

Question 1

At a given point of time and given an ant, the ant found 6 possible routes at its journey. The pheromone amounts on each route are :

9.000000 1.000000 9.000000 6.000000 1.000000 3.000000

If the length of each route which is inversely proportional to the route desirability is known to the ant and lengths are :

38.000000 67.000000 68.000000 11.000000 68.000000 67.000000

Calculate the probability of selecting each route by that given ant

Assume Alpha=0.5 and beta= 0.8

Answer

eta=1/d

eta1=0.026316

eta2=0.014925

eta3=0.014706

eta4=0.090909

eta5=0.014706

eta6=0.014925

P-1=0.216598

P-2=0.045867

P-3=0.135980

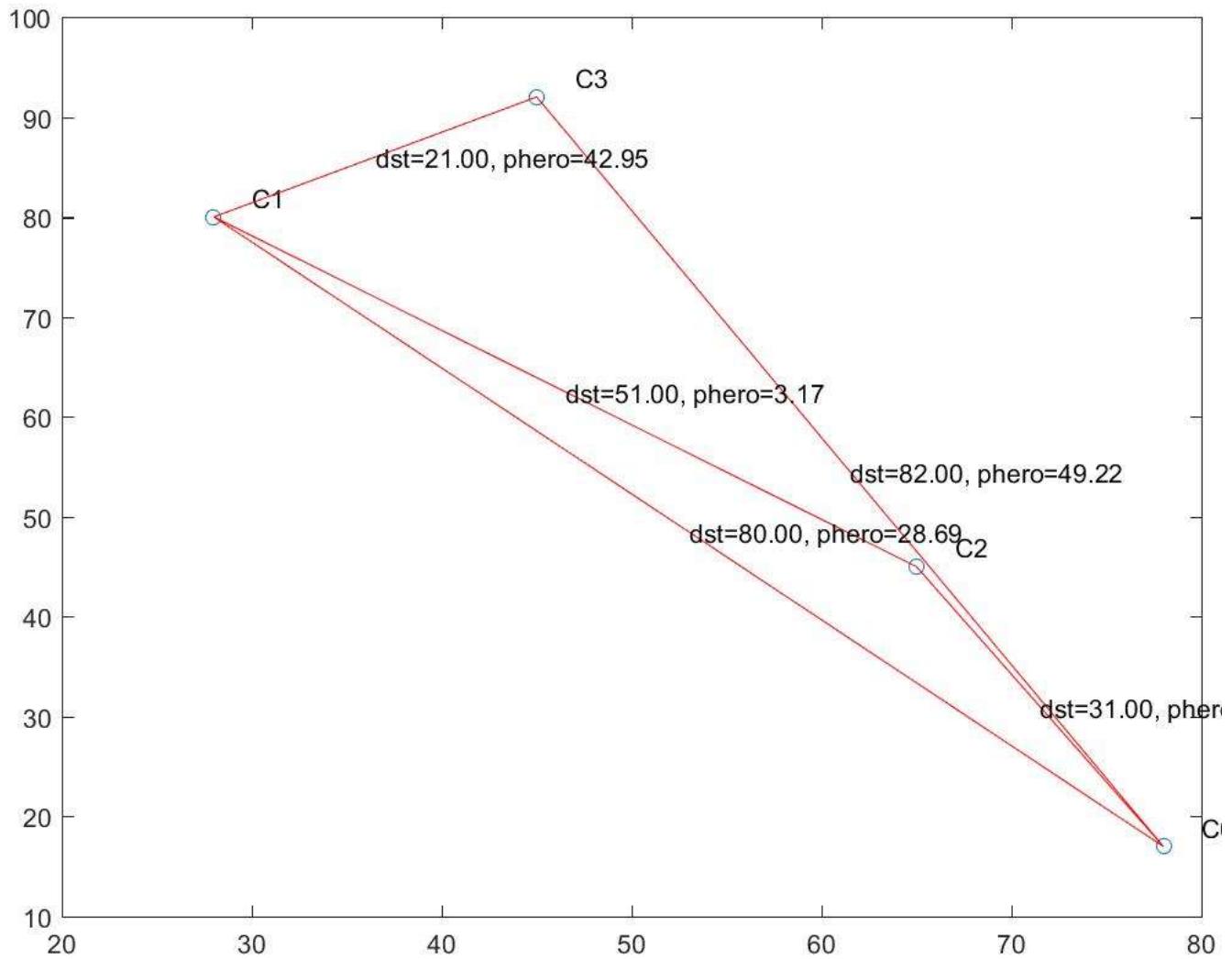
P-4=0.476784

P-5=0.045327

P-6=0.079444

Question 2

In a TSP problem with 4 cities, cities are connected as shown in the figure:



The following table shows the distances between different cities

	C0	C1	C2	C3
C0	0.00	80.00	31.00	82.00
C1	80.00	0.00	51.00	21.00
C2	31.00	51.00	0.00	51.00
C3	82.00	21.00	51.00	0.00

[Distance of 0 means distance is not applicable.

The following table shows the pheromone in units between different cities

	C0	C1	C2	C3
C0	0.00	28.69	36.89	49.22
C1	28.69	0.00	3.17	42.95
C2	36.89	3.17	0.00	0.00
C3	49.22	42.95	0.00	0.00

- Assume that an ant has followed the following route:[0,3,1,2,] and back to source

- Calculate the total cost of the above route.
- Calculate the ant's switching probabilities for the first 2 steps in the above route assuming pheromone exponent parameter $\alpha=0.03$ and heuristic exponent parameter $\beta=0.94$.
- Calculate the updated pheromone amounts after applying the ACO evaporation step assuming $\rho=0.30$.
- Calculate the updated pheromone amounts after applying the ACO depositing step assuming $Q=11.82$.

Answer

- The cost of the aforementioned route:185.00

- b. At node 0 the ant has 3 choices: From C0 to C1 the heuristic value is 0.01 and its pheromone value is 28.69 hence P=0.22
 From C0 to C2 the heuristic value is 0.03 and its pheromone value is 36.89 hence P=0.55
 From C0 to C3 the heuristic value is 0.01 and its pheromone value is 49.22 hence P=0.22
 At node 3 the ant has 1 choices: From C3 to C1 the heuristic value is 0.05 and its pheromone value is 42.95 hence P=1.00
 c. The pheromone matrix will evaporate according to the rule: pheromone = (1-p) * pheromone

	C0	C1	C2	C3
C0	0.00	20.08	25.82	34.45
C1	20.08	0.00	2.22	30.07
C2	25.82	2.22	0.00	0.00
C3	34.45	30.07	0.00	0.00

The route links pheromone will be enhanced by $\Delta = Q/L$ (where L is the path cost)

$\Delta = 0.06$

The updated Pheromone matrix:

