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Practice quiz on Bayes Theorem and the Binomial Theorem

PUNTOS TOTALES DE 9

1. A jewelry store that serves just one customer at a time is concerned about the safety of its isolated customers.

1 / 1 puntos

The store does some research and learns that:

- 10% of the times that a jewelry store is robbed, a customer is in the store.
- A jewelry store has a customer on average 20% of each 24-hour day.
- The probability that a jewelry store is being robbed (anywhere in the world) is 1 in 2 million.

What is the probability that a robbery will occur while a customer is in the store?

- ☐ $\frac{1}{500000}$
- ☐ $\frac{1}{2000000}$
- ☒ $\frac{1}{4000000}$

✓ **Correcto**

What is known is:

A: "a customer is in the store," $P(A) = 0.2$

B: "a robbery is occurring," $P(B) = \frac{1}{2,000,000}$

$P(\text{a customer is in the store} \mid \text{a robbery occurs}) = P(A \mid B)$

$P(A \mid B) = 10\%$

What is wanted:

$P(\text{a robbery occurs} \mid \text{a customer is in the store}) = P(B \mid A)$

By the product rule:

$$P(B \mid A) = \frac{P(A, B)}{P(A)}$$

and $P(A, B) = P(A \mid B)P(B)$

Therefore:

$$P(B \mid A) = \frac{P(A \mid B)P(B)}{P(A)}$$

2. If I flip a fair coin, with heads and tails, ten times in a row, what is the probability that I will get exactly six heads?

1 / 1 puntos

- ☐ 0.021
- ☐ 0.187
- ☒ 0.2051
- ☐ 0.305

✓ **Correcto**

By Binomial Theorem, equals

$$\binom{10}{6} (0.5)^{10}$$

$$= \left(\frac{10!}{4! \times 6!} \right) \left(\frac{1}{1024} \right)$$

$$= 0.2051$$

3. If a coin is bent so that it has a 40% probability of coming up heads, what is the probability of getting exactly 6 heads in 10 throws?

1 / 1 puntos

- ☐ 0.0974
-

- ☐ 0.1219

✓ **Correcto**

$$\binom{10}{6} \times 0.4^6 \times 0.6^4 = 0.1115$$

4. A bent coin has 40% probability of coming up heads on each independent toss. If I toss the coin ten times, what is the probability that I get at least 8 heads?

1 / 1 puntos

- ☐ 0.0312
- ☒ 0.0123
- ☐ 0.0213
- ☐ 0.0132

✓ **Correcto**

The answer is the sum of three binomial probabilities:

$$\left(\binom{10}{8} \times (0.4^8) \times (.6^2) \right) + \left(\binom{10}{9} \times (0.4^9) \times (0.6^1) \right) +$$

$$\left(\binom{10}{10} \times (0.4^{10}) \times (0.6^0) \right)$$

5. Suppose I have a bent coin with a 60% probability of coming up heads. I throw the coin ten

1 / 1 puntos

what is the value of the "likelihood" term in Bayes' Theorem -- the conditional probability of the data given the parameter.

- ☐ 0.122885
- ☐ 0.168835
- ☒ 0.120932
- ☐ 0.043945

✓ **Correcto**

Bayesian "likelihood" --- the p(observed data | parameter) is

p(8 of 10 heads | coin has p = .6 of coming up heads)

$$\binom{10}{8} \times (0.6^8) \times (0.4^2) = 0.120932$$

6. We have the following information about a new medical test for diagnosing cancer.

1 / 1 puntos

Before any data are observed, we know that 5% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer. The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 90% of them get an accurate test result of "Negative"

What is the conditional probability that I have cancer, if I get a "Positive" test result for Cancer?

**Formulas in the feedback section are very long, and do not fit within the standard viewing window. Therefore, the font is a bit smaller and the word "positive test" has been abbreviated as PT.

- ☐ 4.5%
- ☐ 67.9%
- ☐ 9.5%
- ☒ 32.1% probability that I have cancer

✓ **Correcto**

I still have a more than $\frac{2}{3}$ probability of not having cancer

Posterior probability:

p(I actually have cancer | receive a "positive" Test)

By Bayes Theorem:

$$= \frac{\text{(chance of observing a PT if I have cancer)} \times \text{(prior probability of having cancer)}}{\text{(marginal likelihood of the observation of a PT)}}$$

$$= \frac{p(\text{receiving positive test} \mid \text{has cancer}) p(\text{has cancer} \mid \text{before data is observed})}{p(\text{positive} \mid \text{has cancer}) p(\text{has cancer}) + p(\text{positive} \mid \text{no cancer}) p(\text{no cancer})}$$

$$= (90\%)(5\%) / ((90\%)(5\%) + (10\%)(95\%))$$

7. We have the following information about a new medical test for diagnosing cancer.

1 / 1 puntos

Before any data are observed, we know that 8% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer.

The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 95% of them get an accurate test result of "Negative" for cancer.

The other 5% get a false test result of "Positive" for cancer.

What is the conditional probability that I have cancer, if I get a "Negative" test result for Cancer?

- ☐ 88.2%
- ☐ .80%
- ☐ 99.1%
- ☒ 0.9%

✓ **Correcto**

$$\frac{p(\text{negative test} \mid \text{cancer}) p(\text{cancer}) + p(\text{negative test} \mid \text{no cancer}) p(\text{no cancer})}{\frac{(10\%)(8\%)}{(10\%)(8\%) + (95\%)(92\%)}}$$

$$\frac{0.8\%}{0.8\% + 87.4\%}$$

$$\frac{0.8\%}{88.2\%}$$

$$= 0.9\%$$

8. An urn contains 50 marbles -- 40 blue and 10 white. After 50 draws, exactly 40 blue and 10 white are observed.

1 / 1 puntos

You are not told whether the draw was done "with replacement" or "without replacement."

What is the probability that the draw was done with replacement?

- ☐ 87.73%
- ☐ 13.98%
- ☒ 12.27%
- ☐ 1

outcome when 50 draws are made without replacement]

p(40 blue and 10 white | draws with replacement)

S = 40

N = 50

P = .8 [for draws with replacement] because 40 blue of 50 total means p(blue) = 40/50 = .8

$$\left(\binom{50}{40} \right) (0.8^{40}) (0.2^{10})$$

$$= 13.98\%$$

By Bayes' Theorem:

p(draws with replacement | observed data) =

$$= \frac{0.1398}{1.1398}$$

$$= 12.27\%$$

9. According to Department of Customs Enforcement Research: 99% of people crossing into the United States are not smugglers.

1 / 1 puntos

The majority of all Smugglers at the border (65%) appear nervous and sweaty.

Only 8% of innocent people at the border appear nervous and sweaty.

If someone at the border appears nervous and sweaty, what is the probability that they are a Smuggler?

- ☐ 8.57%
- ☒ 7.58%
- ☐ 7.92%
- ☐ 92.42%

✓ **Correcto**

By Bayes' Theorem, the answer is

$$\frac{(.65)(.01)}{((.65)(.01) + (.08)(.99))}$$