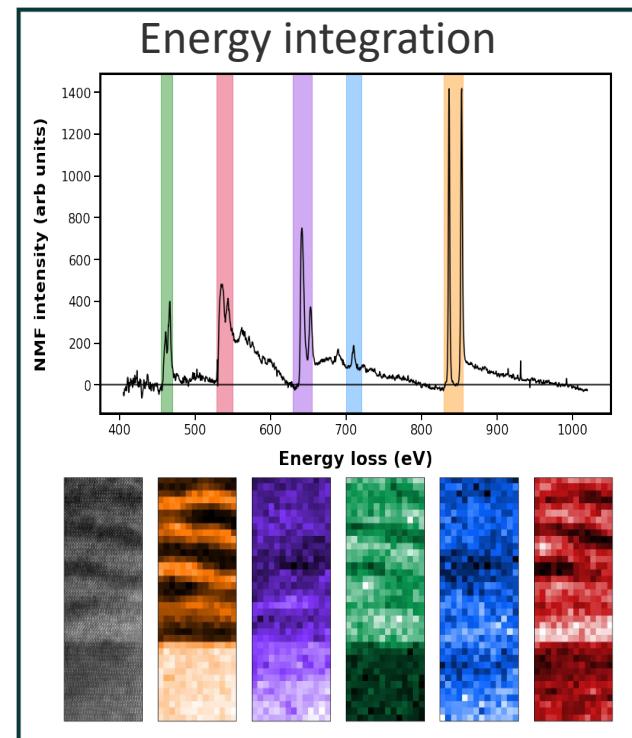
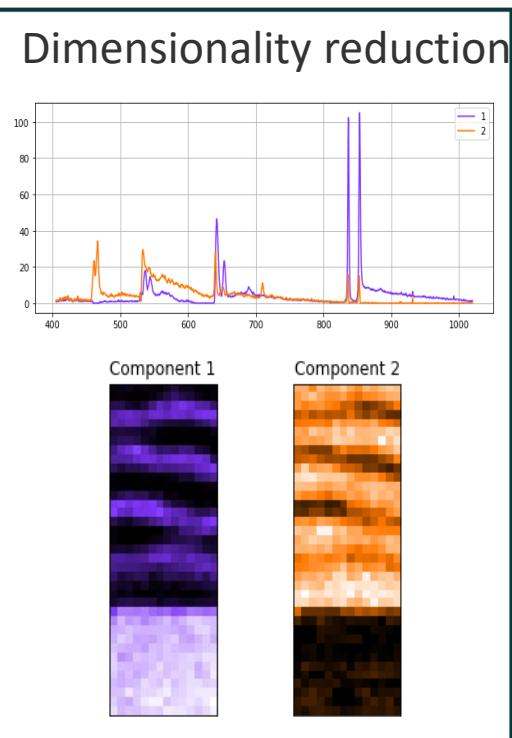
Practical Use Case: EELS

- Self-assembled monolayer of **metal oxide nanoparticles** (F,Sn co-doped indium oxide)
- **Sn** tunes the plasmon resonance by supply of additional e^- (F concentration fixed)
- Variety of geometric configurations also present

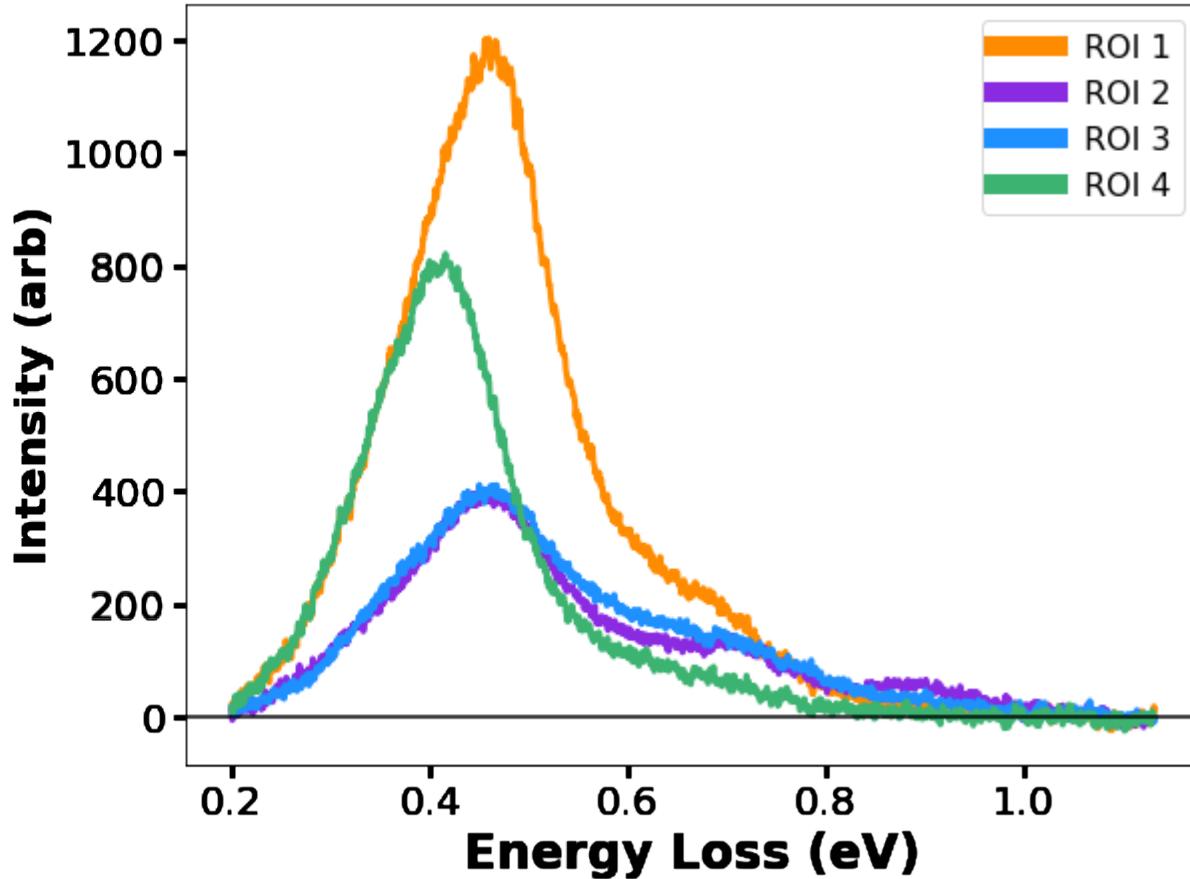
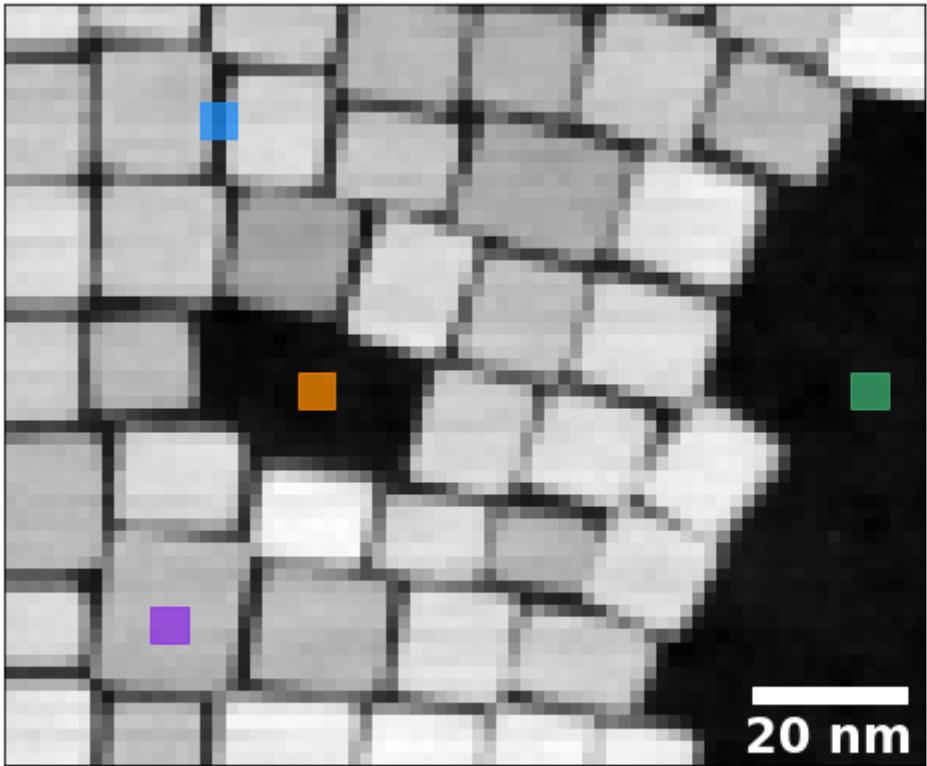


EELS

- Can consider to be another signal in the form of a **1D spectrum**
- Collect EEL spectrum in an (x,y) grid: EELS imaging
- To better visualize / understand these 3D signals, can integrate specific spectral bands, or dimensionally reduce (PCA, NMF) them
- Applications in plasmonics & nanophotonics



