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Лабораторная работа №5
по дисциплине «Методы машинного обучения»
«Обучение на основе временных различий»

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Задание

На основе рассмотренного на лекции примера реализуйте следующие алгоритмы:

- SARSA
- Q-обучение
- Двойное Q-обучение

Для любой среды обучения с подкреплением (кроме рассмотренной на лекции среды Toy Text / Frozen Lake) из библиотеки [Gym](#) (или аналогичной библиотеки).

Lab5

June 21, 2023

```
[ ]: import numpy as np
import matplotlib.pyplot as plt
import gymnasium as gym
from tqdm import tqdm
```

0.0.1

```
[ ]: class BasicAgent:
    '''
        ,
    '''

    #
    ALGO_NAME = '----'

    def __init__(self, env, eps=0.1):
        #
        self.env = env
        #
        self.nA = env.action_space.n
        self.nS = env.observation_space.n
        #
        self.Q = np.zeros((self.nS, self.nA))
        #
        #
        self.eps=eps
        #
        self.episodes_reward = []

    def print_q(self):
        print('Q-', self.ALGO_NAME)
        print(self.Q)

    def get_state(self, state):
        '''
        '''
        if type(state) is tuple:
```

```

        #
        return state[0]
    else:
        return state

def greedy(self, state):
    """
    << >>
    , Q-
    state
    """
    return np.argmax(self.Q[state])

def make_action(self, state):
    """
    """
    if np.random.uniform(0,1) < self.eps:
        # eps
        #
        return self.env.action_space.sample()
    else:
        # , Q-
        return self.greedy(state)

def draw_episodes_reward(self):
    #
    fig, ax = plt.subplots(figsize = (15,10))
    y = self.episodes_reward
    x = list(range(1, len(y)+1))
    plt.plot(x, y, '-', linewidth=1, color='green')
    plt.title(' ')
    plt.xlabel(' ')
    plt.ylabel(' ')
    plt.show()

def learn():
    """
    """
    pass

```

0.0.2 SARSA

```
[ ]: class SARSA_Agent(BasicAgent):
    '''
        SARSA
    '''
    #
    ALGO_NAME = 'SARSA'

    def __init__(self, env, eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000):
        #
        super().__init__(env, eps)
        # Learning rate
        self.lr=lr
        #
        self.gamma = gamma
        #
        self.num_episodes=num_episodes
        # eps
        self.eps_decay=0.00005
        self.eps_threshold=0.01

    def learn(self):
        '''
            SARSA
        '''
        self.episodes_reward = []
        #
        for ep in tqdm(list(range(self.num_episodes))):
            #
            state = self.get_state(self.env.reset())
            #
            done = False
            #
            truncated = False
            #
            tot_rew = 0

            # Q-
            if self.eps > self.eps_threshold:
                self.eps -= self.eps_decay

            #
            action = self.make_action(state)

            #
            while not (done or truncated):
                #
```

```

        next_state, rew, done, truncated, _ = self.env.step(action)

        #
        next_action = self.make_action(next_state)

        #           Q       SARSA
        self.Q[state][action] = self.Q[state][action] + self.lr * \
            (rew + self.gamma * self.Q[next_state][next_action] - self.
↪Q[state][action])

        #
        state = next_state
        action = next_action
        #
        tot_rew += rew
        if (done or truncated):
            self.episodes_reward.append(tot_rew)

```

0.0.3 Q-

```

[ ]: class QLearning_Agent(BasicAgent):
    '''
        Q-Learning
    '''
    #
    ALGO_NAME = 'Q-'

    def __init__(self, env, eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000):
        #
        super().__init__(env, eps)
        # Learning rate
        self.lr=lr
        #
        self.gamma = gamma
        #
        self.num_episodes=num_episodes
        #           eps
        self.eps_decay=0.00005
        self.eps_threshold=0.01

    def learn(self):
        '''
            Q-Learning
        '''
        self.episodes_reward = []
        #
        for ep in tqdm(list(range(self.num_episodes))):

```

```

#
state = self.get_state(self.env.reset())
#
done = False
#
truncated = False
#
tot_rew = 0

#           Q-
if self.eps > self.eps_threshold:
    self.eps -= self.eps_decay

#
while not (done or truncated):
    #
    #   SARSA
    action = self.make_action(state)

    #
    next_state, rew, done, truncated, _ = self.env.step(action)

    #           Q   SARSA (
    # self.Q[state][action] = self.Q[state][action] + self.lr * \
    #   (rew + self.gamma * self.Q[next_state][next_action] -
    ↪ self.Q[state][action])

    #           Q-
    self.Q[state][action] = self.Q[state][action] + self.lr * \
        (rew + self.gamma * np.max(self.Q[next_state]) - self.
    ↪ Q[state][action])

    #
    state = next_state
    #
    tot_rew += rew
    if (done or truncated):
        self.episodes_reward.append(tot_rew)

```

0.0.4 Q-

```

[ ]: class DoubleQLearning_Agent(BasicAgent):
    '''
        Double Q-Learning
    '''
    #
    ALGO_NAME = '   Q-   '

```

```

def __init__(self, env, eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000):
    #
    super().__init__(env, eps)
    #
    self.Q2 = np.zeros((self.nS, self.nA))
    # Learning rate
    self.lr=lr
    #
    self.gamma = gamma
    #
    self.num_episodes=num_episodes
    # eps
    self.eps_decay=0.00005
    self.eps_threshold=0.01

def greedy(self, state):
    """
    << >>
    , Q-
    state
    """
    temp_q = self.Q[state] + self.Q2[state]
    return np.argmax(temp_q)

def print_q(self):
    print(f" Q- {self.ALGO_NAME}")
    print('Q1')
    print(self.Q)
    print('Q2')
    print(self.Q2)

def learn(self):
    """
    Double Q-Learning
    """
    self.episodes_reward = []
    #
    for ep in tqdm(list(range(self.num_episodes))):
        #
        state = self.get_state(self.env.reset())
        #
        done = False
        #
        truncated = False
        #