	C0	C1	C2	C3
C0	0.00	20.08	25.82	34.52
C1	20.08	0.00	2.28	30.07
C2	25.89	2.22	0.00	0.00
C3	34.45	30.13	0.00	0.00

Question 3

Having the following routing table at node 5

	N42	N47	N75	N80	N10
N17	0.23	0.32	0.33	0.14	0.21
N34	0.32	0.21	0.04	0.38	0.28
N6	0.44	0.33	0.13	0.05	0.39
N49	0.02	0.13	0.49	0.42	0.11

Having started at node 47 and reaching node 5 via node 17. Assuming it has been in the network for 9.051536 time units, what effect will it have on the routing table on node 5

assume a and b equals 0.070000 and 0.050000 in order for ABC model

$$\delta r = a/T + b$$

$$\delta r = 0.057733$$

$$r_{1_2} = (r_{1_2} + \delta r) / (1 + \delta r)$$

$$= 0.360449$$

The remaining cells in the source column will be updated by $rks / (1 + \delta r)$

The updated table will be:

	N42	N47	N75	N80	N10
N17	0.23	0.36	0.33	0.14	0.21
N34	0.32	0.20	0.04	0.38	0.28
N6	0.44	0.31	0.13	0.05	0.39
N49	0.02	0.13	0.49	0.42	0.11

Question 4

At a given point of time and given an ant, the ant found 6 possible routes at its journey. The pheromone amounts on each route are :

1.000000 7.000000 7.000000 6.000000 2.000000 6.000000

If the length of each route which is inversely proportional to the route desirability is known to the ant and lengths are :

21.000000 9.000000 15.000000 63.000000 5.000000 17.000000

Calculate the probability of selecting each route by that given ant

Assume Alpha=0.1 and beta= 0.4

Answer

$\eta = 1/d$

$\eta_1 = 0.047619$

$\eta_2 = 0.111111$

$\eta_3 = 0.066667$

$\eta_4 = 0.015873$

$\eta_5 = 0.200000$

$\eta_6 = 0.058824$

$P_1 = 0.123913$

$P_2 = 0.211261$

$P_3 = 0.172218$

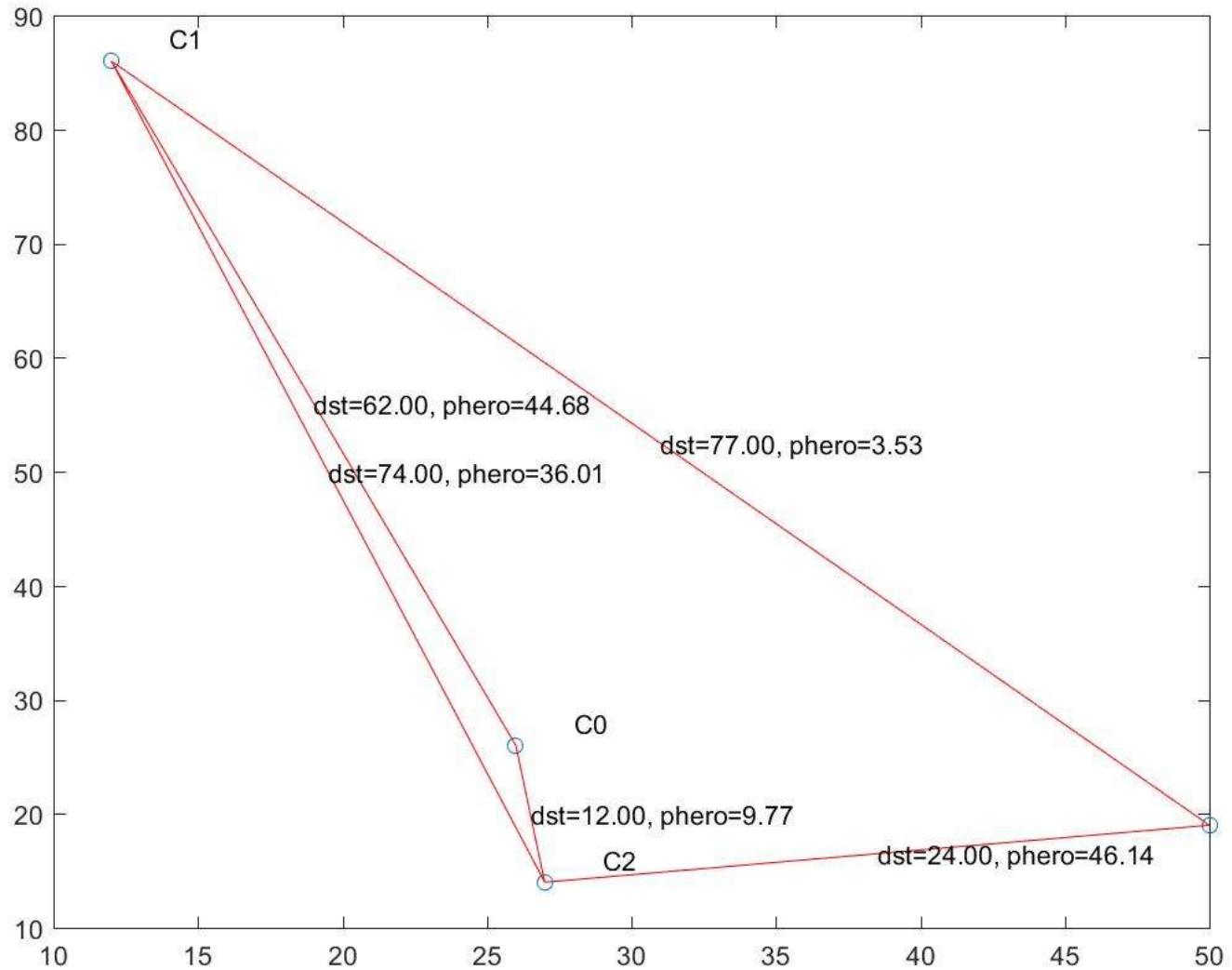
$P_4 = 0.095518$

$P_5 = 0.235787$

$P_6 = 0.161303$

Question 5

In a TSP problem with 4 cities, cities are connected as shown in the figure:



the following table shows the distances between different cities

	C0	C1	C2	C3
C0	0.00	62.00	12.00	25.00
C1	62.00	0.00	74.00	77.00
C2	12.00	74.00	0.00	24.00
C3	25.00	77.00	24.00	0.00

[Distance of 0 means distance is not applicable.

]The following table shows the pheromone in units between different cities

	C0	C1	C2	C3
C0	0.00	44.68	9.77	0.00
C1	44.68	0.00	36.01	3.53
C2	9.77	36.01	0.00	46.14
C3	0.00	3.53	46.14	0.00

- Assume that an ant has followed the following route:[1,0,2,3,] and back to source
 - Calculate the total cost of the above route.
 - Calculate the ant's switching probabilities for the first 3 steps in the above route assuming pheromone exponent parameter $\alpha=0.72$ and heuristic exponent parameter $\beta=0.84$.
 - Calculate the updated pheromone amounts after applying the ACO evaporation step assuming $\rho=0.43$.
 - Calculate the updated pheromone amounts after applying the ACO depositing step assuming $Q=18.82$.