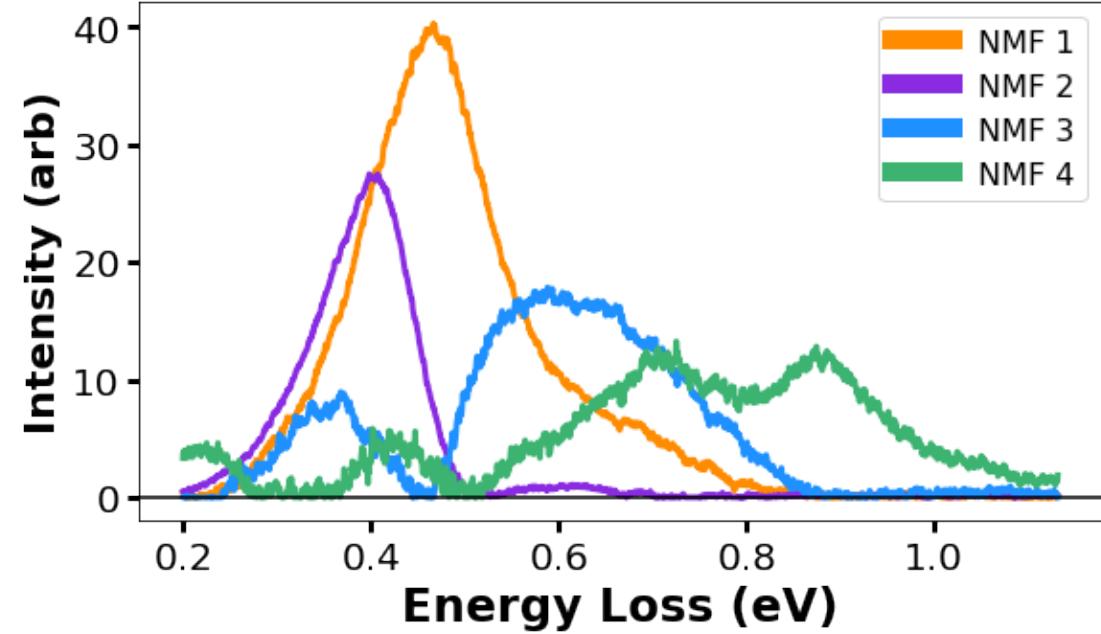
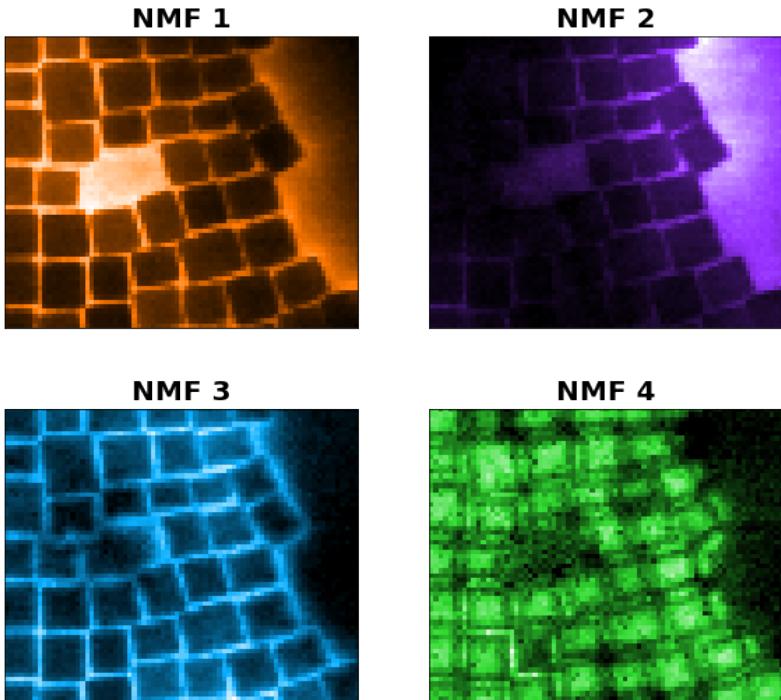
But what about the structure-property relations?



By inspection, we can note some characteristic aspects of spectra from specific types of geometries. However:

- How can we prove it and quantify this relationship?
- How universal is it for similar structures?
- Can we discover structures that will have the properties that we want?

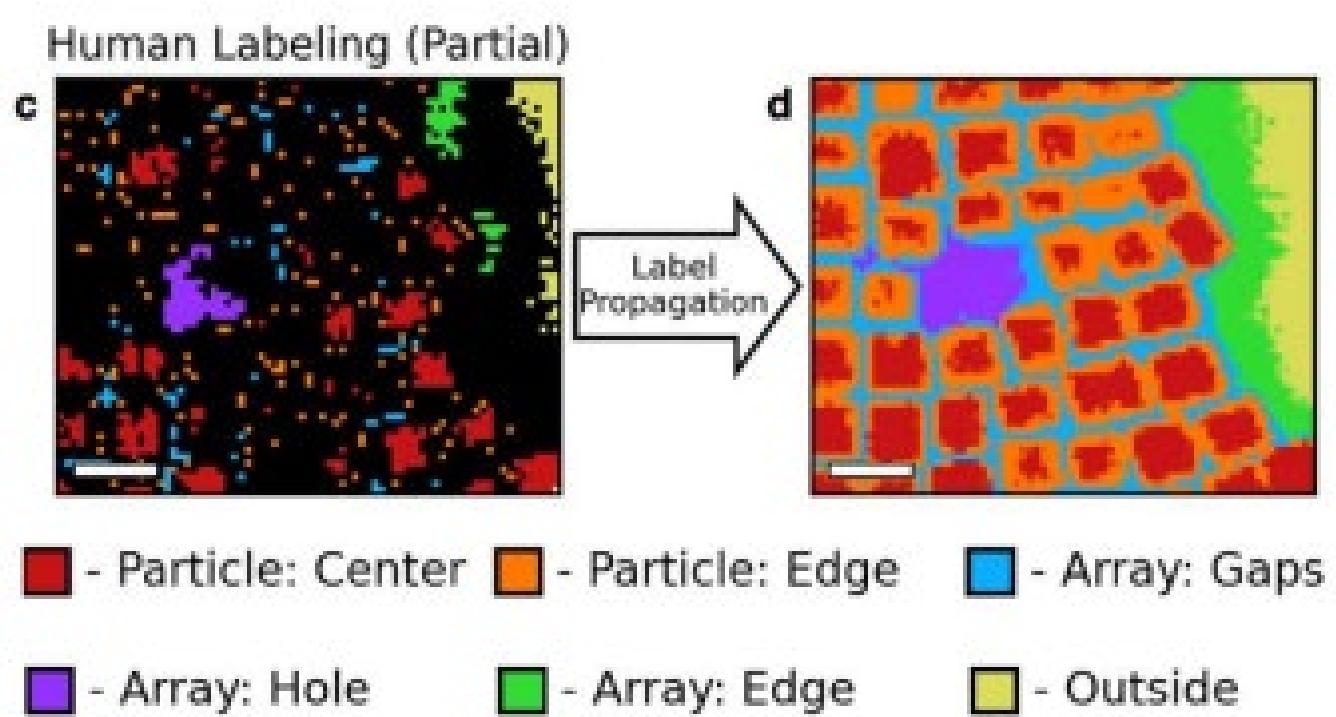
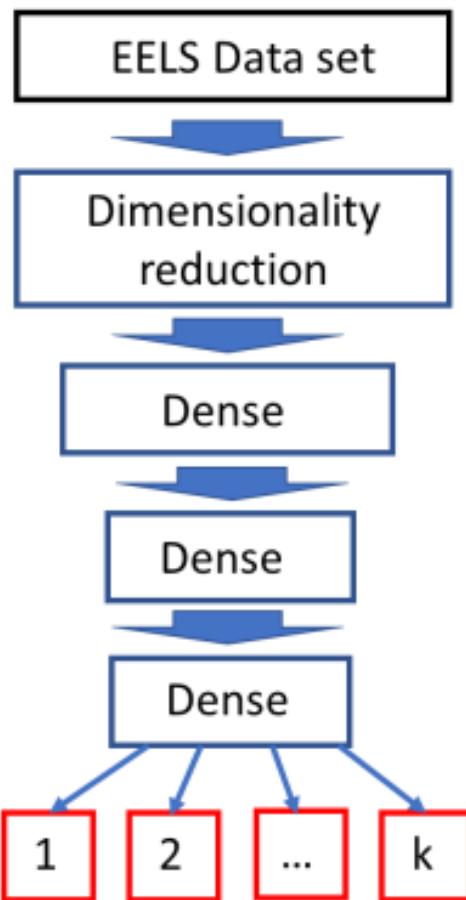
Exploratory data analysis



- Great way to explore system
- Visualization of hyperspectral data

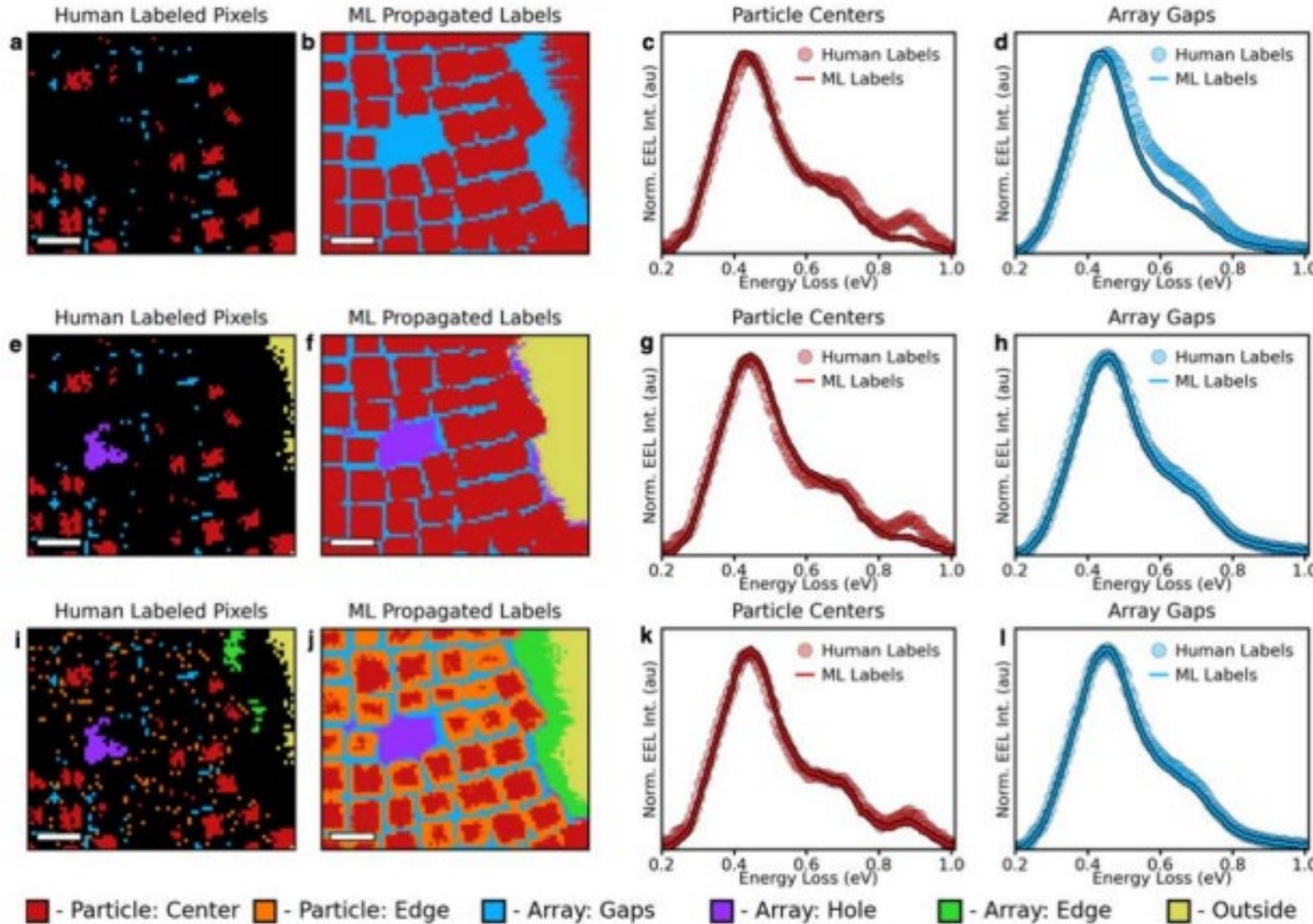
- Multiple modes per pixel
- Non-physical extraction
- No relationship with geometry established

