

# TD 2

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## 1 Constant Propagation

Latice de départ :  $(Z \cup \{\perp, \top\}, \sqsubseteq, \sqcap, \sqcup)$

$a \sqsubseteq b$  si  $a \sqcup b = b$

$a \sqsubseteq b$  si  $a \sqcap b = a$

$f1, f2 [A \rightarrow X]$

$\forall x \in A \ (f1 \sqcup f2)(x) = f1(x) \sqcup f2(x)$

$([A \rightarrow X], \sqsubseteq, \sqcap, \sqcup)$

$([Vars \rightarrow (Z \cup \{\perp, \top\})], \sqsubseteq, \sqcap, \sqcup)$

C'est une analyse forward(En avant).

Equation:

$In(B) = \sqcup_{B' \in Pred(B)} Out(B')$

$Out(B) = F_B(In(B))$

Initialisation

$\forall B \ In(b) = \lambda x \in Var \ . \perp$

Variante de L'initialisation :

$\forall B \ In(B) = \forall x \in Vars \lambda \rightarrow \perp$

## 2 Exercice 75

1.

B1:  $x = 5$

$Y := 0$

B2:  $z := x + y$

$x := z$

B3:  $z := x - y$

$x := z$

B4:  $t := z + x$

On crée un vecteur de forme  $(v1, v2, v3, v4)$  avec  $x \rightarrow v1, y \rightarrow v2, z \rightarrow v3, t \rightarrow v4$

Bloc	In()	Out()	In()	Out()	In()	Out()	In()
B1	( $\perp, \perp, \perp, \perp$ )	(5,0, $\perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	(5,0, $\perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	(5,0, $\perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )
B2	( $\perp, \perp, \perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	(5,0, $\perp, \perp$ )	(5,0,5, $\perp$ )	(5,0, $\perp, \perp$ )	(5,0,5, $\perp$ )	(5,0, $\perp, \perp$ )
B3	( $\perp, \perp, \perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	(5,0, $\perp, \perp$ )	(5,0,5, $\perp$ )	(5,0, $\perp, \perp$ )	(5,0,5, $\perp$ )	(5,0, $\perp, \perp$ )
B4	( $\perp, \perp, \perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	(5,0,5, $\perp$ )	(5,0,5,10)	(5,0,5, $\perp$ )

Optimisation:

B2:  $z := 5$

$x := 5$

B3:  $z := 5$

$x := 5$

B4:  $t := 10$

2.

B1:  $x = 5$

$Y = 1$

B2:  $z := x + y$

$x := z$

B3:  $z := x - y$

$x := z$

B4:  $t := z + x$

Bloc	In()	Out()	In()	Out()	In()	Out()	In()
B1	( $\perp, \perp, \perp, \perp$ )	(5,1, $\perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	(5,1, $\perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	(5,1, $\perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )
B2	( $\perp, \perp, \perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	(5,1, $\perp, \perp$ )	(6,1,6, $\perp$ )	(5,1, $\perp, \perp$ )	(6,1,6, $\perp$ )	(5,1, $\perp, \perp$ )
B3	( $\perp, \perp, \perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	(5,1, $\perp, \perp$ )	(4,1,4, $\perp$ )	(5,1, $\perp, \perp$ )	(4,1,4, $\perp$ )	(5,1, $\perp, \perp$ )
B4	( $\perp, \perp, \perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	( $\perp, \perp, \perp, \perp$ )	( $\top, 1, \top, \perp$ )	( $\top, 1, \top, \top$ )	( $\top, 1, \top, \perp$ )

Optimisation:

B2:  $z := 6$

$x := 6$

B3:  $z := 4$

$x := 4$

### 3 Exercise 76

1.

B1:  $x:=4$   
 $y:=0$   
 $i:=0$ ;

B2:

B3:  $z:=x$   
 $t:=z+y$   
 $i:=i+1$

B4:

On crée un vecteur de forme  $(v1,v2,v3,v4,v5)$  avec  $x \rightarrow v1, y \rightarrow v2, z \rightarrow v3, t \rightarrow v4, i, , t \rightarrow v5$

Bloc	In()	Out()	In()	Out()	In()
B1	$(\perp, \perp, \perp, \perp, \perp)$	$(4, 0, \perp, \perp, 0)$	$(\perp, \perp, \perp, \perp, \perp)$	$(4, 0, \perp, \perp, 0)$	$(\perp, \perp, \perp, \perp, \perp)$
B2	$(\perp, \perp, \perp, \perp, \perp)$	$(\perp, \perp, \perp, \perp, \perp)$	$(4, 0, \perp, \perp, 0)$	$(4, 0, \perp, \perp, 0)$	$(4, 0, \perp, \perp, 0)$
B3	$(\perp, \perp, \perp, \perp, \perp)$	$(\perp, \perp, \perp, \perp, \perp)$	$(\perp, \perp, \perp, \perp, \perp)$	$(\perp, \perp, \perp, \perp, \perp)$	$(4, 0, \perp, \perp, 0)$
B4	$(\perp, \perp, \perp, \perp, \perp)$	$(\perp, \perp, \perp, \perp, \perp)$	$(\perp, \perp, \perp, \perp, \perp)$	$(\perp, \perp, \perp, \perp, \perp)$	$(4, 0, \perp, \perp, 0)$

Out()	In()	Out()	In()	Out()	In()
$(4, 0, \perp, \perp, 0)$	$(\perp, \perp, \perp, \perp, \perp)$	$(4, 0, \perp, \perp, 0)$	$(\perp, \perp, \perp, \perp, \perp)$	$(4, 0, \perp, \perp, 0)$	$(\perp, \perp, \perp, \perp, \perp)$
$(4, 0, \perp, \perp, 0)$	$(4, 0, 4, 4, \top)$	$(4, 0, 4, 4, \top)$	$(4, 0, 4, 4, \top)$	$(4, 0, 4, 4, \top)$	$(4, 0, 4, 4, \top)$
$(4, 0, 4, 4, 1)$	$(4, 0, \perp, \perp, 0)$	$(4, 0, 4, 4, 1)$	$(4, 0, 4, 4, \top)$	$(4, 0, 4, 4, \top)$	$(4, 0, 4, 4, \top)$
$(4, 0, \perp, \perp, 0)$	$(4, 0, \perp, \perp, 0)$	$(4, 0, \perp, \perp, 0)$	$(4, 0, 4, 4, \top)$	$(4, 0, 4, 4, \top)$	$(4, 0, 4, 4, \top)$

Optimisation:

B3:  $z:=4$   
 $t:=4$