```



```

tot_rew = 0

#           Q-
if self.eps > self.eps_threshold:
    self.eps -= self.eps_decay

#
while not (done or truncated):
    #
    #   SARSA
    action = self.make_action(state)

    #
    next_state, rew, done, truncated, _ = self.env.step(action)

    if np.random.rand() < 0.5:
        #
        self.Q[state][action] = self.Q[state][action] + self.lr * \
            (rew + self.gamma * self.Q2[next_state][np.argmax(self.
↪Q[next_state])]) - self.Q[state][action])
        else:
            #
            self.Q2[state][action] = self.Q2[state][action] + self.lr * ↪
↪\
                (rew + self.gamma * self.Q[next_state][np.argmax(self.
↪Q2[next_state])]) - self.Q2[state][action])

        #
        state = next_state
        #
        tot_rew += rew
        if (done or truncated):
            self.episodes_reward.append(tot_rew)

```

```

[ ]: def play_agent(agent):
    '''

    '''
    env2 = gym.make('Taxi-v3', render_mode='human')
    state = env2.reset()[0]
    done = False
    while not done:
        action = agent.greedy(state)
        next_state, reward, terminated, truncated, _ = env2.step(action)
        env2.render()
        state = next_state
        if terminated or truncated:

```

```

        done = True

def run_sarsa():
    env = gym.make('Taxi-v3')
    agent = SARSA_Agent(env)
    agent.learn()
    agent.print_q()
    agent.draw_episodes_reward()
    play_agent(agent)

def run_q_learning():
    env = gym.make('Taxi-v3')
    agent = QLearning_Agent(env)
    agent.learn()
    agent.print_q()
    agent.draw_episodes_reward()
    play_agent(agent)

def run_double_q_learning():
    env = gym.make('Taxi-v3')
    agent = DoubleQLearning_Agent(env)
    agent.learn()
    agent.print_q()
    agent.draw_episodes_reward()
    play_agent(agent)

```

0.0.5 SARSA: eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000

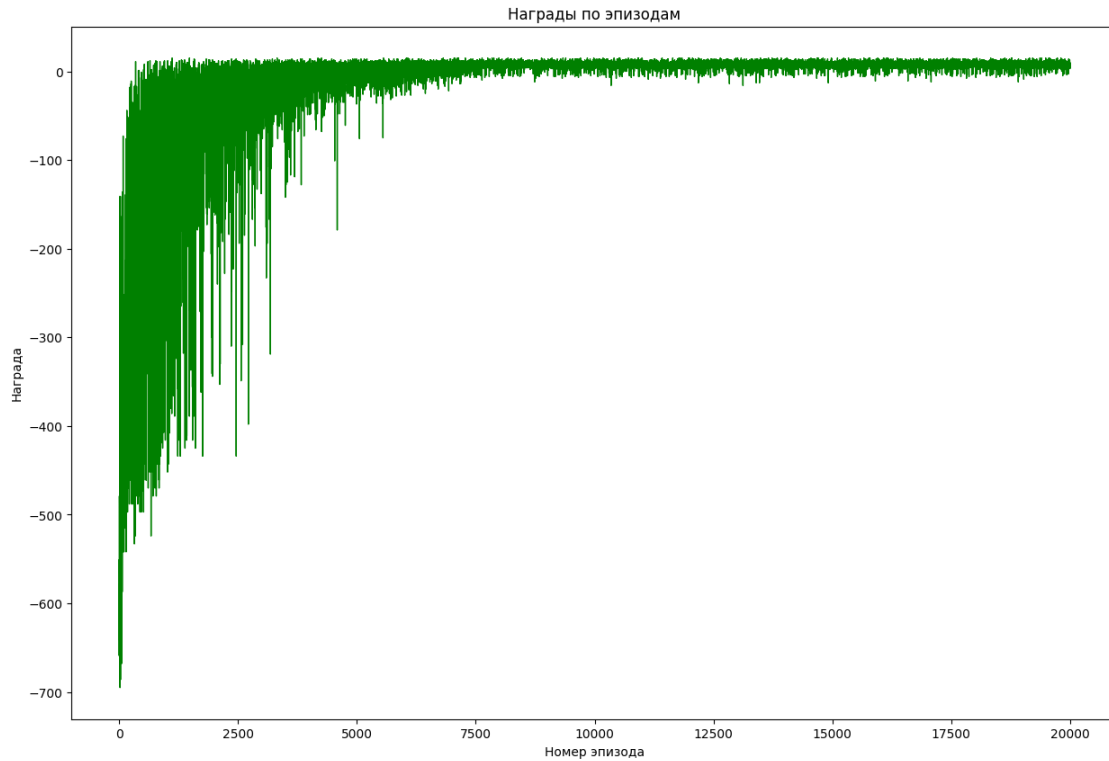
```
[ ]: run_sarsa()
```

```

0%|          | 0/20000 [00:00<?, ?it/s]100%|          | 20000/20000
[00:03<00:00, 6075.86it/s]

Q-          SARSA
[[ 0.         0.         0.         0.         0.
  0.         ]
 [-9.39511871 -7.82633886 -4.61973996 -7.91608244  7.52831391
 -14.58270727]
 [ 0.72064374  2.33945919  2.24226059  1.10286948 13.0813314
 -6.7719644 ]
 ...
 [-3.08864603  5.58824812 -3.13475835 -2.35462461 -7.02756406
 -9.25639657]
 [-7.77032983 -8.05657849 -8.49347554 -1.95002266 -14.61611739
 -14.22935898]
 [ 5.45984704  4.18158543 10.07790051 18.007744  1.41430917
 1.34707593]]

