Tutorial 4: ARIMA

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Finally, a model where you can use SAS EG. Creating ARIMA is going to be a piece of cake for you!

Before you start: Create a new process flow

This tutorial assumes that you have already created a project. You need to open it. For this tutorial we will create a new Process Flow, which will let us separate tutorials from each other and keep our project more organized (described in tutorial 2).

Click on the icon that looks like a sheet of paper → Process Flow → Right click on the icon Process Flow once you see in the pane on the left Process Flow → Call it tutorial4.

When you work with the materials for Tutorial3, make sure you left click on that Process Flow so that all the new datasets you open and create, get opened under that tutorial.

For this tutorial we are going to use QUERY_FOR_BIKESHARINGDAILY, that we created in tutorial 1.

Running a libname statement!

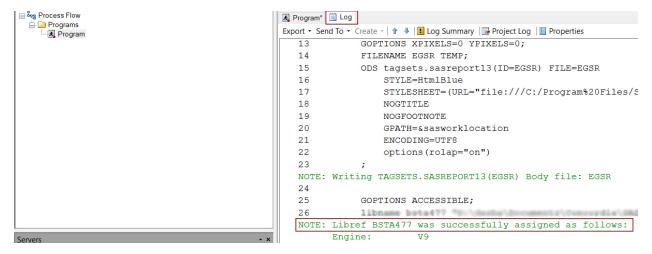
If you work from your own computer and you have assigned a permanent libname statement, you don't have to do anything.

If you are working from the school's computer, then just open a new project and run a libname statement in a SAS program. Make sure that you are in the TUTORIAL4 Process Workflow.

Click on the icon that looks like a sheet of paper → Choose program → Type the libname statement (as shown below)

```
libname bsta477 "C:\bsta477";
```

Remember to always check the log. It will show whether the library has been successfully assigned or not!



Autocorrelation and Partial Correlation Plots

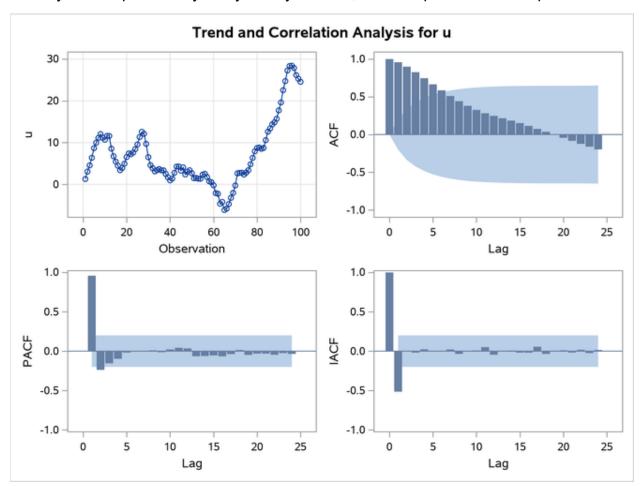
When applying ARIMA we should make sure that our data is stationary and we should also investigate what order of processes we should apply. Shall we use MA, AR or just difference the data?

A. Look at the autocorrelation (ACF) and partial (PACF) autocorrelation plots to estimate what order autocorrelations and what processes we have in the data.

Time series graph. You can visually examine the time series plot and assess whether there seems to be a trend and seasonality. In the case of the output presented here, we may see that the trend is present since the time series data points depart from the mean and don't randomly fluctuate around it. We cannot say much about seasonality, though, since it may be masked by the trend or, perhaps, we would need to zoom in and investigate a short period of time to see the data closer and estimate the presence of seasonality.

ACF and PACF plots. Other clues to look for would be ACF and PACF plots – Autocorrelation and Partial autocorrelation plots. How do we know if we are dealing with strong or moderate autocorrelations? By looking at the confidence interval of 95%, which is represented by the blue ribbon surrounding the mean of 0. All spikes within that blue ribbon would correspond to low or insignificant autocorrelation. The spikes that go over it correspond to moderate or strong autocorrelations. The higher the spikes, the stronger the level of autocorrelations.

When you do a preliminary analysis of your data, SAS will produce this output:



ACF. By looking at the autocorrelation plot we can assess whether there is a trend. A good indicator of a trend is a few autocorrelation coefficient spikes in row that go over the blue ribbon. We would expect strong autocorrelations at time lags of 0 and 1, because when there is no lag (lag0), the data point (say, January 2018) perfectly correlates with itself (with January 2018, which is represented by lag0). At lag1 we would still expect some autocorrelations present since February sales are related to January sales. However, if there is no trend present in the data, we would expect a sudden drop in autocorrelation coefficients for lag2, lag3 and so on. In this case we can see strong autocorrelations up to lag5. So, there is a trend present in the data, which we have already visually identified when we were examined the time series plot.

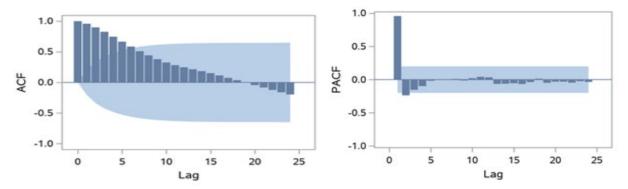
PACF: Sometimes the trend can mask seasonality, and but we can still look at the PACF (partial autocorrelation plot). We should investigate it for spikes exceeding the confidence interval level. We should be looking for the highest spike in a range of spikes. Once identified, that spike may indicate a seasonality interval, i.e. 6 months or 2 months etc. In this case it doesn't seem that there is any seasonality in the data present. But! It can also be masked by the trend. To continue the examination, we

should have a look at this plot again after we difference the data, say, a lag1 for starters. The plot may look different then.

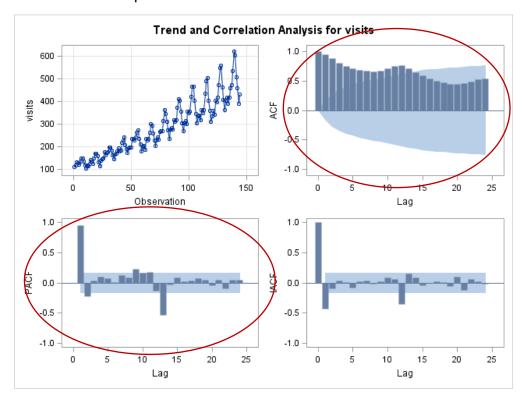
What else are ACF and PACF plots good for?

They are good for assessing which processes you are dealing with and at which order: AR or MA and is it AR(1) or MA(2) etc.? A way to find it out if to look at the ACF and PACF plots.

