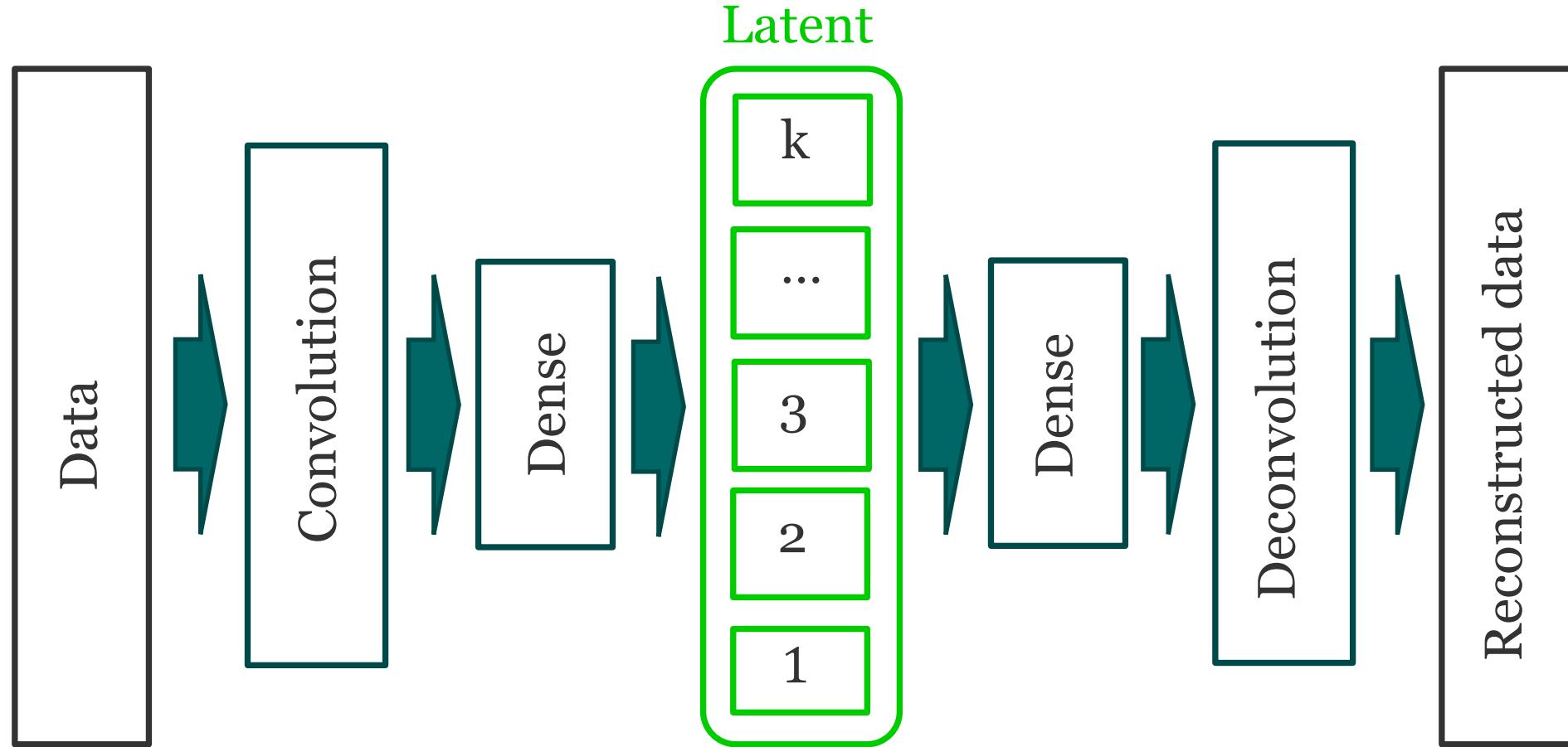


Lecture 22: Simple and Variational Autoencoders

Instructor: Sergei V. Kalinin

Autoencoders



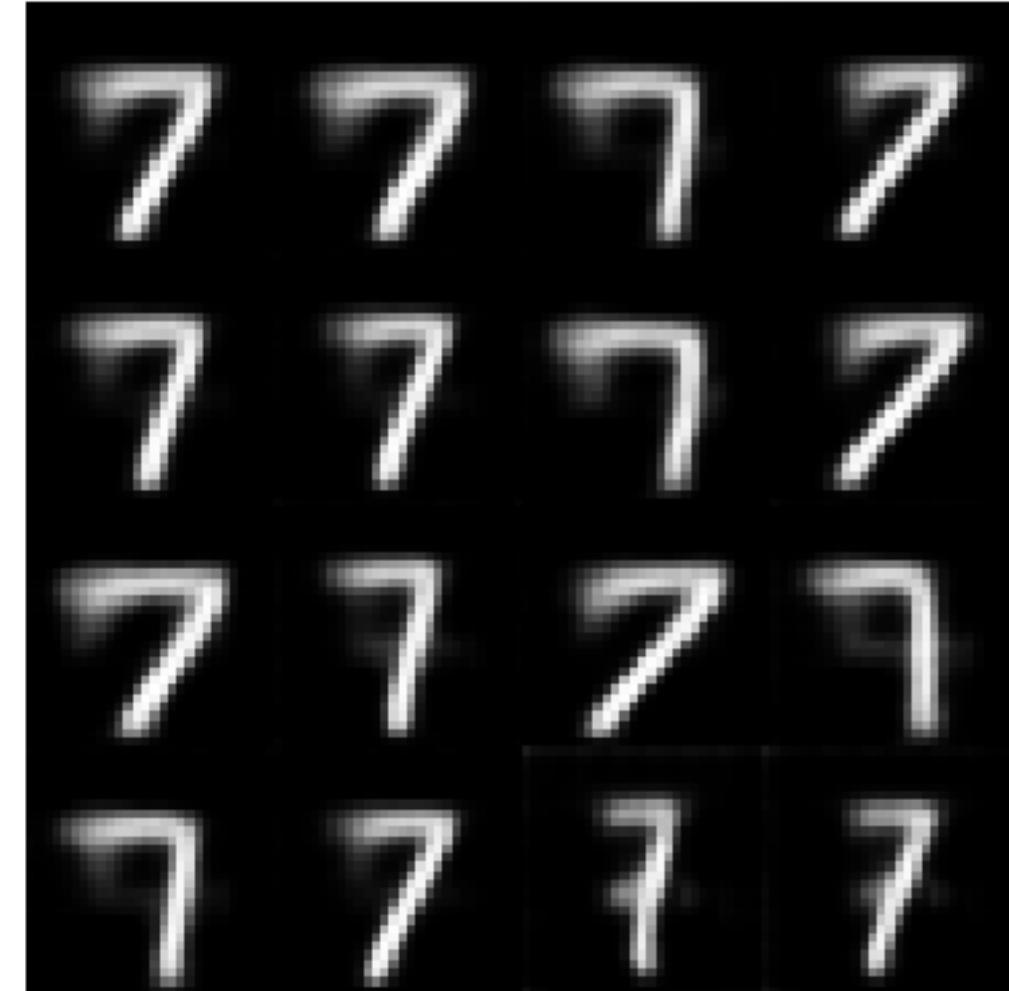
Loss: reconstruction loss

The AE reconstructs data

Input data



Decoded data



Why are AE important?



Geoffrey Hinton

Emeritus Prof. Comp Sci, U.Toronto & Engineering Fellow, Google

Verified email at cs.toronto.edu - [Homepage](#)

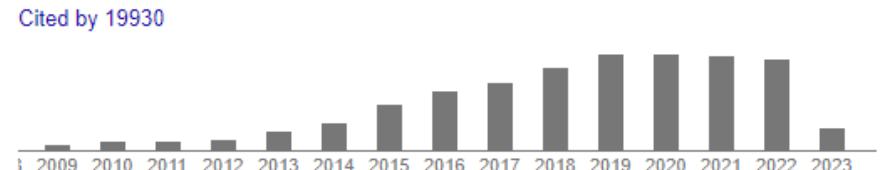
machine learning psychology artificial intelligence cognitive science computer science

FOLLOW

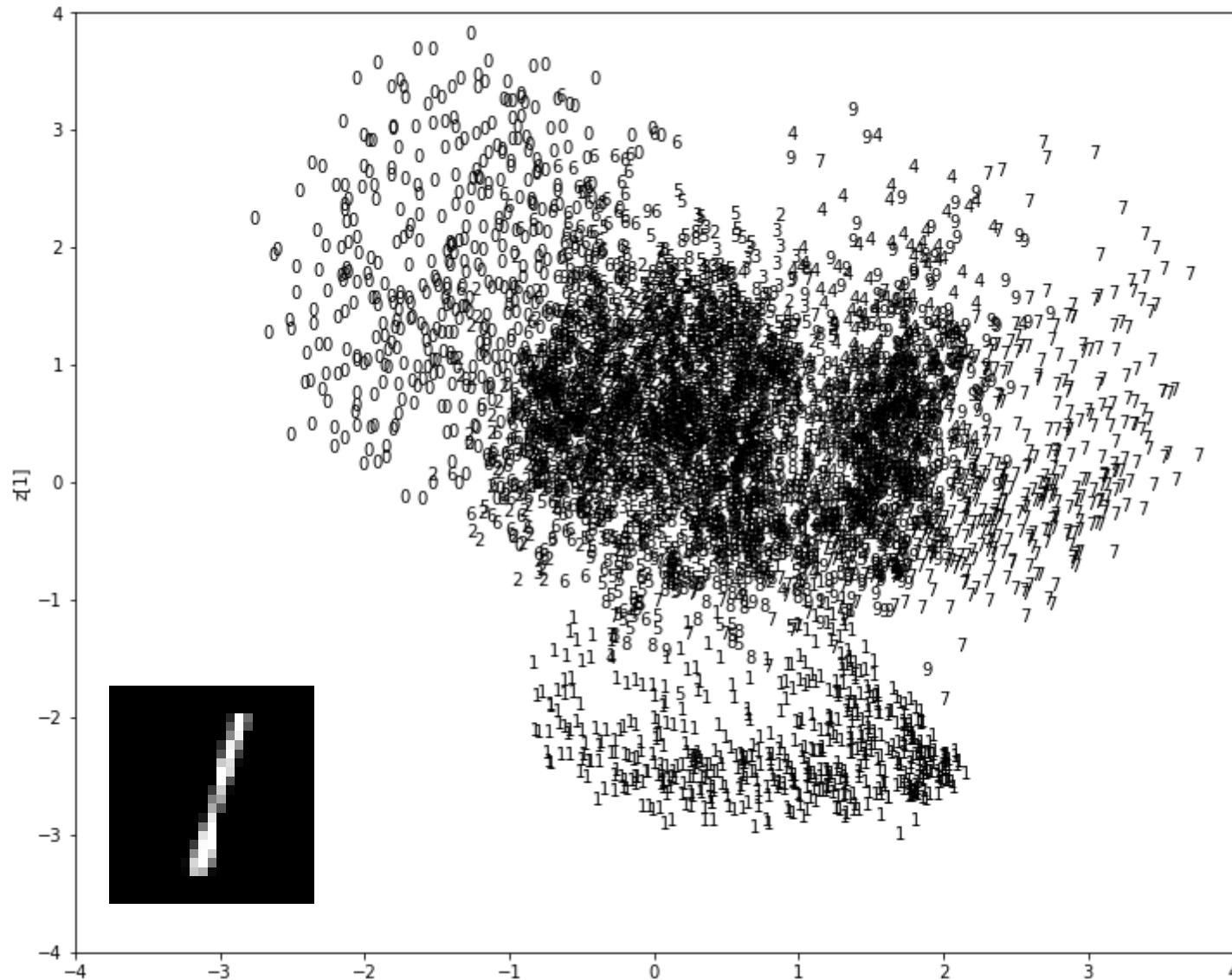
TITLE	CITED BY	YEAR
Imagenet classification with deep convolutional neural networks A Krizhevsky, I Sutskever, GE Hinton Communications of the ACM 60 (6), 84-90	130318	2017
Deep learning Y LeCun, Y Bengio, G Hinton Nature 521 (7553), 436-44	62790	2015
Dropout: a simple way to prevent neural networks from overfitting N Srivastava, G Hinton, A Krizhevsky, I Sutskever, R Salakhutdinov The journal of machine learning research 15 (1), 1929-1958	42078	2014
Visualizing data using t-SNE L van der Maaten, G Hinton Journal of Machine Learning Research 9 (Nov), 2579-2605	35035	2008
Learning representations by back-propagating errors DE Rumelhart, GE Hinton, RJ Williams Nature 323 (6088), 533-536	32239	1986
Learning internal representations by error-propagation DE Rumelhart, GE Hinton, RJ Williams Parallel Distributed Processing: Explorations in the Microstructure of ...	30711	1986
Schemata and sequential thought processes in PDP models. D Rumelhart, P Smolensky, J McClelland, G Hinton Parallel distributed processing: Explorations in the microstructure of ...	28073 *	1986
Learning multiple layers of features from tiny images A Krizhevsky, G Hinton	21876	2009
Rectified linear units improve restricted boltzmann machines V Nair, GE Hinton Proceedings of the 27th international conference on machine learning (ICML ...	21050	2010
Reducing the dimensionality of data with neural networks GE Hinton, RR Salakhutdinov Science 313 (5786), 504-507	19930	2006

Reducing the dimensionality of data with neural networks

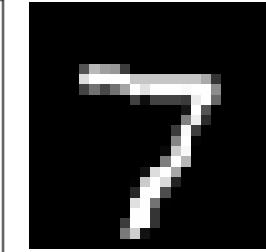
Authors	Geoffrey E Hinton, Ruslan R Salakhutdinov
Publication date	2006/7/28
Journal	Science
Volume	313
Issue	5786
Pages	504-507
Publisher	American Association for the Advancement of Science
Description	High-dimensional data can be converted to low-dimensional codes by training a multilayer neural network with a small central layer to reconstruct high-dimensional input vectors. Gradient descent can be used for fine-tuning the weights in such "autoencoder" networks, but this works well only if the initial weights are close to a good solution. We describe an effective way of initializing the weights that allows deep autoencoder networks to learn low-dimensional codes that work much better than principal components analysis as a tool to reduce the dimensionality of data.



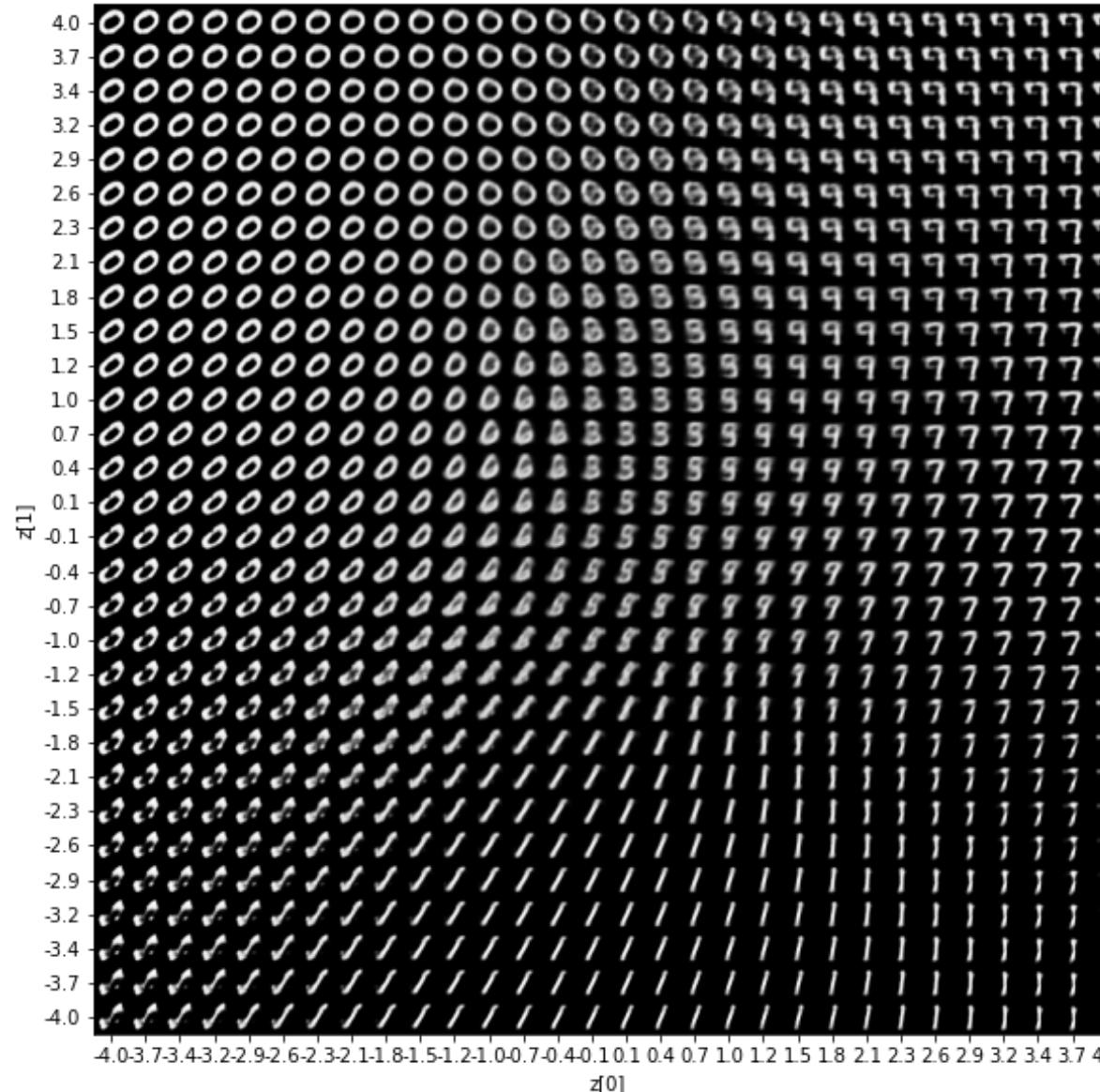
Encoding: Image → Latent Space



Latent distribution: Encoding the data via low dimensional vector



Decoding: Latent Space → Image



Latent representation: Decoding images from uniform grid in latent space

Image Reconstruction

Test color images (Ground Truth)



Test gray images (Input)



Image Reconstruction

Test color images (Ground Truth)



Colorized test images (Predicted)

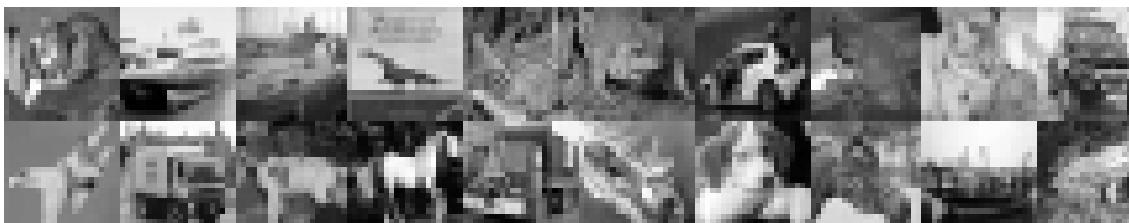


Image Reconstruction

Test color images (Ground Truth)



Test gray images (Input)



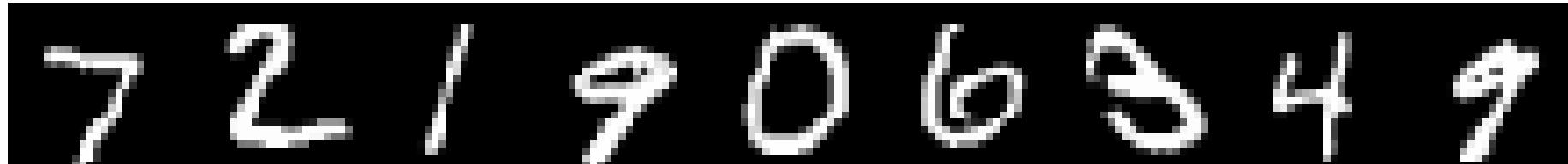
Colorized test images (Predicted)



