

poST Language Transformational Semantics

I. PRELIMINARIES

A. Transformation Relation

A transformation relation is defined as a family of relations $\mapsto_i \in (Po \times C) \times ((Pr \cup \{\Lambda\}) \times C)$, where Po is a set of fragments of poST programs, Pr is a set of fragments of Promela programs, C is a context in which a transformation is executed.

B. Kinds of Transformation Relations

The transformation relation is divided into the following indexed relations:

- \mapsto_A transforms control application (a sequence of poST programs);
- \mapsto_{PgS} transforms sequences of poST programs;
- \mapsto_{Pg} transforms poST programs;
- \mapsto_T transforms types;
- \mapsto_V transforms variable declarations;
- \mapsto_E transforms expressions;
- \mapsto_{St} transforms statements;
- \mapsto_{StS} transforms sequences of statements;
- \mapsto_P transforms process declarations;
- \mapsto_{PS} transforms sequences of process declarations;
- \mapsto_S transforms state declarations;
- \mapsto_{SS} transforms sequences of state declarations;
- \mapsto_R generates Promela names for the corresponding names of variables, processes and process states of the poST program.

C. Context Attributes

The transformation context is specified by the following attributes:

- $VN(n, p, pg)$ returns the name in Promela program corresponding to the name n of a variable v in process p of program pg . If $p = \perp$, v is defined in pg outside processes;
- $PN(n, pg)$ returns the name in Promela program corresponding to the name n of a process in program pg ;
- $SN(n, p, pg)$ returns the name in Promela program corresponding to the name n of a state of process p of program pg ;
- CB is a fragment of Promela program that is a result of transformation of declarations of constant variables of poST programs;
- VB is a fragment of Promela program that is a result of transformation of declarations of non-constant variables of poST programs;
- CPg returns the name of the current program;

- $CP(pg)$ returns the name of the current process of program pg ;
- $CS(p, pg)$ returns the name of the current state of process p of program pg ;
- $FS(p, pg)$ returns the first state of process p of program pg ;
- $NS(s, p, pg)$ returns the next state for state s of process p of program pg ;
- $NP(p, pg)$ returns the next process for process p of program pg ;
- $NPg(pg)$ returns the next program for program p ;
- $Timed(s, p, pg)$ returns true if s contains a timeout statement;
- $Interval$ returns the duration of a scan loop. We consider that it is constant.

II. TRANSFORMATION RULES

Let functions VR , PR and SR specify renaming of variables, processes and states of poST programs in Promela program. They input a name of a variable, process and state, respectively and a transformation context. More exactly, they use only components vn , pn and sn of the context, respectively.

Let $cstate(p, pg)$ specifies a Promela variable that stores the current state of process p of program pg .

Let $timer(p, pg)$ specifies a Promela variable that stores the local time of process p of program pg . If a current state s of process p is timed, the value of variable $timer(p)$ is the number of iteration of scan loop during process p has state s including the current iteration.

Let Λ denote an empty fragment.

Let $s_{stop}(p, pg)$ and $s_{error}(p, pg)$ be Promela names for poST states STOP and ERROR for process p of program pg .

Let $SS(p, pg, c)$ return a state sequence $s_1, \dots, s_n, s_{stop}(p, pg), s_{error}(p, pg)$, where $s_{i+1} = c.NS(s_i, p, pg)$.

Let $SST(p, pg, c)$ be a Promela name for the enumeration type with values from $SS(p, pg, c)$.

Let letters u , v , w (possibly with indexes and primes) denote a fragment, a nonempty sequence of fragments and a sequence of fragments, respectively, of programs both poST and Promela

A. Programs

$$\frac{(u, c) \mapsto_{Pg} (w, c'), (v, c') \mapsto_{Pg, s} (w', c'')}{(u \ v, c) \mapsto_{Pg, s} (w \ w', c'')}$$

$$\frac{(u, c) \mapsto_{pg} (w, c')}{(u, c) \mapsto_{PgS} (w, c')}$$

1 B. Control Application

$$\frac{(app, c) \mapsto_R (w_1, c_1), (v, c_1) \mapsto_{PgS} (f, c_2)}{(v, c) \mapsto_A (f, c_2)}$$