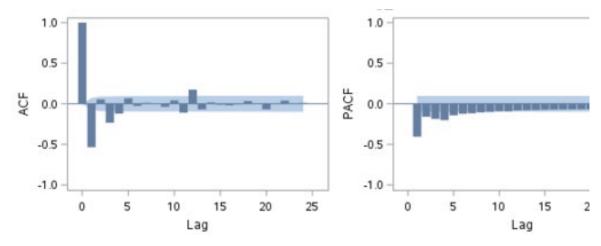
AR process. The plots presented below are typical for AR processes: Autocorrelations gradually fall to zero at the ACF (autocorrelation plot) and there are a few spikes at the Partial autocorrelation plot (PACF).



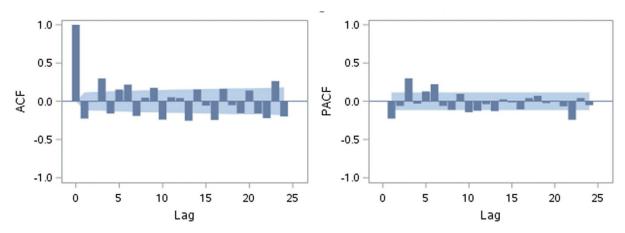
Or another example



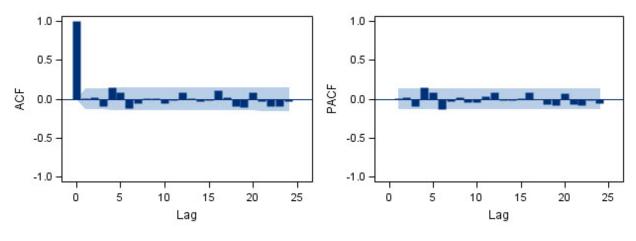
MA process. The plots behavior will be an inverse of what is observed for the AR processes: there are a few spikes at the Autocorrelation plot (ACF) and autocorrelations gradually fall to zero at the Partial autocorrelation plot (PACF).



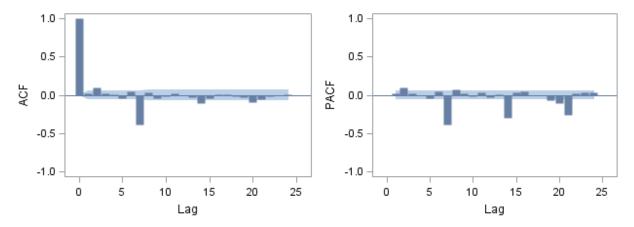
Both processes are present:



An example of stationary data:



An example of seasonality in the data:



How good is your model?

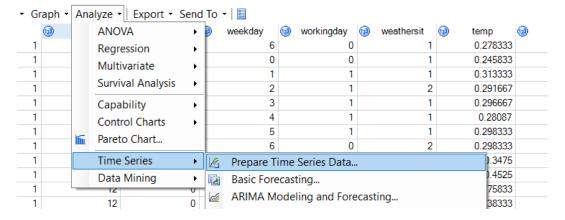
After you have done your forecasting, you should estimate the goodness of fit of your model and look at the residual autocorrelation and partial autocorrelation plots. They should help you identify whether your model is going to be robust and reliable. No autocorrelations or partial autocorrelations should be present.

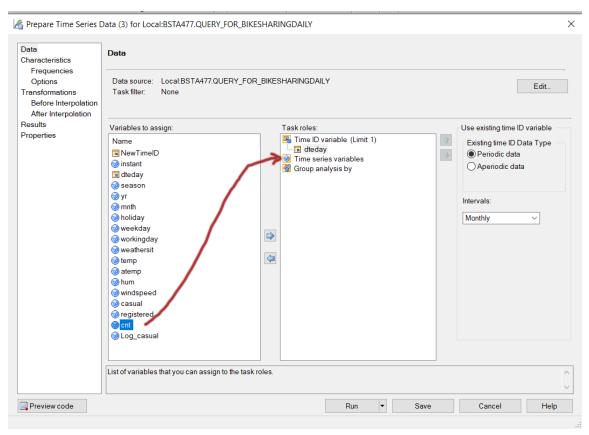
Also, check the Ljung-Box statistics (White Noise in SAS) to see whether any strong correlations are present.

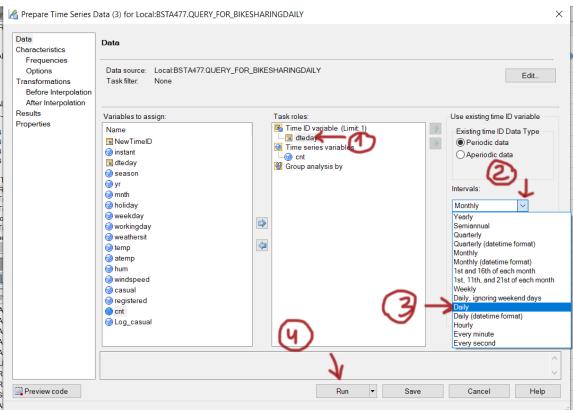
Prepare your time series data for analysis

Open the dataset \rightarrow Analyze \rightarrow Time series \rightarrow Prepare Time Series Data \rightarrow Drag cnt to the Time series variables \rightarrow Click on the Time ID variable \rightarrow Click on the arrow to the right under Intervals \rightarrow Select Daily \rightarrow Click Run to create a temporary dataset, which we are going to be using for the further analysis.

P.S. If you want to save it **permanently**!!!, before you click run, go to Results → Browse → Find the library you assigned before → Give it your name → Save.



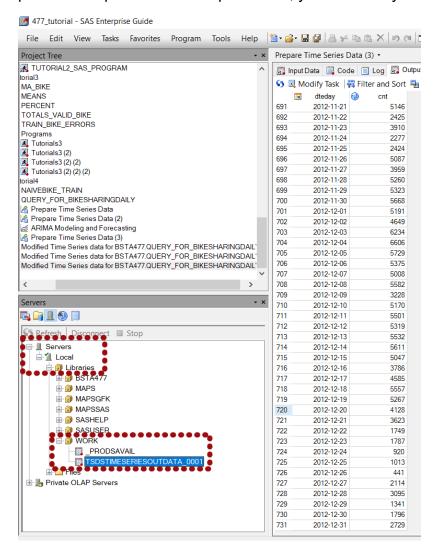




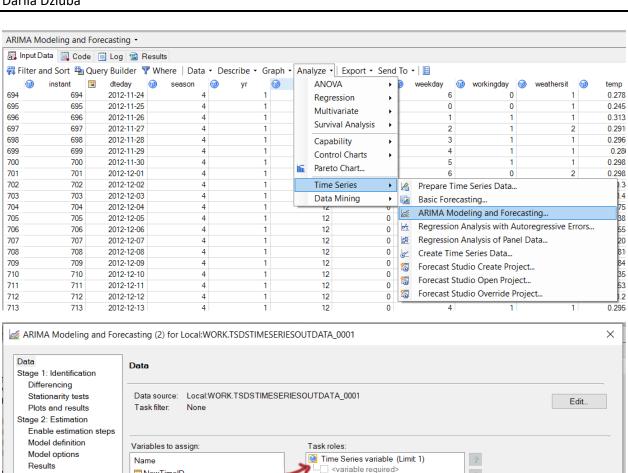
We are going to be using this dataset for further analysis!