Answer

- a. The cost of the aforementioned route: 175.00
 b. At node 1 the ant has 3 choices: From C1 to C2 the heuristic value is 0.01 and its pheromone value is 36.01 hence P=0.39
 From C1 to C3 the heuristic value is 0.01 and its pheromone value is 3.53 hence P=0.07
 From C1 to C0 the heuristic value is 0.02 and its pheromone value is 44.68 hence P=0.53
 At node 0 the ant has 1 choice: From C0 to C2 the heuristic value is 0.08 and its pheromone value is 9.77 hence P=1.00
 At node 2 the ant has 2 choices: From C2 to C3 the heuristic value is 0.04 and its pheromone value is 46.14 hence P=0.75
 From C2 to C1 the heuristic value is 0.01 and its pheromone value is 36.01 hence P=0.25
 c. The pheromone matrix will evaporate according to the rule: pheromone = (1-p)pheromone

	C0	C1	C2	C3
C0	0.00	25.47	5.57	0.00
C1	25.47	0.00	20.53	2.01
C2	5.57	20.53	0.00	26.30
C3	0.00	2.01	26.30	0.00

The route links pheromone will be enhanced by $\Delta = Q/L$ (where L is the path cost)

$\Delta = 0.11$

The updated Pheromone matrix:

	C0	C1	C2	C3
C0	0.00	25.47	5.68	0.00
C1	25.58	0.00	20.53	2.01
C2	5.57	20.53	0.00	26.41
C3	0.00	2.12	26.30	0.00

Question 6

Having the following routing table at node 5

	N90	N60	N87	N92	N53
N70	0.27	0.41	0.14	0.13	0.31
N55	0.13	0.20	0.30	0.02	0.33
N3	0.36	0.09	0.30	0.55	0.10
N42	0.24	0.30	0.26	0.30	0.27

Having started at node 92 and reaching node 5 via node 3. Assuming it has been in the network for 9.371347 time units, what effect will it have on the routing table on node 5

assume a and b equals 0.080000 and 0.080000 in order for ABC model

$$\delta r = a/T + b$$

$$\delta r = 0.088537$$

$$r_{3_4} = (r_{3_4} + \delta r) / (1 + \delta r)$$

$$= 0.587682$$

The remaining cells in the source column will be updated by $rks / (1 + \delta r)$

The updated table will be:

	N90	N60	N87	N92	N53
N70	0.27	0.41	0.14	0.12	0.31
N55	0.13	0.20	0.30	0.02	0.33
N3	0.36	0.09	0.30	0.59	0.10
N42	0.24	0.30	0.26	0.27	0.27

Question 7

At a given point of time and given an ant, the ant found 4 possible routes at its journey. The pheromone amounts on each route are :

6.000000 9.000000 9.000000 7.000000

If the length of each route which is inversely proportional to the route desirability is known to the ant and lengths are :

14.000000 46.000000 5.000000 28.000000

Calculate the probability of selecting each route by that given ant

Assume Alpha=0.7 and beta=0.9

Answer

$\eta = 1/d$

$\eta_1 = 0.071429$

$\eta_2 = 0.021739$

$\eta_3 = 0.200000$

$\eta_4 = 0.035714$

$P_1 = 0.184933$

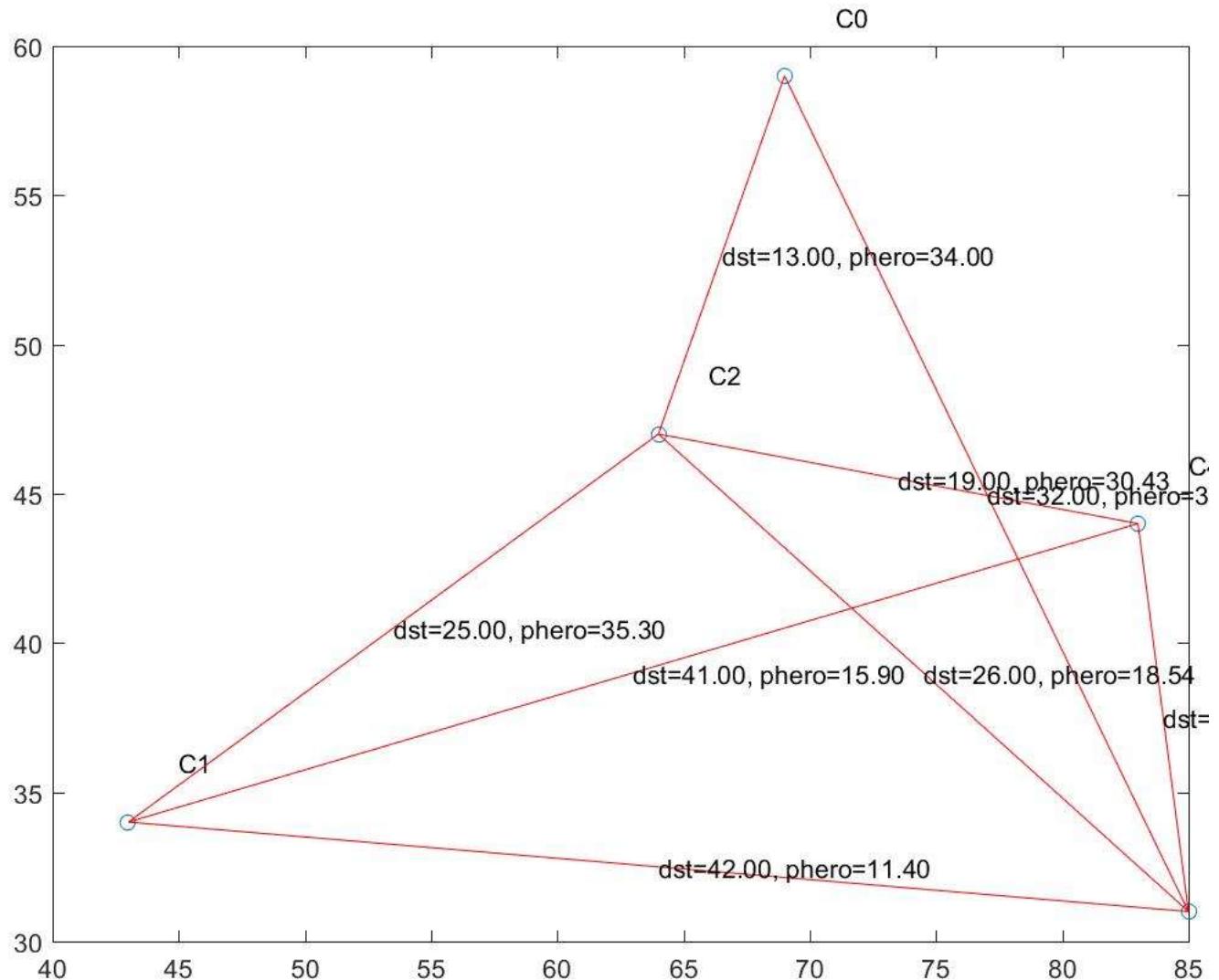
$P_2 = 0.084200$

$P_3 = 0.620471$

P-4=0.110395

Question 8

In a TSP problem with 5 cities, cities are connected as shown in the figure:



the following table shows the distances between different cities

	C0	C1	C2	C3	C4
C0	0.00	36.00	13.00	32.00	21.00
C1	36.00	0.00	25.00	42.00	41.00
C2	13.00	25.00	0.00	26.00	19.00
C3	32.00	42.00	26.00	0.00	13.00
C4	21.00	41.00	19.00	13.00	0.00

[Distance of 0 means distance is not applicable.