```



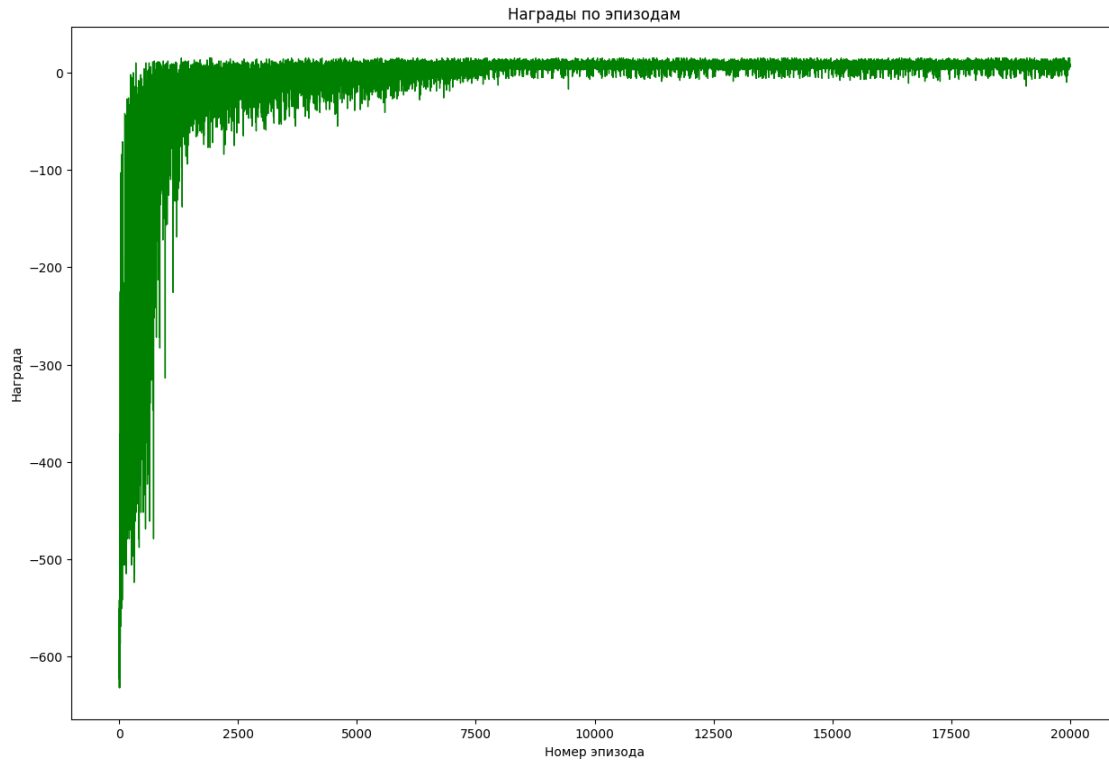
0.0.6 Q- : eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000

```
[ ]: run_q_learning()
```

```
100%|      | 20000/20000 [00:03<00:00, 5488.88it/s]
```

```

Q-      Q-
[[ 0.      0.      0.      0.      0.      0.      ]
 [ 5.55943204  6.43481406  4.66190971  6.25449521  8.36234335 -2.09352707]
 [ 9.16004638 11.34118969  9.82937408 10.403992   13.27445578  2.29056275]
 ...
 [ 1.48773717 13.44572688  1.69519677  0.142458   -3.59137074 -5.56482255]
 [-1.95348732  8.73563506 -2.38814501  0.59149548 -8.87902035 -7.38586058]
 [ 0.      6.46636365  9.54364847 18.59693097  0.87934239  3.81148721]]
```



