

$$1) a) \lim_{x \rightarrow 6} \frac{x^2 - 36}{x^2 - x - 30} = \frac{(x-6)(x+6)}{(x-6)(x+5)} = \frac{x+6}{x+5} = \frac{12}{11}$$

$$b) \lim_{x \rightarrow 7} \frac{x^2 - 49}{x^2 - 13x + 42} = \frac{(x-7)(x+7)}{(x-7)(x-6)} = \frac{x+7}{x-6} = \frac{14}{1} = 14$$

b)

$$2) \lim_{x \rightarrow 0} \frac{3x \operatorname{tg} 4x}{1 - \cos 4x} = 3 \operatorname{tg} 4 \lim_{x \rightarrow 0} \frac{x}{\cos(4)x} =$$

$$\operatorname{tg}(0) = \sin(0)/\cos(0)$$

$$= 3 \frac{\sin(4)}{\cos(4)} \cdot \frac{0 \cdot 0}{\cos(4) \cdot 0} = \frac{3 \sin(4) \cdot 0 \cdot 0}{\cos(4)(1 - \cos(4)) \cdot 0} = \frac{0}{\cos(4) \cdot 1} = 0$$

$$c) \lim_{x \rightarrow \infty} \left(\frac{4x}{4x+3} \right)^{\frac{5x^2}{7x-1}}$$

$$m) \lim_{x \rightarrow 0} \frac{5^x - 1}{x} = \ln 5$$

~~$$\lim_{x \rightarrow 0} \frac{f(x)}{g(x)} = \lim_{x \rightarrow 0} \frac{f'(x)}{g'(x)}$$~~

$$3) \lim_{x \rightarrow \infty} \frac{\ln(x^2 - x + 1)}{\ln(x^{10} + x + 1)} = \lim_{x \rightarrow \infty} \frac{\frac{1}{x^2 - x + 1} \frac{d}{dx}(x^2 - x + 1)}{\frac{1}{x^{10} + x + 1} \frac{d}{dx}(x^{10} + x + 1)} = \frac{1}{5}$$