2 C. Types

$$\frac{u \in \{\text{DINT}, \text{LINT}, \text{UDINT}, \text{ULINT}, \text{REAL}, \text{LREAL}, \text{DWORD}, \text{LWORD}\}}{(u, c) \mapsto_T (\text{int}, c)}$$

$$\frac{u \in \{\text{SINT}, \text{INT}, \text{WORD}\}}{(u, c) \mapsto_T (\text{short}, c)}$$

$$\frac{u \in \{\text{USINT}, \text{BYTE}\}}{(u, c) \mapsto_T (\text{byte}, c)}$$

$$\frac{u \in \{\text{UINT}, \text{TIME}\}}{(u, c) \mapsto_T (\text{unsigned}, c)}$$

$$\frac{u_3 \neq \text{TIME}, (u_1, c) \mapsto_E (w_1, c_1), (u_2, c_1) \mapsto_E (w_2, c_2), (u_3, c_2) \mapsto_T (w_3, c_3)}{(\text{ARRAY}[u_1:u_2] \text{ OF } u_3, c) \mapsto_T (w_3[], c_3)}$$

$$(\text{BOOL}, c) \mapsto_T (\text{bool}, c)$$

3 The string types STRING and WSTRING are not supported.

4 D. Expressions

1) Boolean Operators:

$$\frac{(u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 \text{ XOR } u_2, c) \mapsto_E (u'_1 \wedge u'_2, c)}$$

$$\frac{(u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 \text{ OR } u_2, c) \mapsto_E (u'_1 \vee u'_2, c)}$$

$$\frac{(u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 \text{ AND } u_2, c) \mapsto_E (u'_1 \& u'_2, c)}$$

$$\frac{(u, c) \mapsto_E (u', c')}{(\text{NOT } u, c) \mapsto_E (\neg u', c')}$$

2) Relation Operators:

$$\frac{(u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 = u_2, c) \mapsto_E (u'_1 == u'_2, c)}$$

$$\frac{(u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 <> u_2, c) \mapsto_E (u'_1 != u'_2, c)}$$

$$\frac{(u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 < u_2, c) \mapsto_E (u'_1 < u'_2, c)}$$

$$\frac{(u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 > u_2, c) \mapsto_E (u'_1 > u'_2, c)}$$

$$\frac{(u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 \leq u_2, c) \mapsto_E (u'_1 \leq u'_2, c)}$$

$$\frac{(u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 \geq u_2, c) \mapsto_E (u'_1 \geq u'_2, c)}$$

3) Arithmetic Operators:

$$\frac{\circ \in \{+, -, *, /\}, (u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 \circ u_2, c) \mapsto_E (u'_1 \circ u'_2, c)}$$

$$\frac{(u_1, c) \mapsto_E (u'_1, c_1), (u_2, c_1) \mapsto_E (u'_2, c_2)}{(u_1 \text{ MOD } u_2, c) \mapsto_E (u'_1 \% u'_2, c)}$$

$$\frac{(u, c) \mapsto_E (u', c')}{(-u, c) \mapsto_E (-u', c')}$$

The operator $(**)$ of exponentiation is not supported.

4) State-handling Operators:

$$\frac{n = cstate(u, c.CPg)}{(\text{PROCESS } u \text{ IN STATE ACTIVE}, c) \mapsto_E (n != s_{stop}(u, c.CPg) \ \& \ n != s_{error}(u, c.CPg), c)}$$

$$\frac{n = cstate(u, c.CPg)}{(\text{PROCESS } u \text{ IN STATE INACTIVE}, c) \mapsto_E (n = s_{stop}(u, c.CPg) \ || \ n = s_{error}(u, c.CPg), c)}$$

$$\frac{n = cstate(u, c.CPg)}{(\text{PROCESS } u \text{ IN STATE STOP}, c) \mapsto_E (n = s_{stop}(u, c.CPg), c)}$$

$$\frac{n = cstate(u, c.CPg)}{(\text{PROCESS } u \text{ IN STATE ERROR}, c) \mapsto_E (n = s_{error}(u, c.CPg), c)}$$

E. Renaming

The relation \mapsto_R generates Promela names for the corresponding names of variables, processes and process states of the poST program. it also fills the attributes VN , PN and SN of the transformation context.