]The following table shows the pheromone in units between different cities

	C0	C1	C2	C3	C4
C0	0.00	0.00	34.00	38.62	0.00
C1	0.00	0.00	35.30	11.40	15.90
C2	34.00	35.30	0.00	18.54	30.43
C3	38.62	11.40	18.54	0.00	45.51
C4	0.00	15.90	30.43	45.51	0.00

- Assume that an ant has followed the following route:[2,4,1,3,0,] and back to source
 - Calculate the total cost of the above route.

- b. Calculate the ant's switching probabilities for the first 2 steps in the above route assuming pheromone exponent parameter $\alpha=0.85$ and heuristic exponent parameter $\beta=0.44$.
c. Calculate the updated pheromone amounts after applying the ACO evaporation step assuming $\rho=0.90$.
d. Calculate the updated pheromone amounts after applying the ACO depositing step assuming $Q=1.33$.

Answer

- a. The cost of the aforementioned route: 147.00
b. At node 2 the ant has 4 choices: From C2 to C3 the heuristic value is 0.04 and its pheromone value is 18.54 hence $P=0.15$
From C2 to C4 the heuristic value is 0.05 and its pheromone value is 30.43 hence $P=0.26$
From C2 to C0 the heuristic value is 0.08 and its pheromone value is 34.00 hence $P=0.34$
From C2 to C1 the heuristic value is 0.04 and its pheromone value is 35.30 hence $P=0.26$
At node 4 the ant has 2 choices: From C4 to C1 the heuristic value is 0.02 and its pheromone value is 15.90 hence $P=0.20$
From C4 to C3 the heuristic value is 0.08 and its pheromone value is 45.51 hence $P=0.80$
c. The pheromone matrix will evaporate according to the rule: $\text{pheromone} = (1-\rho)\text{pheromone}$

	C0	C1	C2	C3	C4
C0	0.00	0.00	3.40	3.86	0.00
C1	0.00	0.00	3.53	1.14	1.59
C2	3.40	3.53	0.00	1.85	3.04
C3	3.86	1.14	1.85	0.00	4.55
C4	0.00	1.59	3.04	4.55	0.00

The route links pheromone will be enhanced by $\Delta=Q/L$ (where L is the path cost)

$\Delta=0.01$

The updated Pheromone matrix:

	C0	C1	C2	C3	C4
C0	0.00	0.00	3.41	3.86	0.00
C1	0.00	0.00	3.53	1.15	1.59
C2	3.40	3.53	0.00	1.85	3.05
C3	3.87	1.14	1.85	0.00	4.55
C4	0.00	1.60	3.04	4.55	0.00

Question 9

Having the following routing table at node 5

	N19	N1	N32	N68	N61
N52	0.30	0.13	0.04	0.11	0.39
N42	0.41	0.22	0.49	0.07	0.35
N27	0.10	0.28	0.25	0.42	0.08
N47	0.19	0.38	0.22	0.41	0.17

Having started at node 68 and reaching node 5 via node 47. Assuming it has been in the network for 7.476628 time units, what effect will it have on the routing table on node 5

assume a and b equals 0.060000 and 0.020000 in order for ABC model

$$\delta r = a/T + b$$

$$\delta r = 0.028025$$

$$r_{47-4} = (r_{47-4} + \delta r) / (1 + \delta r)$$

$$= 0.424816$$

The remaining cells in the source column will be updated by $r_{\text{ks}} / (1 + \delta r)$

The updated table will be:

	N19	N1	N32	N68	N61
N52	0.30	0.13	0.04	0.10	0.39
N42	0.41	0.22	0.49	0.07	0.35
N27	0.10	0.28	0.25	0.41	0.08
N47	0.19	0.38	0.22	0.42	0.17

Question 10

At a given point of time and given an ant, the ant found 5 possible routes at its journey. The pheromone amounts on each route are :

3.000000 1.000000 1.000000 2.000000 7.000000

If the length of each route which is inversely proportional to the route desirability is known to the ant and lengths are :

30.000000 49.000000 18.000000 1.000000 37.000000

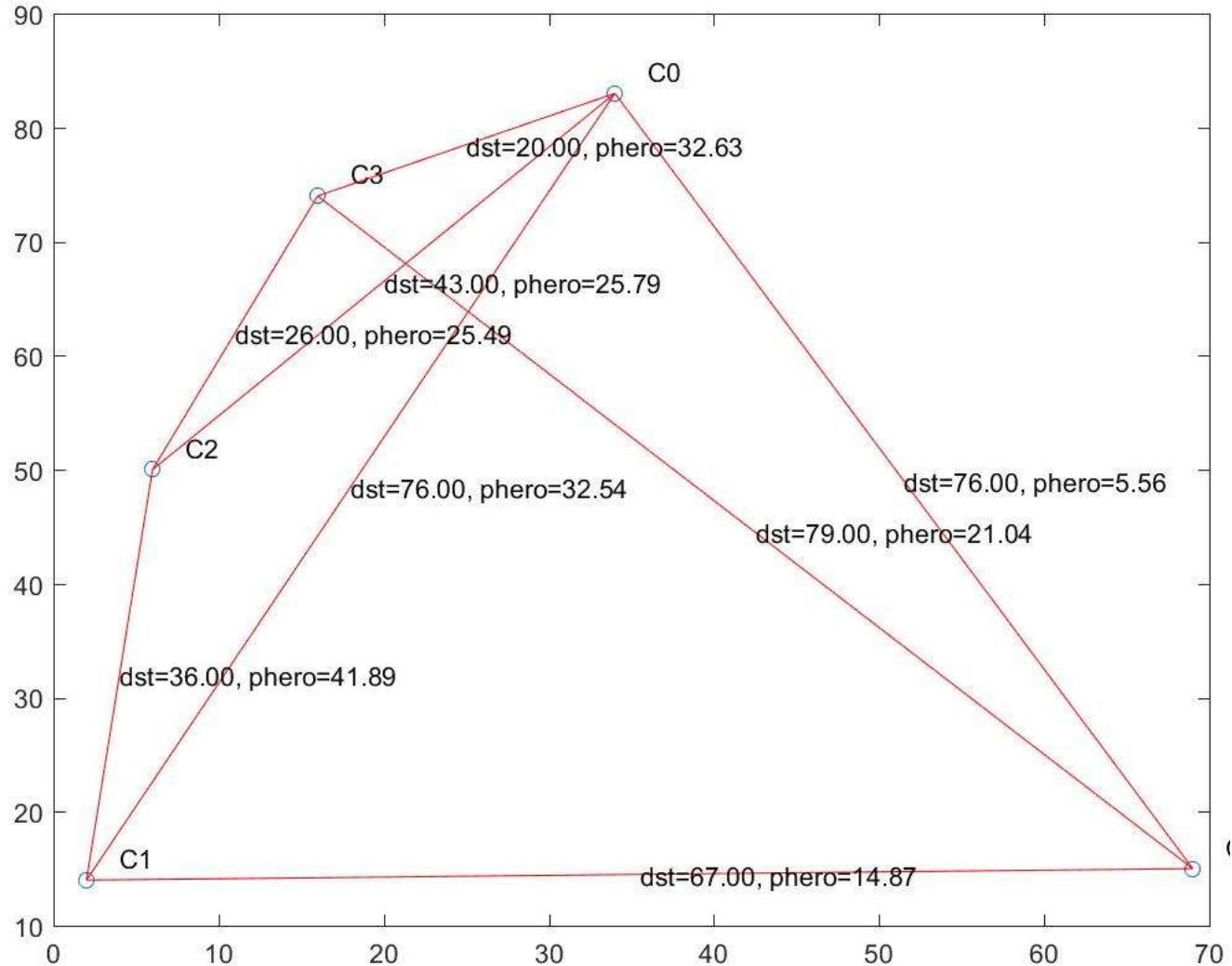
Calculate the probability of selecting each route by that given ant