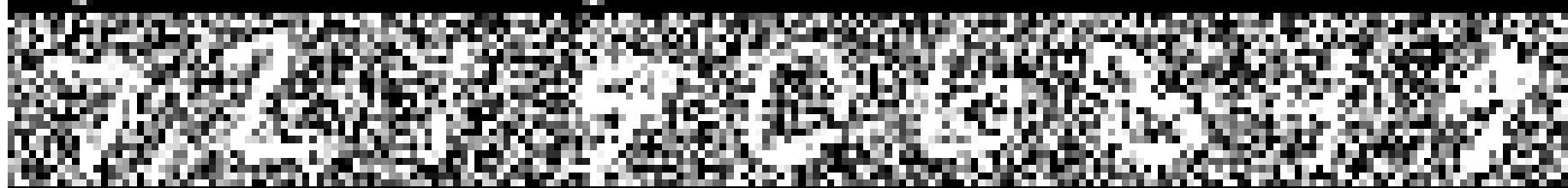
- **Training:** pairs of the grayscale and color images
- **Application:** new grayscale images (from the same distribution)
- **Concern:** has to be from the same distribution

Image Denoising

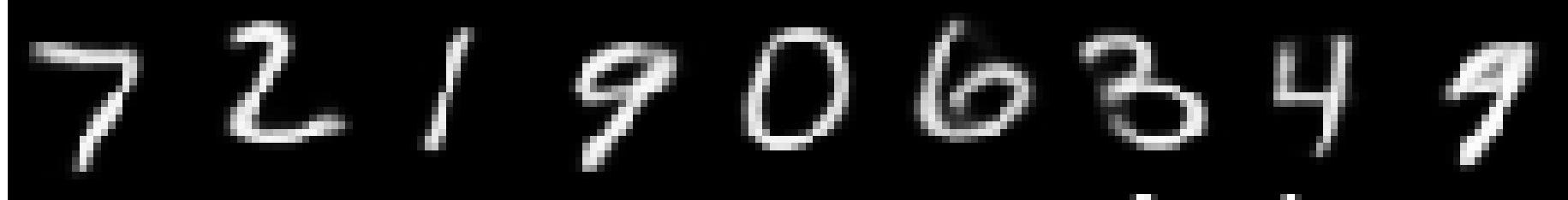
Ground truth



Noisy input



Reconstruction



- **Training:** pairs of the high-noise and low-noise images
- **Application:** new high noise images (from the same distribution)
- **Concern:** has to be from the same distribution

Variational Autoencoders



Diederik P. Kingma

Other names ▾

 FOLLOW

Research Scientist, [Google Brain](#)
Verified email at google.com - [Homepage](#)

Machine Learning Deep Learning Neural Networks Generative Models Variational Inference

TITLE	CITED BY	YEAR
Adam: A Method for Stochastic Optimization DP Kingma, J Ba Proceedings of the 3rd International Conference on Learning Representations ...	141306	2014
Auto-Encoding Variational Bayes DP Kingma, M Welling arXiv preprint arXiv:1312.6114	26540	2013
Semi-Supervised Learning with Deep Generative Models DP Kingma, S Mohamed, DJ Rezende, M Welling Advances in Neural Information Processing Systems, 3581-3589	2946	2014

- Variational Autoencoder (VAE): uses “reparameterization trick” to sample from the latent space
- Can be used for same tasks as AE
- Have a much better-behaved latent space: **disentanglement of the representations**

VAE Training

Latent manifold → Image space

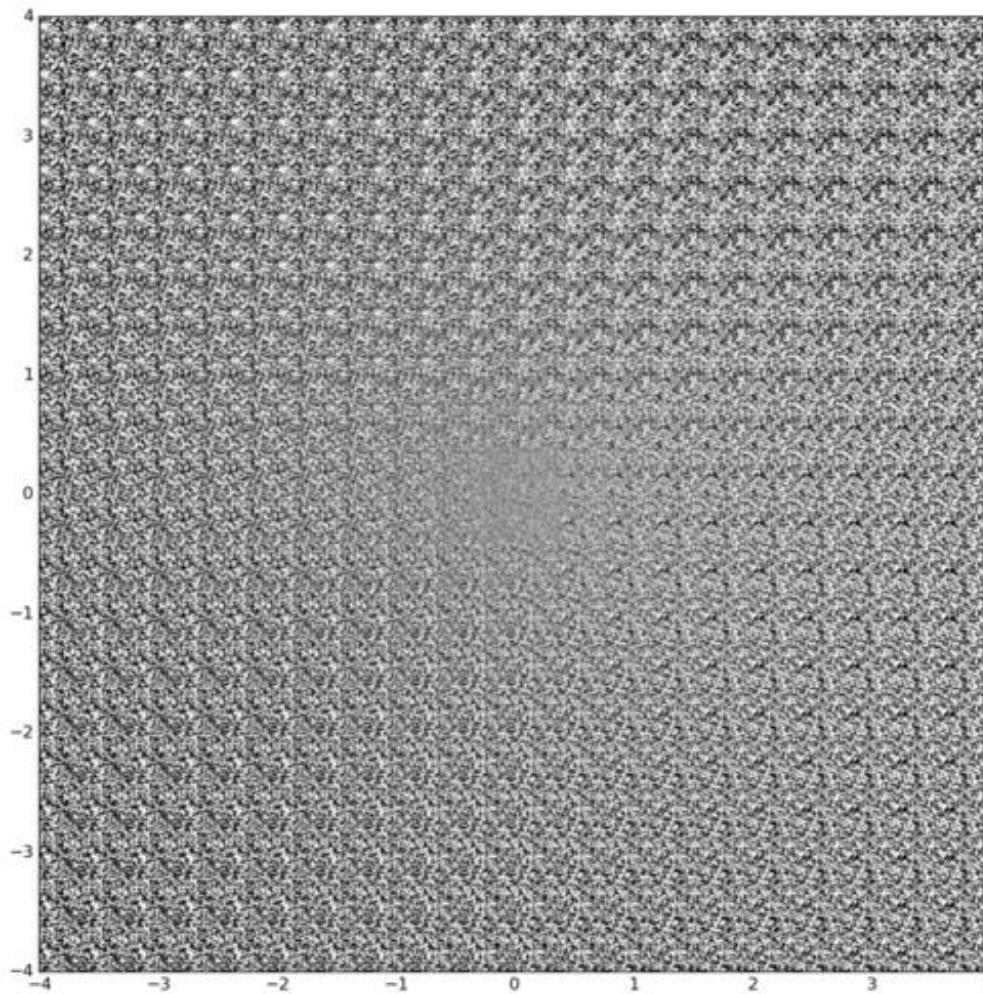
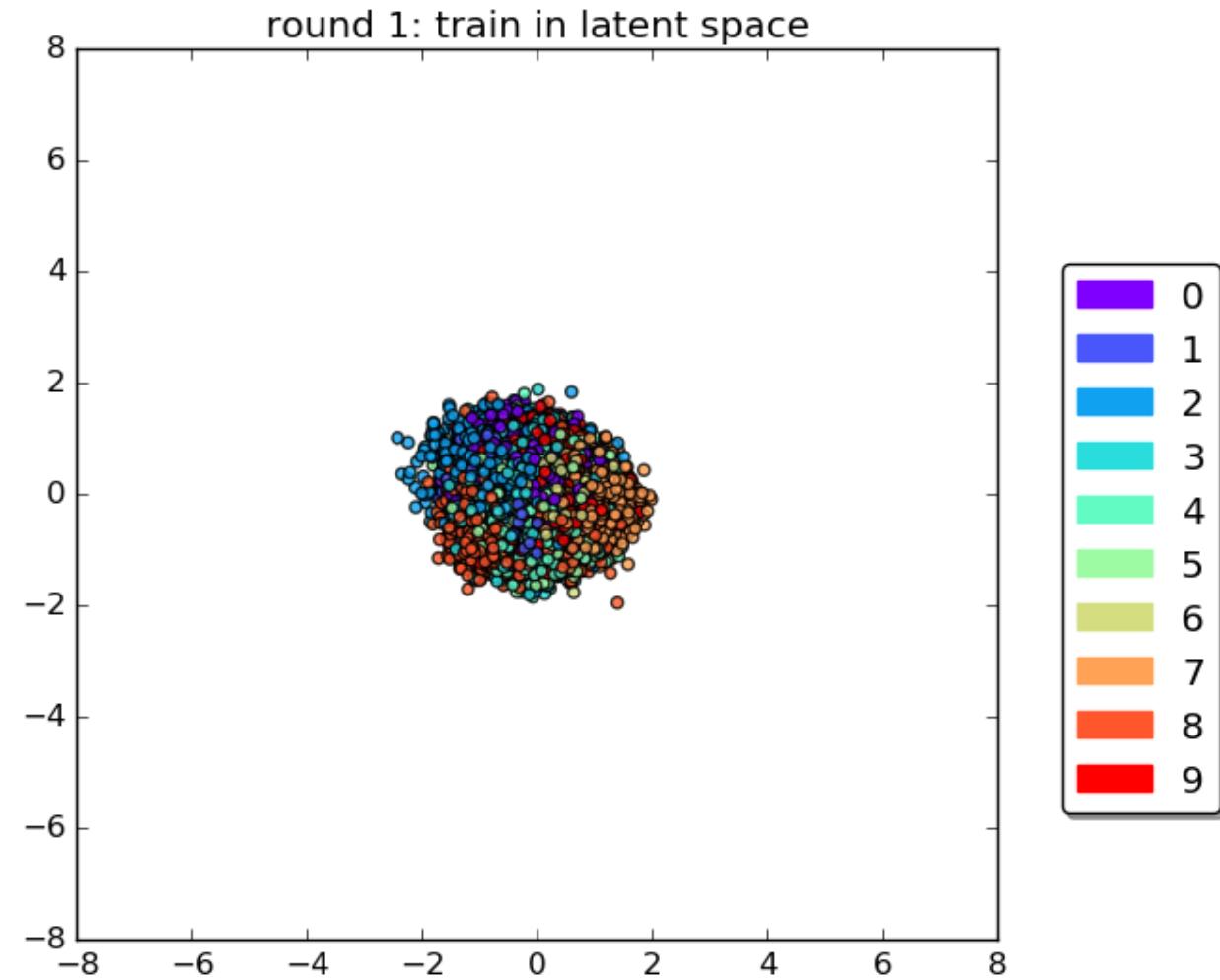


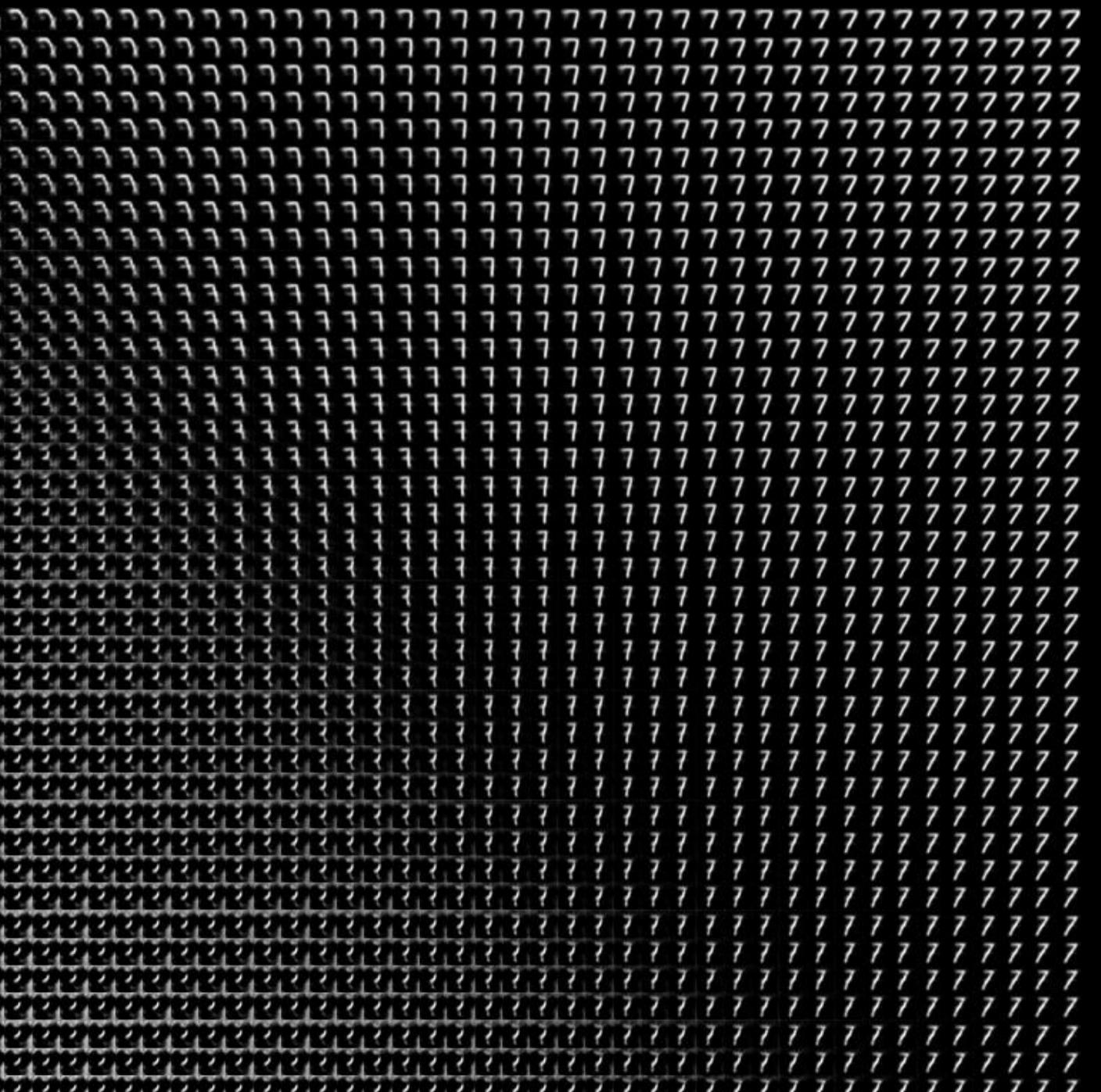
Image space → Latent space



Autoencoder latent representation

A 10x10 grid of numbers where each row and column contains the digits 0 through 9 in sequence. The first few rows are as follows:
Row 1: 0 1 2 3 4 5 6 7 8 9
Row 2: 0 1 2 3 4 5 6 7 8 9
Row 3: 0 1 2 3 4 5 6 7 8 9
Row 4: 0 1 2 3 4 5 6 7 8 9
Row 5: 0 1 2 3 4 5 6 7 8 9
Row 6: 0 1 2 3 4 5 6 7 8 9
Row 7: 0 1 2 3 4 5 6 7 8 9
Row 8: 0 1 2 3 4 5 6 7 8 9
Row 9: 0 1 2 3 4 5 6 7 8 9
Row 10: 0 1 2 3 4 5 6 7 8 9

Autoencoder latent representation (digit 7)



VAE latent representation

The image shows a massive grid of binary digits (0s and 1s) arranged in a specific pattern. The pattern forms a large, stylized digit '7'. The '7' is oriented vertically, with its top curve extending from approximately the middle-left of the grid down to the bottom-right. The interior of the '7' is filled with binary digits, while the exterior is mostly composed of '0's. The '7' is rendered in white against a black background.

VAE latent representation (digit 7)

The image consists of a large grid of black digits on a white background. The grid is composed of approximately 100 columns and 100 rows. Each row contains a unique sequence of digits, starting from 1 and increasing sequentially. The first few rows show the following sequences:

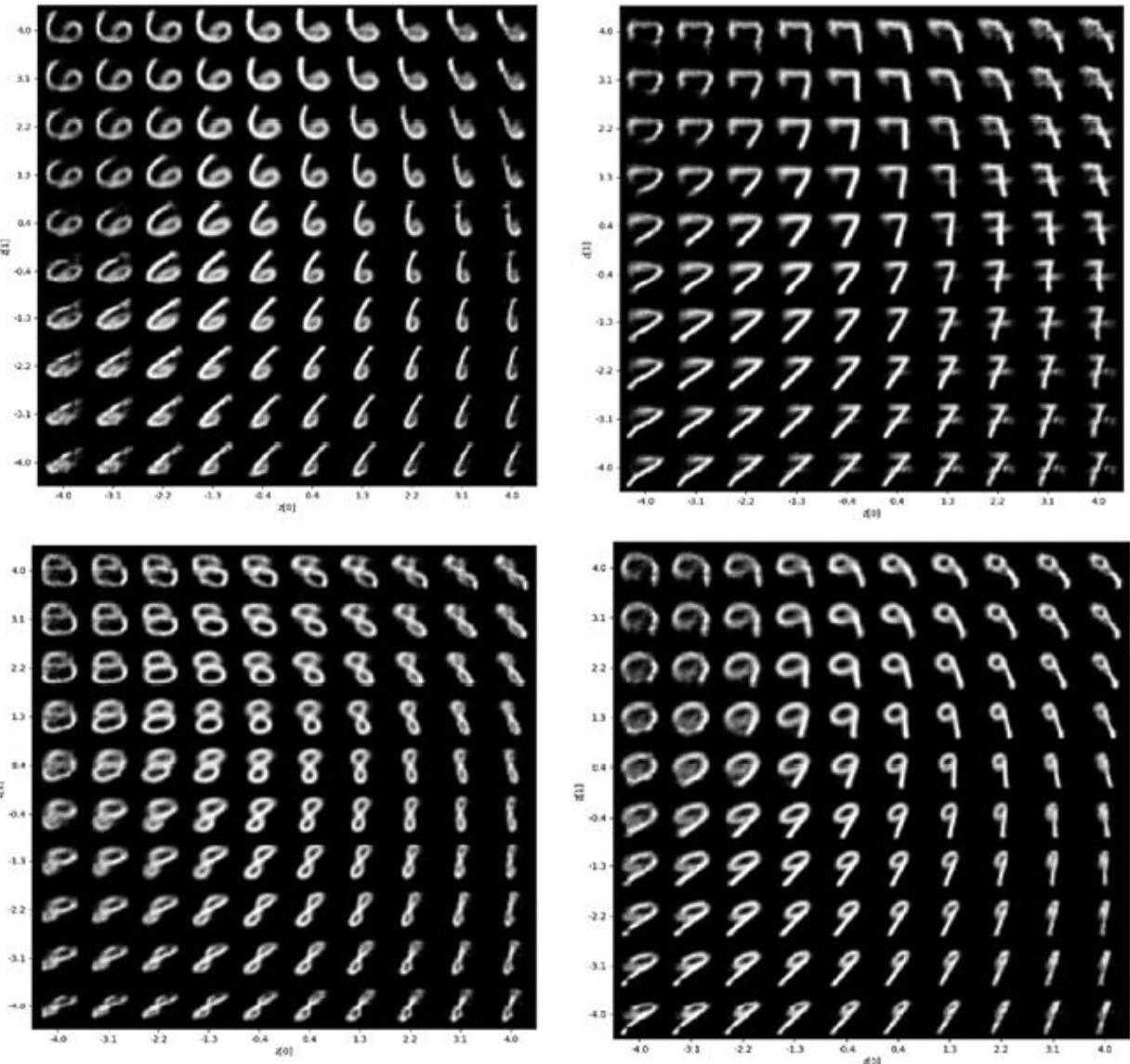
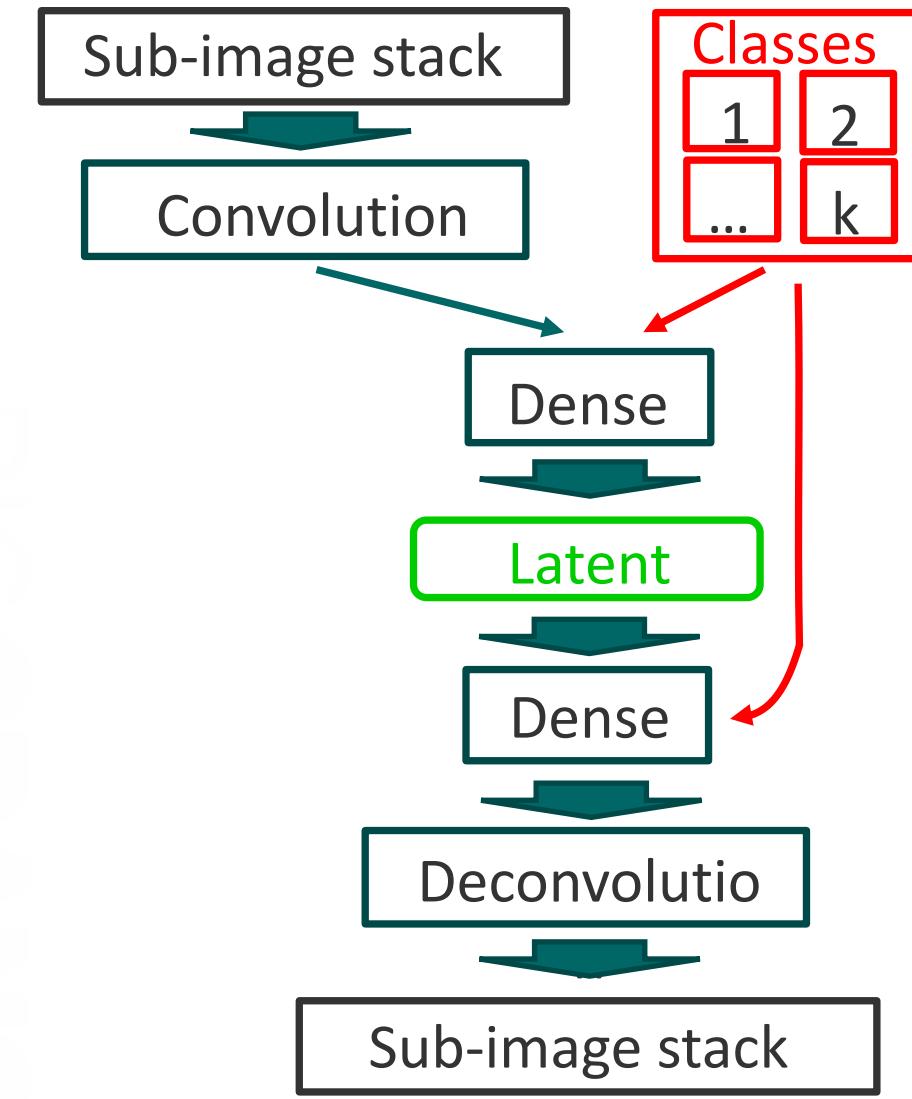
- Row 1: 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, ...
- Row 2: 2, 3, 4, 5, 6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, ...
- Row 3: 3, 4, 5, 6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, ...
- Row 4: 4, 5, 6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, ...
- Row 5: 5, 6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, ...
- Row 6: 6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, ...
- Row 7: 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, ...
- Row 8: 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, ...
- Row 9: 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, ...
- Row 10: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, ...