Strategy 1: Labelling



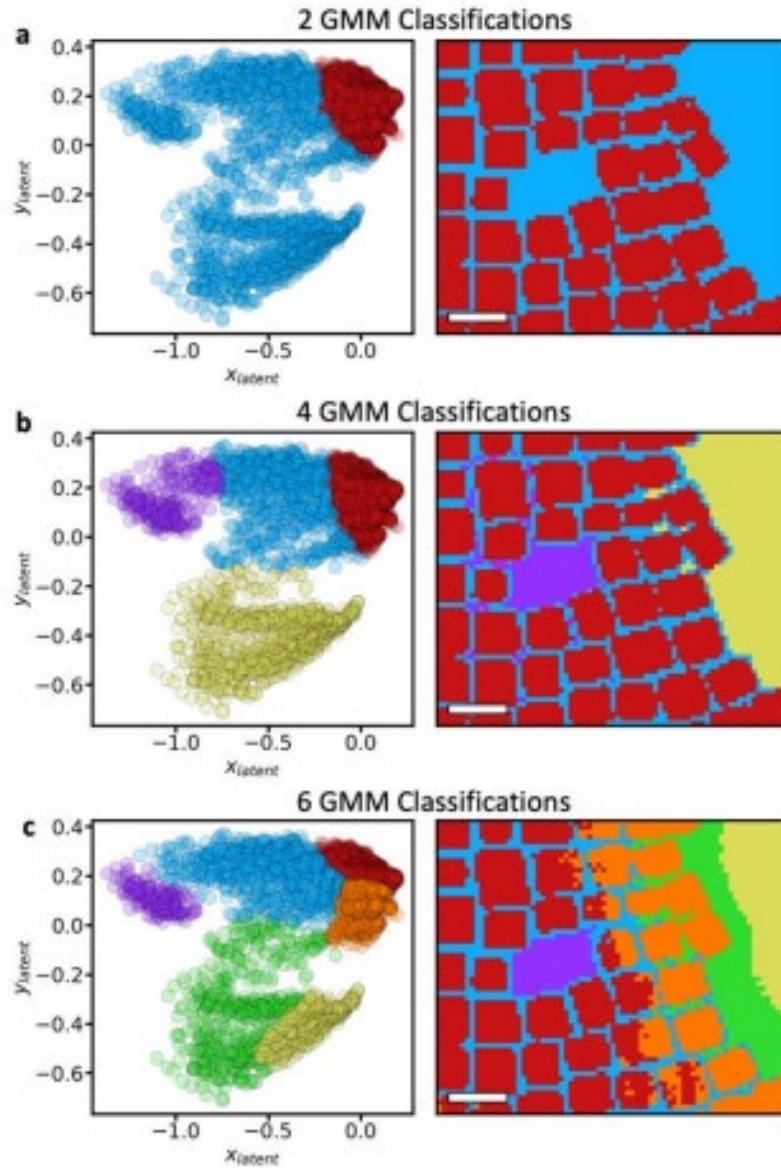
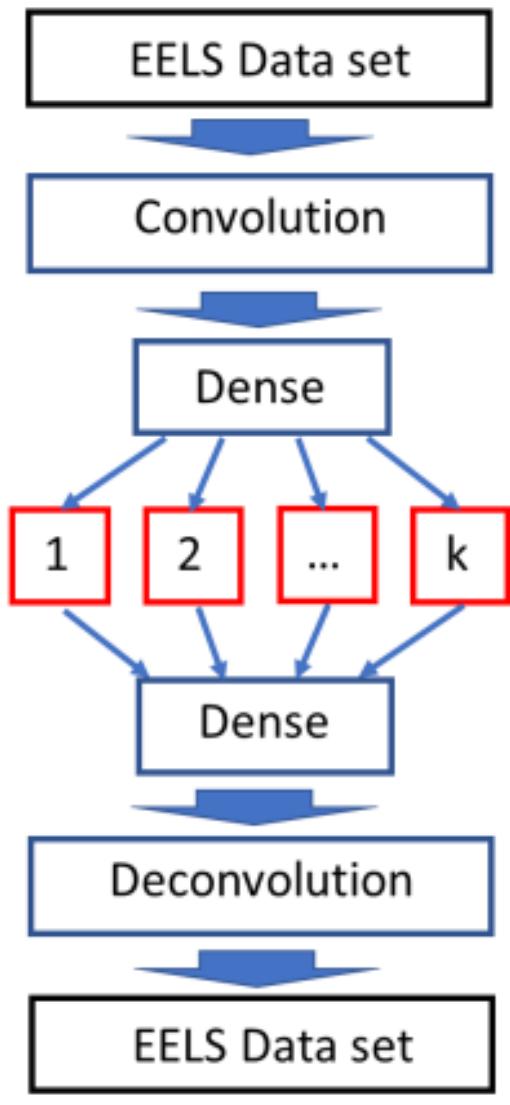
- Define attributes by semi-manual inspection
- Create training data set
- Train the classifier
- Apply the classifier to the remainder of the data set

Strategy 1: Labelling



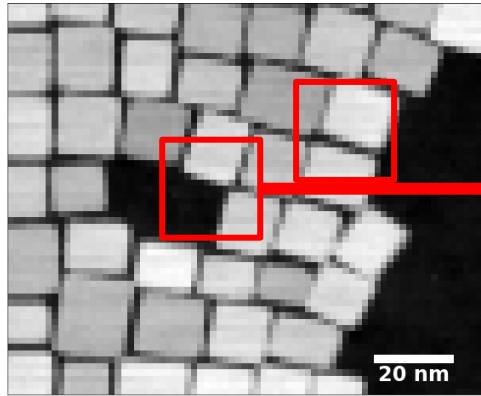
- Problem: human labels can be ambiguous

Strategy 2: AE Labels

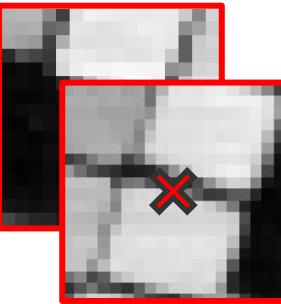


- Unsupervised learning on spectral data: we make conclusions based on maps

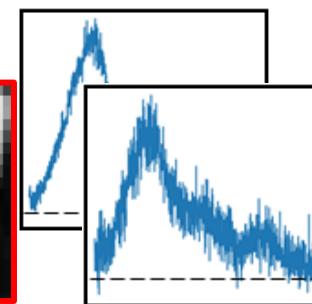
Strategy 3: im2spec



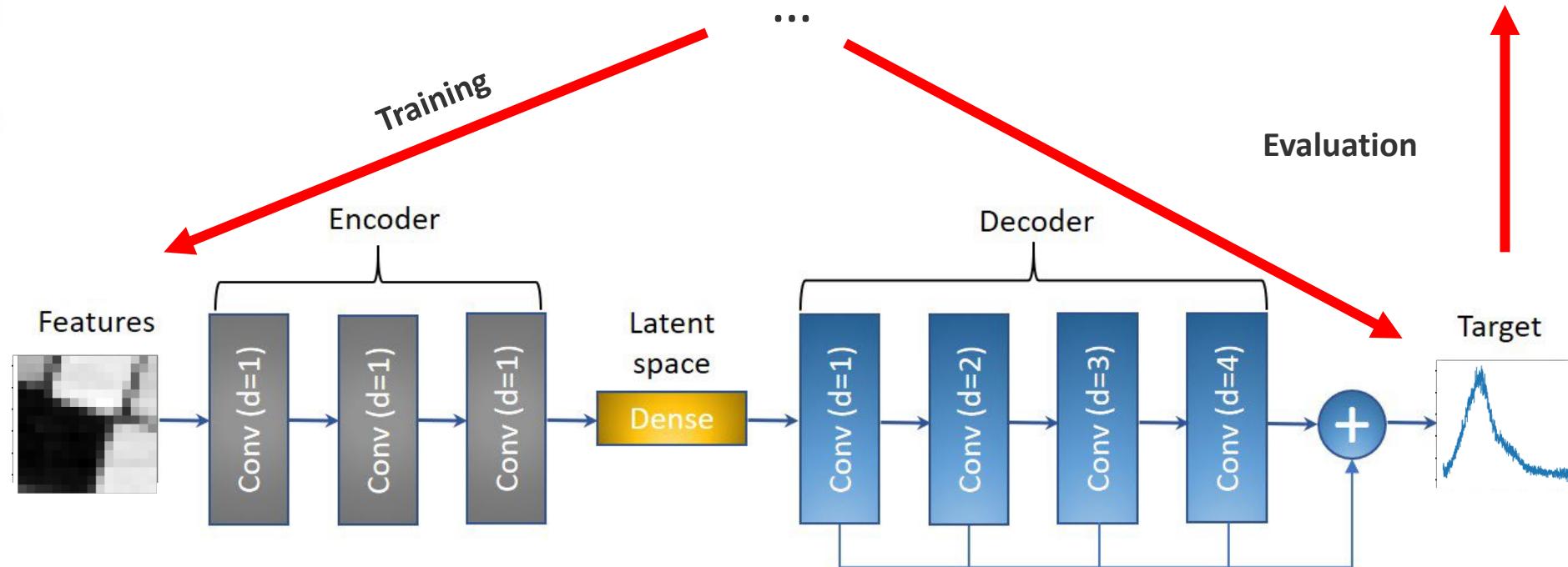
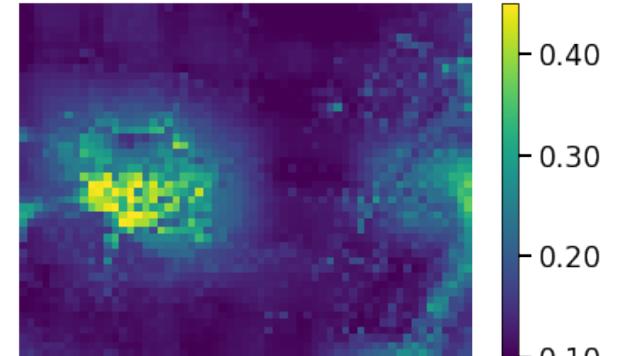
Spatial Descriptor