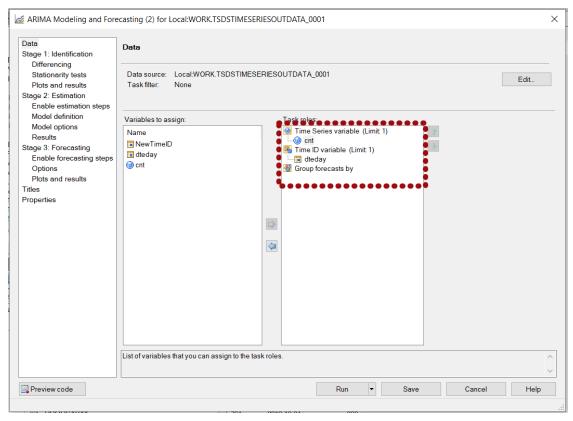
ARIMA: Step 1 – examine your data

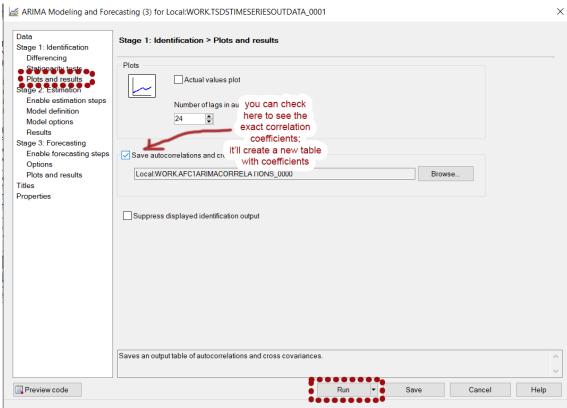
We are going to work with the dataset that we have just prepared for analysis in the previous step. It should be open. If not, you can easily locate it in the work library:

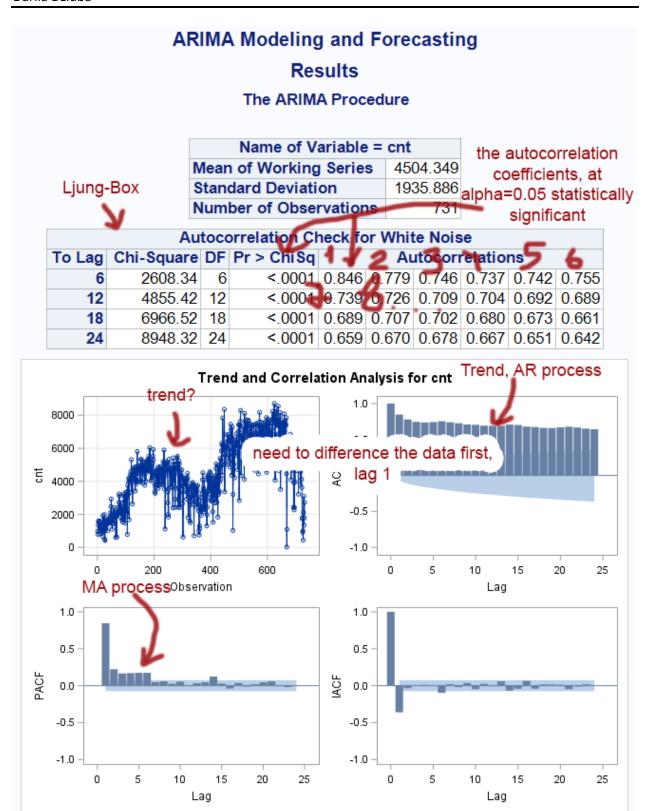


Open the dataset \rightarrow Analyze \rightarrow Time series \rightarrow ARIMA Modelling and Forecasting \rightarrow Data: Drag cnt to the right, under Time Series variable \rightarrow Stage1: Identification \rightarrow Plots and results \rightarrow if you want to: Save acutoccorelations and cross covariances. It will give you a table with exact autocorrelations \rightarrow Run \rightarrow Study the autocorrelation and partial autocorrelation plots to decide if differencing is needed, whether there are AR or/and MA processes are present as well as what order.