As the rows continue, they follow a repeating pattern of digits, with each subsequent row starting at the next digit value in the sequence.

VAE latent representation (digit 8)

A 100x100 grid of digit 8s, representing a VAE latent representation for digit 8. The digits are rendered in a light gray color against a white background.

Conditional VAE



Note the trends in the latent representation for each digit: **disentanglement of the representations**

Word Embeddings

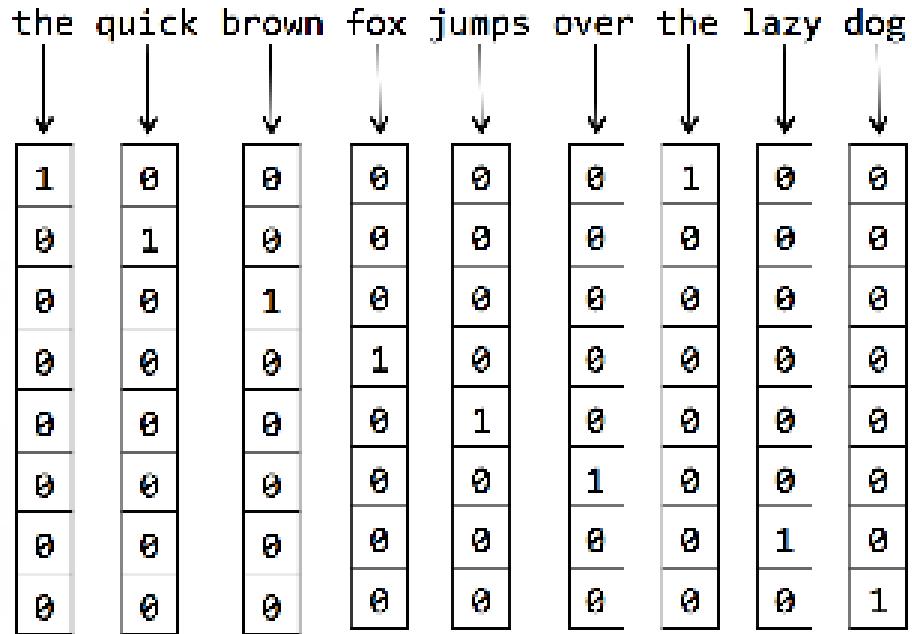
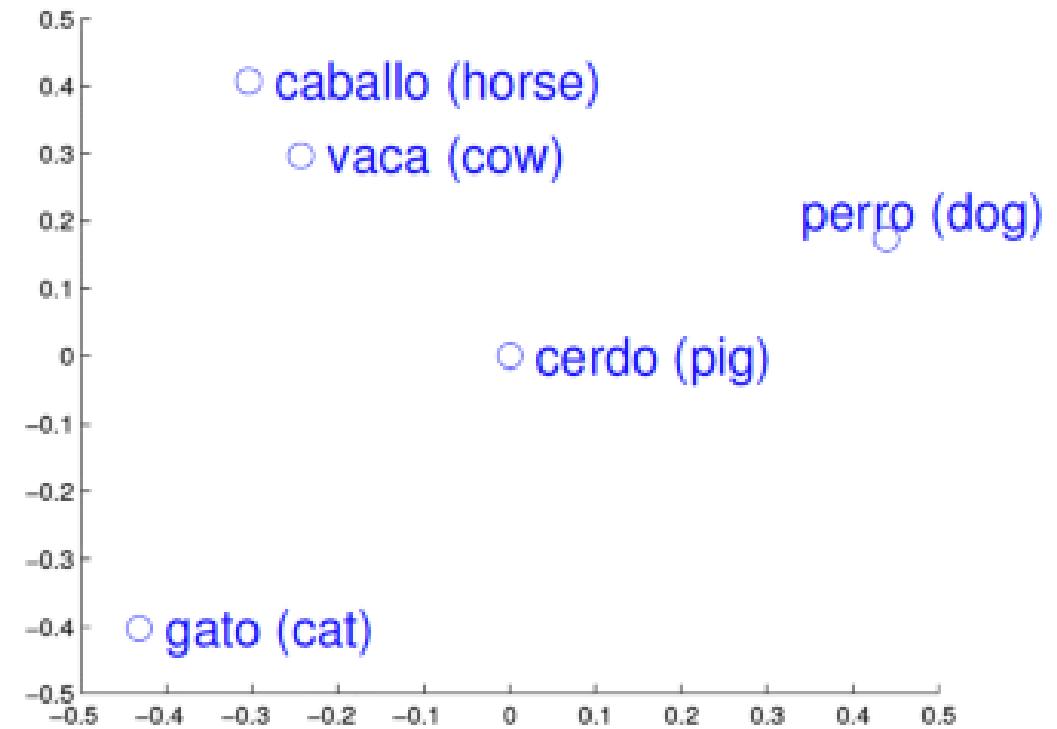
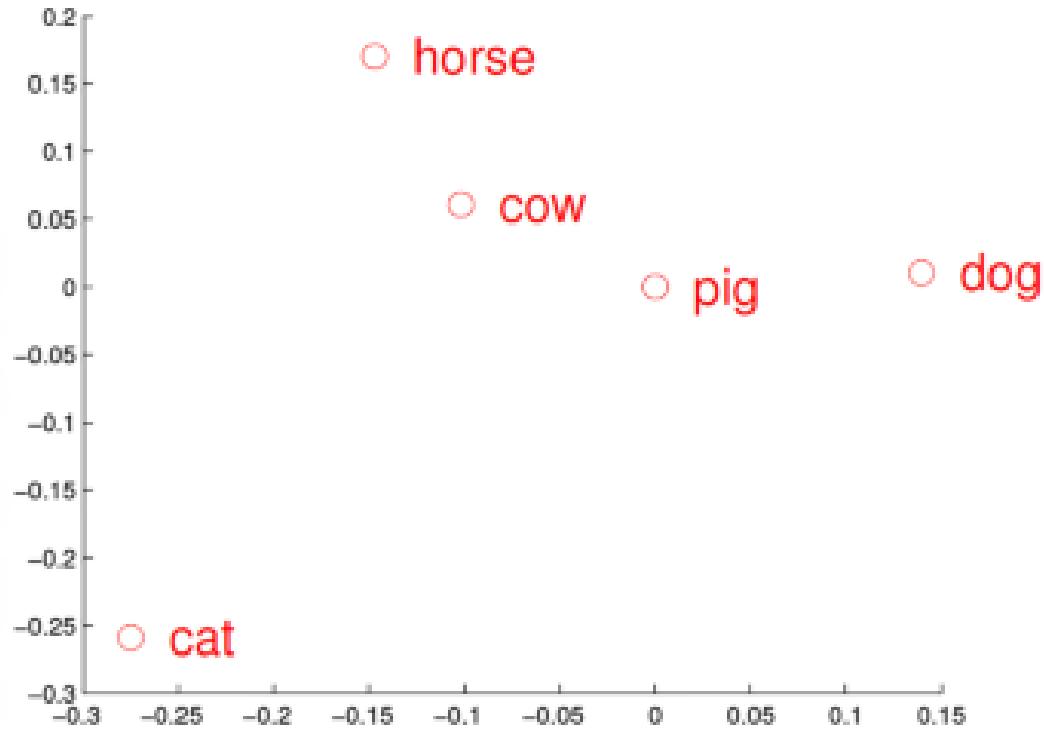


Figure 1: The Skip-gram model architecture. The training objective is to learn word vector representations that are good at predicting the nearby words.

<https://medium.com/geekculture/word-embeddings-in-ai-10a9e430cb59>

https://proceedings.neurips.cc/paper_files/paper/2013/file/9aa42b31882ec039965f3c4923ce901b-Paper.pdf

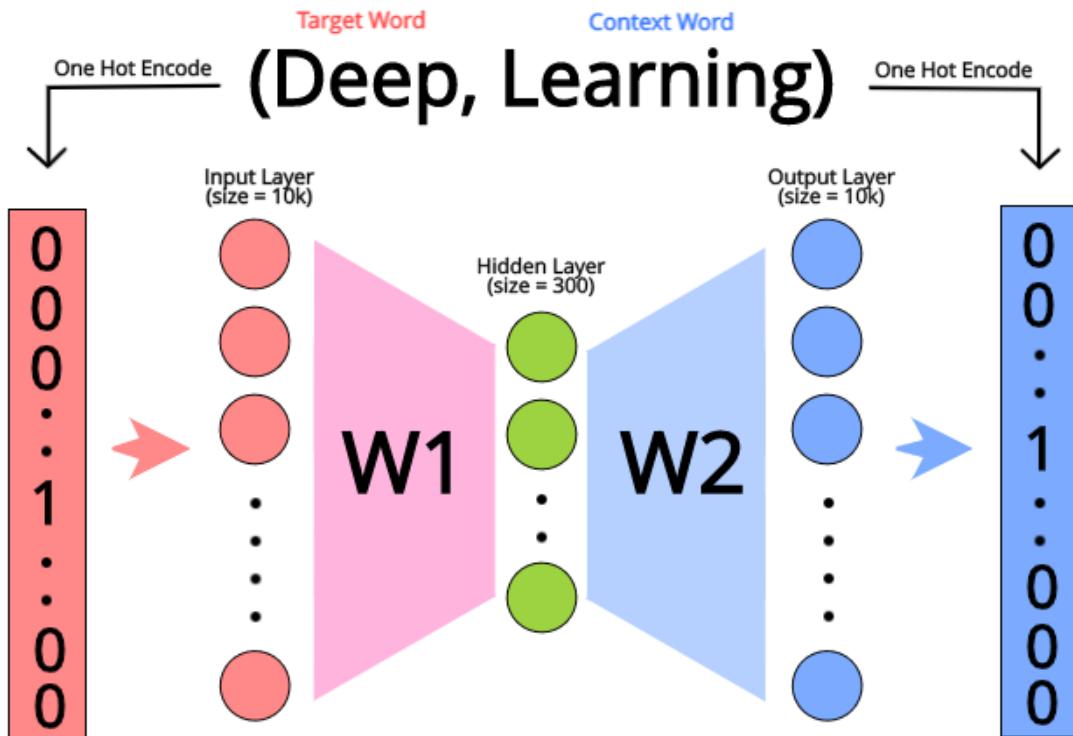
Word Embeddings



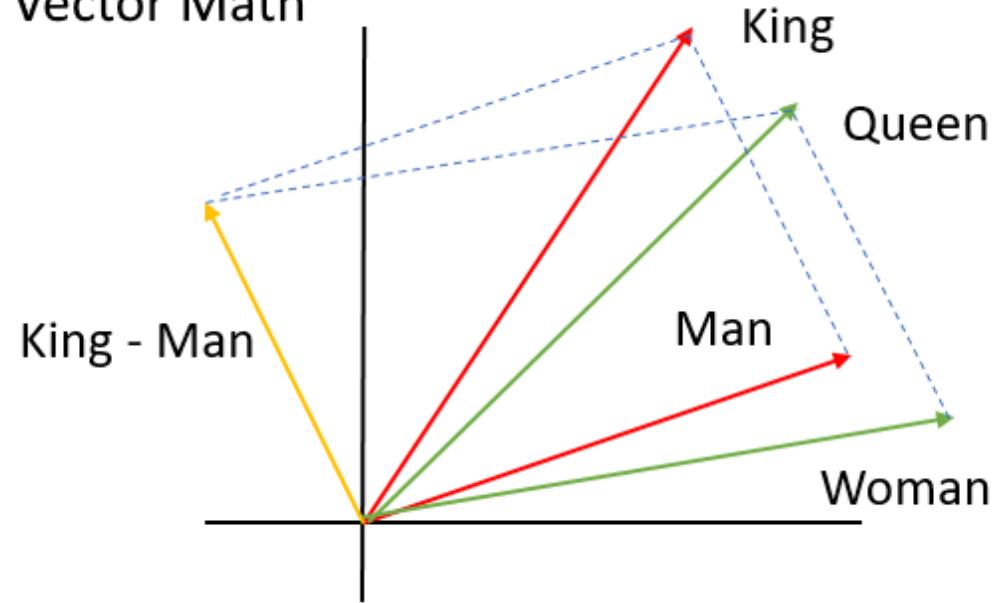
<https://medium.com/geekculture/word-embeddings-in-ai-10a9e430cb59>

Word Vectors

Skip Gram Architecture

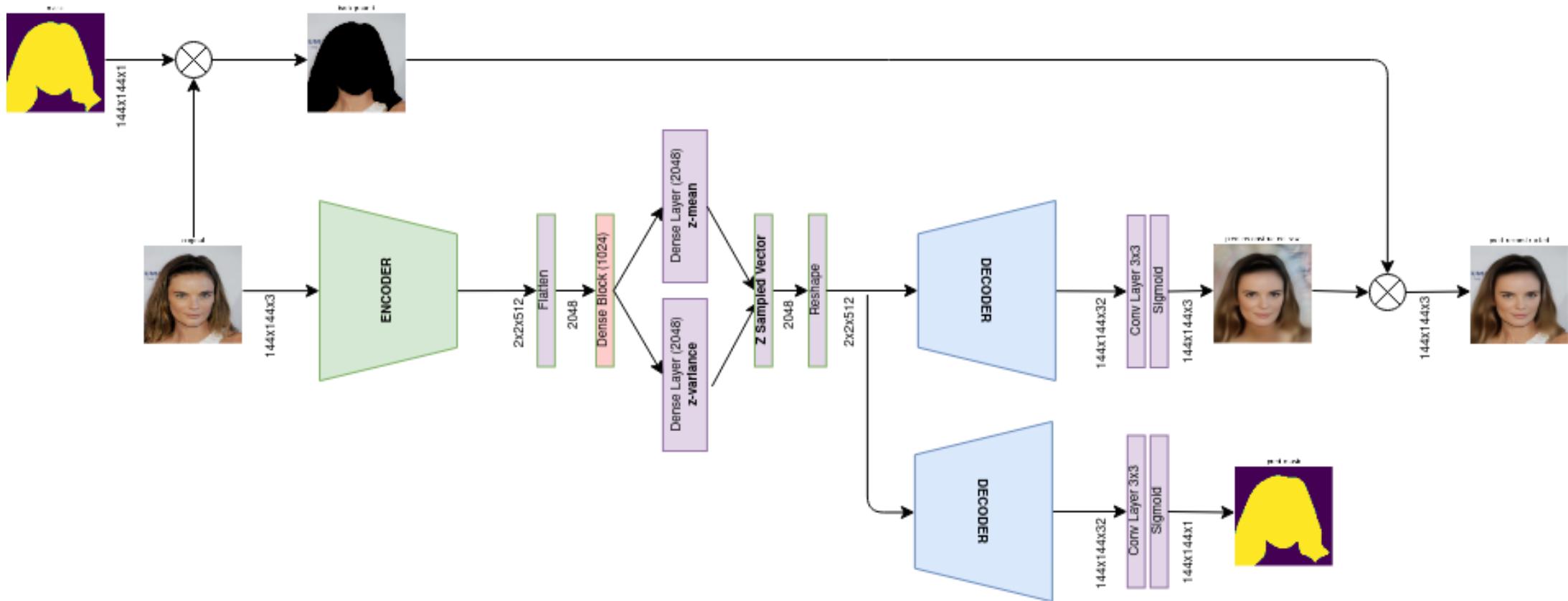


Vector Math



<https://medium.com/analytics-vidhya/word-embeddings-in-nlp-word2vec-glove-fasttext-24d4d4286a73>

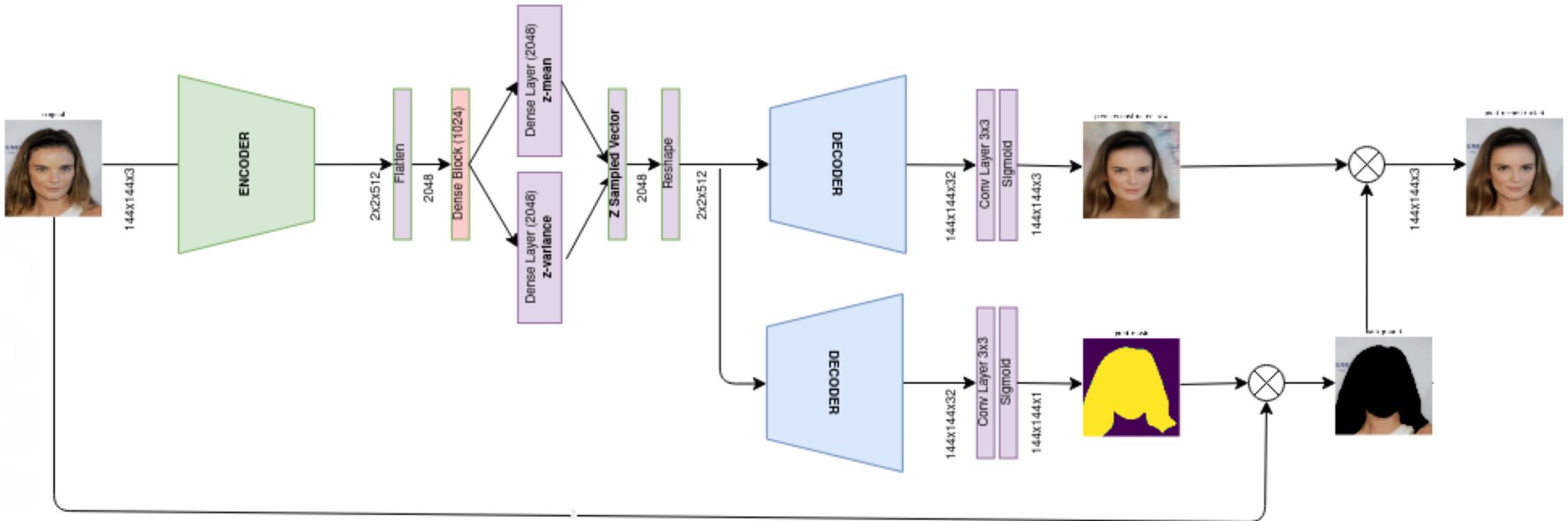
Making Deep Fakes with VAE



During training, the labels of the face masks are used too, which replaces the background of the reconstructed image such that the loss function is applied only over the face pixels.