Spectral Descriptor

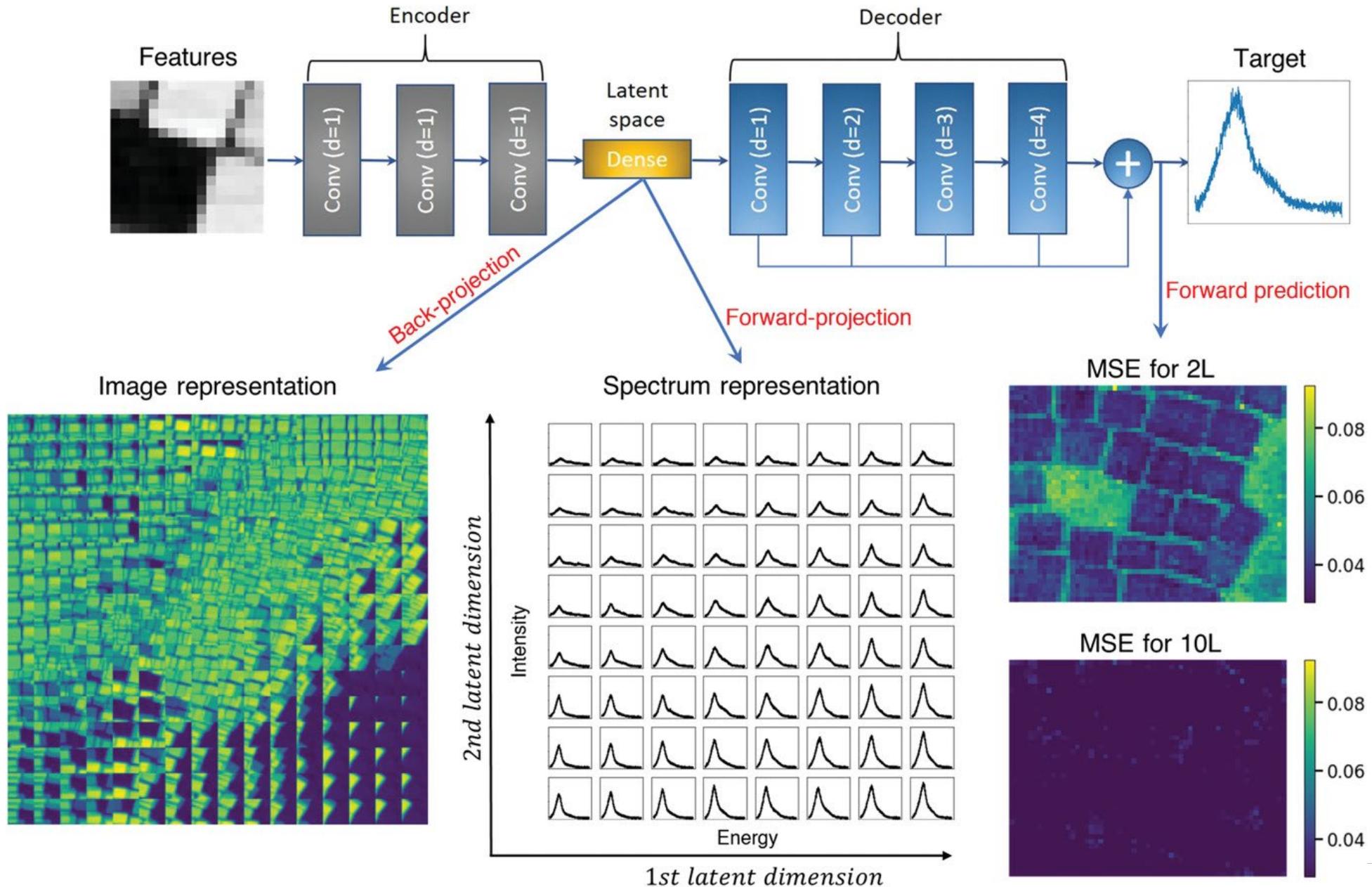


Uncertainty MSE

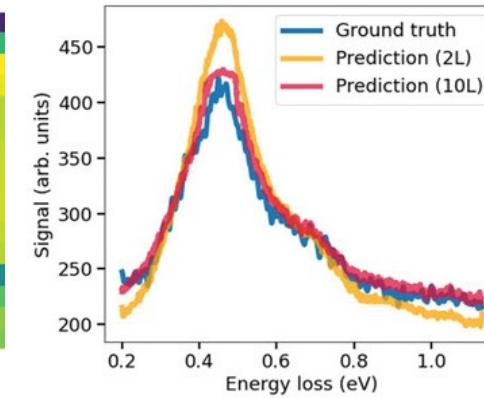
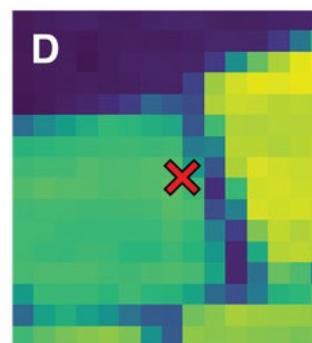
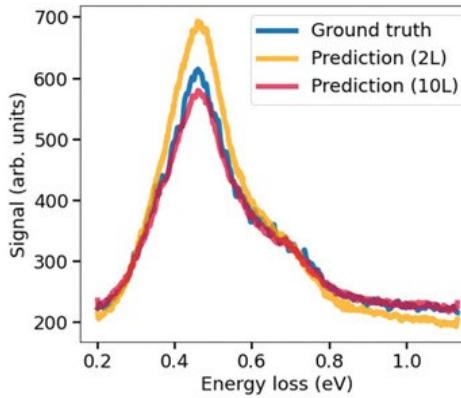
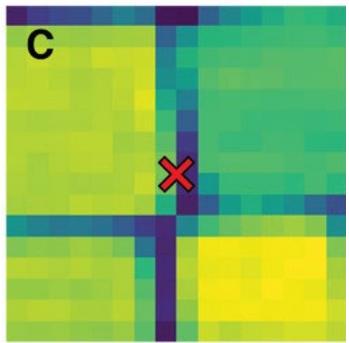
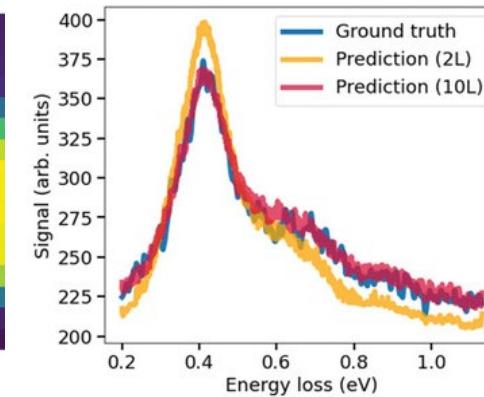
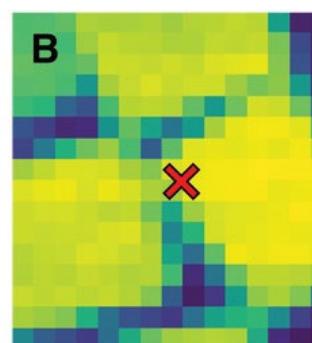
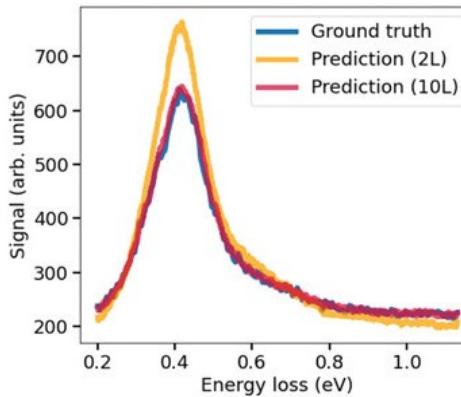
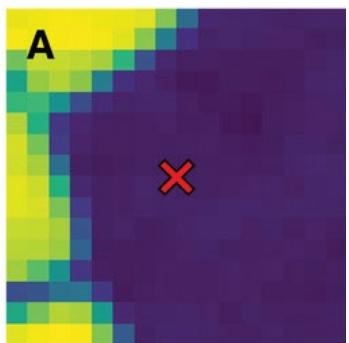


What if we create a network that encodes structure, and decodes spectra?