0.0.7 Q- : eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000

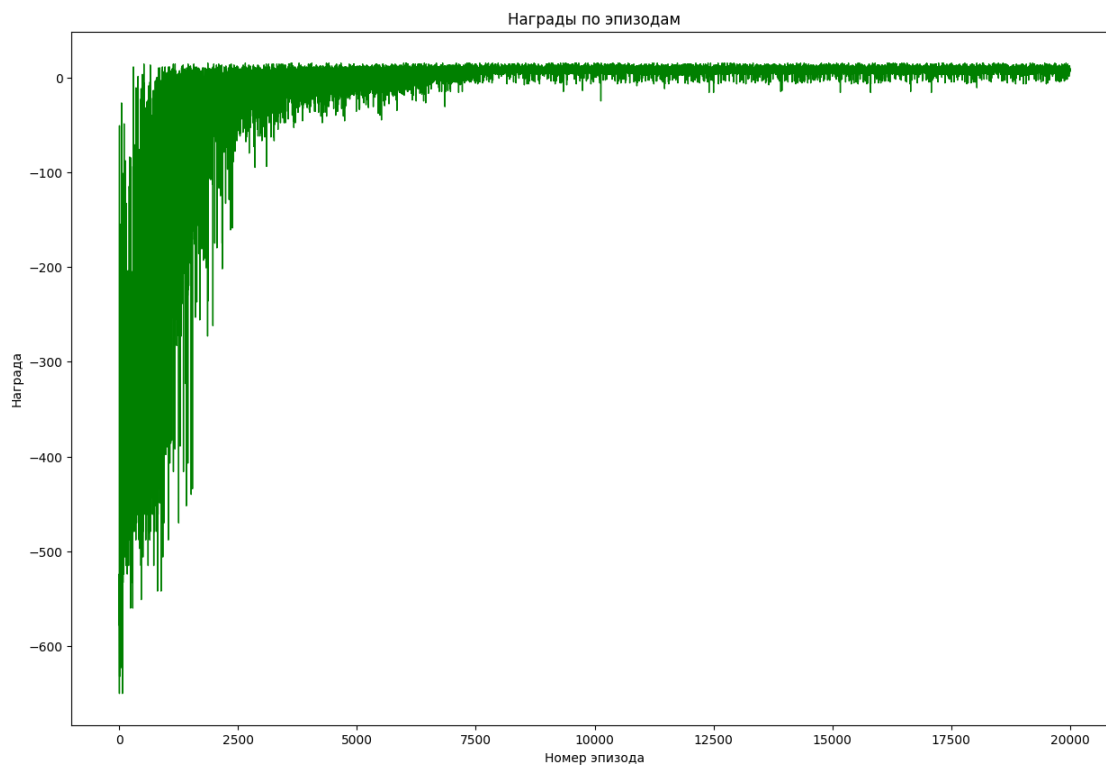
```
[ ]: run_double_q_learning()
```

```
100%|      | 20000/20000 [00:04<00:00, 4883.75it/s]
```

```

    Q-          Q-
Q1
[[ 0.00000000e+00  0.00000000e+00  0.00000000e+00  0.00000000e+00
  0.00000000e+00  0.00000000e+00]
 [ 1.16163046e+00  6.45016960e-01  1.00769948e+00  3.72291477e+00
  8.36234335e+00 -5.01468586e+00]
 [ 6.09505909e+00  8.36560187e+00 -4.07224966e-01  7.05822996e+00
  1.32744558e+01  6.45841012e-01]
...
 [-7.99180545e-01  1.07550337e+01 -1.44867522e+00 -2.35590222e+00
 -5.86881524e+00 -5.62712420e+00]
 [-3.98247635e+00  4.37814489e+00 -3.92624883e+00 -2.60475579e+00
 -5.10770158e+00 -7.54219253e+00]
 [ 2.78683960e+00  2.85534245e+00  0.00000000e+00  1.83727537e+01
  4.18884557e-01 -7.50927475e-03]]
Q2
[[ 0.          0.          0.          0.          0.          0.          ]
 [-0.2934294   3.26994885 -1.42217566  5.04477693  8.36234335 -5.90593791]]
```

```
[ 5.90112017  5.46169946  2.42918746  3.80673123 13.27445578 -0.5747265 ]  
...  
[-2.10538343 11.9391959  -1.57538495 -1.53177373 -3.18288299 -4.73475405]  
[-3.74525344  3.01047271 -3.83516418 -4.04781581 -4.80672105 -5.4513151 ]  
[ 3.14380145  1.05446787  1.51034447 18.44538414 -3.68630097  0.42193263]]
```



Lab5

June 22, 2023

```
[ ]: import numpy as np
import matplotlib.pyplot as plt
import gymnasium as gym
from tqdm import tqdm
```

0.0.1

```
[ ]: class BasicAgent:
    '''
        ,
    '''

    #
    ALGO_NAME = '----'

    def __init__(self, env, eps=0.1):
        #
        self.env = env
        #
        self.nA = env.action_space.n
        self.nS = env.observation_space.n
        #
        self.Q = np.zeros((self.nS, self.nA))
        #
        #
        self.eps=eps
        #
        self.episodes_reward = []

    def print_q(self):
        print('Q-', self.ALGO_NAME)
        print(self.Q)

    def get_state(self, state):
        '''
        '''
        if type(state) is tuple:
```

```

        #
        return state[0]
    else:
        return state

def greedy(self, state):
    """
    << >>
    , Q-
    state
    """
    return np.argmax(self.Q[state])

def make_action(self, state):
    """
    """
    if np.random.uniform(0,1) < self.eps:

        # eps
        #
        return self.env.action_space.sample()
    else:
        # , Q-
        return self.greedy(state)

def draw_episodes_reward(self):
    #
    fig, ax = plt.subplots(figsize = (15,10))
    y = self.episodes_reward
    x = list(range(1, len(y)+1))
    plt.plot(x, y, '-', linewidth=1, color='green')
    plt.title(' ')
    plt.xlabel(' ')
    plt.ylabel(' ')
    plt.show()

def learn():
    """
    """
    pass

```

0.0.2 SARSA

```
[ ]: class SARSA_Agent(BasicAgent):
    '''
        SARSA
    '''
    #
    ALGO_NAME = 'SARSA'

    def __init__(self, env, eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000):
        #
        super().__init__(env, eps)
        # Learning rate
        self.lr=lr
        #
        self.gamma = gamma
        #
        self.num_episodes=num_episodes
        # eps
        self.eps_decay=0.00005
        self.eps_threshold=0.01

    def learn(self):
        '''
            SARSA
        '''
        self.episodes_reward = []
        #
        for ep in tqdm(list(range(self.num_episodes))):
            #
            state = self.get_state(self.env.reset())
            #
            done = False
            #
            truncated = False
            #
            tot_rew = 0

            # Q-
            if self.eps > self.eps_threshold:
                self.eps -= self.eps_decay

            #
            action = self.make_action(state)

            #
            while not (done or truncated):
                #
```



```

        next_state, rew, done, truncated, _ = self.env.step(action)

        #
        next_action = self.make_action(next_state)

        #           Q       SARSA
        self.Q[state][action] = self.Q[state][action] + self.lr * \
            (rew + self.gamma * self.Q[next_state][next_action] - self.
↪Q[state][action])

        #
        state = next_state
        action = next_action
        #
        tot_rew += rew
        if (done or truncated):
            self.episodes_reward.append(tot_rew)