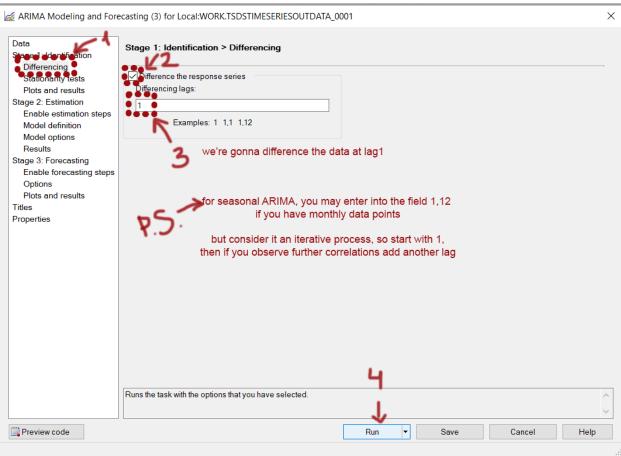


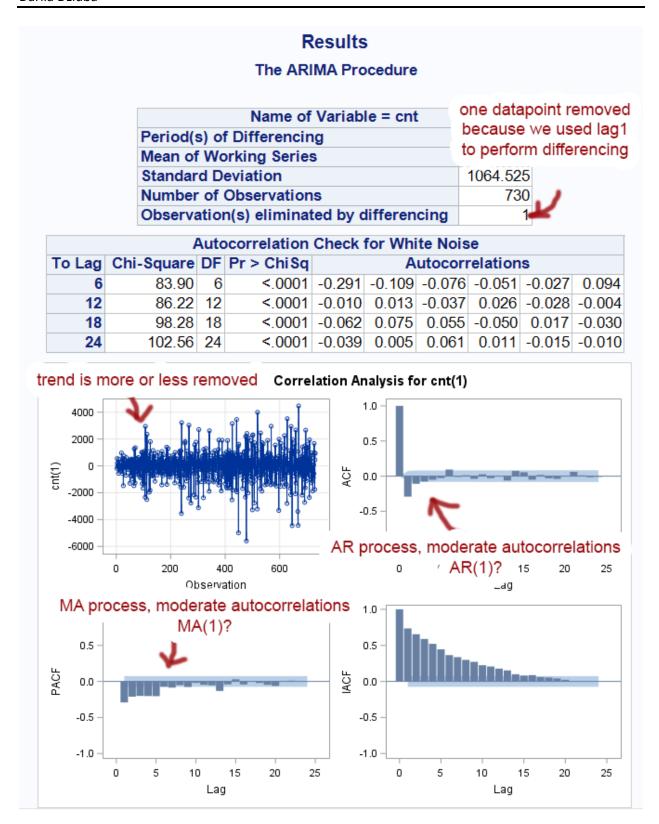










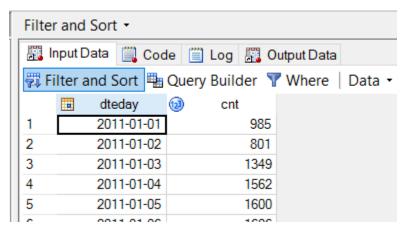


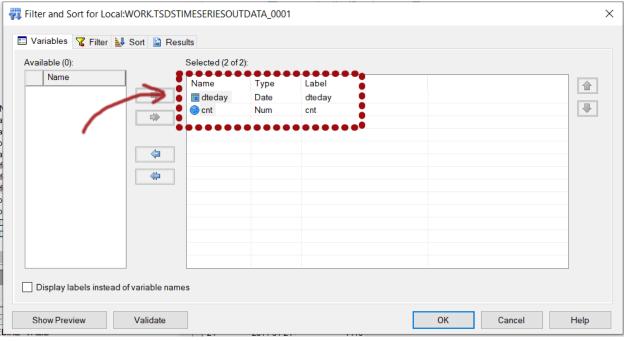
ARIMA: Step 2 – Build your Model

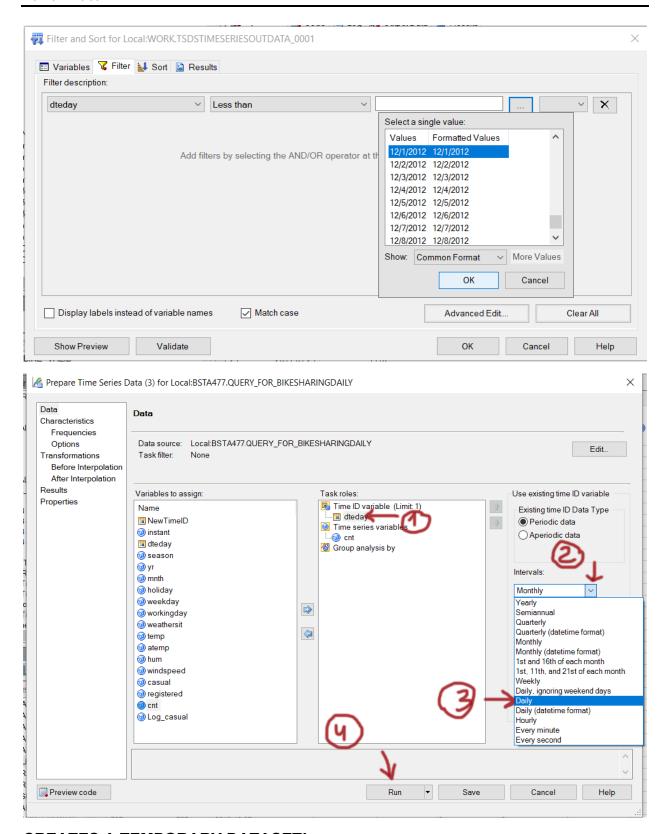
A. Create a Training Dataset

Discussed in Tutorial3: Filter and Sort, condition: dteday; less then 12/01/2012

Open the dataset → Filter and Sort → Variables: Drag the variables you will need for the forecast to the right (date and the variable you want to forecast) → Filter: Set the filtering values (dteday; less then; December 1, 2012) → Results: Permanently save the dataset: Replace the WORK library with the one you ran at the beginning of the session – BSTA477 → OK

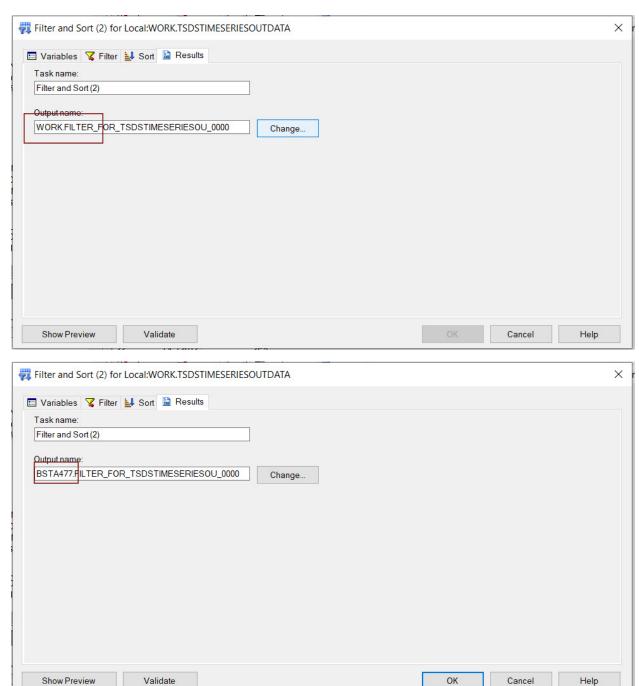






CREATES A TEMPORARY DATASET!

To create a permanent dataset, before you hit "RUN", go to Results and change the library name for bsta477 or click on change, find your library and give your dataset a name and store it there.