Im2spec: latent space visualization

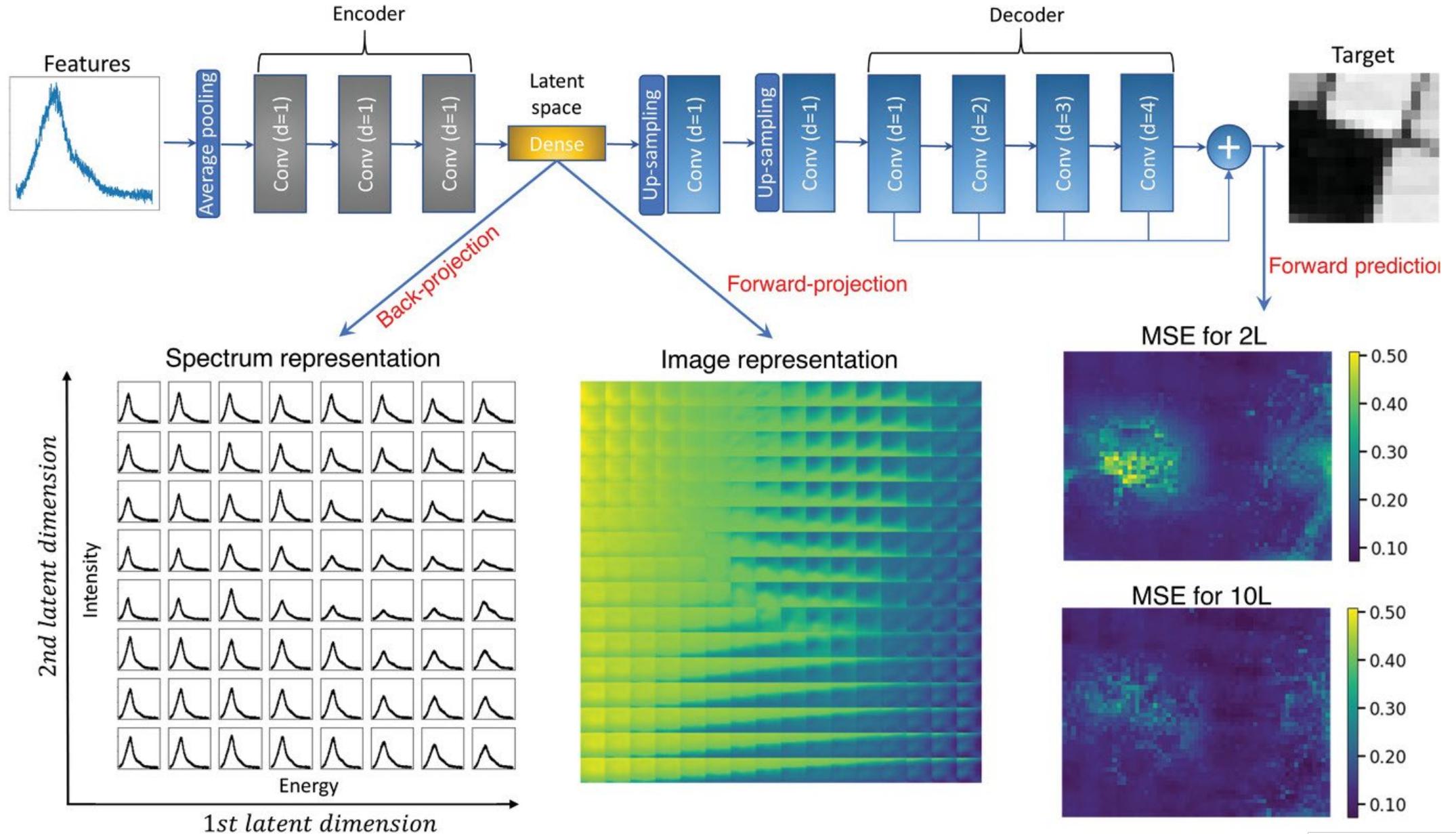


Im2spec prediction

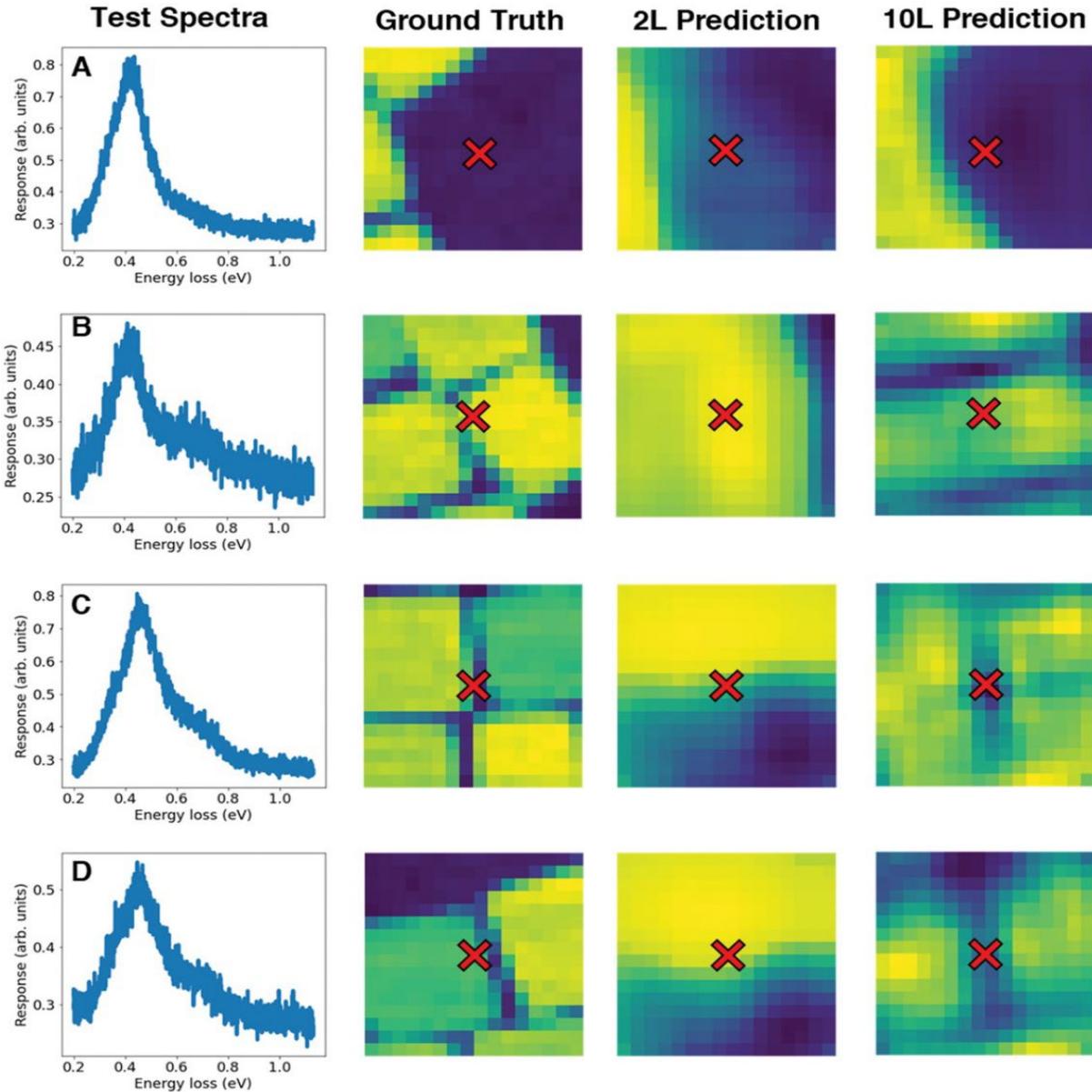


- After training, predict the spectral response of a geometric arrangement that the network has **never encountered**
- **Library** of geometric-plasmonic relationships
- Can be used for solution of inverse design in nanophotonics and other fields

Spec2im



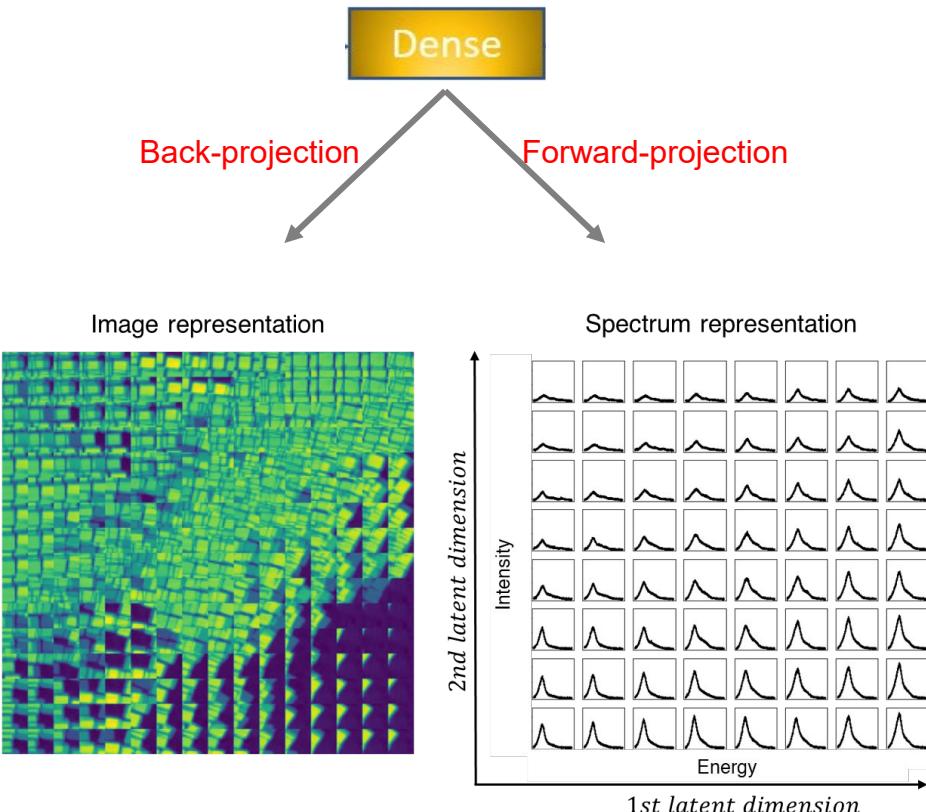
Spec2im predictions



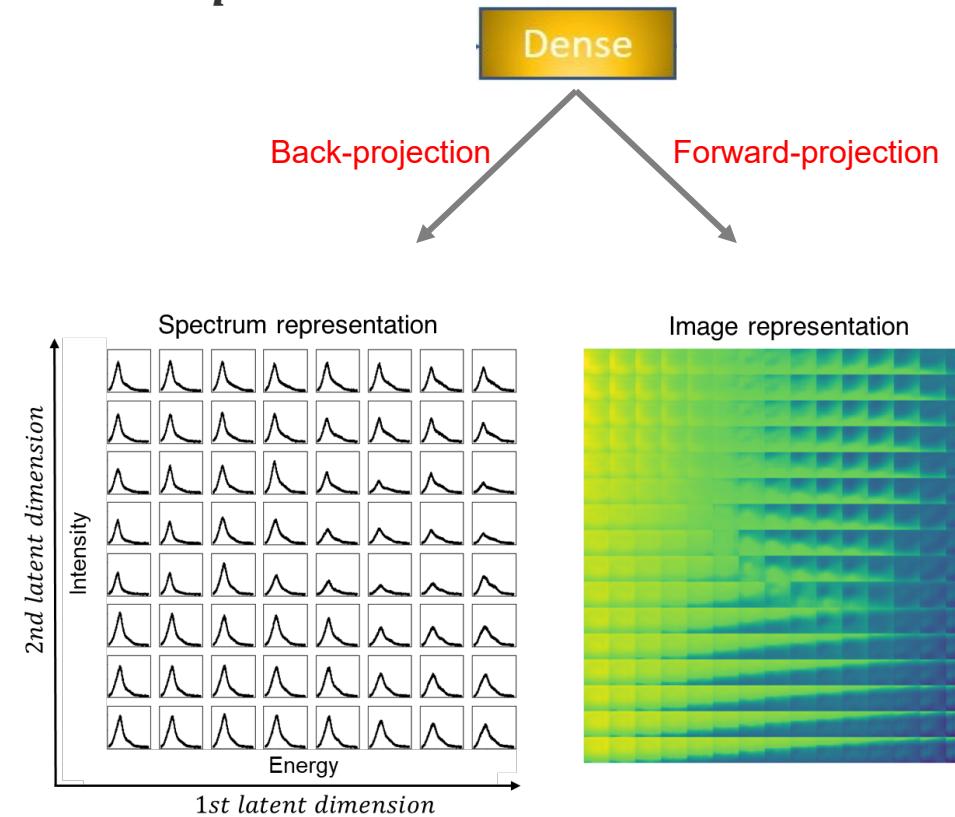
- After training, predict the spectral response of a geometric arrangement that the network has **never encountered**
- **2L** and **10L** refers to number of latent dimensions chosen