<https://rtoledo.me/post/2021-05-31-edit-face-attributes-using-vae/edit-face-attributes-using-vae/>

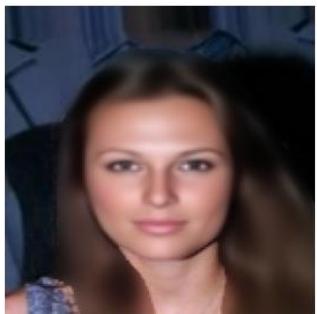
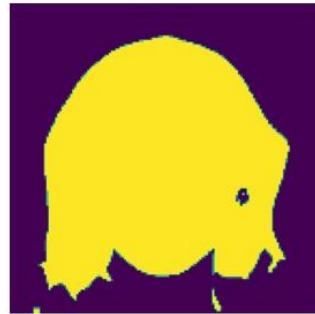
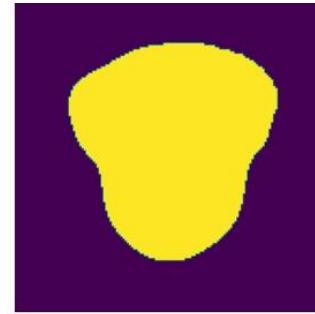
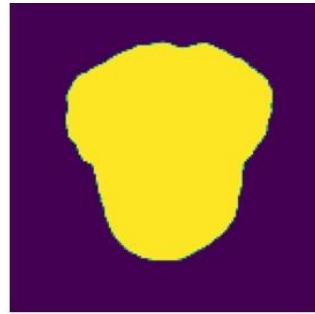
Making Deep Fakes with VAE



In the prediction mode, the background replacement is done by the predicted mask itself, not requiring any extra input but a sample image.

<https://rtoledo.me/post/2021-05-31-edit-face-attributes-using-vae/edit-face-attributes-using-vae/>

Reconstruction



<https://rtoledo.me/post/2021-05-31-edit-face-attributes-using-vae/edit-face-attributes-using-vae/>

Changing Attributes



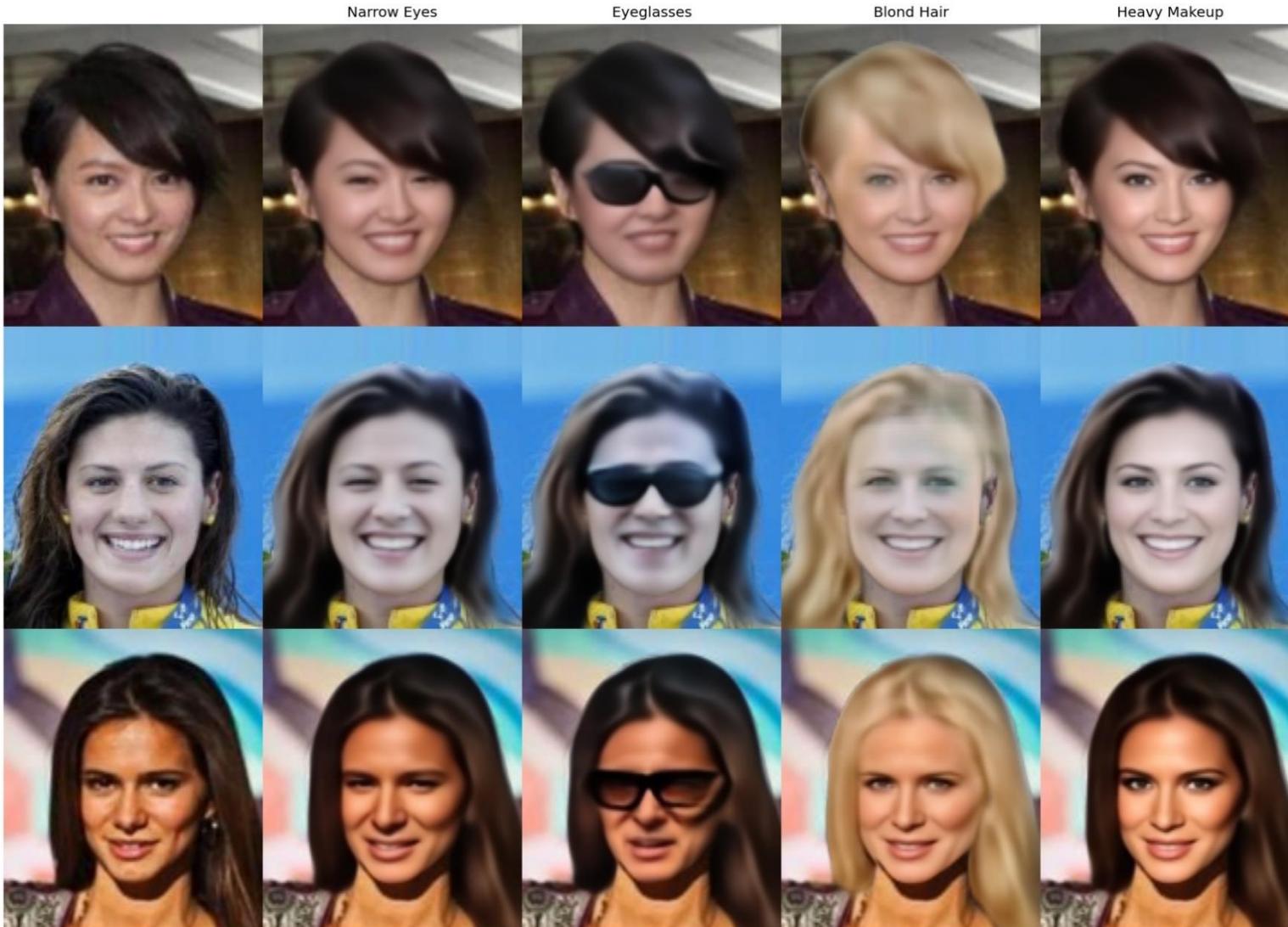
<https://rtoledo.me/post/2021-05-31-edit-face-attributes-using-vae/edit-face-attributes-using-vae/>

Changing Attributes



<https://rtoledo.me/post/2021-05-31-edit-face-attributes-using-vae/edit-face-attributes-using-vae/>

Changing Attributes

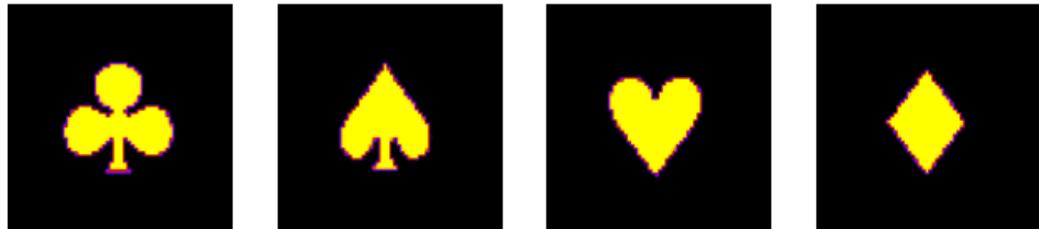


<https://rtoledo.me/post/2021-05-31-edit-face-attributes-using-vae/edit-face-attributes-using-vae/>

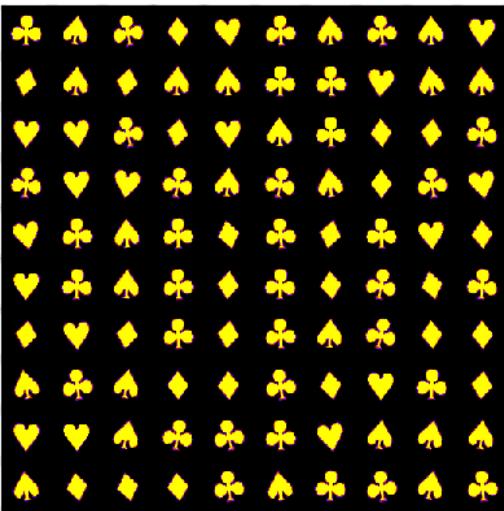
VAE on Cards

Introduce the **cards** data set:

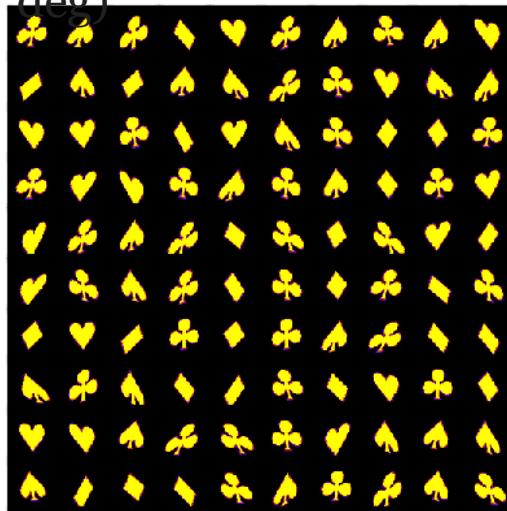
- Classical 4 hands (diamonds, clubs, pikes, hearts)
- Interesting similarities (pires and hearts)
- And invariances on affine transforms (e.g. diamonds)



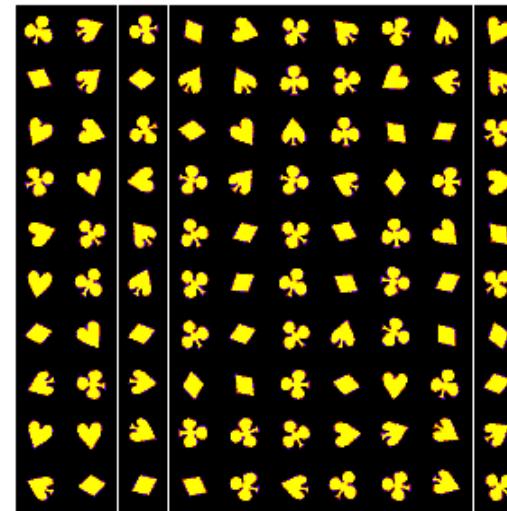
Cards 1: Low R (12 deg) and low S (1 deg)



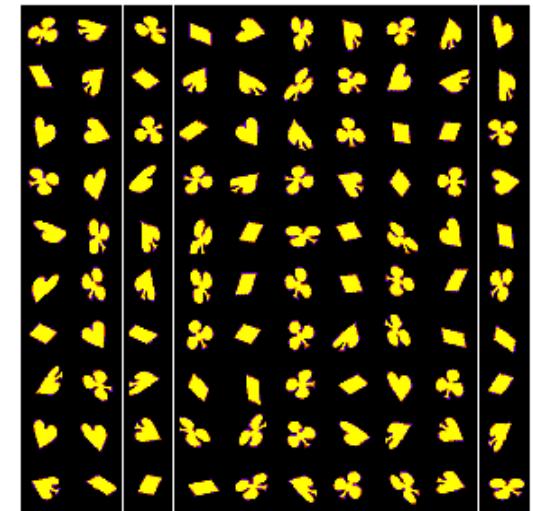
Cards 2: Low R (12 deg) and high S (20 deg)



Cards 3: High R (120 deg) and Low S (1 deg)



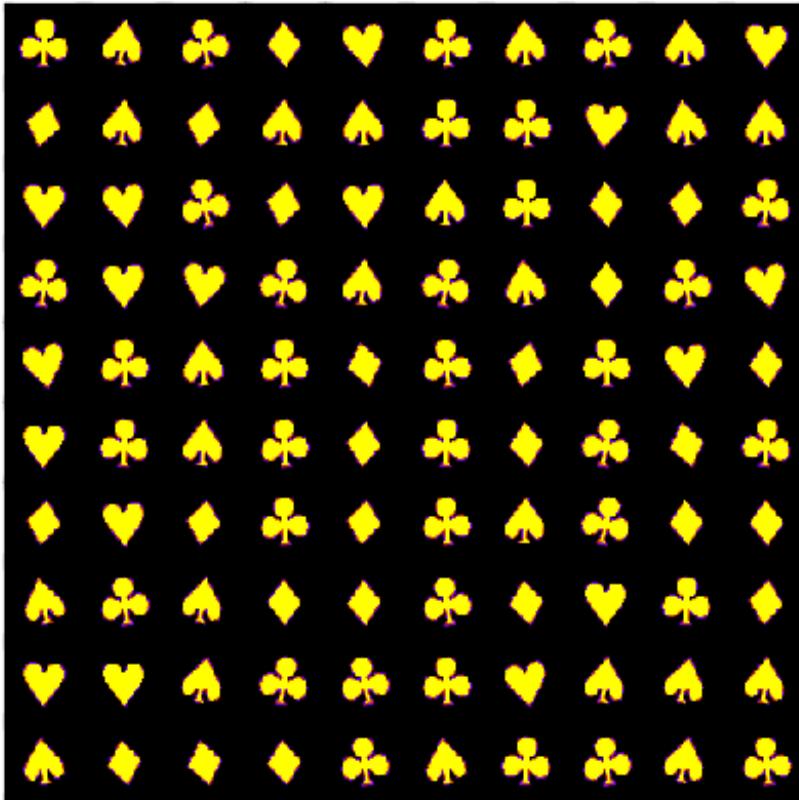
Cards 4: High R (120 deg) and high S (20 deg)



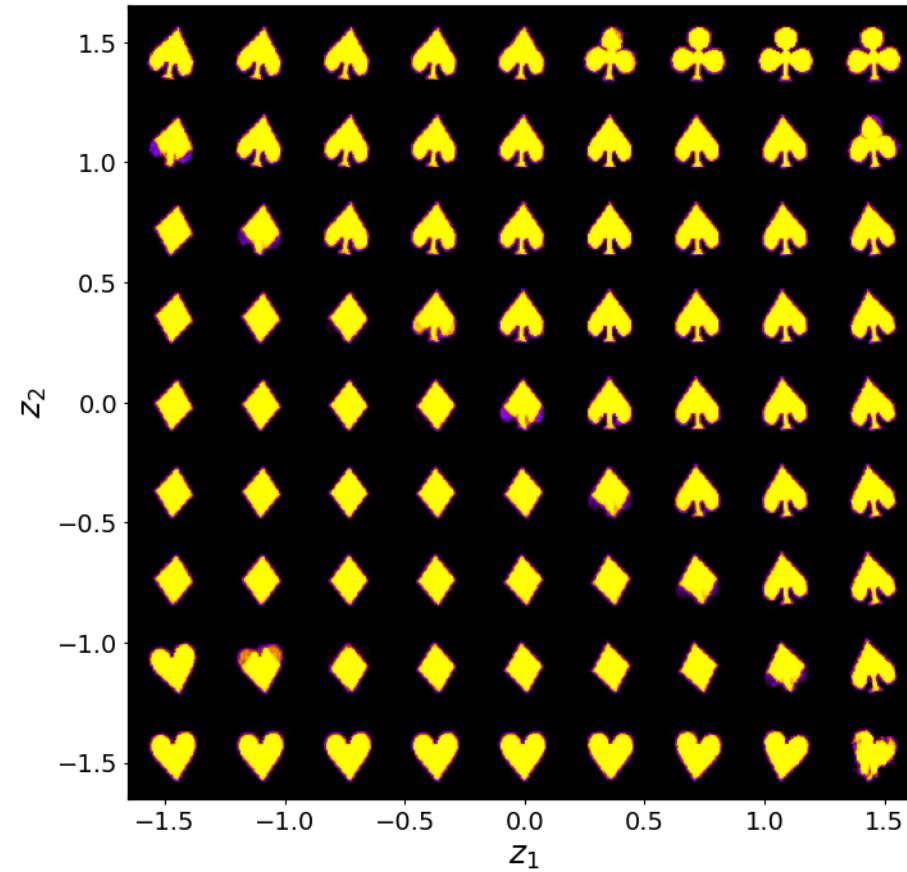
- Shear, rotations, and translations are **known** factors of variability (or traits) in data
- Can VAE disentangle representations and **discover** these factors of variability

VAE on Cards

Example of data

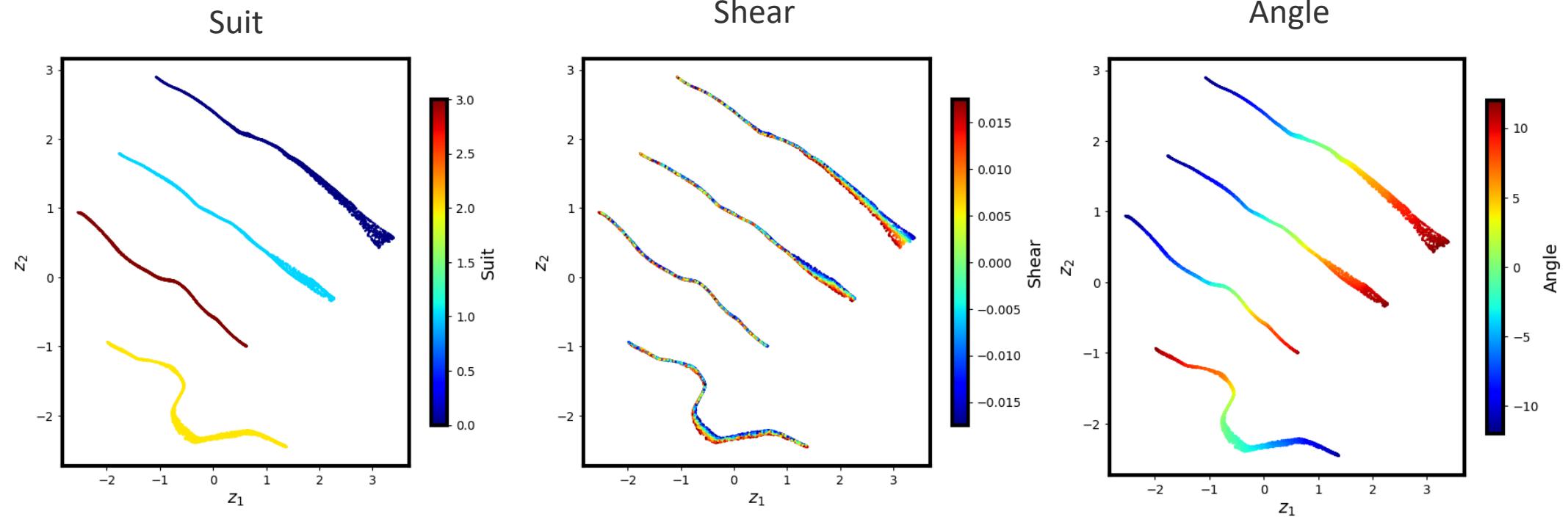


Latent representation



Cards 1: Low rotation (12 deg) and low shear (1 deg)

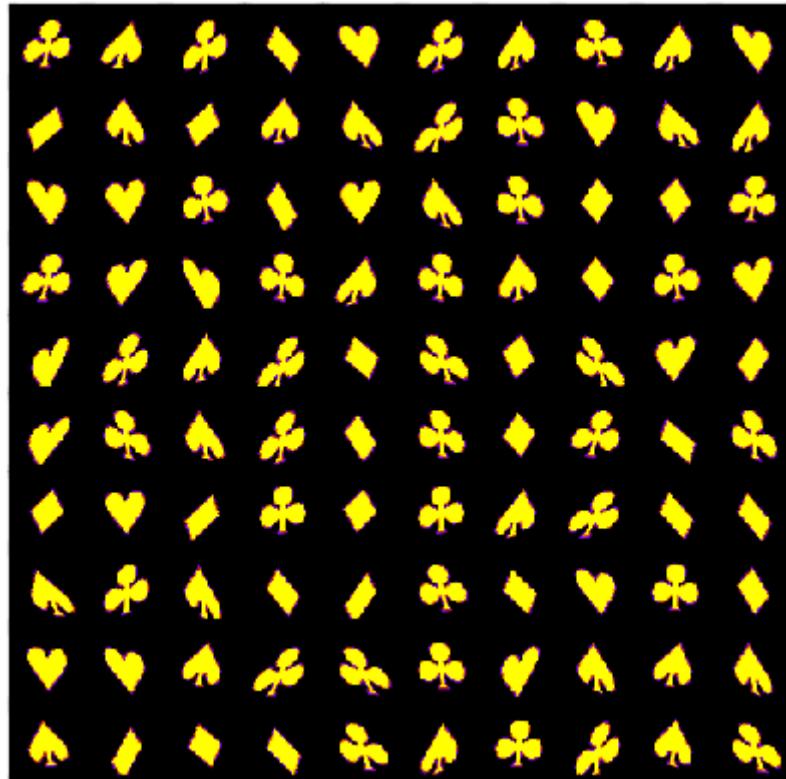
VAE on Cards



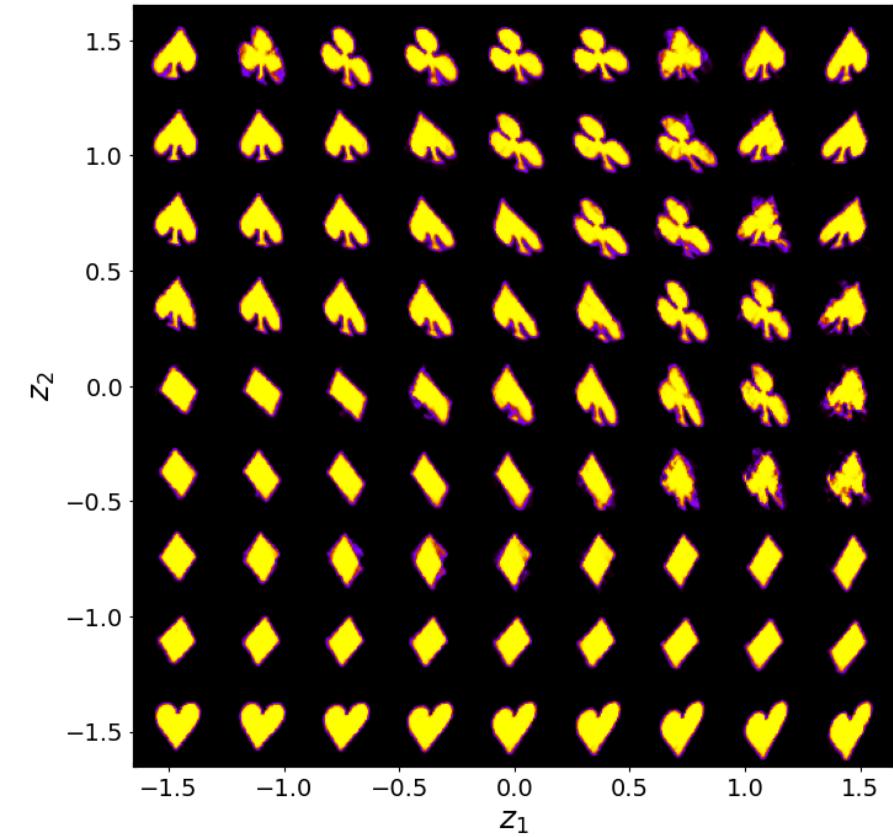
Cards 1: Low rotation (12 deg) and low shear (1 deg)