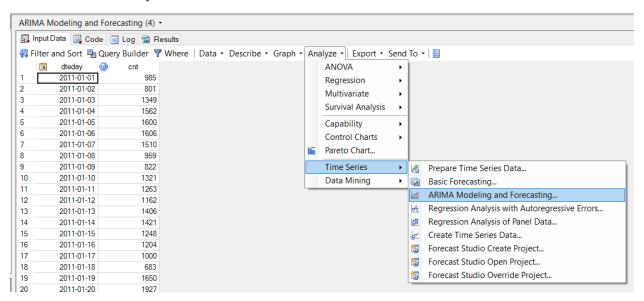
B. Difference the data, estimate AR and MA orders

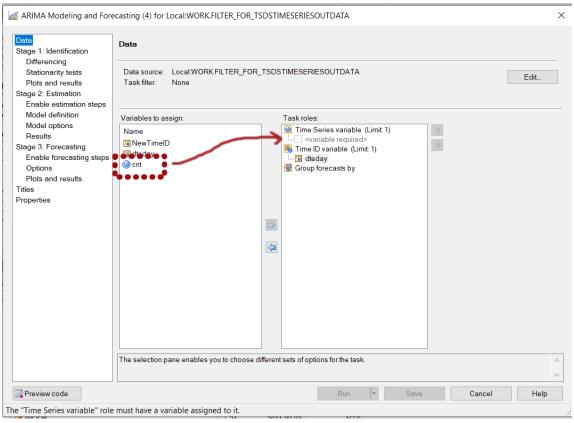
We are going to use the newly created **TRAIN dataset** with accumulated values of total member and non-member rides on a daily basis. As we can see from the table above, we now only have 700 points of data.

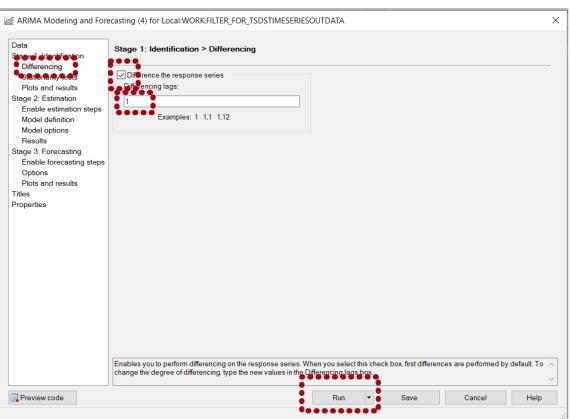
Difference the data.

Repeat Step 1 on the Train Dataset.

We have discussed already that we would need to difference the data due to the presence of the trend: Open the file you want to use for forecasting → Analyze → Time Series → ARIMA Modelling and Forecasting → Data: Drag the cnt to the right to the Time Series Variable → Stage 1: Identification → Differencing → Difference the response series → Leave at default → Run



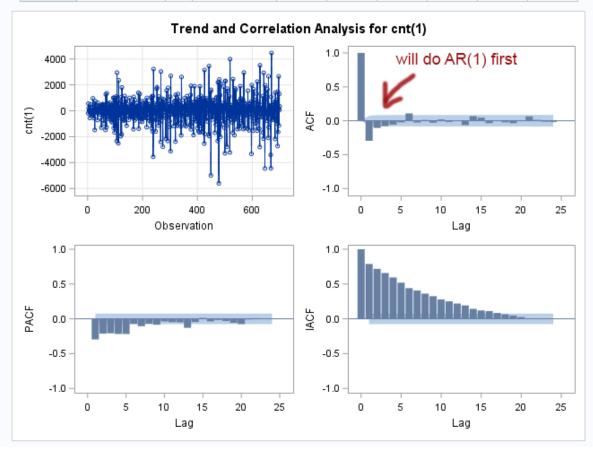




Results The ARIMA Procedure

Name of Variable = cnt					
Period(s) of Differencing	1				
Mean of Working Series	6.699571				
Standard Deviation	1066.822				
Number of Observations	699				
Observation(s) eliminated by differencing	1				

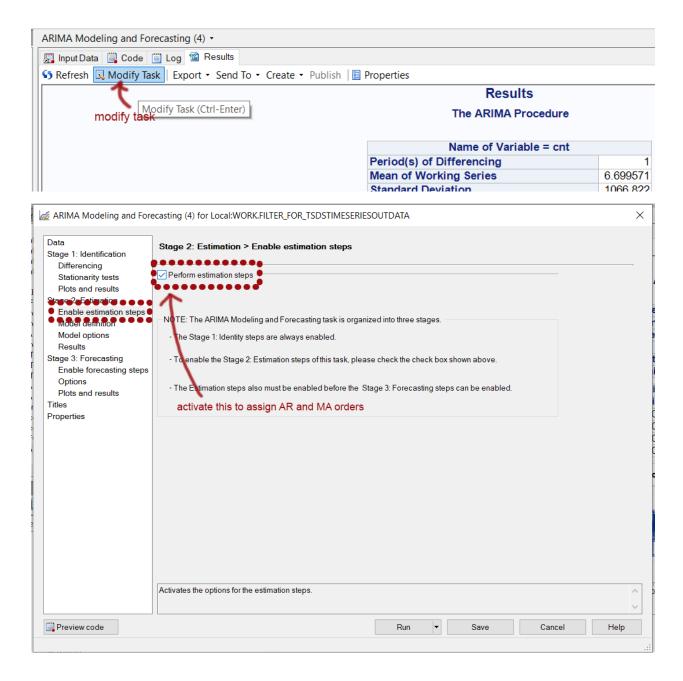
Autocorrelation Check for White Noise									
To Lag	Chi-Square	DF	Pr > ChiSq	Autocorrelations					
6	84.85	6	<.0001	-0.296	-0.107	-0.080	-0.057	-0.024	0.108
12	86.49	12	<.0001	-0.026	0.012	-0.029	0.018	-0.017	0.002
18	95.37	18	<.0001	-0.064	0.067	0.045	-0.035	0.000	-0.023
24	99.73	24	<.0001	-0.036	0.007	0.064	0.013	-0.014	-0.018

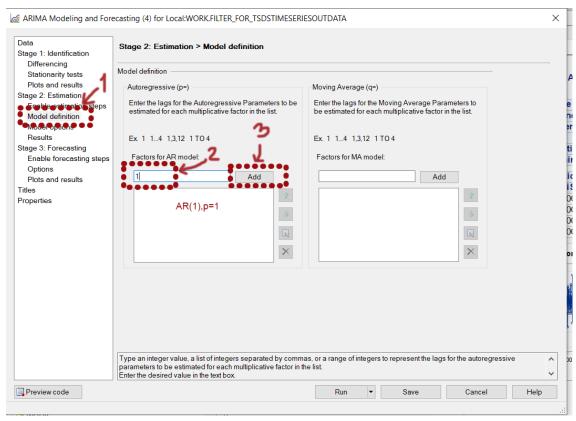


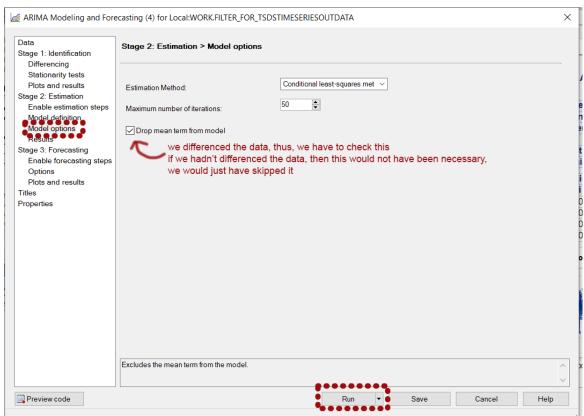
Estimate AR or/and MA parameters.