Spec2im and im2spec

"*im2spec*" Latent space



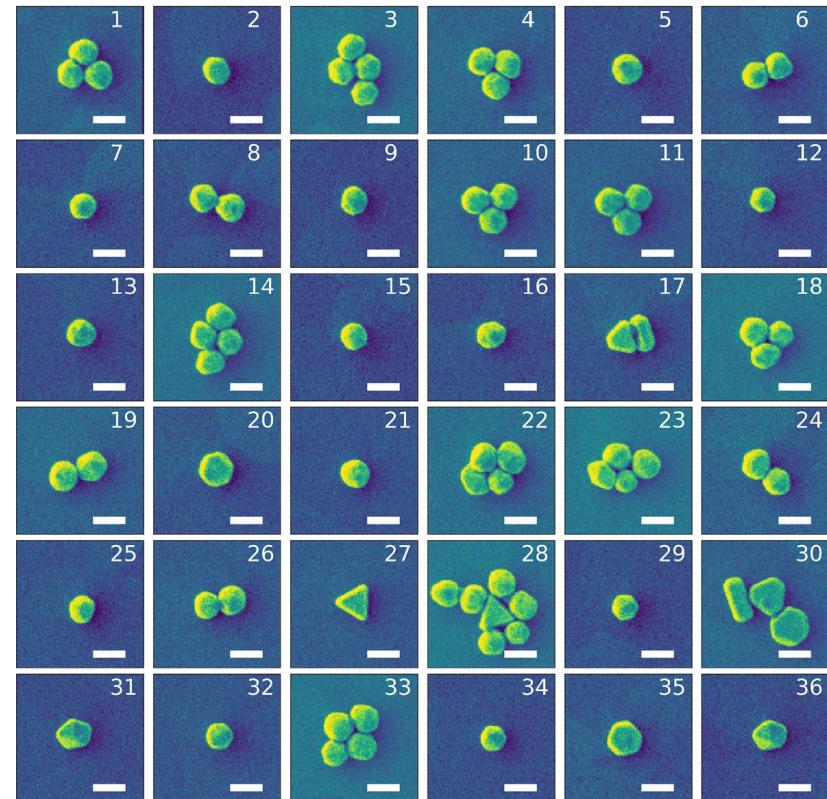
"*spec2im*" Latent space



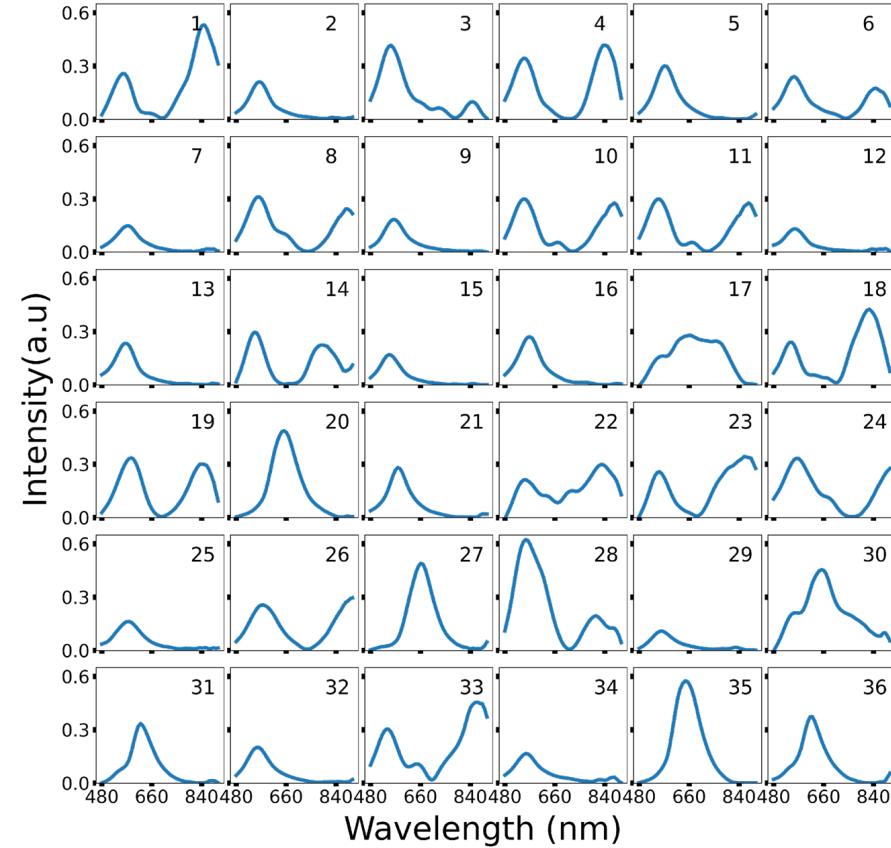
- Problem with *im2spec* and *spec2im*: they are generative only wrt. one transformation

Dual VAE: structure-property relationships

SEM images: “Structure Information”

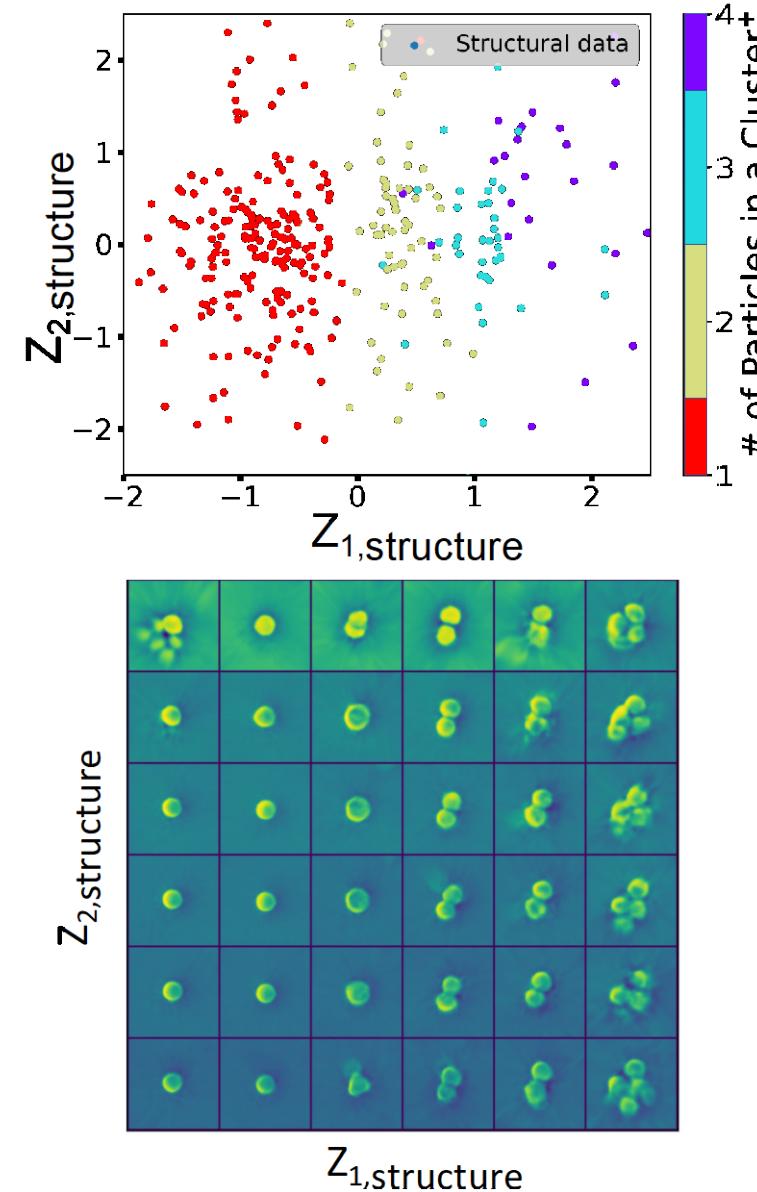
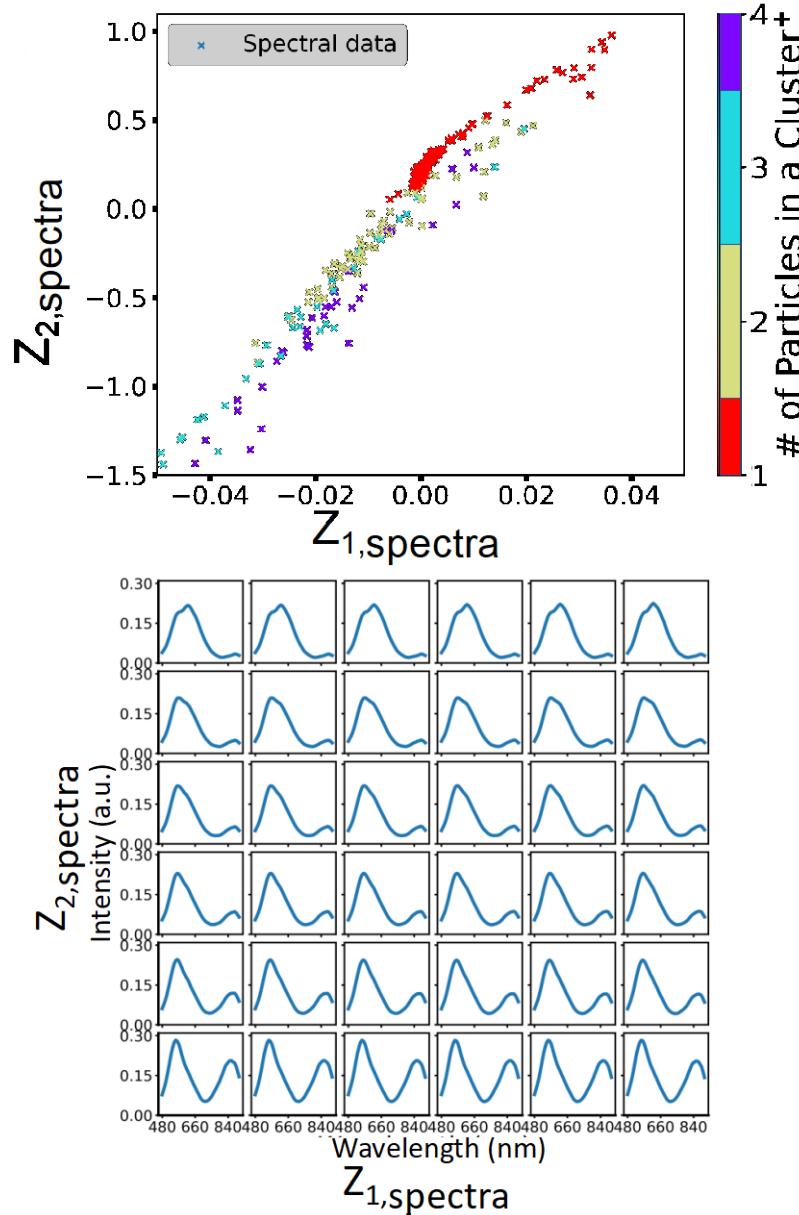


Hyperspectral microscope: “Property Information”