$$\frac{v_1 \in \{\text{VAR}, \text{VAR CONSTANT}, \text{VAR_INPUT}, \text{VAR_OUTPUT}, \text{VAR_IN_OUT}\}, n = VR(u, c), c_1 = c[VN(u, c.CP(c.CPg), c.CPg) := n], (w, c_1) \mapsto_R (w', c_2)}{(v_1 \ u \ v_2 \ \text{END_VAR } w, c) \mapsto_R (w', c_2)}$$

$$\frac{n = PR(u, c), c_1 = c[PN(u, c.CPg) := n], (w_1, c_1[CP(c.CPg) := u]) \mapsto_R (w'_1, c_2), (w_2, c_2[CP(c.CPg) := \perp]) \mapsto_R (w'_2, c_3)}{(\text{PROCESS } u \ w_1 \ \text{END_PROCESS } w_2, c) \mapsto_R (w'_2, c_3)}$$

$$\frac{n = SR(u, c), (w_2, c) \mapsto_R (w'_2, c_1)}{(\text{STATE } u \ w_1 \ \text{END_STATE } w_2, c) \mapsto_R (w'_2, c_1)}$$

$$\frac{(w_1, c[CP(c.CPg) := u]) \mapsto_R (w'_1, c_1), (w_2, c_1[CP(c.CPg) := \perp]) \mapsto_R (w'_2, c_2)}{(\text{PROGRAM } u \ w_1 \ \text{END_PROGRAM } w_2, c) \mapsto_R (w'_2, c_2)}$$

$$(\Lambda, c) \mapsto_R (\Lambda, c)$$

F. Variable Declarations

$$\frac{v \in \{VAR, VAR_INPUT, VAR_OUTPUT, VAR_IN_OUT\}, \quad n = c.VN(u_1, c.CP(c.CPg), c.CPg), \quad (u_2, c) \mapsto_t (u'_2, c_1)}{(v \ u_1 : u_2 \ \text{END_VAR}, c) \mapsto_{St} (\Lambda, c_1[VB := c_1.VB \ u'_2 \ n;])}$$

$$\frac{v \in \{VAR, VAR_INPUT, VAR_OUTPUT, VAR_IN_OUT\}, \quad n = c.VN(u_1, c.CP(c.CPg), c.CPg), \quad (u_2, c) \mapsto_t (u'_2, c_1), (u_3, c_1) \mapsto_e (u'_3, c_2)}{(v \ u_1 : u_2 = u_3 \ \text{END_VAR}, c) \mapsto_{St} (\Lambda, c_2[VB := c_2.VB \ u'_2 \ n = u'_3;])}$$

$$\frac{n = c.VN(u_1, c.CP(c.CPg), c.CPg), \quad (u_3, c) \mapsto_e (u'_3, c_1)}{(\text{VAR CONST } u_1 : u_2 = u_3 \ \text{END_VAR}, c) \mapsto_{St} (\Lambda, c_1[CB := c_1.CB \ \#define \ n \ u'_3;])}$$

G. ST Statements

1) Assignment:

$$\frac{n = c.VN(u_1, c.CP(c.CPg), c.CPg), \quad (u_2, c) \mapsto_e (u'_2, c_1)}{(u_1 := u_2, c) \mapsto_{St} (n = u'_2, c_1)}$$

2) If Statements:

$$\frac{(u, c) \mapsto_e (u', c_1), (v, c_1) \mapsto_{st,s} (v', c_2)}{(\text{IF } u \ \text{THEN } v \ \text{END_IF}, c) \mapsto_{St} (\text{if } :: u' \rightarrow \{v'\} :: \text{else} \rightarrow \text{skip}; \text{fi}, c_2)}$$

$$\frac{(u, c) \mapsto_e (u', c_1), (v_1, c_1) \mapsto_{st,s} (v'_1, c_2), (v_2, c_2) \mapsto_{st,s} (v'_2, c_3)}{(\text{IF } u \ \text{THEN } v_1 \ \text{ELSE } v_2 \ \text{END_IF}, c) \mapsto_{St} (\text{if } :: u' \rightarrow \{v'_1\} :: \text{else} \rightarrow \{v'_2\} \ \text{fi}; c_3)}$$

$$\frac{(u, c) \mapsto_e (u', c_1), (v_1, c_1) \mapsto_{st,s} (v'_1, c_2), (\text{IF } v_2, c_2) \mapsto_{st,s} (v'_2, c_3)}{(\text{IF } u \ \text{THEN } v_1 \ \text{ELSEIF } v_2, c) \mapsto_{St} (\text{if } :: u' \rightarrow \{v'_1\} :: \text{else} \rightarrow v'_2 \ \text{fi}; c_3)}$$