Assume Alpha=0.3 and beta= 0.9

Answer
 $\eta = 1/d$
 $\eta_1 = 0.033333$
 $\eta_2 = 0.020408$
 $\eta_3 = 0.055556$
 $\eta_4 = 1.000000$
 $\eta_5 = 0.027027$
 $P_1 = 0.044298$
 $P_2 = 0.020487$
 $P_3 = 0.050456$
 $P_4 = 0.837465$
 $P_5 = 0.047294$

Question 11

In a TSP problem with 5 cities, cities are connected as shown in the figure:



the following table shows the distances between different cities

	C0	C1	C2	C3	C4
C0	0.00	76.00	43.00	20.00	76.00
C1	76.00	0.00	36.00	62.00	67.00
C2	43.00	36.00	0.00	26.00	72.00
C3	20.00	62.00	26.00	0.00	79.00
C4	76.00	67.00	72.00	79.00	0.00

[Distance of 0 means distance is not applicable.

]The following table shows the pheromone in units between different cities

	C0	C1	C2	C3	C4

C0	0.00	32.54	25.79	32.63	5.56
C1	32.54	0.00	41.89	0.00	14.87
C2	25.79	41.89	0.00	25.49	0.00
C3	32.63	0.00	25.49	0.00	21.04
C4	5.56	14.87	0.00	21.04	0.00

- Assume that an ant has followed the following route:[3,2,1,0,4,] and back to source

- Calculate the total cost of the above route.
- Calculate the ant's switching probabilities for the first 1 steps in the above route assuming pheromone exponent parameter $\alpha=0.40$ and heuristic exponent parameter $\beta=0.30$.
- Calculate the updated pheromone amounts after applying the ACO evaporation step assuming $\rho=0.31$.
- Calculate the updated pheromone amounts after applying the ACO depositing step assuming $Q=4.22$.

Answer

- The cost of the aforementioned route:293.00
- At node 3 the ant has 3 choices:From C3 to C4 the heuristic value is 0.01 and its pheromone value is 21.04 hence P=0.23
From C3 to C0 the heuristic value is 0.05 and its pheromone value is 32.63 hence P=0.42
From C3 to C2 the heuristic value is 0.04 and its pheromone value is 25.49 hence P=0.35
- The pheromone matrix will evaporate according to the rule:pheromone=(1-p)pheromone

	C0	C1	C2	C3	C4
C0	0.00	22.45	17.80	22.51	3.84
C1	22.45	0.00	28.90	0.00	10.26
C2	17.80	28.90	0.00	17.59	0.00
C3	22.51	0.00	17.59	0.00	14.52
C4	3.84	10.26	0.00	14.52	0.00

The route links pheromone will be enhanced by $\Delta=Q/L$ (where L is the path cost)

$\Delta=0.01$

The updated Pheromone matrix:

	C0	C1	C2	C3	C4
C0	0.00	22.45	17.80	22.51	3.85
C1	22.47	0.00	28.90	0.00	10.26
C2	17.80	28.92	0.00	17.59	0.00
C3	22.51	0.00	17.60	0.00	14.52
C4	3.84	10.26	0.00	14.53	0.00

Question 12

Having the following routing table at node 5

	N52	N98	N49	N68	N40
N4	0.58	0.16	0.34	0.47	0.11
N28	0.27	0.32	0.05	0.07	0.37
N75	0.15	0.50	0.31	0.26	0.39
N32	0.00	0.02	0.30	0.21	0.14

Having started at node 52 and reaching node 5 via node 75.Assuming it has been in the network for 7.394795 time units, what effect will it have on the routing table on node 5

assume a and b equals 0.050000 and 0.080000 in order for ABC model

$$\delta r = a/T + b$$

$$\delta r = 0.086762$$

$$r_{3_1} = (r_{3_1} + \delta r) / (1 + \delta r)$$

$$= 0.218177$$

The remaining cells in the source column will be updated by $rks/(1+\delta r)$

The updated table will be:

	N52	N98	N49	N68	N40
N4	0.53	0.16	0.34	0.47	0.11
N28	0.25	0.32	0.05	0.07	0.37
N75	0.22	0.50	0.31	0.26	0.39
N32	0.00	0.02	0.30	0.21	0.14

Question 13

At a given point of time and given an ant, the ant found 6 possible routes at its journey. The pheromone amounts on each route are :

2.000000 1.000000 8.000000 6.000000 0.000000 9.000000

If the length of each route which is inversely proportional to the route desirability is known to the ant and lengths are :