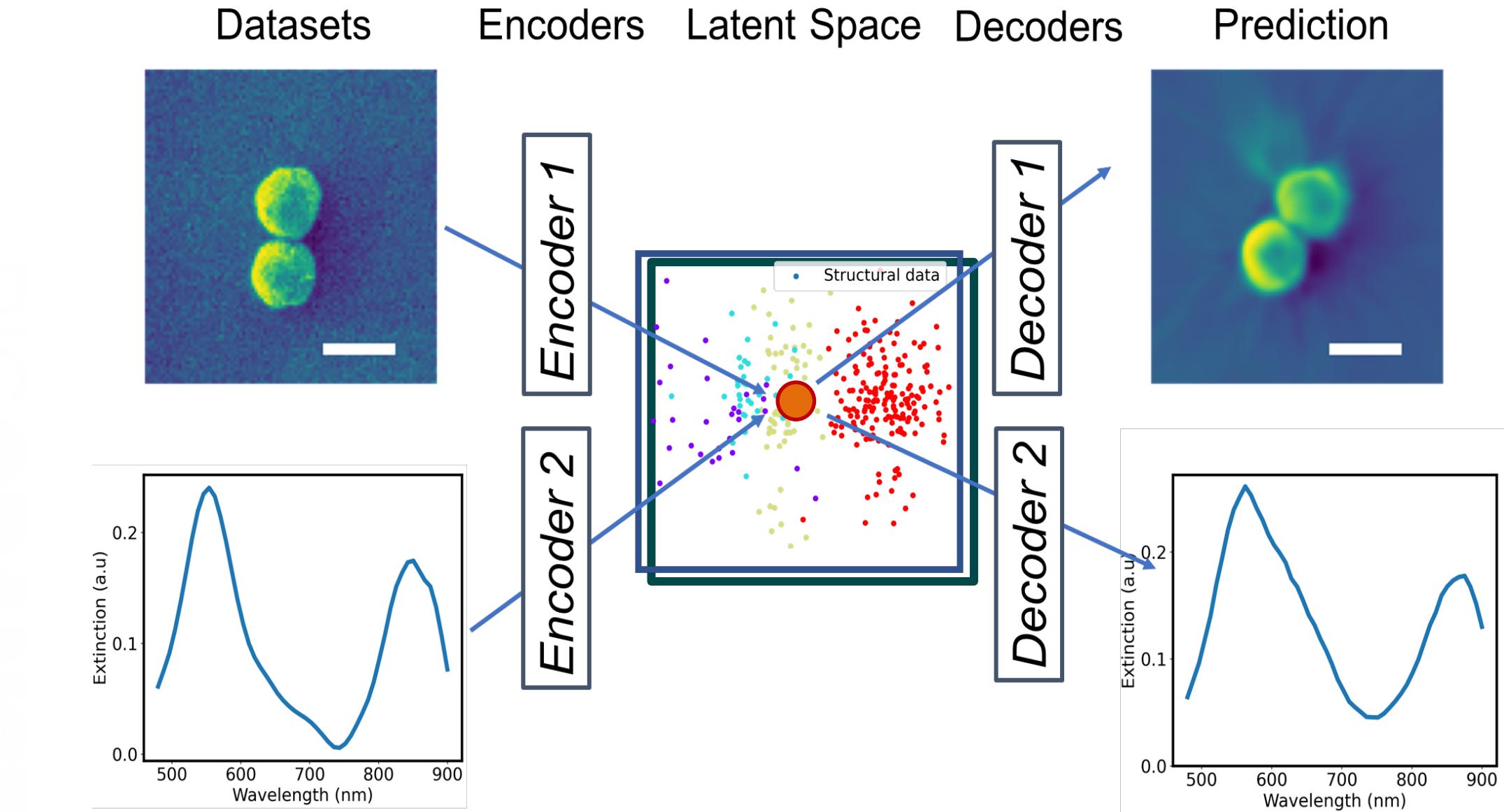


- Far field optical spectroscopy: images and spectra
- Here, we also have simple labels (number of clusters)

Separated VAE

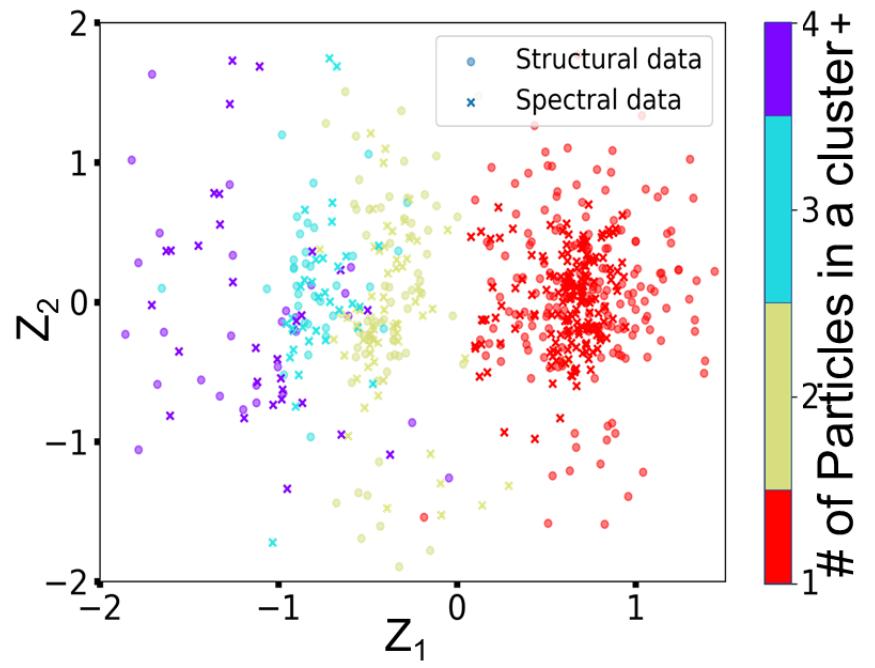


Dual VAE



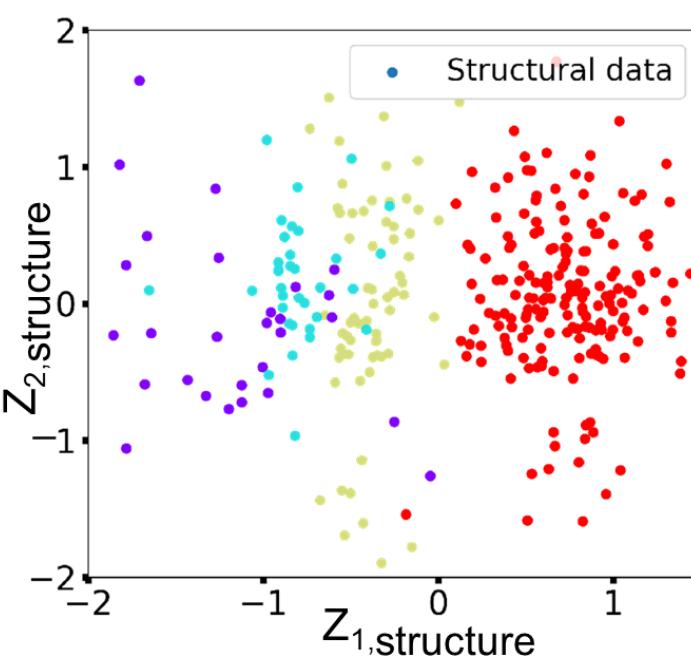
Dual VAE: Latent Distributions

“Dual Latent Space”

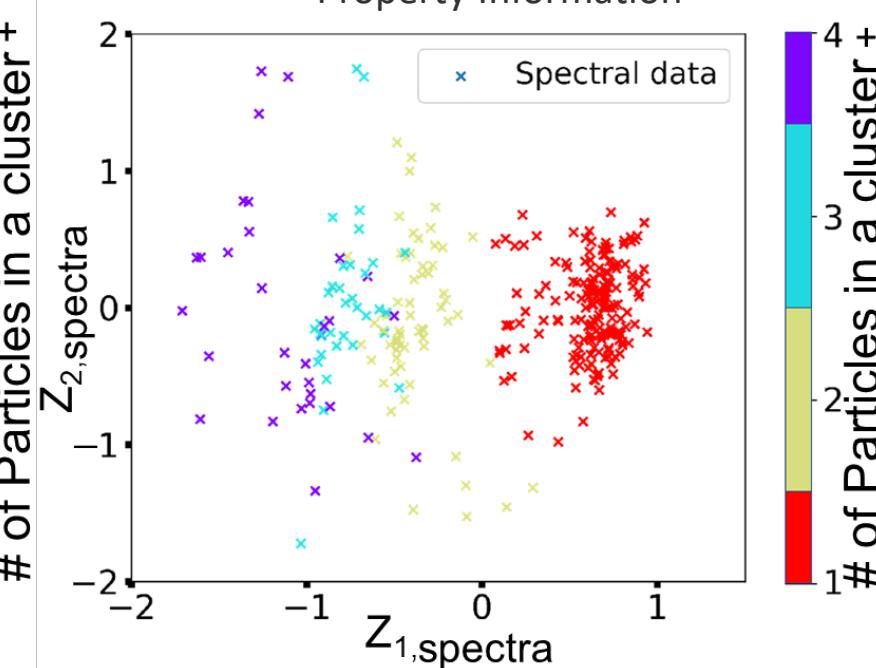


Latent Space Representation

“Structure Information”

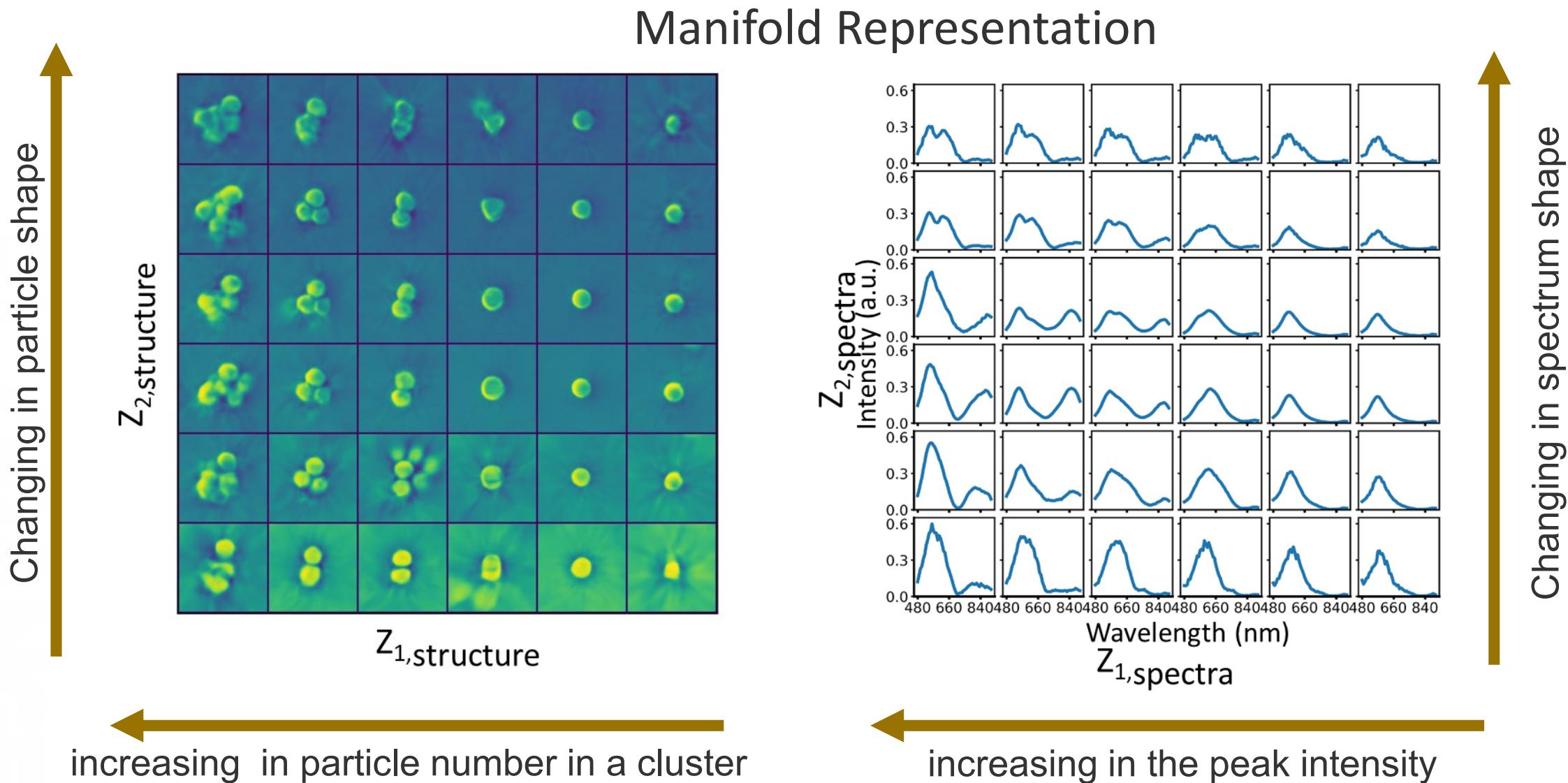


“Property Information”