VAE on Cards

Example of data

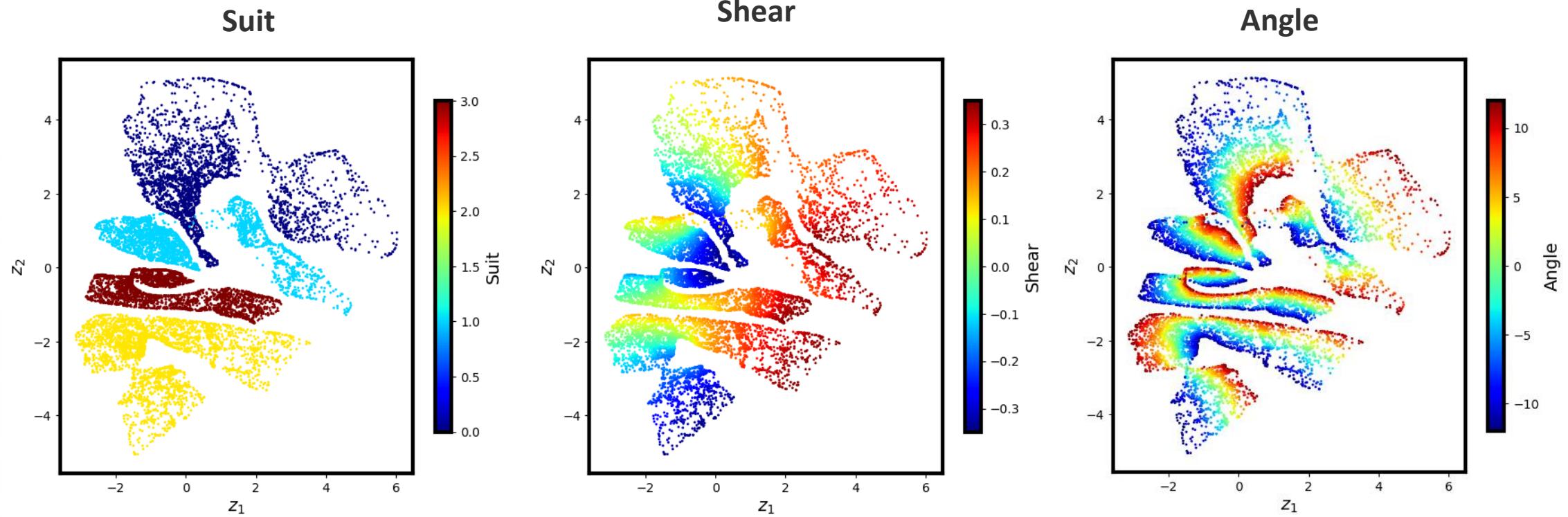


Latent representation



Cards 2: Low rotation (12 deg) and high shear (20 deg)

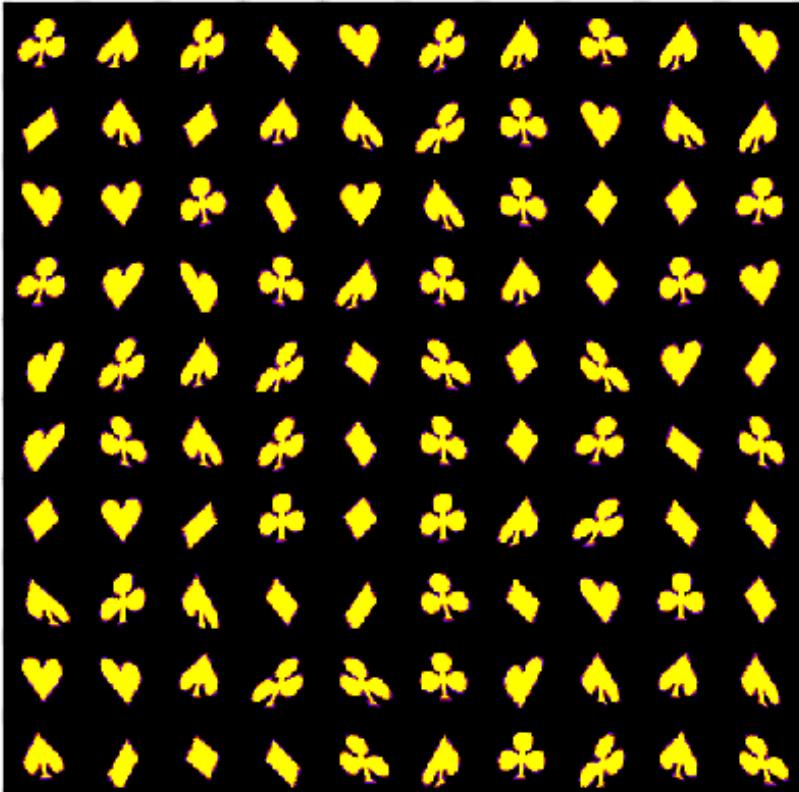
VAE on Cards



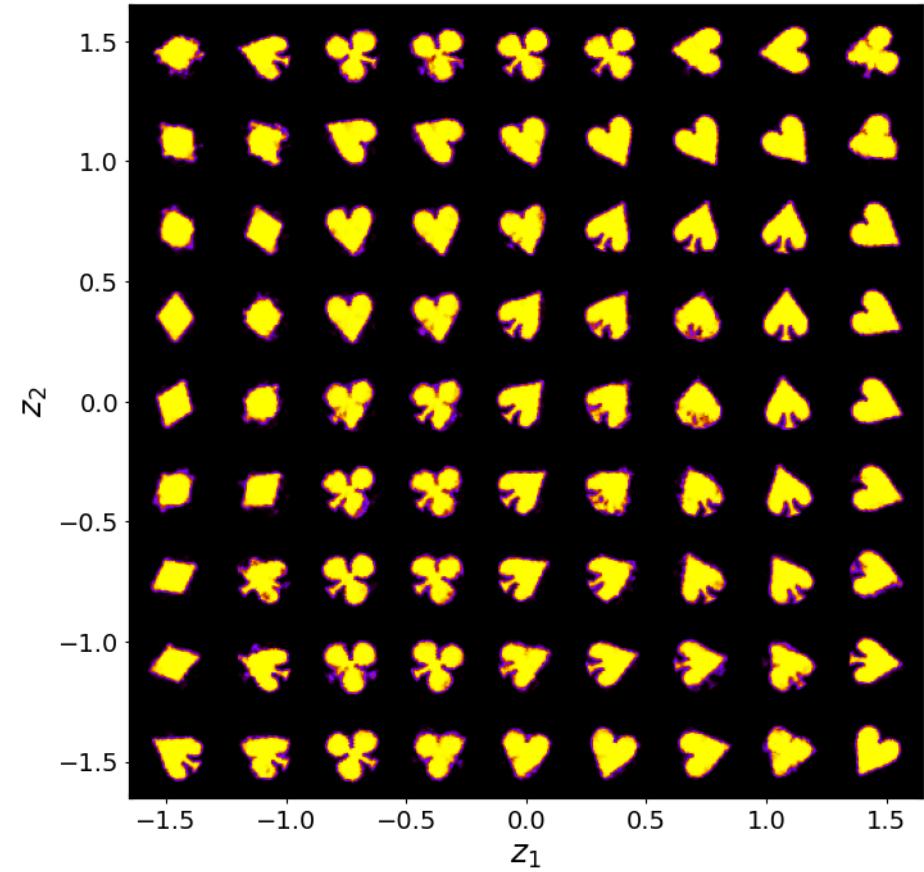
Cards 2: Low rotation (12 deg) and high shear (20 deg)

VAE on Cards

Example of data

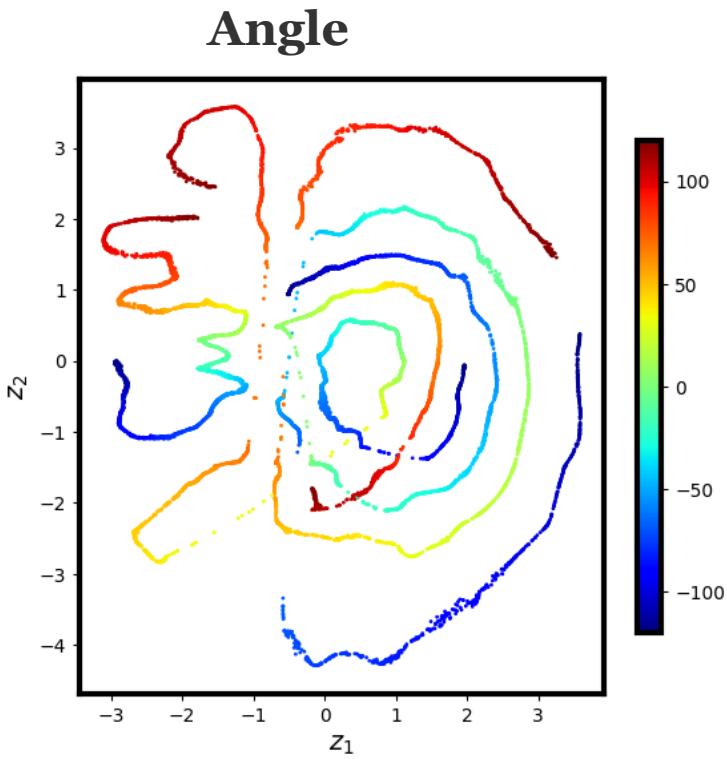
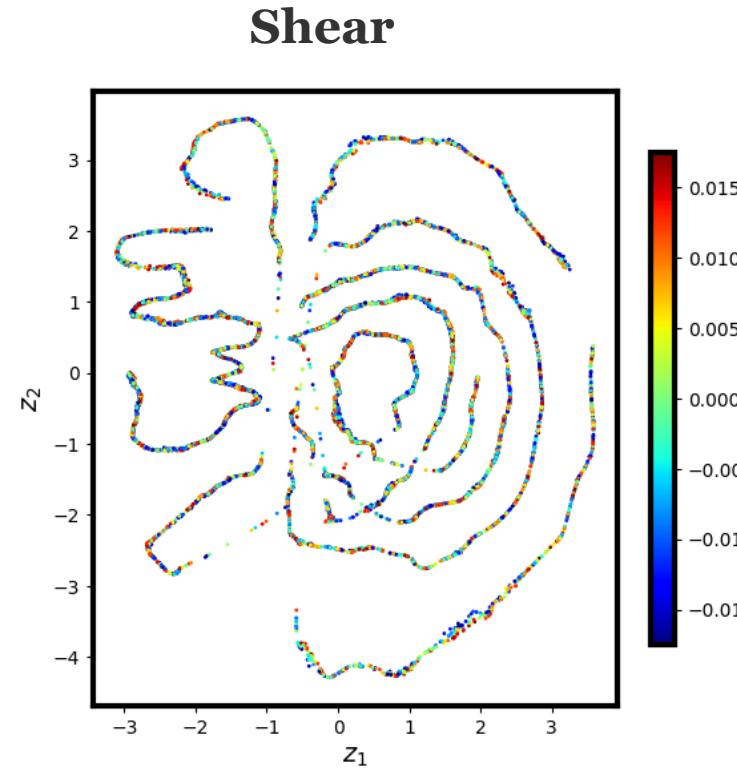
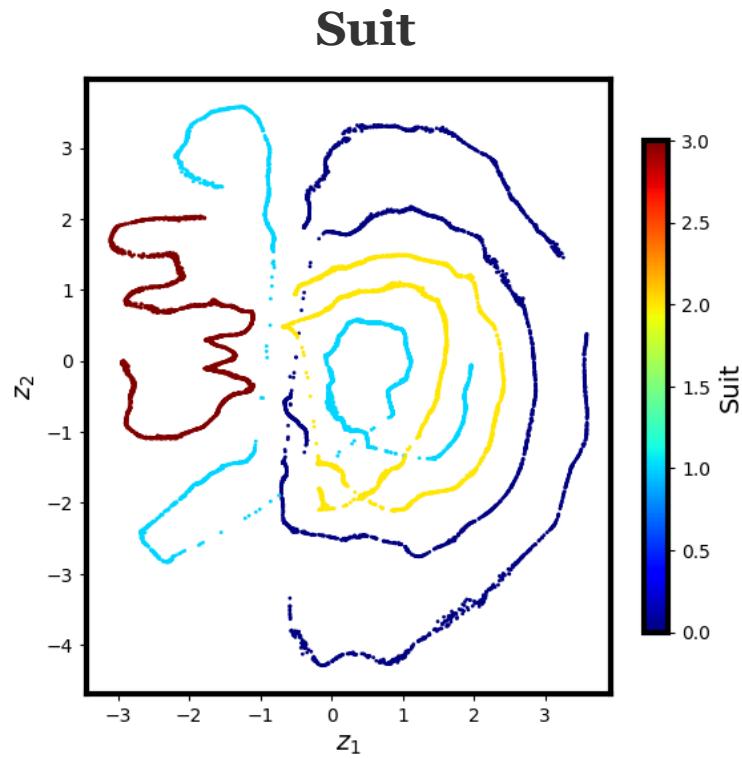


Latent representation



Cards 3: High rotation (120 deg) and low shear (1 deg)

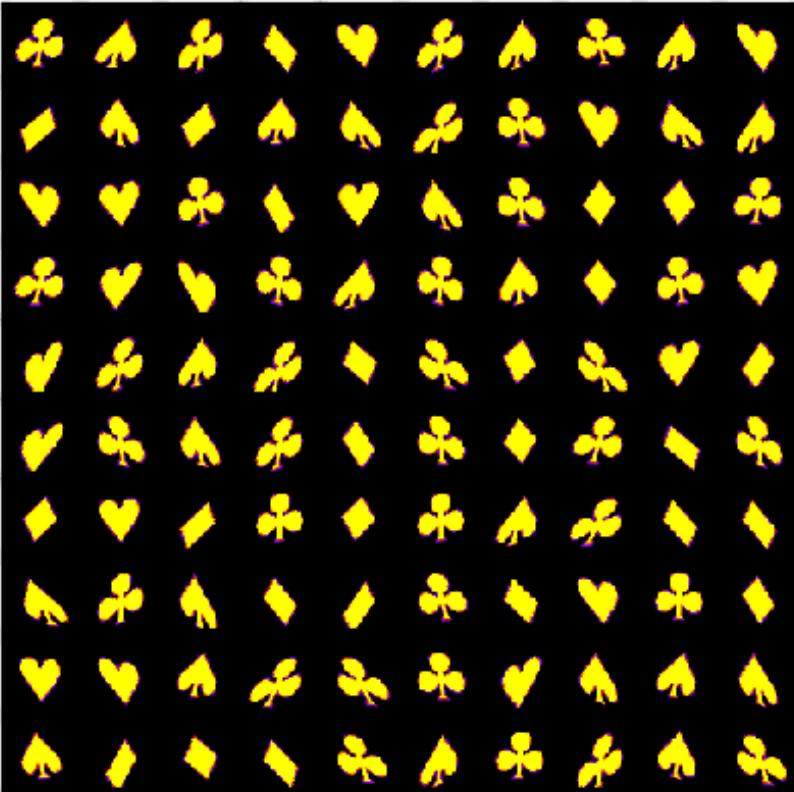
VAE on Cards



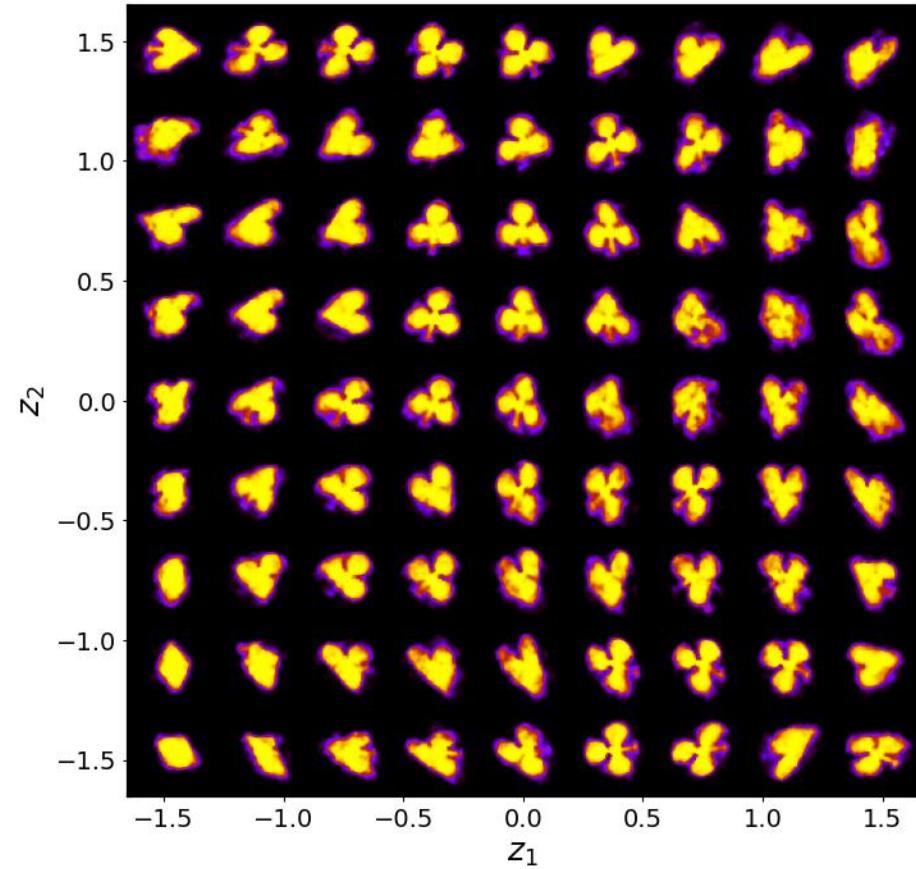
Cards 3: High rotation (120 deg) and low shear (1 deg)