```

0.0.3 Q-

```

[ ]: class QLearning_Agent(BasicAgent):
    '''
        Q-Learning
    '''
    #
    ALGO_NAME = 'Q-'

    def __init__(self, env, eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000):
        #
        super().__init__(env, eps)
        # Learning rate
        self.lr=lr
        #
        self.gamma = gamma
        #
        self.num_episodes=num_episodes
        #           eps
        self.eps_decay=0.00005
        self.eps_threshold=0.01

    def learn(self):
        '''
            Q-Learning
        '''
        self.episodes_reward = []
        #
        for ep in tqdm(list(range(self.num_episodes))):

```

```

#
state = self.get_state(self.env.reset())
#
done = False
#
truncated = False
#
tot_rew = 0

#           Q-
if self.eps > self.eps_threshold:
    self.eps -= self.eps_decay

#
while not (done or truncated):
    #
    #   SARSA
    action = self.make_action(state)

    #
    next_state, rew, done, truncated, _ = self.env.step(action)

    #           Q   SARSA (
    # self.Q[state][action] = self.Q[state][action] + self.lr * \
    #   (rew + self.gamma * self.Q[next_state][next_action] -
    ↪ self.Q[state][action])

    #           Q-
    self.Q[state][action] = self.Q[state][action] + self.lr * \
        (rew + self.gamma * np.max(self.Q[next_state]) - self.
    ↪ Q[state][action])

    #
    state = next_state
    #
    tot_rew += rew
    if (done or truncated):
        self.episodes_reward.append(tot_rew)

```

0.0.4 Q-

```

[ ]: class DoubleQLearning_Agent(BasicAgent):
    '''
        Double Q-Learning
    '''
    #
    ALGO_NAME = '   Q-   '

```

```

def __init__(self, env, eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000):
    #
    super().__init__(env, eps)
    #
    self.Q2 = np.zeros((self.nS, self.nA))
    # Learning rate
    self.lr=lr
    #
    self.gamma = gamma
    #
    self.num_episodes=num_episodes
    # eps
    self.eps_decay=0.00005
    self.eps_threshold=0.01

def greedy(self, state):
    """
    << >>
    , Q-
    state
    """
    temp_q = self.Q[state] + self.Q2[state]
    return np.argmax(temp_q)

def print_q(self):
    print(f" Q- {self.ALGO_NAME}")
    print('Q1')
    print(self.Q)
    print('Q2')
    print(self.Q2)

def learn(self):
    """
    Double Q-Learning
    """
    self.episodes_reward = []
    #
    for ep in tqdm(list(range(self.num_episodes))):
        #
        state = self.get_state(self.env.reset())
        #
        done = False
        #
        truncated = False
        #

```

```

tot_rew = 0

#           Q-
if self.eps > self.eps_threshold:
    self.eps -= self.eps_decay

#
while not (done or truncated):
    #
    # SARSA
    action = self.make_action(state)

    #
    next_state, rew, done, truncated, _ = self.env.step(action)

    if np.random.rand() < 0.5:
        #
        self.Q[state][action] = self.Q[state][action] + self.lr * \
            (rew + self.gamma * self.Q2[next_state][np.argmax(self.
↪Q[next_state])]) - self.Q[state][action])
        else:
            #
            self.Q2[state][action] = self.Q2[state][action] + self.lr * ↪
↪\
                (rew + self.gamma * self.Q[next_state][np.argmax(self.
↪Q2[next_state])]) - self.Q2[state][action])

    #
    state = next_state
    #
    tot_rew += rew
    if (done or truncated):
        self.episodes_reward.append(tot_rew)

```

```

[ ]: def play_agent(agent):
    '''

    '''
    env2 = gym.make('CliffWalking-v0', render_mode='human')
    state = env2.reset()[0]
    done = False
    while not done:
        action = agent.greedy(state)
        next_state, reward, terminated, truncated, _ = env2.step(action)
        env2.render()
        state = next_state
        if terminated or truncated:

```

```

done = True

def run_sarsa():
    env = gym.make('CliffWalking-v0')
    agent = SARSA_Agent(env)
    agent.learn()
    agent.print_q()
    agent.draw_episodes_reward()
    play_agent(agent)

def run_q_learning():
    env = gym.make('CliffWalking-v0')
    agent = QLearning_Agent(env)
    agent.learn()
    agent.print_q()
    agent.draw_episodes_reward()
    play_agent(agent)

def run_double_q_learning():
    env = gym.make('CliffWalking-v0')
    agent = DoubleQLearning_Agent(env)
    agent.learn()
    agent.print_q()
    agent.draw_episodes_reward()
    play_agent(agent)