of Particles in a cluster +

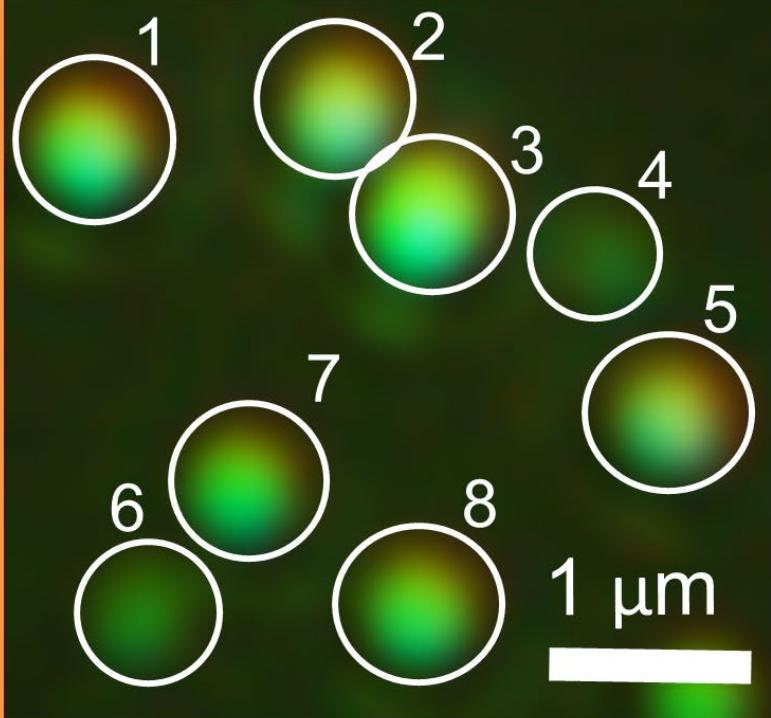
Dual VAE: Latent Representations



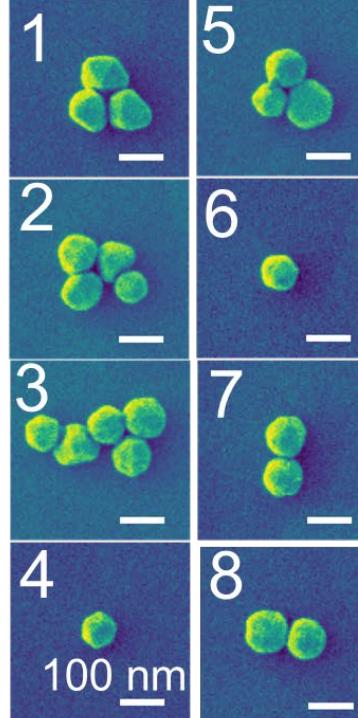
Dual VAE: Predictions

Example

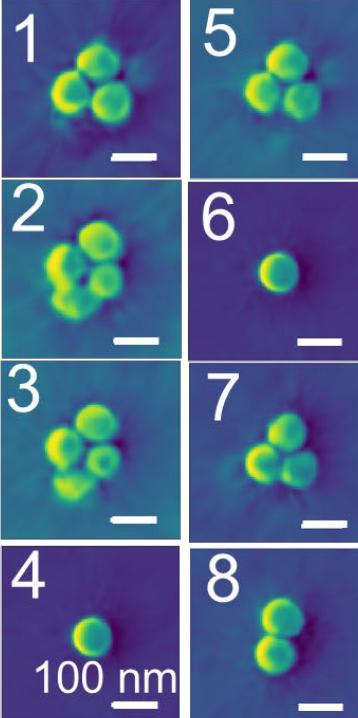
Darkfield Image



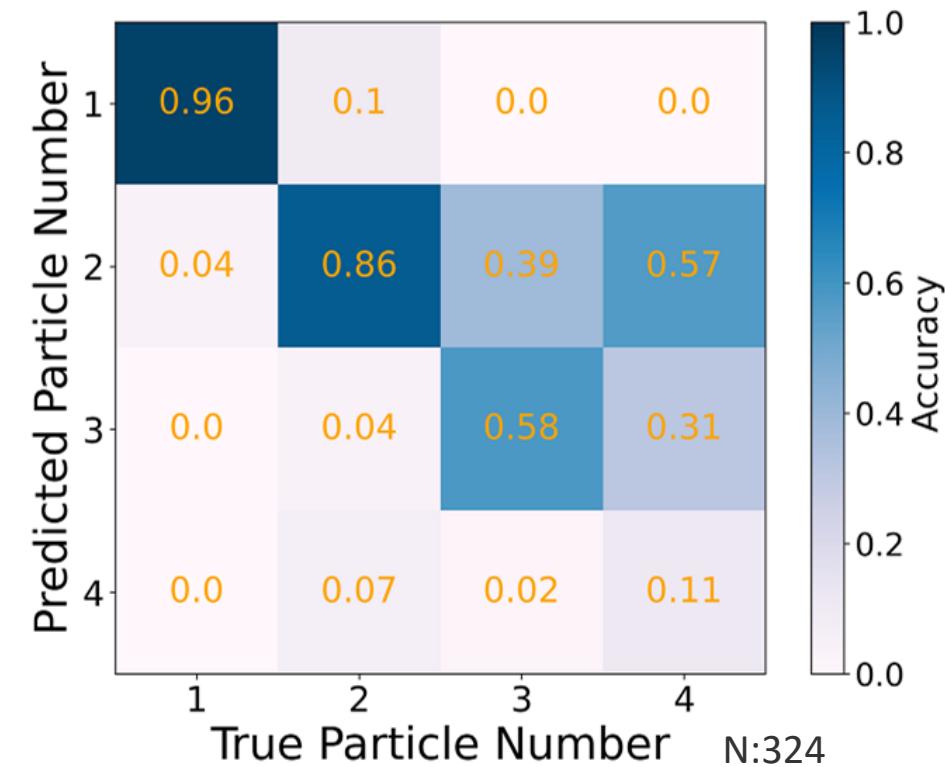
Ground Truth



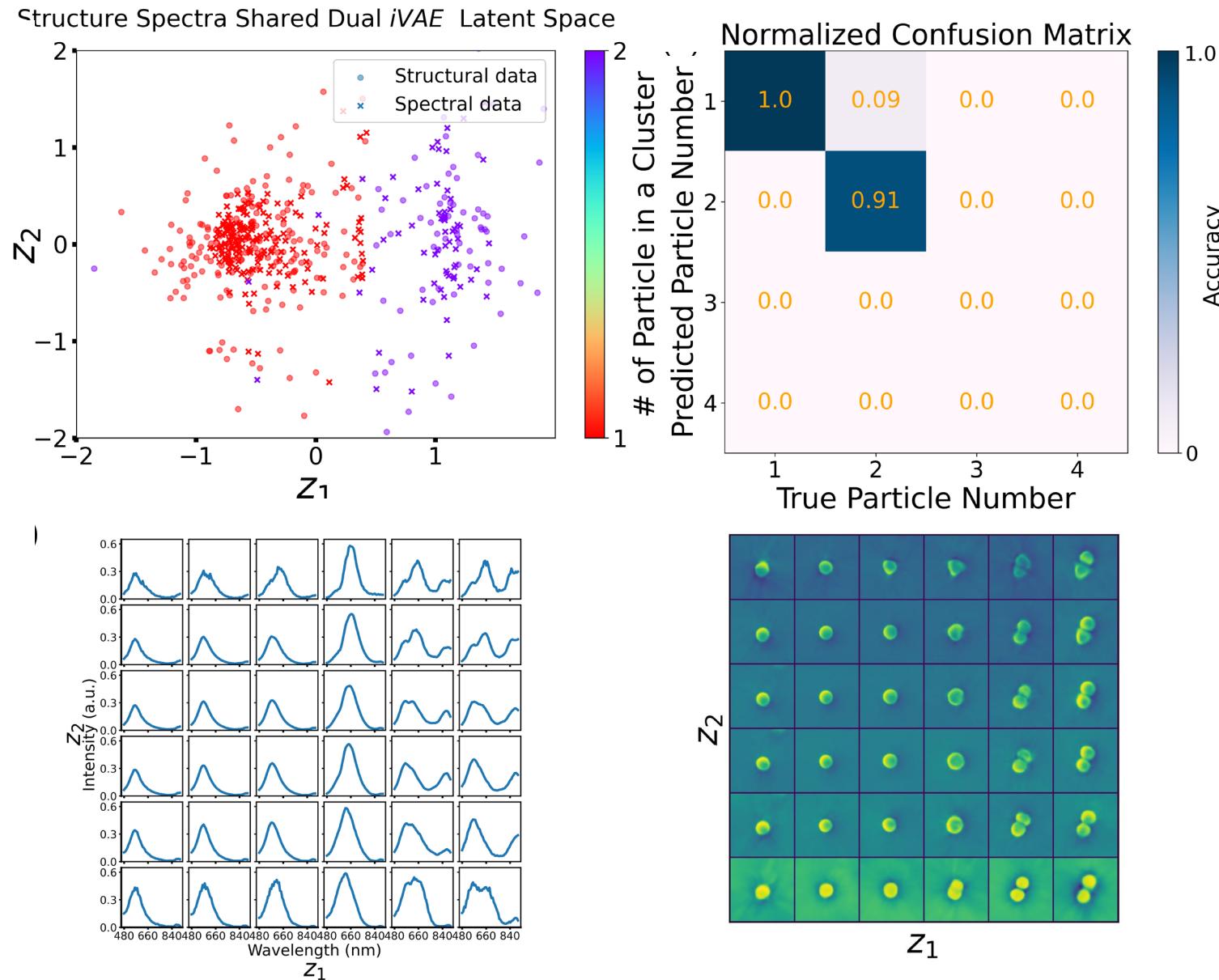
Prediction



Overall Particles



Dual VAE: Predictions for only 1 and 2 mers



Questions to ask when using ML

Data science:

- What is the dimensionality of feature and target spaces
- How variable are the features in these spaces ([VAE can help](#))
- How much data do I have?

Domain knowledge:

- How predictive do I expect this relationship to be
- What other factors matter from materials side
- Can measurements introduce additional factors of variance?

Experiment planning:

- How much data can I have?
- Is it a static learning problem, or am I interested in ML-assisted experiment?