VAE on Cards

Example of data

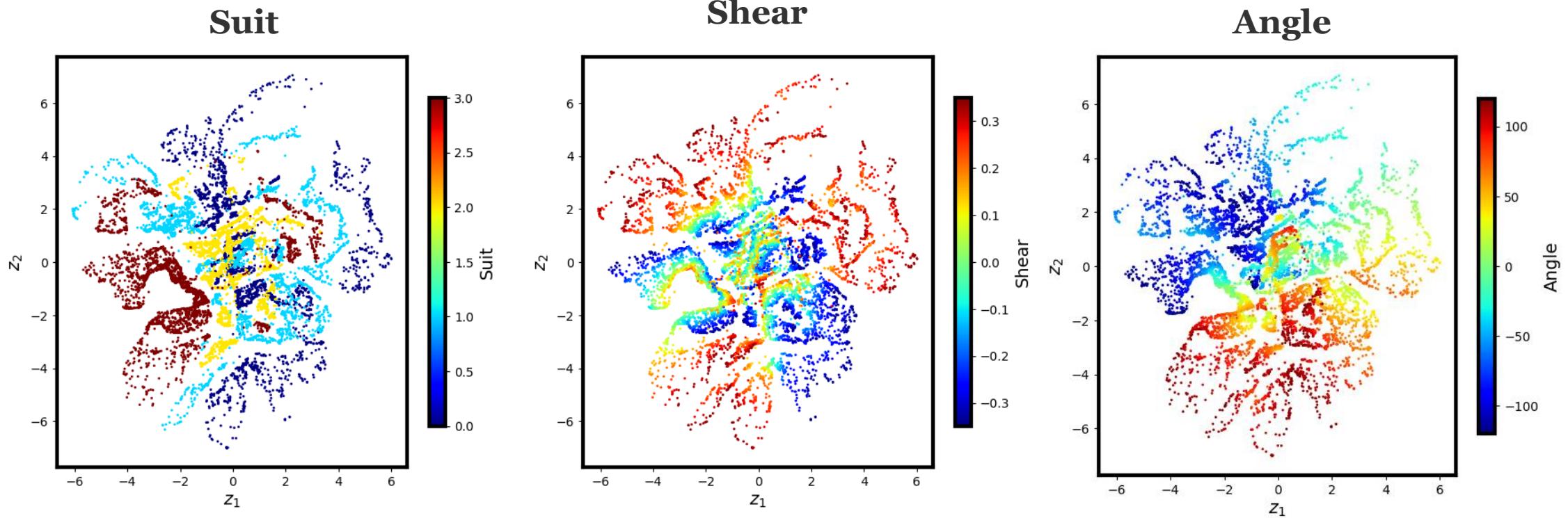


Latent representation



Cards 4: High rotation (120 deg) and high shear (20 deg)

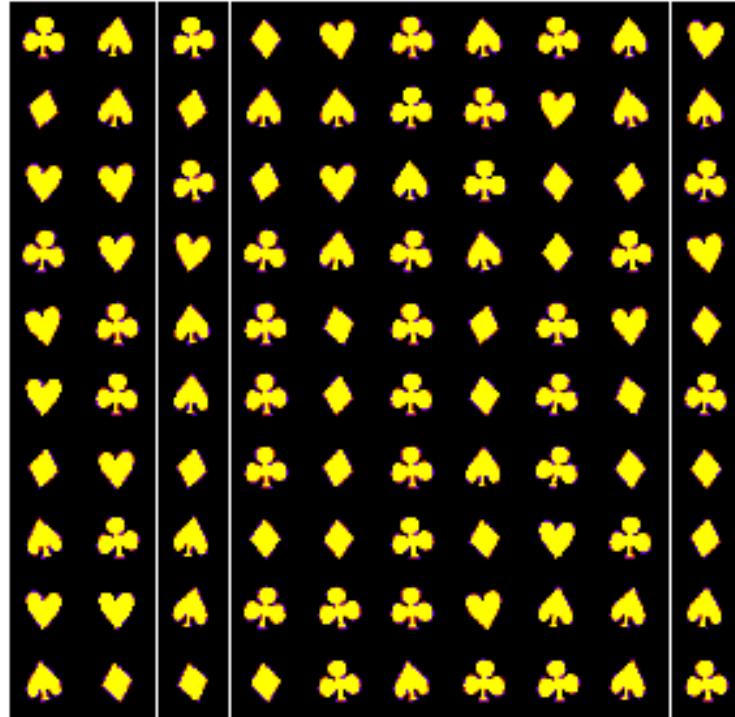
VAE on Cards



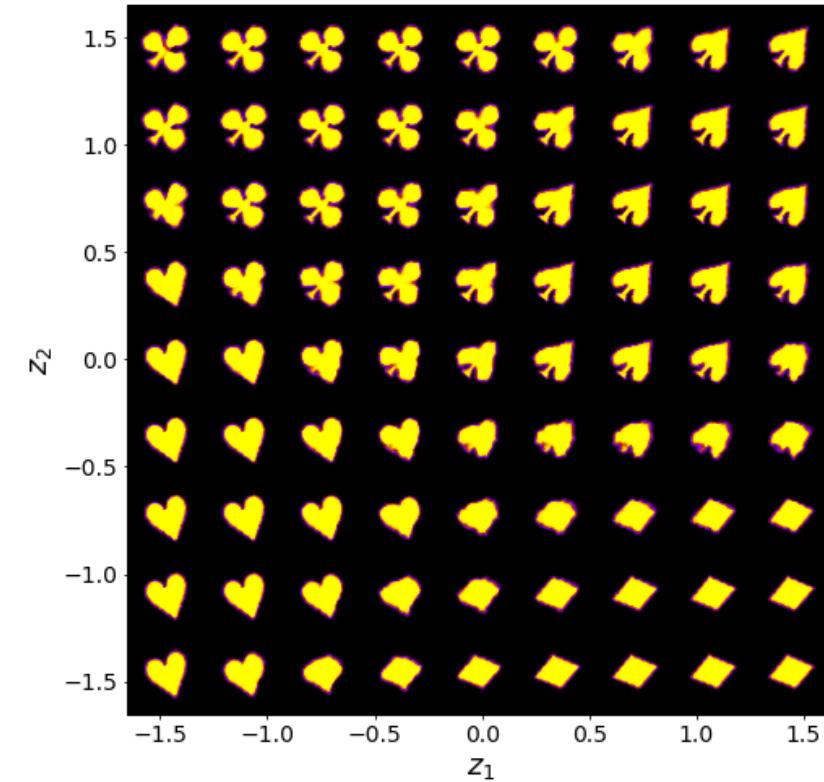
Cards 4: High rotation (120 deg) and high shear (20 deg)

rVAE on Cards

Example of data

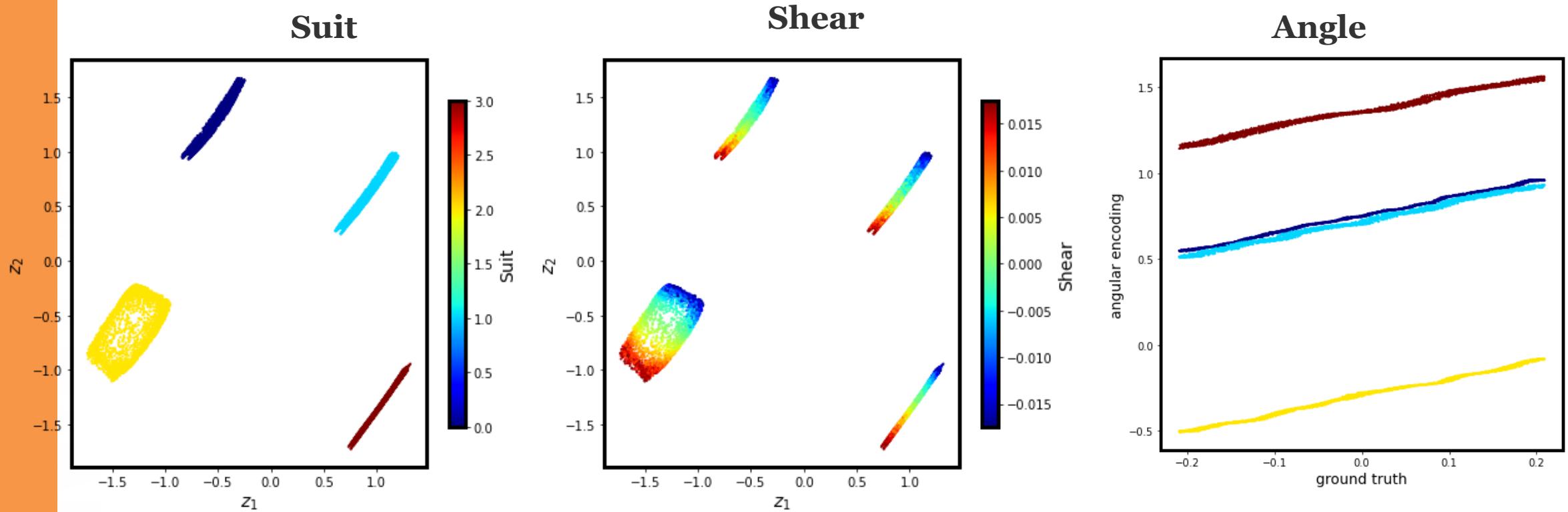


Latent representation



Cards 1: Low rotation (12 deg) and low shear (1 deg)

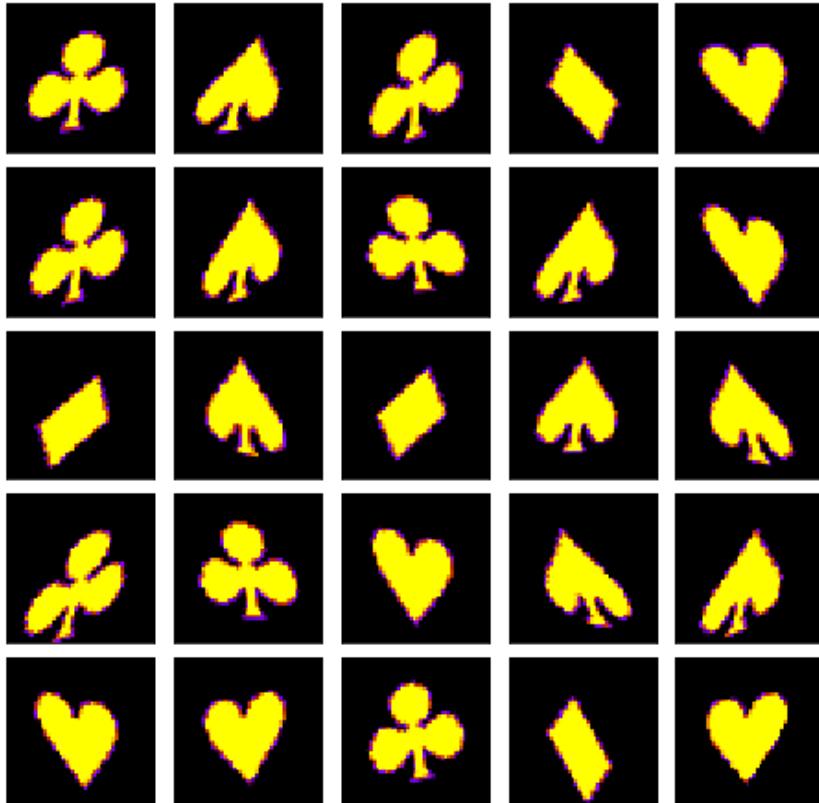
rVAE on Cards



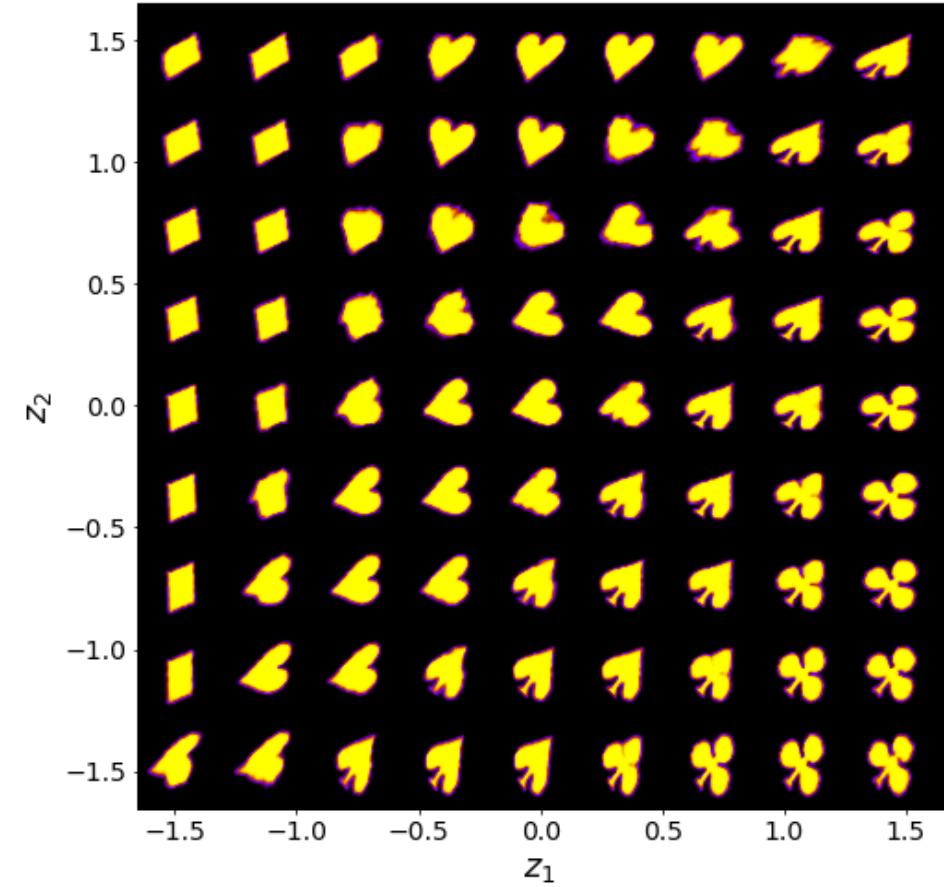
Cards 1: Low rotation (12 deg) and low shear (1 deg)

rVAE on Cards

Example of data

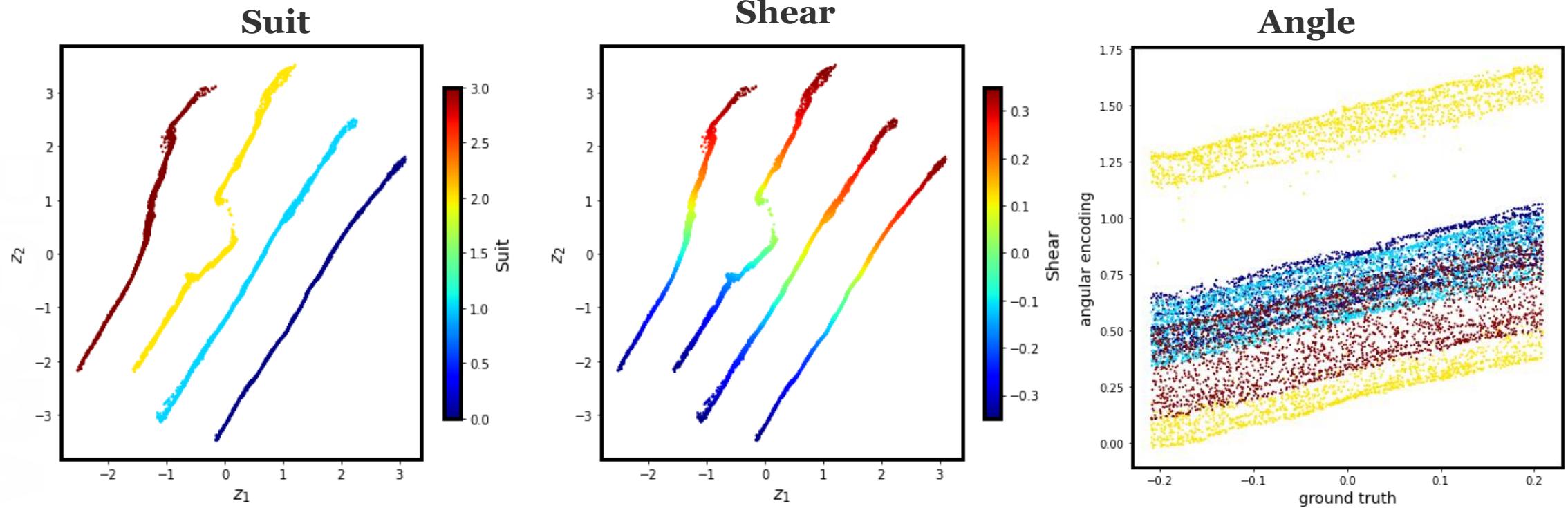


Latent representation



Cards 2: Low rotation (12 deg) and high shear (20 deg)

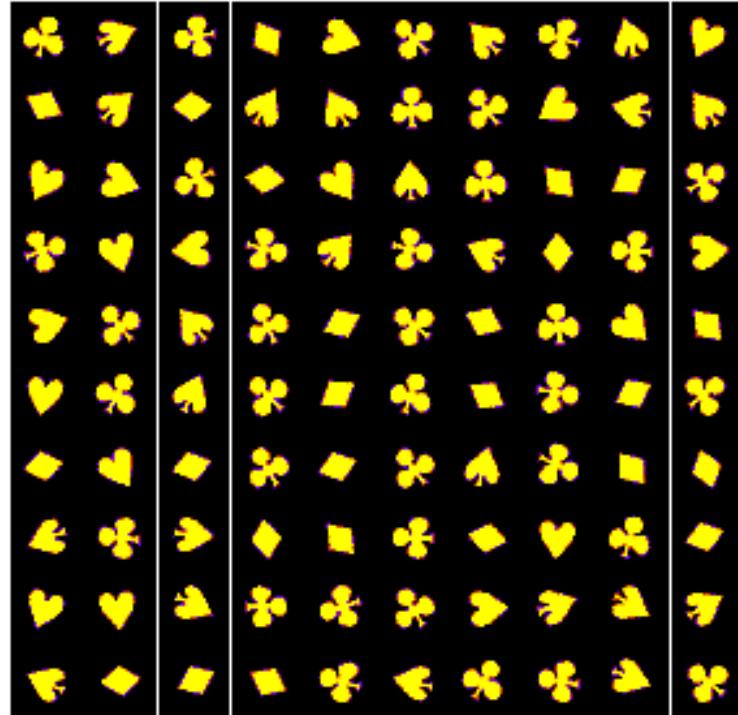
rVAE on Cards



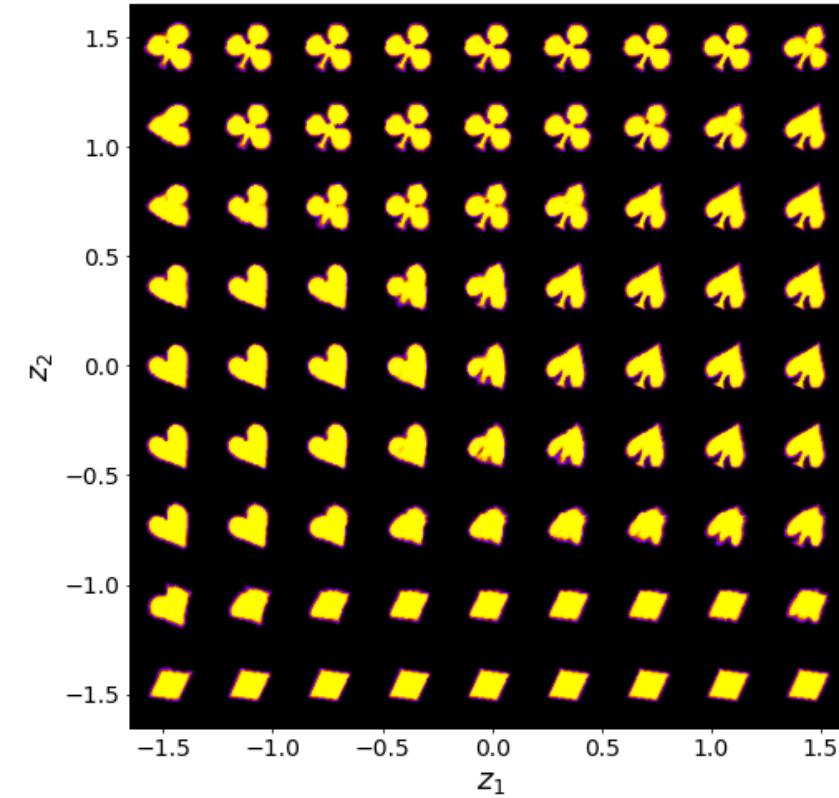
Cards 2: Low rotation (12 deg) and high shear (20 deg)

rVAE on Cards

Example of data

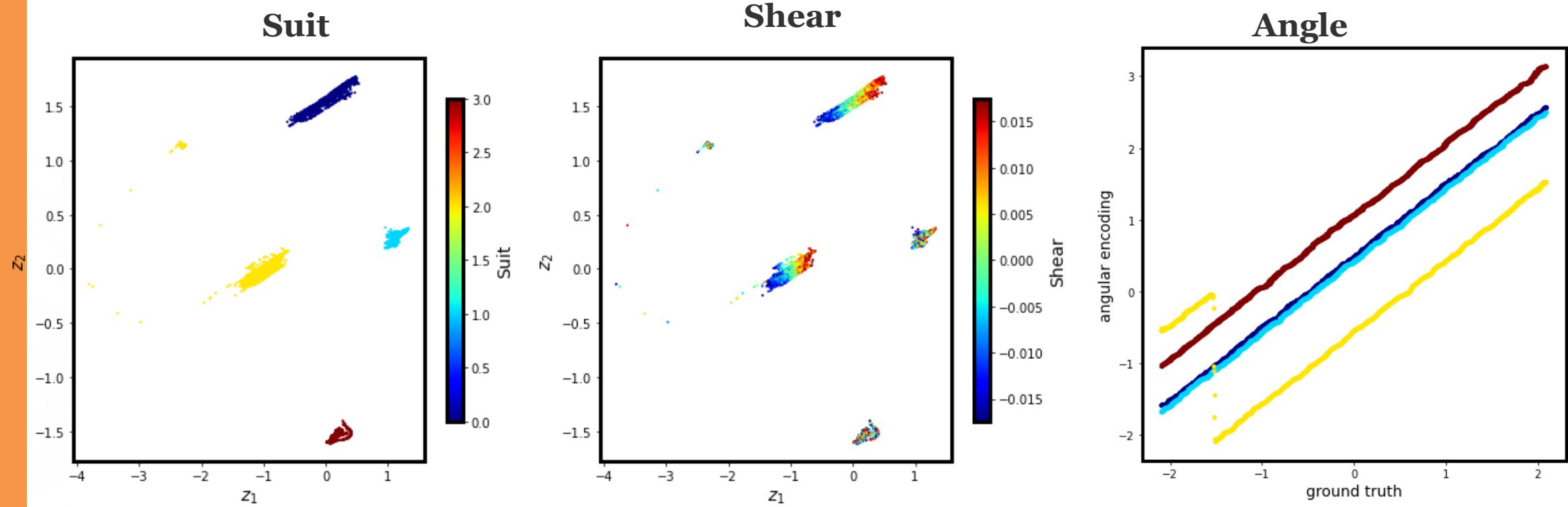


Latent representation



Cards 3: High rotation (120 deg) and low shear (1 deg)