3) Case Statements:

$$\frac{(u, c) \mapsto_e (u', c_1), (v_1, c_1) \mapsto_{st,s} (v'_1, c_2), \quad n \text{ is a fresh name}, (v_2, c_2[\text{caseVal} := n]) \mapsto_{cases} (v'_2, c_3)}{(\text{CASE } u \ \text{OF } v_1 \ \text{ELSE } v_2 \ \text{END_CASE}, c) \mapsto_{St} (\text{int } n = v'_1; \text{if } v'_1 :: \text{else} \rightarrow \{v'_2\} \ \text{fi}; c_3)}$$

$$\frac{v_1 : v_2 \text{ is a case branch}, (v_1, c) \mapsto_{labels} (v'_1, c_1), \quad (v_2, c_1) \mapsto_{st,s} (v'_2, c_2) \mapsto_{cases} (v'_3, c_3)}{(v_1 : v_2, c) \mapsto_{cases} (:: v'_1 \rightarrow \{v'_2\}, c_3)}$$

$$\frac{u \text{ is a label}, n = c.\text{caseVal}, (v, c) \mapsto_{labels} (v', c')}{(u \ v, c) \mapsto_{labels} (n == u \ || \ v', c')}$$

$$\frac{u \text{ is a label}, n = c.\text{caseVal}}{(u, c) \mapsto_{labels} (n == u, c')}$$

4) While Statements:

$$\frac{(u, c) \mapsto_e (u', c_1), (v, c_1) \mapsto_{st,s} (v', c_2)}{(\text{WHILE } u \ \text{DO } v \ \text{END_WHILE}, c) \mapsto_{St} (\text{do } :: u' \rightarrow \{v'\} :: \text{else} \rightarrow \text{break}; \text{od}; c_2)}$$

5) Repeat Statements:

$$\frac{(v, c) \mapsto_{st,s} (v', c_1), (u, c_1) \mapsto_e (u', c_2)}{(\text{REPEAT } v \ \text{UNTIL } u \ \text{END_REPEAT}, c) \mapsto_{St} (v' \ \text{do } :: u' \rightarrow \{v'\} :: \text{else} \rightarrow \text{break}; \text{od}; c_2)}$$

6) For Statements:

$$\frac{n = c.VN(u, c.CPg, c.CP), (u_1, c) \mapsto_{st,s} (u'_1, c_1), \quad (u_2, c_1) \mapsto_e (u'_2, c_2), (v, c_2) \mapsto_e (v', c_3)}{(\text{FOR } u := u_1 \ \text{TO } u_2 \ \text{DO } v \ \text{END_FOR}, c) \mapsto_{St} (n = u'_1; \text{do } :: n \leq u'_2 \rightarrow \{v' \ n = n + 1\} :: \text{else} \rightarrow \text{break}; \text{od}; c_3)}$$

$$\frac{n = c.VN(u, c.CPg, c.CP), (u_1, c) \mapsto_{st,s} (u'_1, c_1), \quad (u_2, c_1) \mapsto_e (u'_2, c_2), (u_3, c_2) \mapsto_e (u'_3, c_3), \quad (v, c_3) \mapsto_e (v', c_4)}{(\text{FOR } u := u_1 \ \text{TO } u_2 \ \text{BY } u_3 \ \text{DO } v \ \text{END_FOR}, c) \mapsto_{St} (n = u'_1; \text{do } :: n \leq u'_2 \rightarrow \{v' \ n = n + u'_3\} :: \text{else} \rightarrow \text{break}; \text{od}; c_4)}$$

H. Process-handling Statements

1) Start statements:

$$\frac{n = c.\text{state}(u, c.CPg), \quad s = FS(c.CS(u, c.CPg), u, c.CPg), \quad s' = c.SN(s, u, c.CPg), \text{Timed}(s, u, c.CPg) = \text{false}}{(\text{START PROCESS } u, c) \mapsto_{St} (n = s'; c[CS(u, c.CPg) := s])}$$

$$\frac{n = c.\text{state}(u, c.CPg), \quad s = FS(c.CS(u, c.CPg), u, c.CPg), \quad s' = c.SN(s, u, c.CPg), \text{Timed}(s, u, c.CPg) = \text{true}, \quad t = \text{timer}(u, c.CPg)}{(\text{START PROCESS } u, c) \mapsto_{St} (n = s'; t = 1; c[CS(u, c.CPg) := s])}$$

$$\frac{cp = c.CP(c.CPg), n = c.\text{state}(cp, c.CPg), \quad s = FS(c.CS(cp, c.CPg), cp, c.CPg), \quad s' = c.SN(s, cp, c.CPg), \text{Timed}(s, cp, c.CPg) = \text{false}}{(\text{RESTART}, c) \mapsto_{St} (n = s'; c[CS(cp, c.CPg) := s])}$$

The intermediate transformation relations \mapsto_{cases} and \mapsto_{labels} specify transformation of case branches and case labels, respectively.