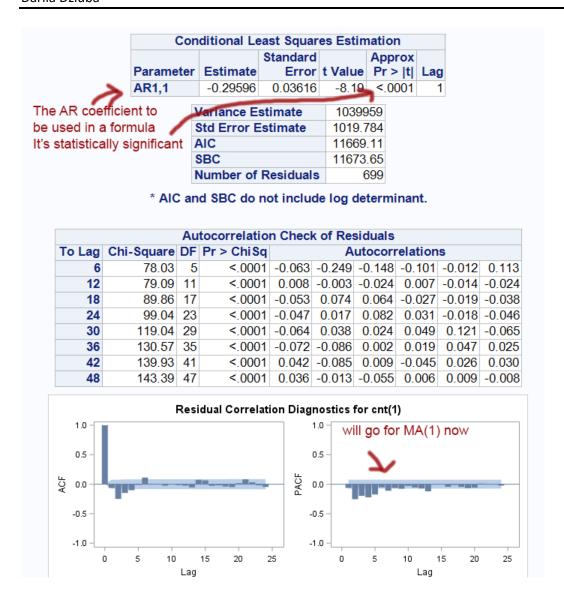
We are going to estimate AR parameters here:

With the results open, click: Modify task \rightarrow Stage 2: Estimation \rightarrow Enable estimation steps \rightarrow Check: Perform estimation steps \rightarrow Model definition: We're going to start with AR(1): under Factors for AR model enter 1 \rightarrow Click Add \rightarrow Model Options: Check Drop mean term from model (should be done only when you difference the data) \rightarrow Run \rightarrow Explore the results





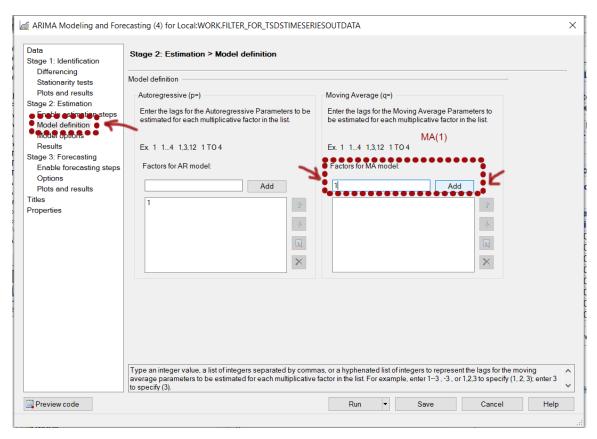


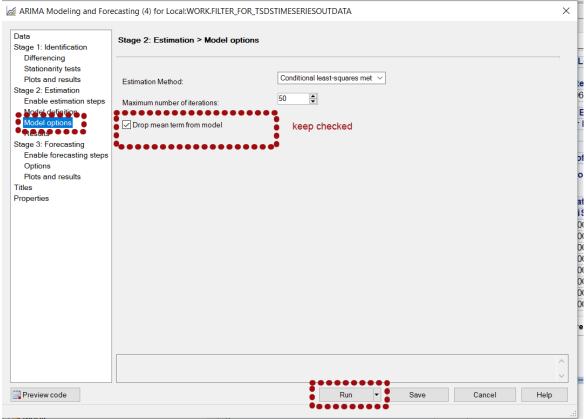


We can see that now we need to add an MA process to the ARIMA model:

With the results open, click: Modify task \rightarrow Stage 2: Estimation \rightarrow Enable estimation steps \rightarrow Check: Perform estimation steps \rightarrow Model definition: Don't change anything for the AR, we're going to add MA: under Factors for MA model enter 1 \rightarrow Click Add \rightarrow Model Options: Keep the Drop mean term from model checked (should be done only when you difference the data) \rightarrow Run \rightarrow Explore the results





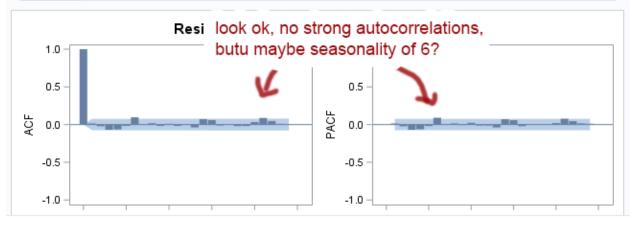


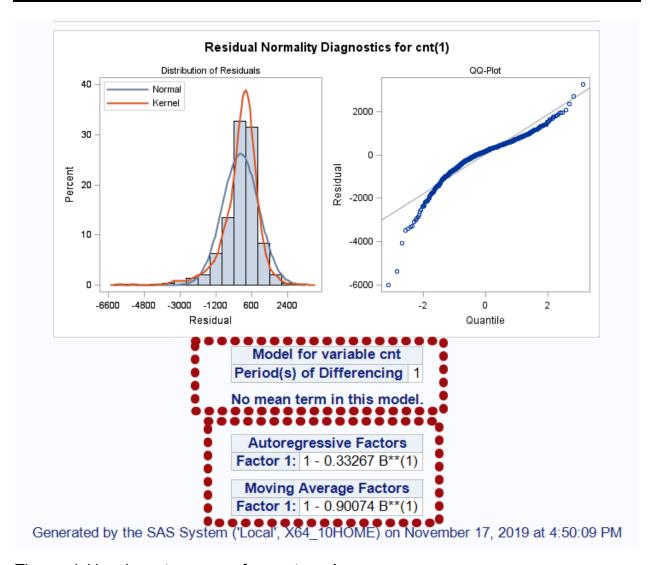
Co	Conditional Least Squares Estimation						
Paramete	r Estimate	Standard Error	t Value	Approx Pr > t	Lag		
MA1,1	0.90074	0.02036	44.23	<.0001	1		
AR1,1	0.33267	0.04419	7.53	<.0001	1		
\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	Variance E		8378		•••		
V	Std Error E	Estimate	915.3				
\IC 11519.08							
MA and AR coefficients 3C 11528.18							
to be used in the form	ula nber of	Residuals	. (699			

* AIC and SBC do not include log determinant.