36.000000 38.000000 42.000000 53.000000 60.000000 27.000000

Calculate the probability of selecting each route by that given ant

Assume Alpha=0.1 and beta= 0.7

Answer

eta=1/d

eta1=0.027778

eta2=0.026316

eta3=0.023810

eta4=0.018868

eta5=0.016667

eta6=0.037037

P-1=0.192212

P-2=0.172680

P-3=0.198210

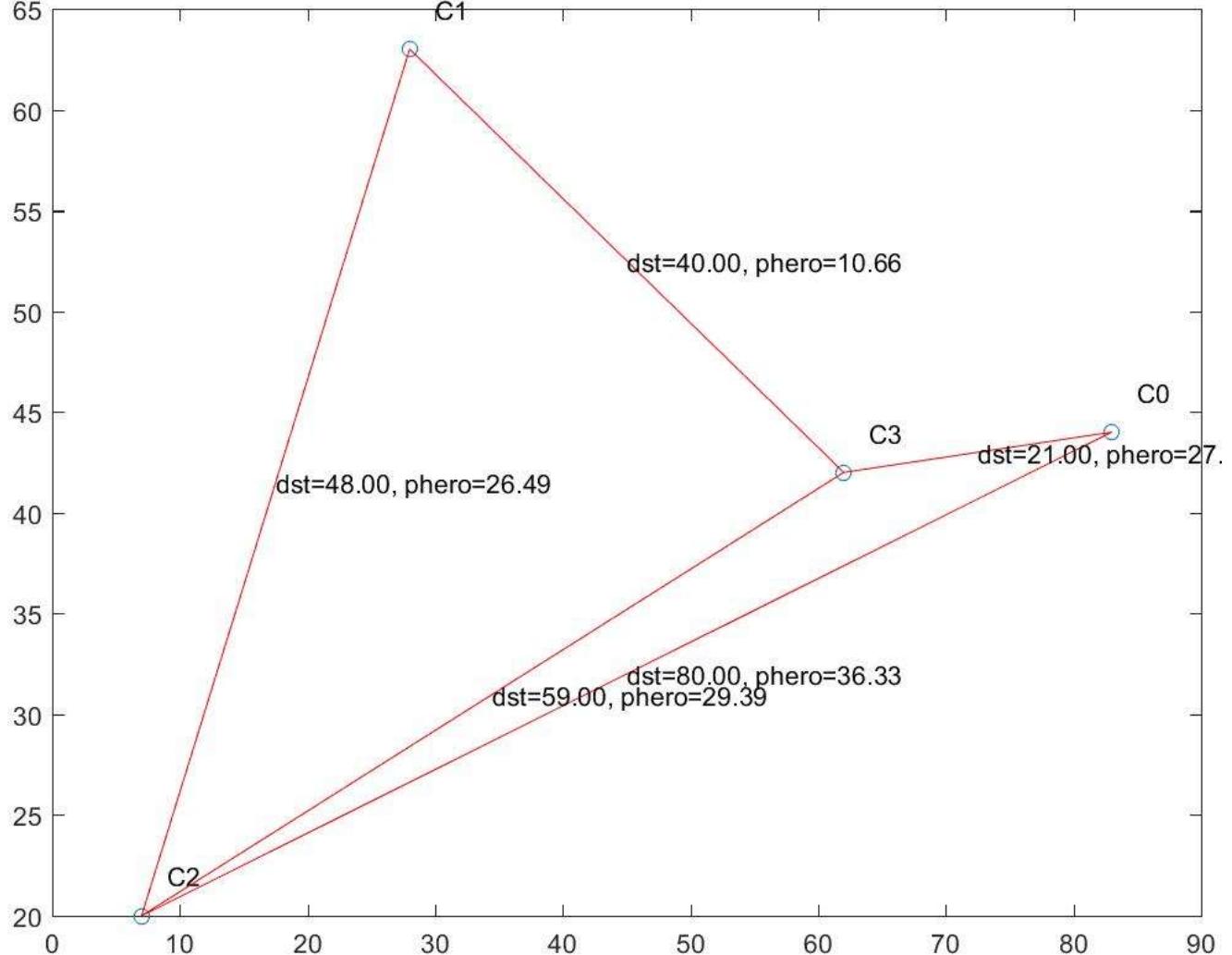
P-4=0.163649

P-5=0.000000

P-6=0.273250

Question 14

In a TSP problem with 4 cities, cities are connected as shown in the figure:



the following table shows the distances between different cities

	C0	C1	C2	C3
C0	0.00	58.00	80.00	21.00
C1	58.00	0.00	48.00	40.00

C2	80.00	48.00	0.00	59.00
C3	21.00	40.00	59.00	0.00

[Distance of 0 means distance is not applicable.

]The following table shows the pheromone in units between different cities

	C0	C1	C2	C3
C0	0.00	0.00	36.33	27.60
C1	0.00	0.00	26.49	10.66
C2	36.33	26.49	0.00	29.39
C3	27.60	10.66	29.39	0.00

- Assume that an ant has followed the following route:[0,2,1,3,] and back to source

- Calculate the total cost of the above route.
- Calculate the ant's switching probabilities for the first 3 steps in the above route assuming pheromone exponent parameter $\alpha=0.22$ and heuristic exponent parameter $\beta=0.41$.
- Calculate the updated pheromone amounts after applying the ACO evaporation step assuming $\rho=0.63$.
- Calculate the updated pheromone amounts after applying the ACO depositing step assuming $Q=22.21$.

Answer

- The cost of the aforementioned route:189.00
- At node 0 the ant has 2 choices:From C0 to C2 the heuristic value is 0.01 and its pheromone value is 36.33 hence P=0.38
From C0 to C3 the heuristic value is 0.05 and its pheromone value is 27.60 hence P=0.62
- At node 2 the ant has 2 choices:From C2 to C3 the heuristic value is 0.02 and its pheromone value is 29.39 hence P=0.48
From C2 to C1 the heuristic value is 0.02 and its pheromone value is 26.49 hence P=0.52
- At node 1 the ant has 1 choices:From C1 to C3 the heuristic value is 0.03 and its pheromone value is 10.66 hence P=1.00
- The pheromone matrix will evaporate according to the rule:pheromone=(1- ρ)pheromone

	C0	C1	C2	C3
C0	0.00	0.00	13.44	10.21
C1	0.00	0.00	9.80	3.94
C2	13.44	9.80	0.00	10.87
C3	10.21	3.94	10.87	0.00

The route links pheromone will be enhanced by $\Delta=Q/L$ (where L is the path cost)

$\Delta=0.12$

The updated Pheromone matrix:

	C0	C1	C2	C3
C0	0.00	0.00	13.56	10.21
C1	0.00	0.00	9.80	4.06
C2	13.44	9.92	0.00	10.87
C3	10.33	3.94	10.87	0.00

Question 15

Having the following routing table at node 5

	N91	N68	N38	N62	N24
N55	0.18	0.37	0.06	0.20	0.45
N93	0.24	0.12	0.46	0.35	0.34
N80	0.00	0.50	0.47	0.10	0.00
N27	0.58	0.01	0.01	0.34	0.21

Having started at node 62 and reaching node 5 via node 93.Assuming it has been in the network for 0.839863 time units, what effect will it have on the routing table on node 5

assume a and b equals 0.030000 and 0.080000 in order for ABC model

$$\delta r = a/T + b$$

$$\delta r = 0.115720$$

$$r_{2_4} = (r_{2_4} + \delta r) / (1 + \delta r)$$

$$= 0.421434$$

The remaining cells in the source column will be updated by $rks/(1+\delta r)$

The updated table will be:

	N91	N68	N38	N62	N24
N55	0.18	0.37	0.06	0.18	0.45
N93	0.24	0.12	0.46	0.42	0.34
N80	0.00	0.50	0.47	0.09	0.00
N27	0.58	0.01	0.01	0.31	0.21

Question 16

At a given point of time and given an ant, the ant found 3 possible routes at its journey. The pheromone amounts on each route are :

5.000000 8.000000 7.000000

If the length of each route which is inversely proportional to the route desirability is known to the ant and lengths are :

10.000000 31.000000 25.000000

Calculate the probability of selecting each route by that given ant

Assume Alpha=0.5 and beta= 0.6

Answer

eta=1/d

eta1=0.100000

eta2=0.032258

eta3=0.040000

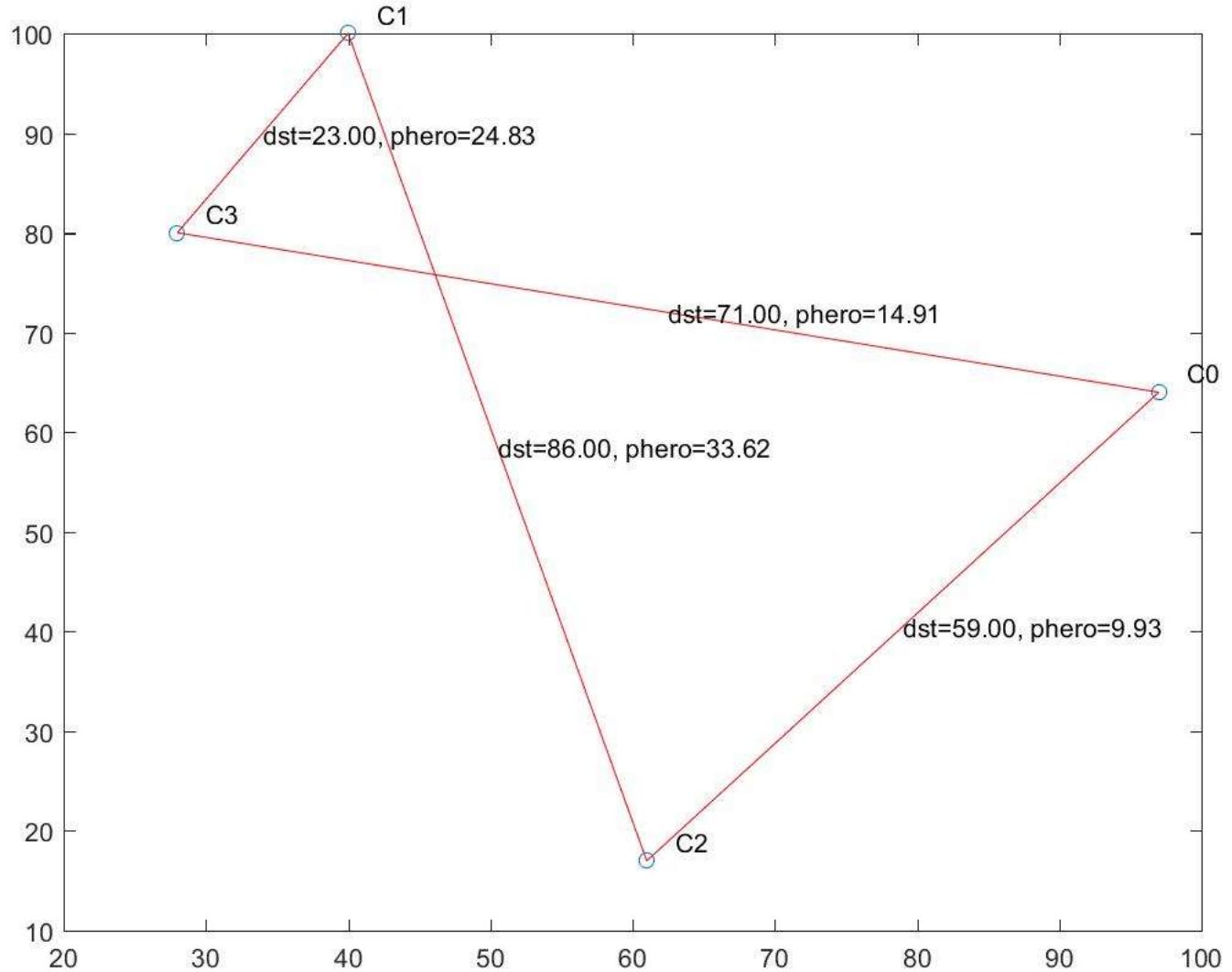
P-1=0.430223

P-2=0.276017

P-3=0.293760

Question 17

In a TSP problem with 4 cities, cities are connected as shown in the figure:



the following table shows the distances between different cities

	C0	C1	C2	C3
C0	0.00	67.00	59.00	71.00
C1	67.00	0.00	86.00	23.00
C2	59.00	86.00	0.00	71.00

C3	71.00	23.00	71.00	0.00
----	-------	-------	-------	------

[Distance of 0 means distance is not applicable.

]The following table shows the pheromone in units between different cities

	C0	C1	C2	C3
C0	0.00	0.00	9.93	14.91
C1	0.00	0.00	33.62	24.83
C2	9.93	33.62	0.00	0.00
C3	14.91	24.83	0.00	0.00

- Assume that an ant has followed the following route:[1,2,0,3,] and back to source

- Calculate the total cost of the above route.
- Calculate the ant's switching probabilities for the first 3 steps in the above route assuming pheromone exponent parameter $\alpha=0.41$ and heuristic exponent parameter $\beta=0.01$.
- Calculate the updated pheromone amounts after applying the ACO evaporation step assuming $\rho=0.70$.
- Calculate the updated pheromone amounts after applying the ACO depositing step assuming $Q=20.27$.