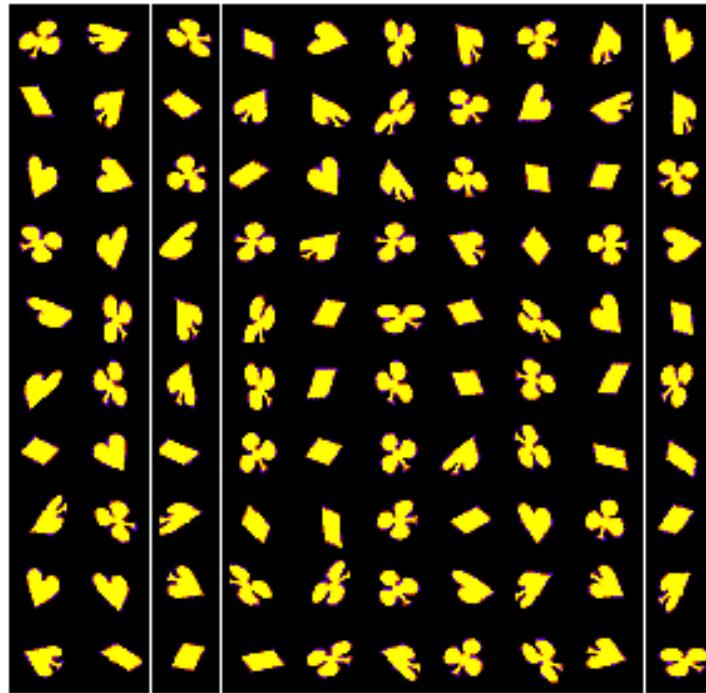
rVAE on Cards



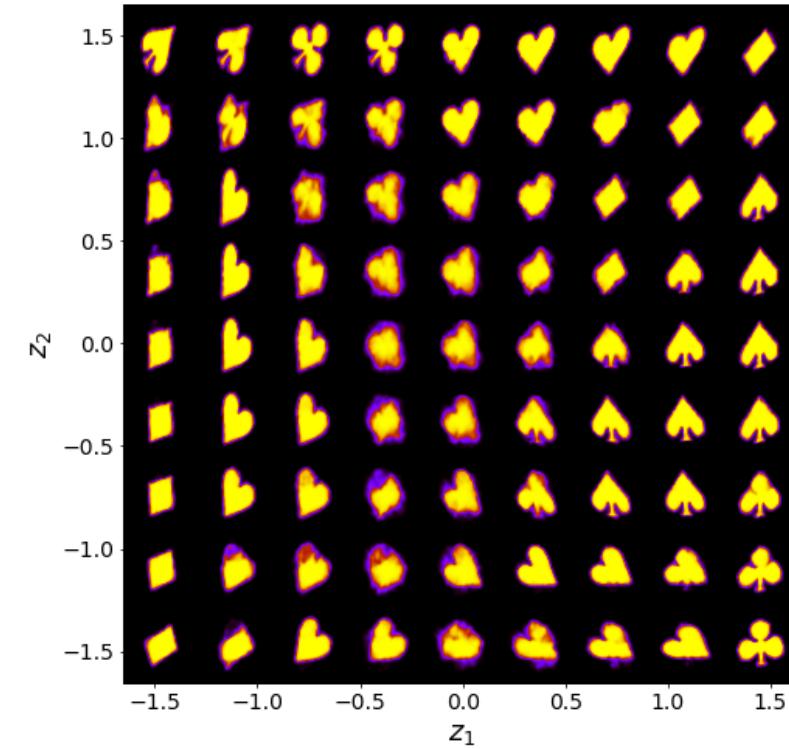
Cards 3: High rotation (120 deg) and low shear (1 deg)

rVAE on Cards

Example of data

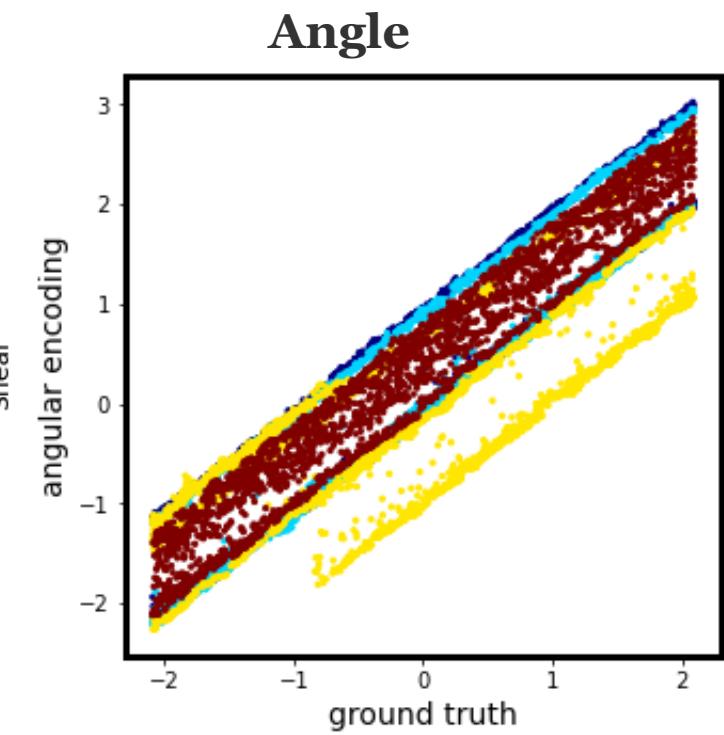
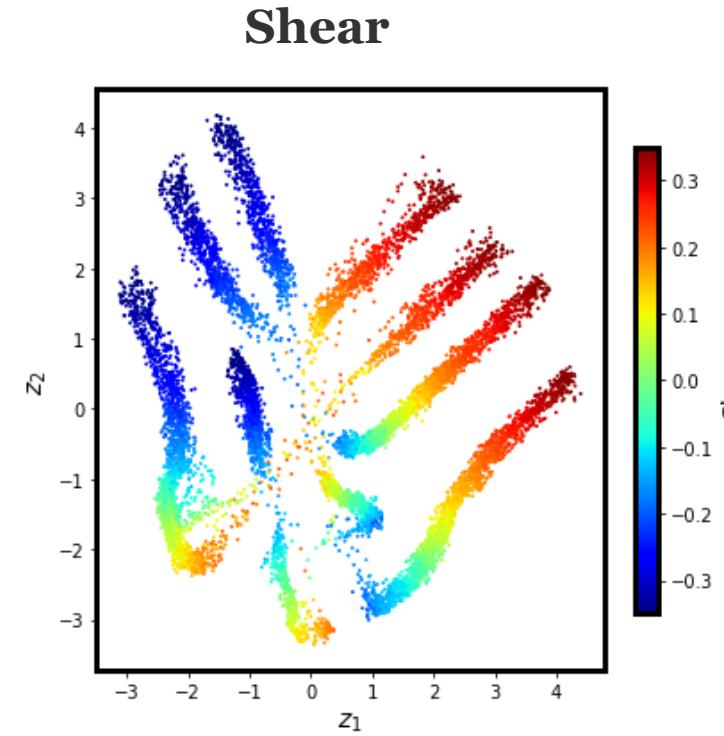
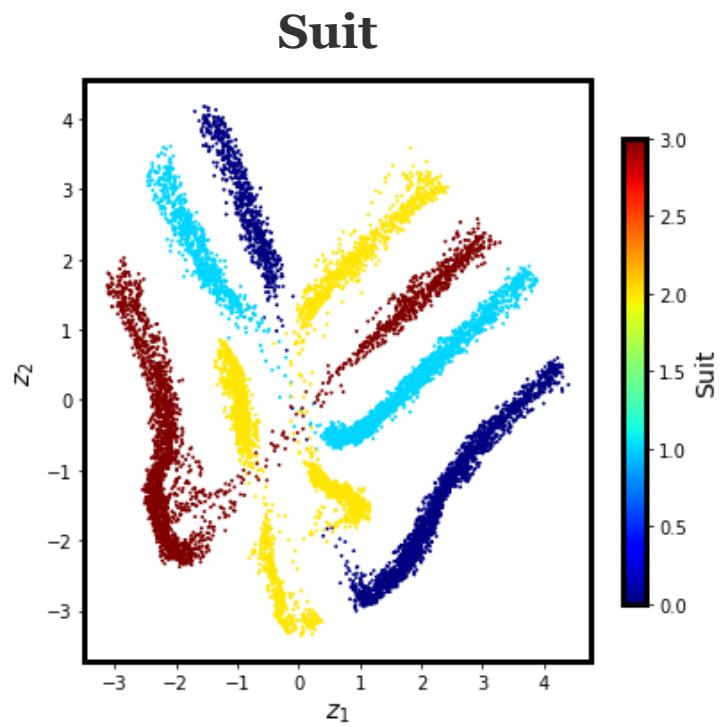


Latent representation



Cards 4: High rotation (120 deg) and high shear (20 deg)

rVAE on Cards

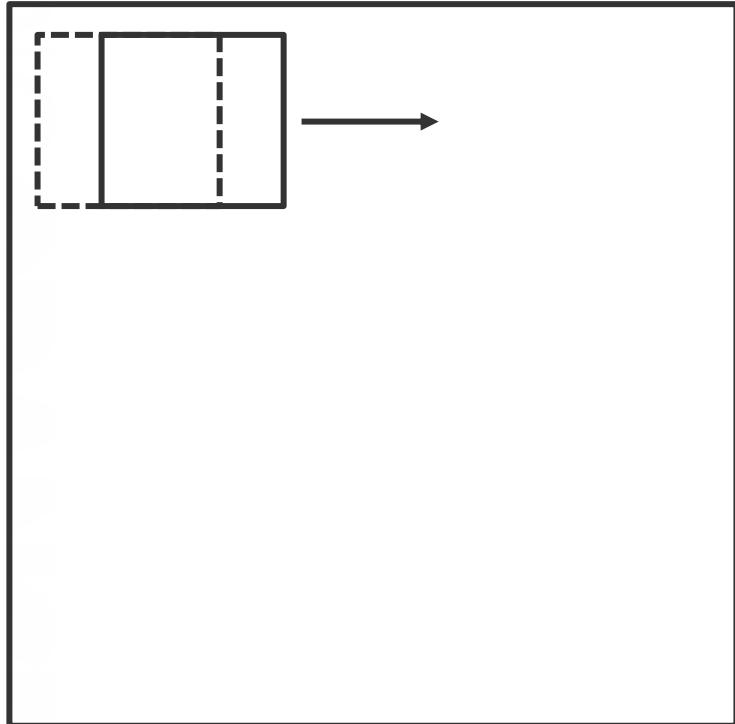


Cards 4: High rotation (120 deg) and high shear (20 deg)

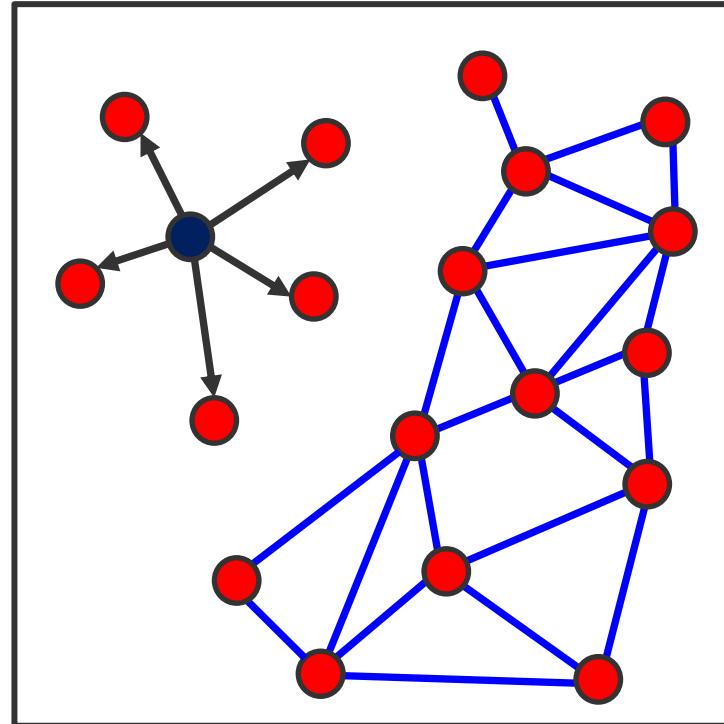
Describing the building blocks

- The classical physical descriptions (symmetry, etc) can be defined locally only in Bayesian sense
- We can argue that local descriptors are simple, if not necessarily known
- And the rules that guide their emergence are also simple, if not known

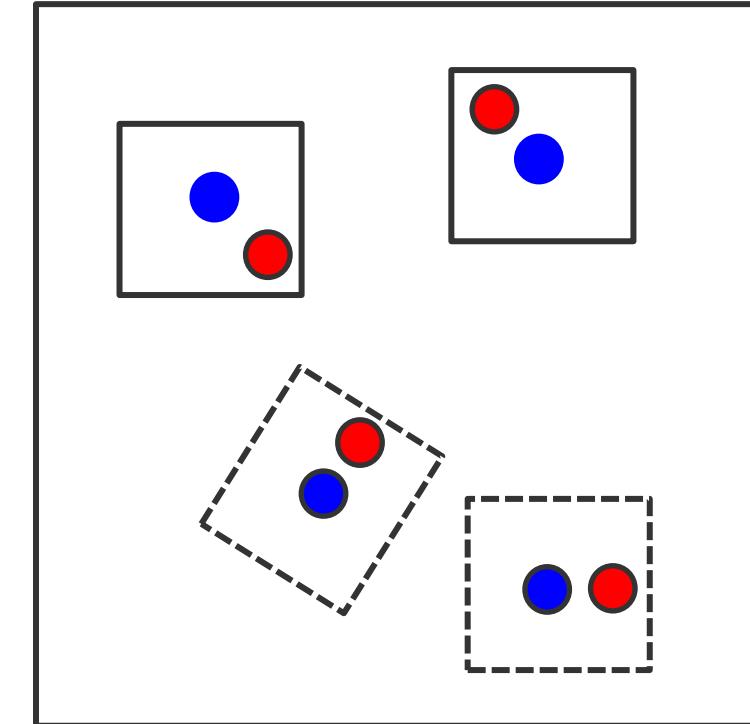
Continuous translational symmetry



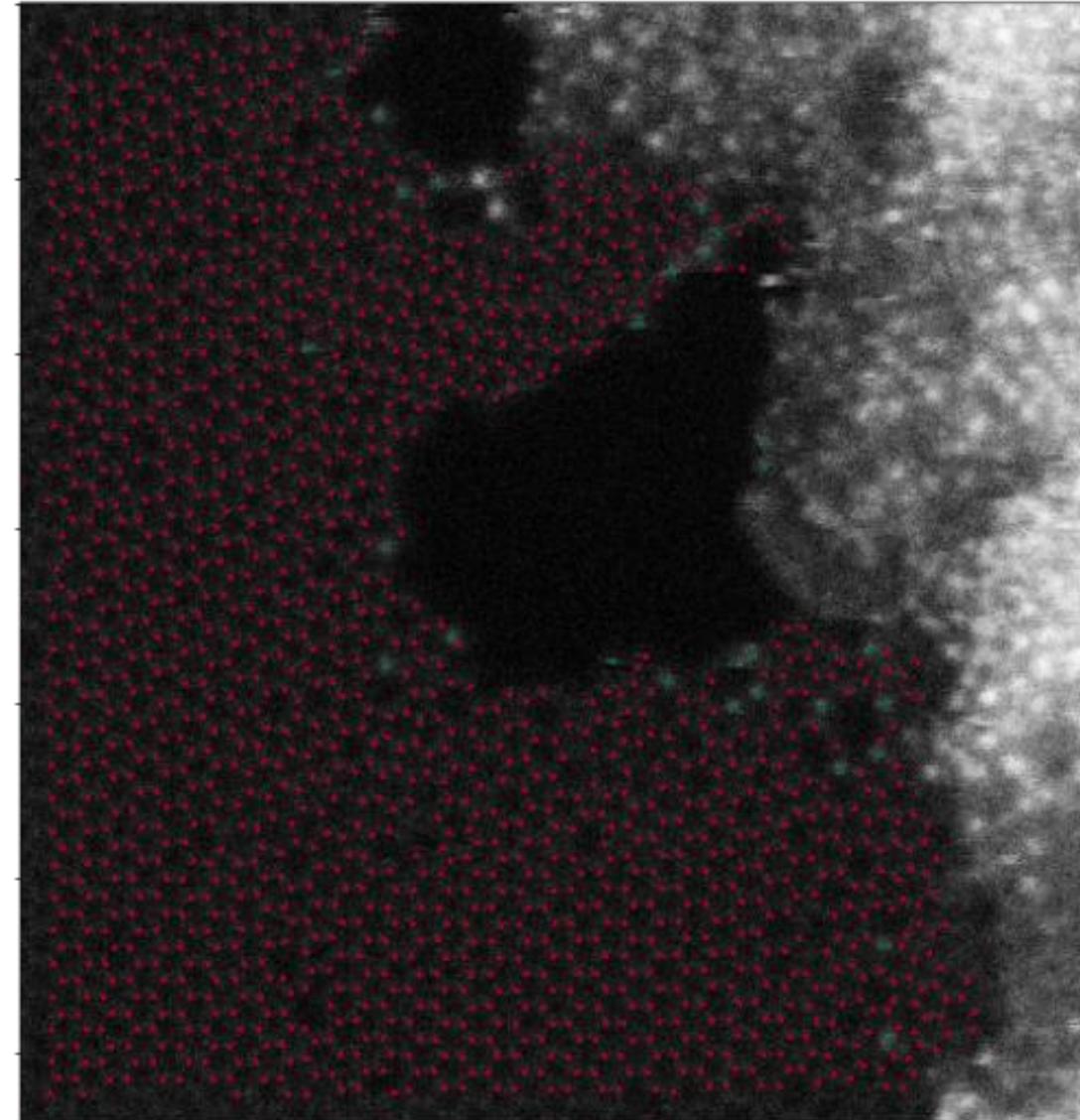
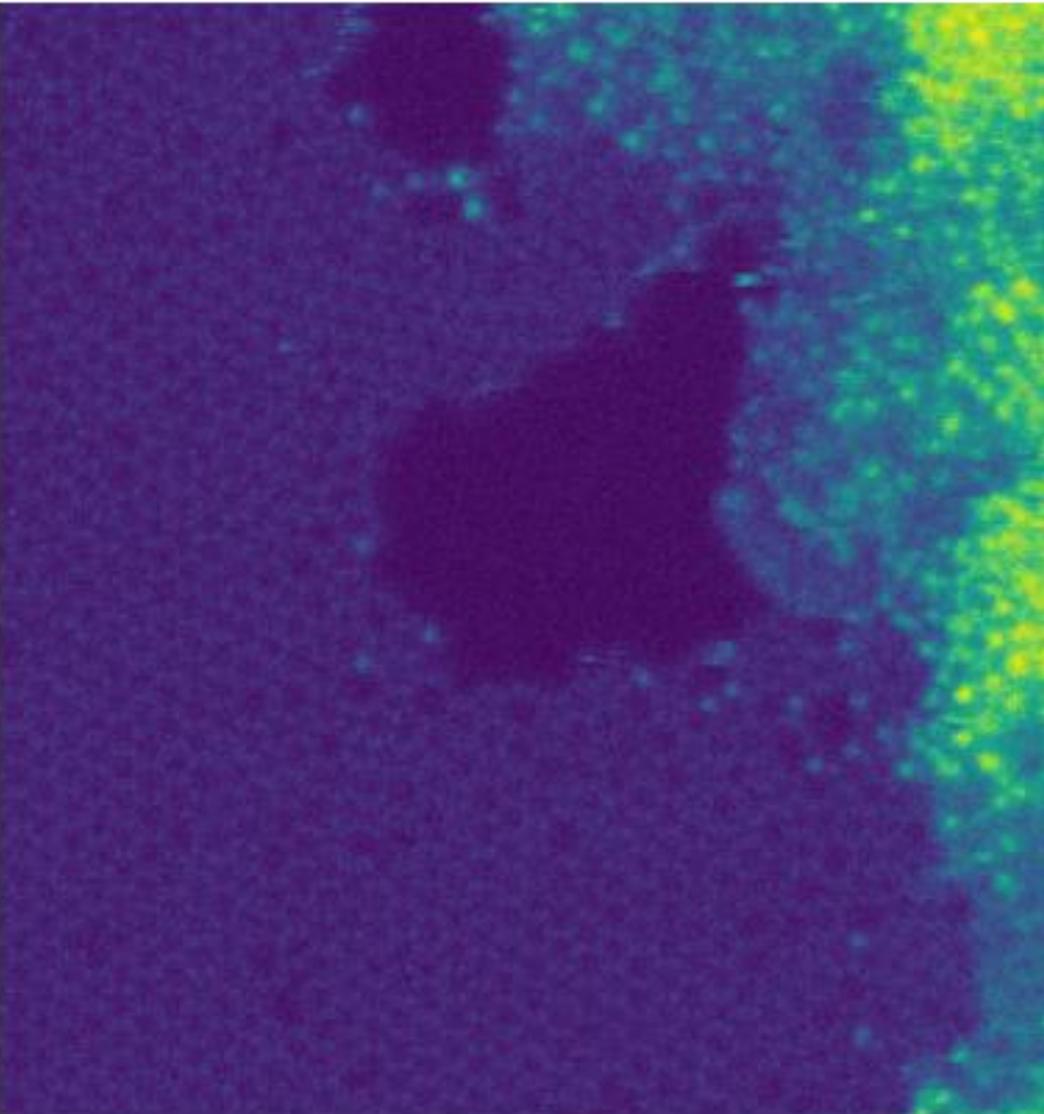
Atom based descriptions