Correlations of Parameter Estimates							
Parameter	MA1,1	AR1,1					
MA1,1	1.000	0.588					
AR1,1	0.588	1.000					

Autocorrelation Check of Residuals									
To Lag	Chi-Square	DF	Pr > ChiSq	Autocorrelations					
6	13.38	4	0.0096	0.016	-0.020	-0.068	-0.062	-0.016	0.098
12	14.13	10	0.1673	0.008	0.019	-0.015	0.012	-0.015	-0.004
18	21.91	16	0.1460	-0.035	0.074	0.061	-0.010	-0.000	-0.017
24	30.60	22	0.1046	-0.017	0.035	0.089	0.049	0.012	-0.003
30	53.25	28	0.0027	-0.026	0.068	0.056	0.062	0.122	-0.060
36	63.56	34	0.0016	-0.054	-0.092	-0.004	0.007	0.049	0.017
42	73.37	40	0.0010	0.053	-0.078	0.024	-0.045	0.035	0.025
48	75.79	46	0.0037	0.038	0.002	-0.035	0.014	0.019	-0.000





The model is adequate, we can forecast now!

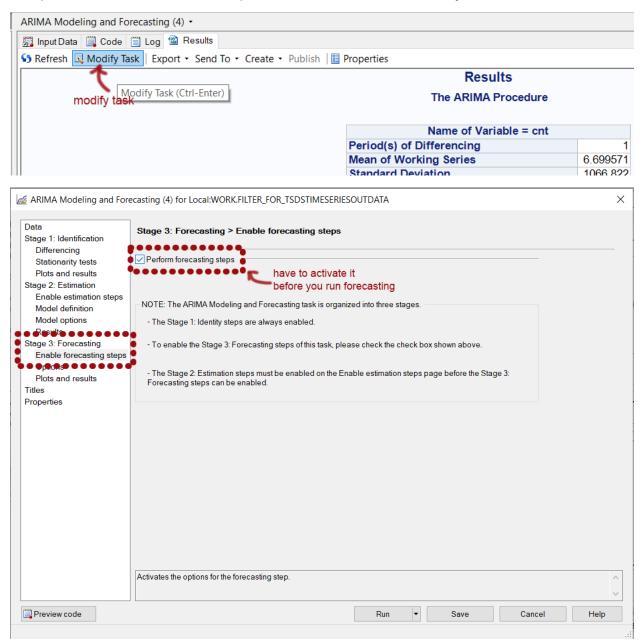
ARIMA: Step 3 - Forecast Total Rides for the Validation Period

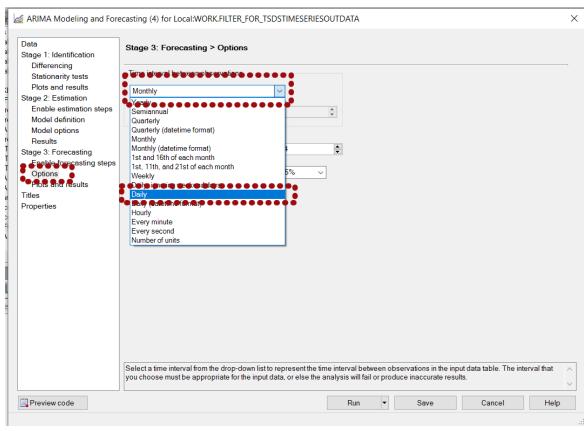
If you remember, we only used the training dataset to build our model. Now, it is time to use it by estimating how well it performs on new data, i.e. the validation data. For this we need to forecast those 31 days we have left out from the training dataset and then compare them to the actual datapoints and assess the accuracy of the model.

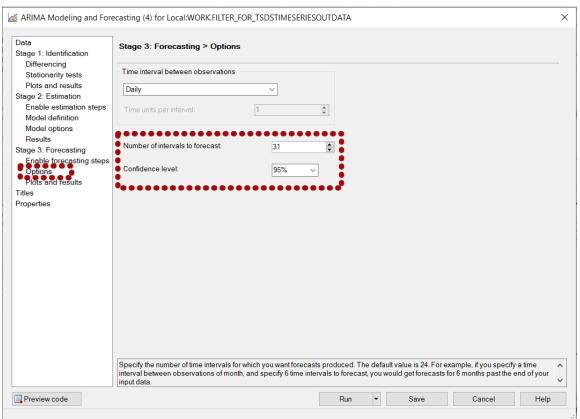
With the results open, click: Modify task → Stage 3: Forecasting → Enable forecasting steps → Check: Perform forecasting steps → Options → Time interval between observations: Set it to Daily → Number of intervals to forecast: 31 (December of 2012 has 31 days) → Confidence level 95% → Plots and results → Forecasting plots options: Check forecasts, Residuals → You can export forecasts to calculate residuals for the validation dataset: Save forecasts → Run

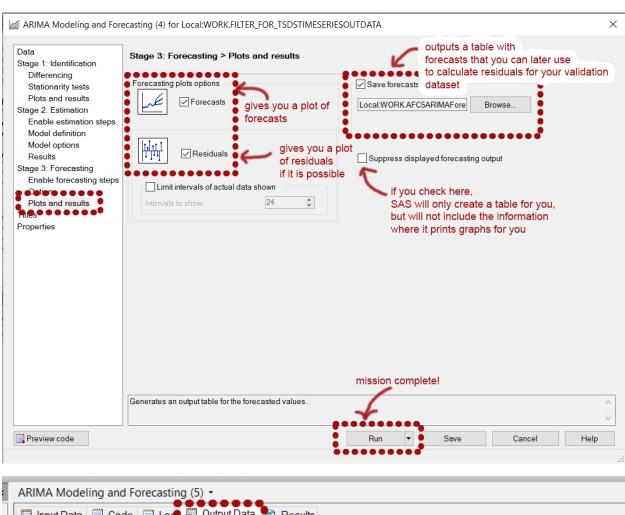
→ To the left of the Results tab, click on Output Data → Export → Select the extension as XLXS (remember to choose the location where you want to save your file; now you'll be able to use it to calculate residuals for the validation dataset by retrieving actual CNT values).