```

0.0.5 SARSA: eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000

```
[ ]: run_sarsa()
```

```

0%|          | 0/20000 [00:00<?, ?it/s]100%|          | 20000/20000
[00:02<00:00, 7673.73it/s]

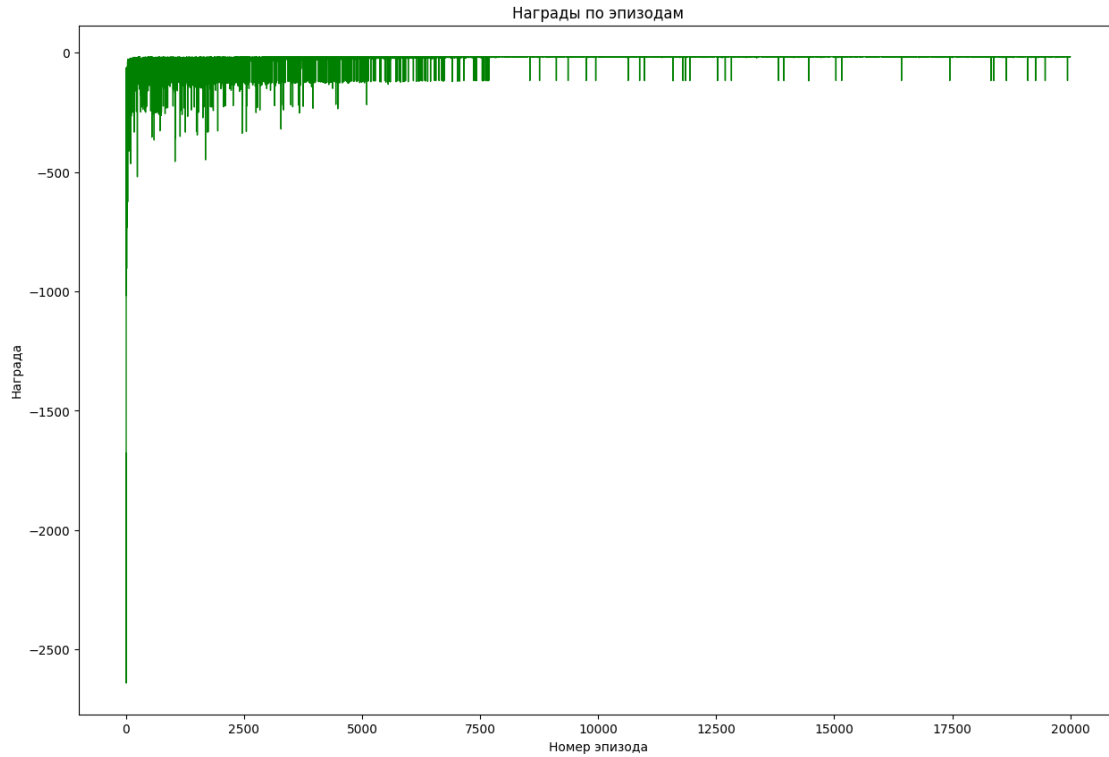
```

Q-	SARSA		
[-13.23268491	-12.44924206	-14.14831971	-13.21756225]
[-12.45494055	-11.67549393	-13.20950629	-13.4035355]
[-11.69529513	-10.84139566	-12.57271256	-12.64912424]
[-10.87218618	-9.9998437	-11.76705827	-11.90242225]
[-10.06010061	-9.1837413	-11.09200247	-11.06105557]
[-9.25122716	-8.34921633	-10.17854914	-10.23577852]
[-8.38617936	-7.4893919	-9.4211632	-9.53270723]
[-7.55922396	-6.60501981	-8.51359079	-8.58745887]
[-6.63714748	-5.70849155	-7.68342711	-7.75050899]
[-5.77551649	-4.80404568	-5.54444773	-6.83273798]
[-4.84843535	-3.88159414	-4.15313036	-5.99035878]
[-3.94294948	-3.91932543	-2.9404	-5.05266446]
[-13.17392746	-13.34637305	-14.89641159	-13.95140211]
[-12.42665153	-16.47657546	-29.01680815	-17.65084815]

```

[ -11.66567482 -16.68672111 -20.5102616 -17.8414342 ]
[ -10.86919026 -15.61148531 -32.42843662 -18.47134339]
[ -10.15820666 -16.98428296 -25.91981234 -17.14481683]
[ -9.25234558 -15.06992891 -26.94642106 -15.56501666]
[ -8.41619366 -12.26754446 -16.97101777 -16.54237379]
[ -7.53755978 -12.37958957 -29.74526021 -14.20447512]
[ -6.66052327 -9.36973255 -17.07372286 -12.09477326]
[ -7.35783232 -3.97032385 -15.92247357 -10.53564895]
[ -5.4088259 -3.02463449 -3.46600362 -5.67229515]
[ -4.08753469 -2.95444307 -1.98 -4.06757945]
[ -13.89391328 -14.71450139 -15.58969982 -14.75950388]
[ -13.34619252 -31.16288633 -126.36814692 -19.96574689]
[ -16.50520592 -34.06474865 -122.34482628 -25.91373421]
[ -16.90923146 -19.95245543 -110.86121513 -24.70884421]
[ -15.33529128 -29.425508 -108.8013712 -18.97302926]
[ -13.66564486 -17.65124734 -130.70426823 -22.69681827]
[ -13.53784948 -22.76811558 -117.95302017 -25.04003713]
[ -13.60826709 -24.78443046 -98.17996515 -21.38798081]
[ -10.39753932 -12.42324541 -121.66256427 -14.49835846]
[ -8.19363547 -14.65103168 -111.03711951 -20.27325864]
[ -6.59063812 -1.98406991 -125.98873843 -20.06085201]
[ -3.33434516 -1.98019898 -1. -2.98974388]
[ -14.61157293 -114.40445387 -15.41952684 -16.28296638]
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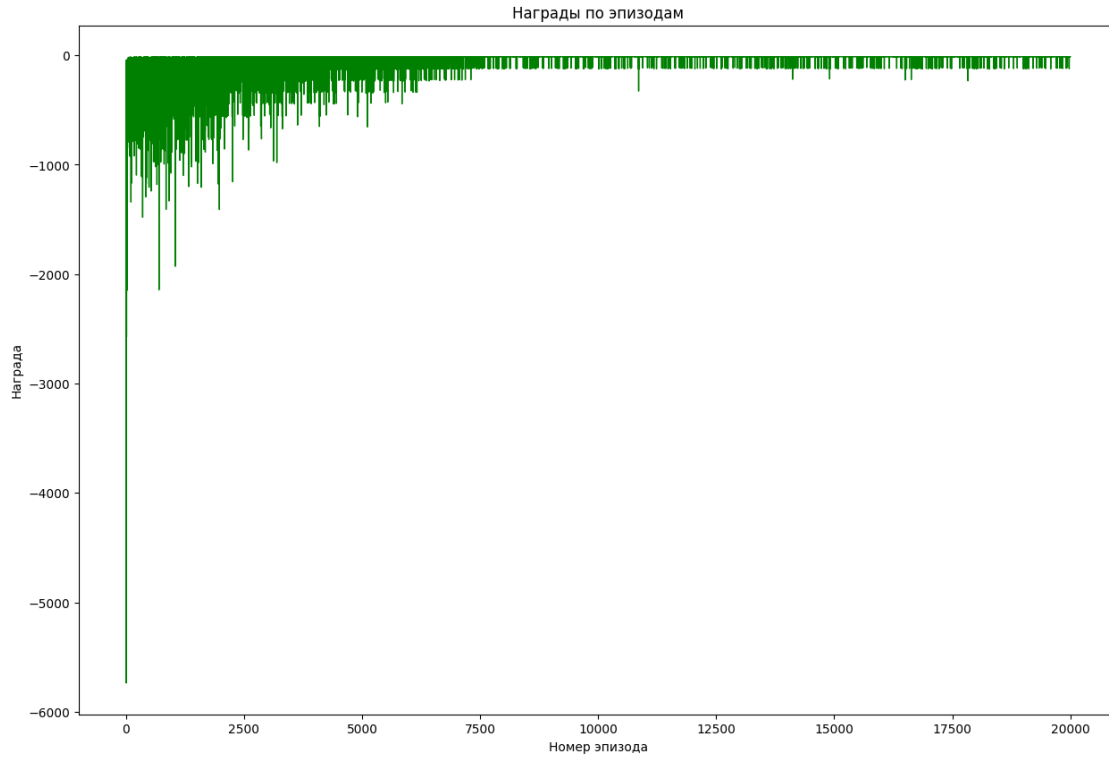
0.0.6 Q- : eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000

