

# Note on KR and Graph Mining

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## 1 Feature Comparison

### 1.1 IDP

**Pro:**

- can model inductive definitions
- allows core formulation in a high-level language (NP)
- handles aggregates
- has support for variety of constraints

**Cons:**

- cannot handle negative case  $NP^{NP}$  complexity
- cannot model subgraph isomorphism independence
- cannot handle dominance, i.e., when one model is preferred over another

**ASP** Mostly the same but in theory can handle  $NP^{NP}$ , in practice however, it would require encoding tricks and unavoidably lead to the same problem as in IDP – indexing homomorphism enumeration.

### 1.2 proB

**Pro:**

- can model negative case
- can model subgraph isomorphism independence

**Cons:**

- cannot handle inductive definitions
  - cannot handle different types of aggregates (? needs to be checked again)
- the rest of constraints?

## 2 Code in ProB and IDP

proB encoding

```
MACHINE PositiveAndNegative
INCLUDES PositivePatterns, NegativePatterns, Labels
SETS
  Vertices = {x1,x2,x3,x4,x5,x6,x7,x8}
CONSTANTS
  Label,
  Template,
  ChosenVertices
DEFINITIONS
  SET_PREF_TIME_OUT == 35000; SET_PREF_MAX_INITIALISATIONS == 1;
  homomorph_with(iso,ToGraph) == (
    iso : ChosenVertices >-> graph_domain(ToGraph) &
    !x.(x:ChosenVertices => Label(x) = node_label(ToGraph,iso(x))) &
    ! (x,y).( x|->y : Template
      => (x:ChosenVertices & y:ChosenVertices => iso(x)|->iso(y) : graph_edges(ToGraph))
    ) /* small optimisation: instead of TU ; does not seem to improve runtime */
  );
  homomorph_with_n(iso,ToGraph) == (
    iso : ChosenVertices >-> ngraph_domain(ToGraph) &
    !x.(x:ChosenVertices => Label(x) = nnode_label(ToGraph,iso(x))) &
    ! (x,y).( x|->y : Template
      => (x:ChosenVertices & y:ChosenVertices => iso(x)|->iso(y) : ngraph_edges(ToGraph))
    ) /* small optimisation: instead of TU ; does not seem to improve runtime */
  );
  CUSTOM_GRAPH_NODES == { node,col | node : Vertices & col = Label(node)};
  CUSTOM_GRAPH_EDGES == { n1,n2 | n1|->n2:Template & n1:ChosenVertices & n2:ChosenVertices}
PROPERTIES /* for simplicity we assume a global labeling function */
  Label : Vertices --> Labels &
  Label = {(x1,a), (x2,b), (x3,c), (x4,d), (x5,e), (x6,f), (x7,g), (x8,k)} &
  Template = {(x1,x2), (x2,x3), (x3,x4), (x4,x5), (x5,x6), (x6,x7), (x7,x8)} &
  ChosenVertices <: dom(Template) \ / ran(Template) &
  card({p|p:graph & #isop.(homomorph_with(isop,p))}) >= 50 &
  card({p|p:ngraph & #isop.(homomorph_with_n(isop,p))}) <= 50 &
  card(ChosenVertices) = 4 & /* solution found in 8.8 seconds for card = 4*/
  /* additionally request that we have some connectivity of the selected subgraph */
  !v.(v:ChosenVertices => #w.(w:ChosenVertices & (v|->w : Template or w|->v : Template)))
OPERATIONS /* These operations are just there to show some aspects of the solution found */
  /* show which vertices and edges have been selected as the solution pattern */
  Pattern(v,lv,w,lw) = SELECT v:ChosenVertices & w:ChosenVertices & v|->w:Template &
    lv=Label(v) & lw=Label(w) THEN skip
END;
MatchedPositivePattern(p,isop) = SELECT p:graph & homomorph_with(isop,p) THEN skip END;
MatchedNegativePattern(p,isop) = SELECT p:ngraph & homomorph_with_n(isop,p) THEN skip END
END
```

```

vocabulary V{
  type t_var isa nat
  type graph
  invar(t_var)
  pattern_in(graph)
  extern vocabulary Vout
  type label
  type node isa nat
  node_label(graph, node, label)
  t_label(t_var, label)
  edge(graph, node, node)
  threshold:int
  partial f(graph, t_var):node
  t_edge(t_var, t_var)
    path(t_var, t_var)
}
theory T:V{
  // frequency
  #{ graph : pattern_in(graph) } >= threshold.
  // homomorphism definition
  pattern_in(g) & invar(x) <=> ? y: y=f(g,x).
  //injectivity
  pattern_in(g) & invar(x) & invar(y) & x ~= y      => f(g, x) ~= f(g, y).
  pattern_in(g) & invar(x) & invar(y) & t_edge(x,y) => edge(g, f(g,x), f(g,y)).
  pattern_in(g) & invar(x) & t_label(x, lx)          => node_label(g, f(g,x), lx).
  {
    path(x,y) <- t_edge(x,y) & invar(x) & invar(y).
    path(y,x) <- path(x,y).
    path(x,y) <- ?z: path(x,z) & t_edge(z,y) & invar(y).
  }
  !x y : x ~= y & invar(x) & invar(y) => path(x,y).
  // Cardinality constraint on the size of the query, replace NNN with number
  ?NNNx: invar(x).
  // *Nogoods*
}

```

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