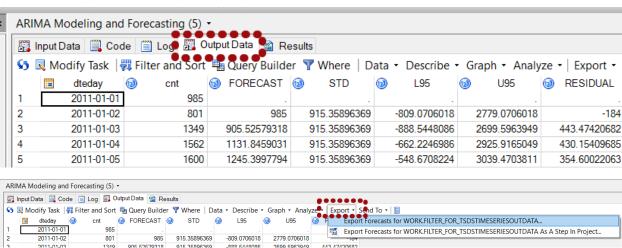
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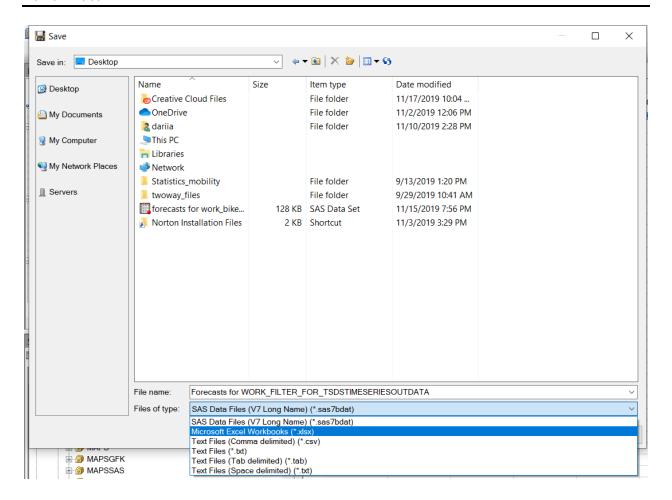








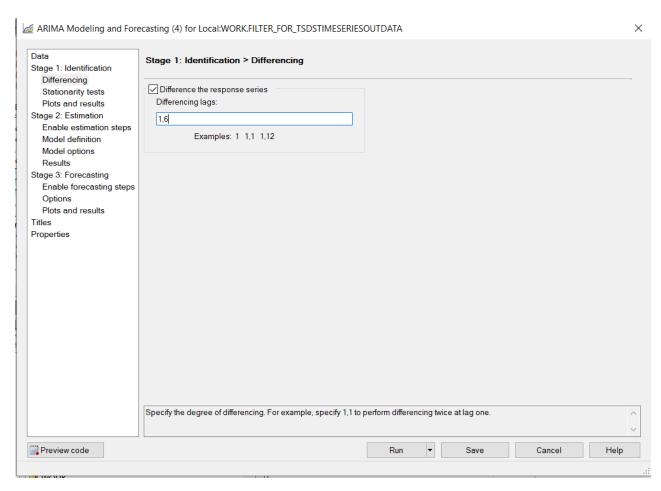




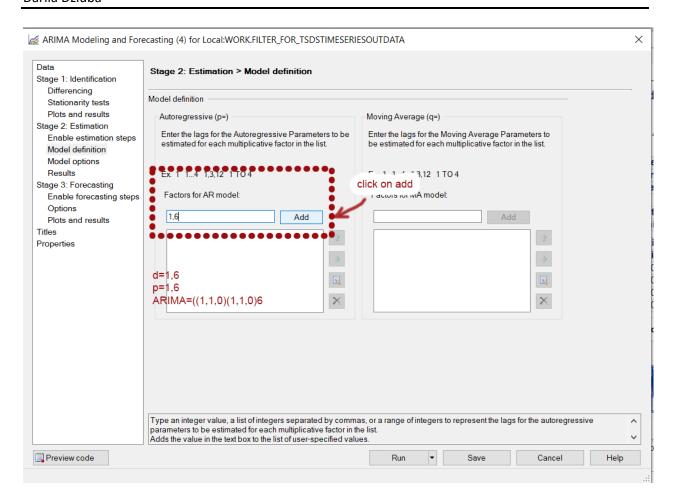
Seasonal ARIMA: How to Input Values

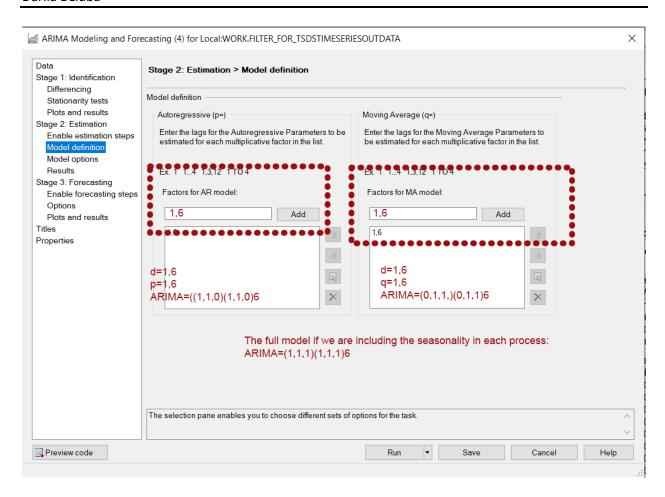
For seasonal ARIMA, you just have to enter two lags, the non-seasonal one and the seasonal one.

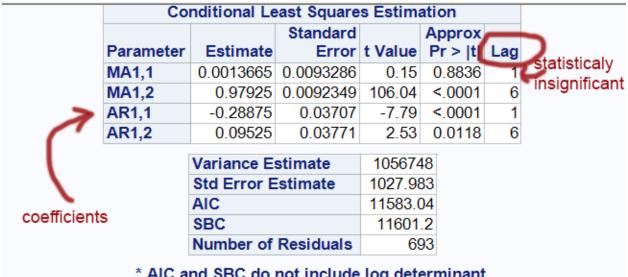
Double differencing at lag1 and at lag6



Setting AR at lag1 and adding a seasonal lag of 6







* AIC and SBC do not include log determinant.

Correlations of Parameter Estimates								
Parameter MA1,1 MA1,2 AR1,1 AR1								
MA1,1	1.000	-0.405	0.188	-0.152				
MA1,2	-0.405	1.000	-0.003	0.244				
AR1,1	0.188	-0.003	1.000	0.004				
AR1,2	-0.152	0.244	0.004	1.000				

	Autocorrelation Check of Residuals								
To Lag	Chi-Square	DF	Pr > ChiSq	Autocorrelations					
6	60.42	2	<.0001	-0.062	-0.238	-0.141	-0.077	-0.005	0.015
12	64.50	8	<.0001	0.056	0.010	-0.027	0.020	-0.009	-0.037
18	73.99	14	<.0001	-0.040	0.079	0.055	-0.028	-0.011	-0.039
24	81.58	20	<.0001	-0.031	0.009	0.073	0.041	-0.026	-0.043
30	102.39	26	<.0001	-0.052	0.048	0.012	0.054	0.126	-0.069
36	111.92	32	<.0001	-0.066	-0.078	-0.006	0.021	0.038	0.028
42	120.65	38	<.0001	0.052	-0.077	0.009	-0.044	0.023	0.027
48	126.36	44	<.0001	0.036	0.005	-0.073	0.025	0.008	-0.018