$$\frac{v_1 : v_2 \text{ is a case branch}, n = c.\text{caseVal}, \quad (v_1, c) \mapsto_{labels} (v'_1, c_1), (v_2, c_1) \mapsto_{st,s} (v'_2, c_2), \quad (v_3, c_2[\text{caseVal} := n]) \mapsto_{cases} (v'_3, c_3)}{(v_1 : v_2 \ v_3, c) \mapsto_{cases} (:: v'_1 \rightarrow \{v'_2\} \ v'_3, c_3)}$$

$$\begin{array}{c}
cp = c.CP(c.CPg), n = cstate(cp, c.CPg), \\
s = FS(c.CS(cp, c.CPg), cp = c.CP(c.CPg), , c.CPg), \\
s' = c.SN(s, cp, c.CPg), Timed(s, cp, c.CPg) = true, \\
t = timer(cp, c.CPg), \\
\hline
(RESTART, c) \mapsto_{St} (n = s'; t = 1; c[CS(cp, c.CPg) := s])
\end{array}$$

2) Stop statements:

$$\begin{array}{c}
\frac{n = cstate(u, c.CPg)}{(STOP\ PROCESS\ u, c) \mapsto_{St}} \\
(n = s; c[CS(u, c.CPg) := STOP]) \\
\\
\frac{n = cstate(c.CP(c.CPg), c.CPg)}{(STOP, c) \mapsto_{St}} \\
(n = s; c[CS(c.CP(c.CPg), c.CPg) := STOP])
\end{array}$$

3) Error statements:

$$\begin{array}{c}
\frac{n = cstate(u, c.CPg)}{(ERROR\ PROCESS\ u, c) \mapsto_{St}} \\
(n = s; c[CS(u, c.CPg) := ERROR]) \\
\\
\frac{n = cstate(c.CP(c.CPg), c.CPg)}{(ERROR, c) \mapsto_{St}} \\
(n = s; c[CS(c.CP(c.CPg), c.CPg) := ERROR])
\end{array}$$

4) Set statements:

$$\begin{array}{c}
cp = c.CP(c.CPg), n = cstate(cp, c.CPg), \\
u' = c.SN(u, cp, c.CPg), Timed(u, cp, c.CPg) = false \\
\hline
(SET\ STATE\ u, c) \mapsto_{St} (n = u'; c[CS(cp, c.CPg) := u])
\end{array}$$

$$\begin{array}{c}
cp = c.CP(c.CPg), n = cstate(cp, c.CPg), \\
u' = c.SN(u, cp, c.CPg), Timed(u, cp, c.CPg) = true, \\
t = timer(u, cp, c.CPg), \\
\hline
(SET\ STATE\ u, c) \mapsto_{St} \\
(n = u'; t = 1; c[CS(cp, c.CPg) := u])
\end{array}$$

$$\begin{array}{c}
cp = c.CP(c.CPg), n = cstate(cp, c.CPg), \\
u = NS(c.CS, cp, c.CPg), \\
u' = c.SN(u, cp, c.CPg), Timed(u, cp, c.CPg) = false \\
\hline
(SET\ NEXT, c) \mapsto_{St} (n = u'; c[CS(cp, c.CPg) := u])
\end{array}$$

$$\begin{array}{c}
cp = c.CP(c.CPg), n = cstate(cp, c.CPg), \\
u = NS(c.CS, cp, c.CPg), u' = c.SN(u, cp, c.CPg), \\
Timed(u, cp, c.CPg) = true, t = timer(u, cp, c.CPg), \\
\hline
(SET\ NEXT, c) \mapsto_{St} \\
(n = u'; t = 1; c[CS(cp, c.CPg) := u])
\end{array}$$

5) Time-handling Statements:

$$\begin{array}{c}
cp = c.CP(c.CPg), \\
Timed(c.CS(cp, c.CPg), cp, c.CPg) = false \\
\hline
(RESET\ TIMER, c) \mapsto_{St} (\Lambda, c) \\
\\
cp = c.CP(c.CPg), \\
Timed(c.CS(cp, c.CPg), cp, c.CPg) = true, \\
t = timer(cp, c.CPg) \\
\hline
(RESET\ TIMER, c) \mapsto_{St} (t = 1; , c) \\
\\
t = timer(c.CP(c.CPg), c.CPg), \\
u' = \lceil u / c.Interval \rceil, \\
(v, c) \mapsto_{st,s} (v', c_1) \\
\hline
(TIMOUT\ u\ THEN\ v\ END_TIMEOUT, c) \mapsto_{St} \\
(if :: t > u' -> \{t = 1; v'\} :: else -> t = t + 1; fi; , c_1)
\end{array}$$