Localized sub-images

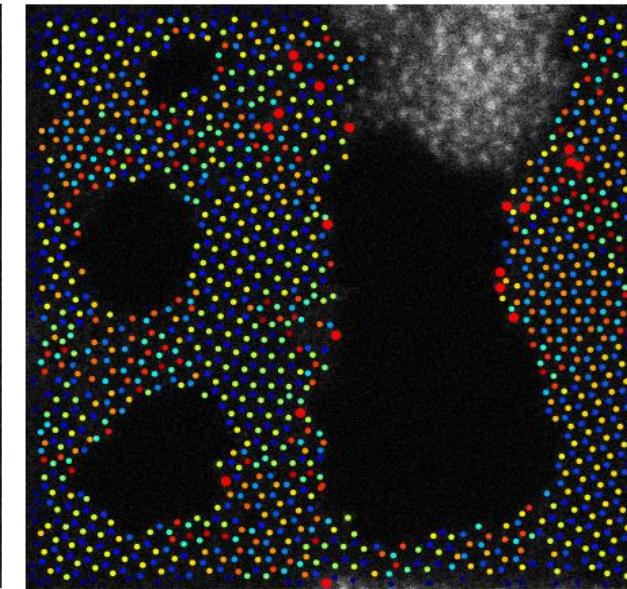
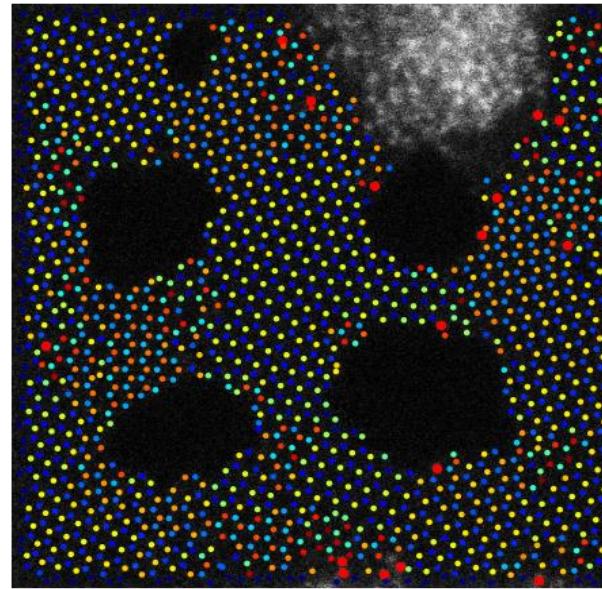
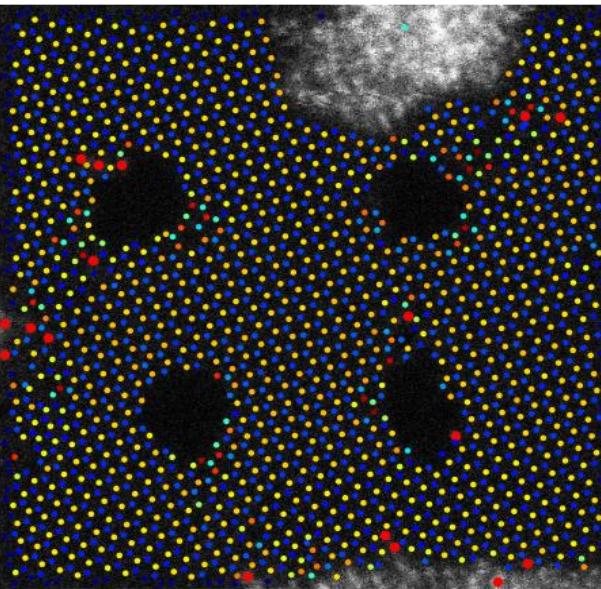


Off to chemically-disordered systems

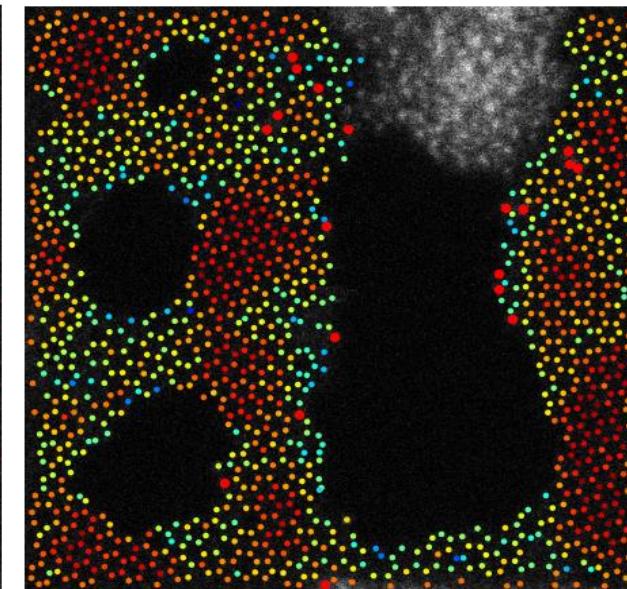
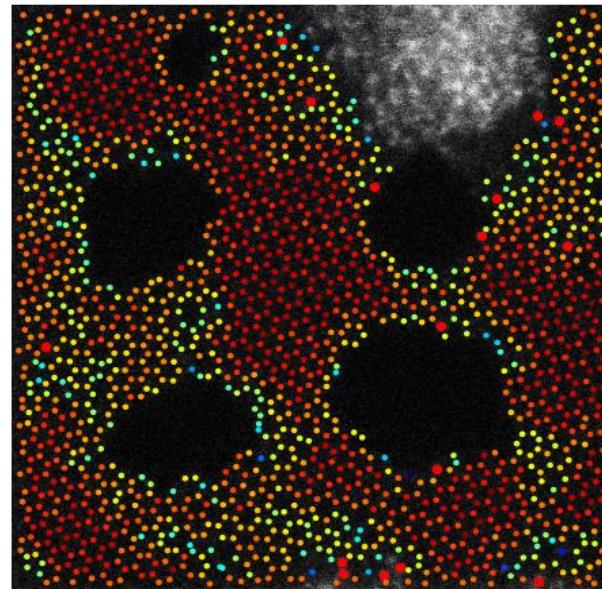
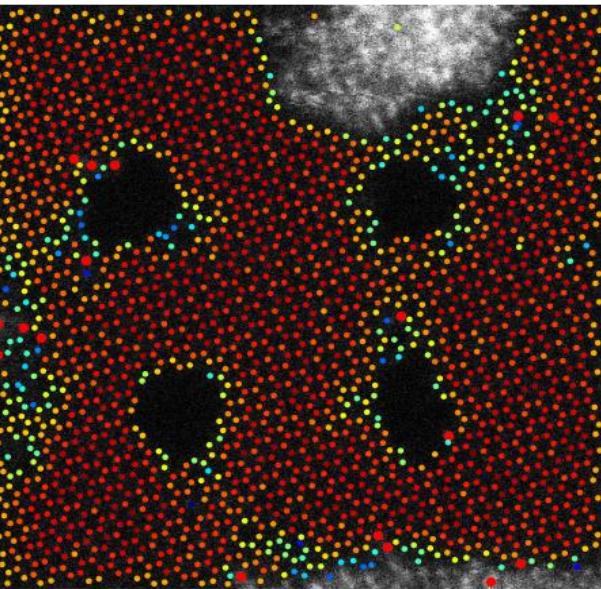


rVAE analysis at different time steps

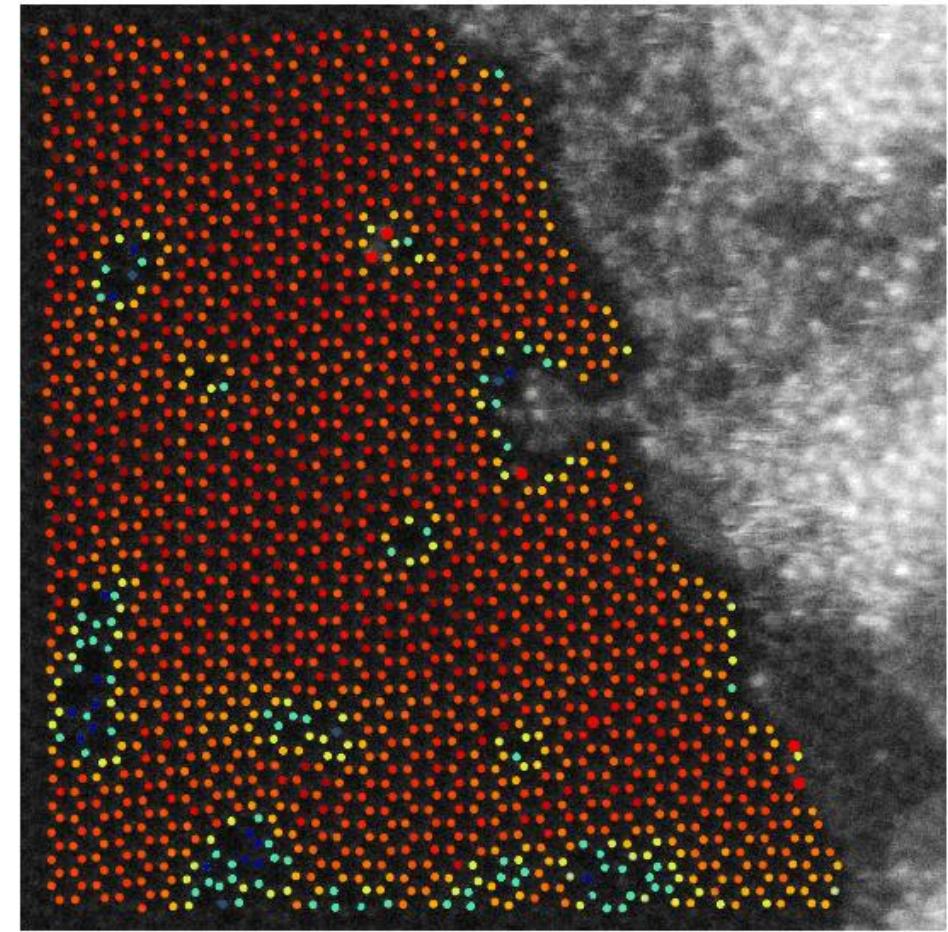
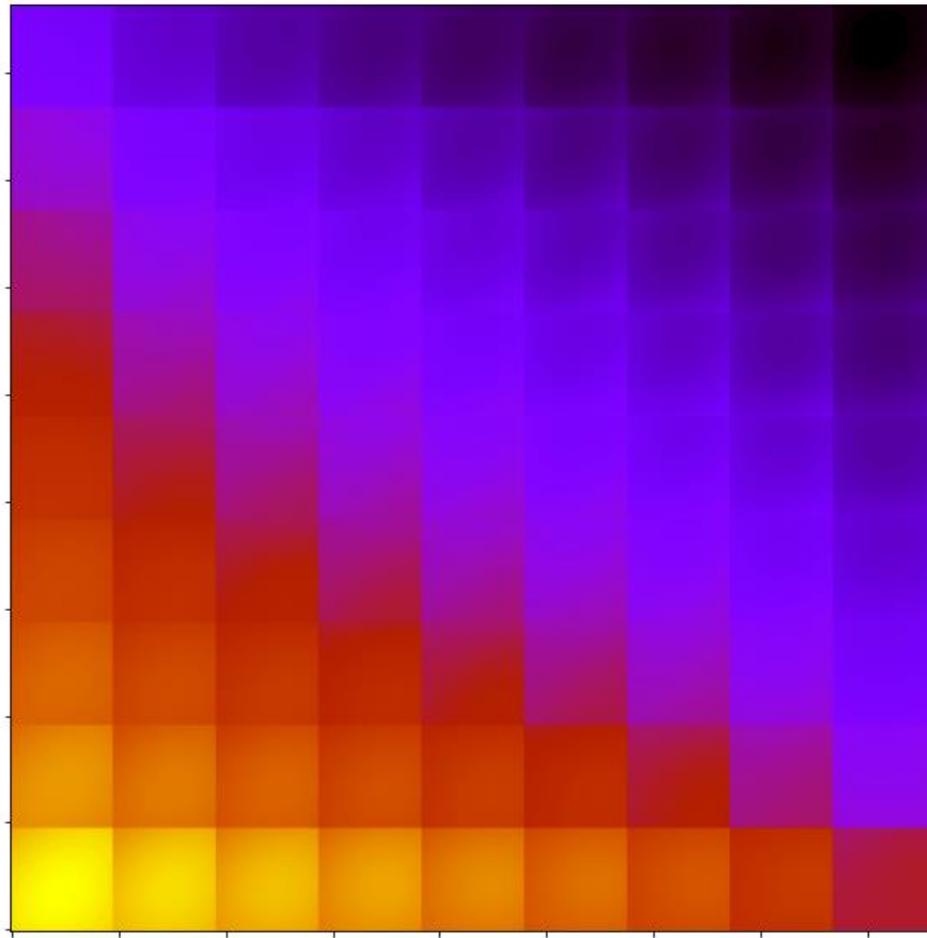
Angle



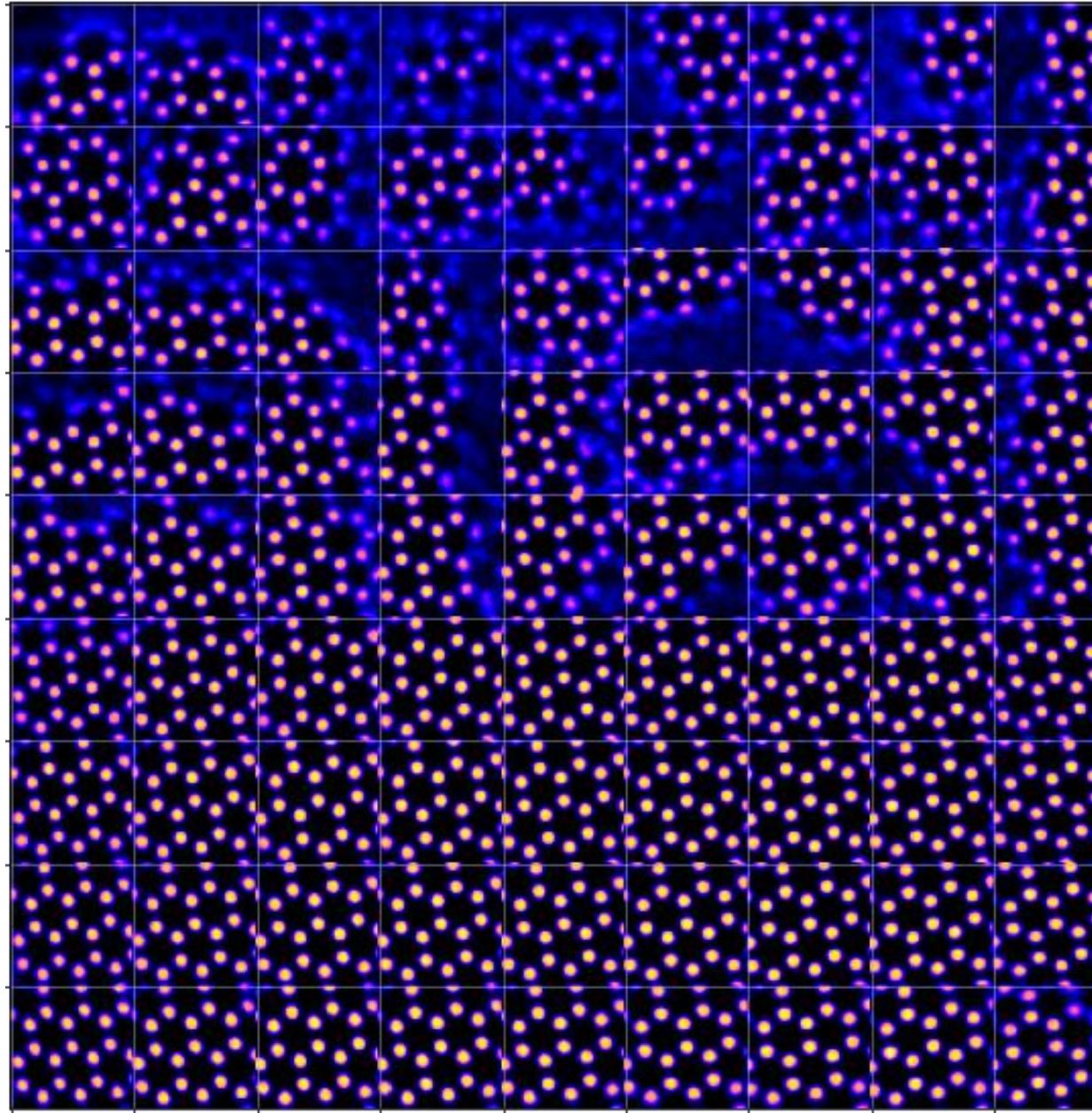
Latent variable



There is nothing as beautiful as training VAE



Next step: skip-rVAE



Unsupervised discovery of molecules