```
[ ]: run_q_learning()
```

100%| | 20000/20000 [00:02<00:00, 7060.42it/s]

Q-	Q-	Q-	Q-
[-12.62716012	-12.30066353	-12.30187123	-12.53106295]
[-12.07218236	-11.54852805	-11.54851636	-12.11875414]
[-11.42779808	-10.76413781	-10.76413919	-12.16847347]
[-10.57702507	-9.96342977	-9.96342972	-11.42478967]
[-9.9027344	-9.14635907	-9.14635904	-10.7323342]
[-9.10277569	-8.31261174	-8.31261174	-9.80236621]
[-8.29075731	-7.46184883	-7.46184883	-9.13145237]
[-7.4603197	-6.59372333	-6.59372333	-8.30611621]
[-6.58453374	-5.70788095	-5.70788095	-7.43266689]
[-5.69808106	-4.80396016	-4.80396016	-6.54830251]
[-4.77048085	-3.881592	-3.881592	-5.67970024]
[-3.85517669	-3.74152451	-2.9404	-4.70627397]
[-13.03839926	-11.54888054	-11.54888054	-12.31783472]
[-12.31686436	-10.76416381	-10.76416381	-12.31789838]
[-11.54878676	-9.96343246	-9.96343246	-11.54888044]
[-10.76415382	-9.14635966	-9.14635966	-10.76416365]
[-9.96343031	-8.31261189	-8.31261189	-9.96343245]

[illegible]



0.0.7 Q- : eps=0.4, lr=0.1, gamma=0.98, num_episodes=20000

```
[ ]: run_double_q_learning()
```

```
0%|          | 0/20000 [00:00<?, ?it/s]100%|          | 20000/20000
[00:02<00:00, 6718.46it/s]
```

```
Q-          Q-
Q1
[[ -15.03480352 -13.96217453 -12.32230003 -14.82268257]
 [ -13.7147303  -13.2499411  -11.54906998 -14.33643105]
 [ -12.81266898 -14.47698313 -10.78932154 -14.66383856]
 [ -13.42803396 -11.47301851 -10.0188274  -12.13172171]
 [ -11.31325571 -10.77256639  -9.14882818 -12.7290895 ]
 [ -11.56242234 -10.65416174  -8.33248595 -11.30154597]
 [ -10.66153285 -10.61448073  -7.59024673 -11.20785512]
 [ -10.2525893  -9.65393915  -6.83089794 -10.31010697]
 [  -9.55535575 -11.34013494  -6.2468964  -10.4420707 ]
 [  -8.88901743  -5.15805226  -5.55624811  -7.49357761]
 [  -4.93387568  -3.90417767  -8.26339178  -8.97559953]
 [  -4.32036073  -4.28170187  -2.94061165  -4.91503919]
 [ -13.13117418 -11.54888054 -11.56698742 -12.34185644]
 [ -12.3192548  -10.76422298 -10.76416381 -12.31810624]
 [ -11.57107435  -9.98597752  -9.96343246 -11.55419573]
```

[-11.17201602	-9.14635966	-9.19267055	-10.79078294]
[-9.97576733	-8.31572057	-8.31261189	-9.96655246]
[-9.4434069	-7.51769995	-7.46184887	-9.25573982]
[-8.5863678	-6.82564741	-6.59372334	-8.34738322]
[-8.31345366	-6.0192416	-5.70788096	-7.54135764]
[-7.20641636	-4.89457495	-4.80396016	-7.10136596]
[-9.76495001	-6.5084585	-3.881592	-6.50636395]
[-4.90001143	-2.9404	-2.82206552	-4.77136939]
[-3.89792973	-2.93915145	-1.98	-5.62332046]
[-12.31790293	-10.76416381	-12.31790293	-11.54888054]
[-11.54888054	-9.96343246	-111.31790293	-11.54888054]
[-10.76416381	-9.14635966	-111.31790293	-10.76416381]
[-9.96343246	-8.31261189	-111.31790293	-9.96343246]
[-9.14635966	-7.46184887	-111.31790293	-9.14635966]
[-8.31261189	-6.59372334	-111.31790293	-8.31261189]
[-7.46184887	-5.70788096	-111.31790293	-7.46184887]
[-6.59372334	-4.80396016	-111.31790293	-6.59372334]
[-5.70788096	-3.881592	-111.31790293	-5.70788096]
[-4.80396016	-2.9404	-111.31790293	-4.80396016]
[-5.20634293	-1.98	-111.31790293	-3.881592]
[-2.9404	-1.98	-1.	-2.9404]
[-11.54888054	-111.31790293	-12.31790293	-12.31790293]
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[0.	0.	0.	0.]
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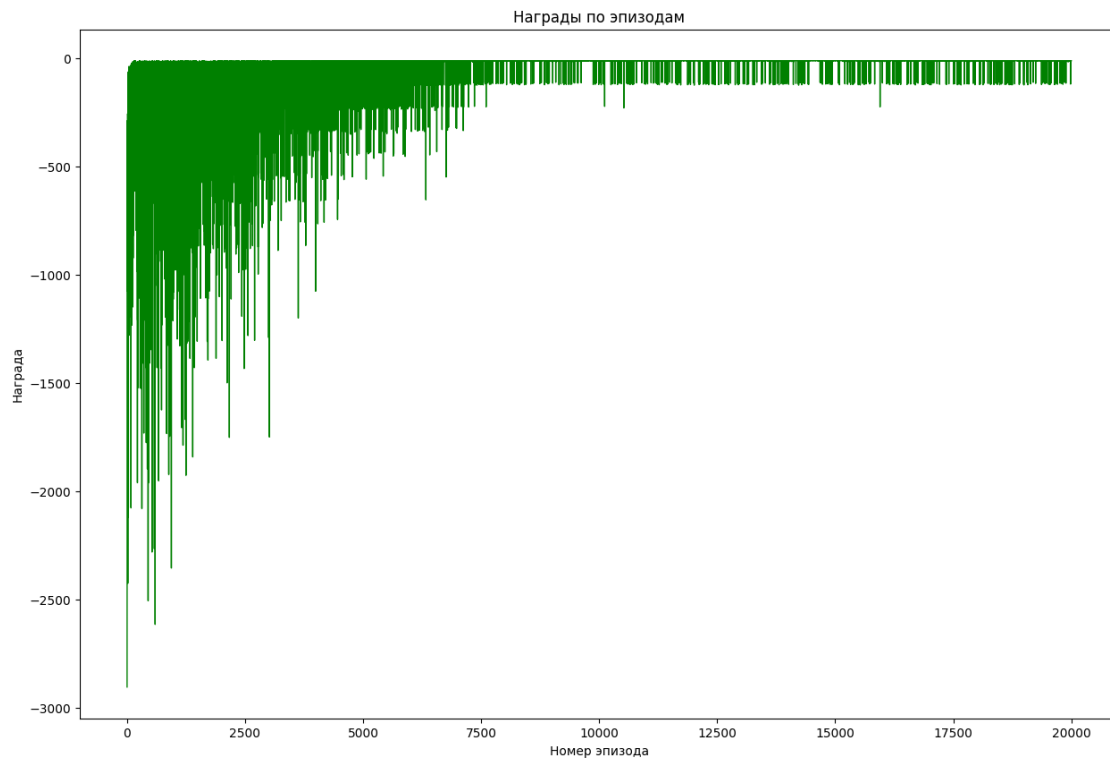
Q2

[-15.13898105	-14.32381453	-12.33766728	-15.42049931]
[-13.30661702	-13.22022211	-11.54896719	-14.7253205]
[-13.1569111	-12.12323786	-10.76501363	-12.65767022]
[-12.3223195	-12.85927305	-10.02728743	-13.53417177]
[-11.93460369	-10.49832192	-9.14701041	-12.43739036]
[-11.18535804	-11.52614607	-8.36375519	-10.92710904]
[-10.30942737	-9.9026903	-7.52550216	-10.10652428]
[-10.24995713	-10.91493566	-6.73108938	-10.38467829]
[-9.66191857	-8.47767518	-5.82286404	-9.18476604]
[-7.98984369	-9.06477142	-10.36917949	-8.39480054]
[-7.14394848	-3.88935579	-3.0064895	-7.80777961]
[-4.10619778	-4.14614242	-2.94043699	-7.63097265]
[-13.16545749	-11.54888054	-11.55525827	-12.33208842]
[-12.31920849	-10.76419416	-10.76416381	-12.31794082]

```

[ -11.71263134  -9.97211536  -9.96343246  -11.55285812]
[ -11.03648746  -9.14635966  -9.15281165  -10.77331658]
[  -9.97479528  -8.32735686  -8.31261189  -9.9663456  ]
[  -9.30734431  -7.54761851  -7.46184887  -9.24280442]
[  -8.76268076  -6.71879852  -6.59372334  -8.41714579]
[  -8.24483529  -5.80260824  -5.70788096  -7.58570949]
[  -8.25061721  -5.69000502  -4.80396016  -6.86921384]
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[ -12.31790293 -10.76416381 -12.31790293 -11.54888054]
[ -11.54888054 -9.96343246 -111.31790293 -11.54888054]
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[ -11.54888054 -111.31790293 -12.31790293 -12.31790293]
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[  0.          0.          0.          0.          ]
[  0.          0.          0.          0.          ]
[  0.          0.          0.          0.          ]]

```



The Kernel crashed while executing code in the the current cell or a previous cell. Please review the code in the cell(s) to identify a possible cause of the failure. Click [here](https://aka.ms/vscodeJupyterKernelCrash) for more info. View Jupyter [log](command:jupyter.viewOutput) for further details.