Answer

- The cost of the aforementioned route:239.00
- At node 1 the ant has 2 choices:From C1 to C2 the heuristic value is 0.01 and its pheromone value is 33.62 hence $P=0.53$
From C1 to C3 the heuristic value is 0.04 and its pheromone value is 24.83 hence $P=0.47$
- At node 2 the ant has 1 choices:From C2 to C0 the heuristic value is 0.02 and its pheromone value is 9.93 hence $P=1.00$
- At node 0 the ant has 1 choices:From C0 to C3 the heuristic value is 0.01 and its pheromone value is 14.91 hence $P=1.00$
- The pheromone matrix will evaporate according to the rule:pheromone=(1-p)pheromone

	C0	C1	C2	C3
C0	0.00	0.00	2.98	4.47
C1	0.00	0.00	10.09	7.45
C2	2.98	10.09	0.00	0.00
C3	4.47	7.45	0.00	0.00

The route links pheromone will be enhanced by $\Delta=Q/L$ (where L is the path cost)

$\Delta=0.08$

The updated Pheromone matrix:

	C0	C1	C2	C3
C0	0.00	0.00	2.98	4.56
C1	0.00	0.00	10.17	7.45
C2	3.06	10.09	0.00	0.00
C3	4.47	7.53	0.00	0.00

Question 18

Having the following routing table at node 5

	N69	N14	N51	N70	N90
N97	0.37	0.14	0.17	0.20	0.05
N71	0.06	0.56	0.35	0.20	0.65
N38	0.35	0.27	0.07	0.13	0.11
N23	0.23	0.04	0.41	0.47	0.20

Having started at node 51 and reaching node 5 via node 97.Assuming it has been in the network for 6.629329 time units, what effect will it have on the routing table on node 5

assume a and b equals 0.080000 and 0.080000 in order for ABC model

$$\delta r = a/T + b$$

$$\delta r = 0.092068$$

$$r_{1_3} = (r_{1_3} + \delta r) / (1 + \delta r)$$

$$= 0.238480$$

The remaining cells in the source column will be updated by $rks/(1+\delta r)$

The updated table will be:

	N69	N14	N51	N70	N90
N97	0.37	0.14	0.24	0.20	0.05
N71	0.06	0.56	0.32	0.20	0.65
N38	0.35	0.27	0.07	0.13	0.11
N23	0.23	0.04	0.37	0.47	0.20

Question 19

At a given point of time and given an ant, the ant found 4 possible routes at its journey. The pheromone amounts on each route are :

3.000000 7.000000 10.000000 8.000000

If the length of each route which is inversely proportional to the route desirability is known to the ant and lengths are :

58.000000 49.000000 42.000000 53.000000

Calculate the probability of selecting each route by that given ant

Assume Alpha=0.5 and beta= 0.9

Answer

$\eta_1=1/d$

$\eta_{11}=0.017241$

$\eta_{12}=0.020408$

$\eta_{13}=0.023810$

$\eta_{14}=0.018868$

$P_{11}=0.143060$

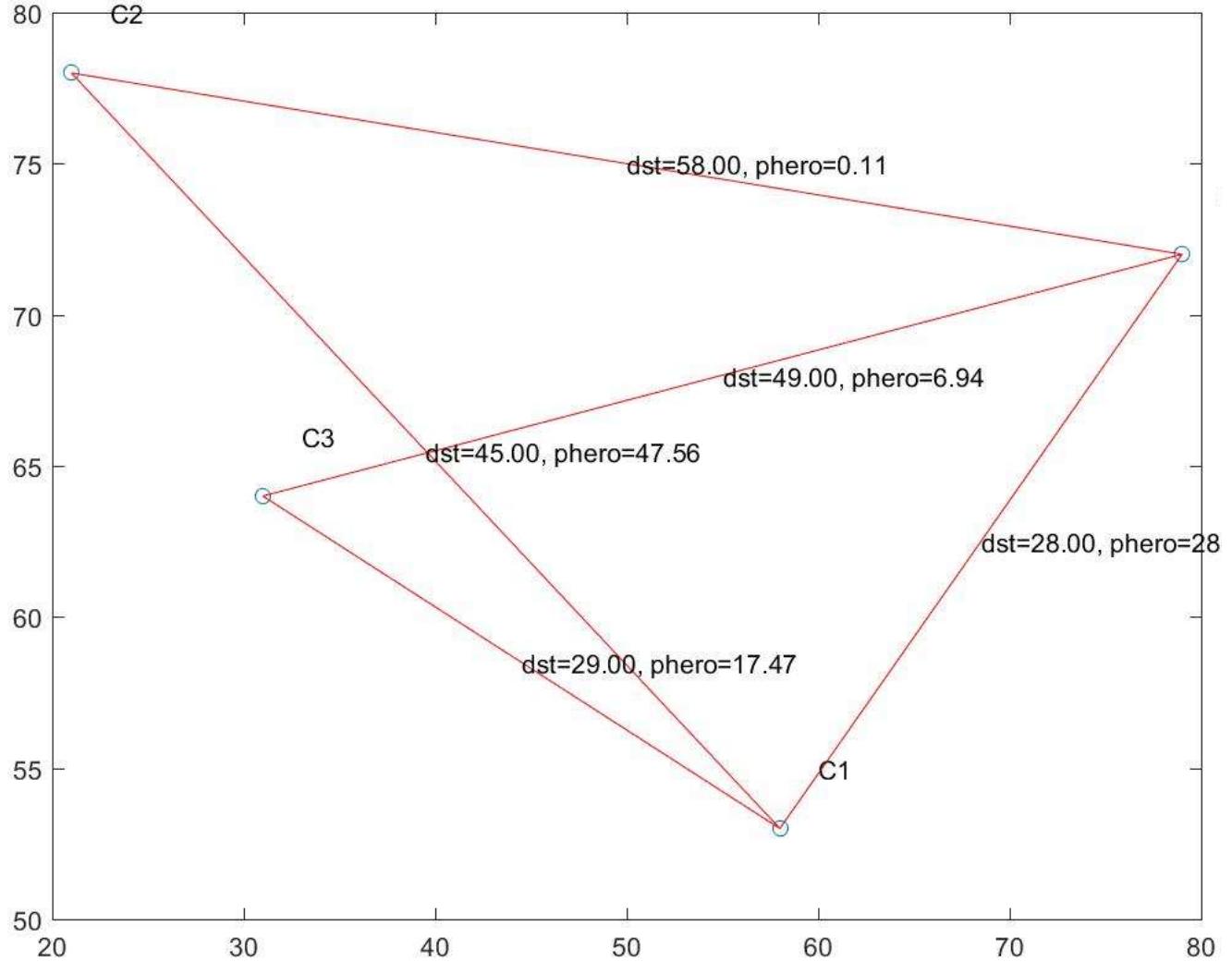
$P_{12}=0.254341$

$P_{13}=0.349237$

$P_{14}=0.253362$

Question 20

In a TSP problem with 4 cities, cities are connected as shown in the figure:



the following table shows the distances between different cities

	C0	C1	C2	C3
C0	0.00	28.00	58.00	49.00
C1	28.00	0.00	45.00	29.00
C2	58.00	45.00	0.00	17.00
C3	49.00	29.00	17.00	0.00

[Distance of 0 means distance is not applicable.

[The following table shows the pheromone in units between different cities

	C0	C1	C2	C3
C0	0.00	28.25	0.11	6.94
C1	28.25	0.00	47.56	17.47
C2	0.11	47.56	0.00	0.00
C3	6.94	17.47	0.00	0.00

- Assume that an ant has followed the following route:[3,0,2,1,] and back to source

- Calculate the total cost of the above route.
- Calculate the ant's switching probabilities for the first 3 steps in the above route assuming pheromone exponent parameter $\alpha=0.64$ and heuristic exponent parameter $\beta=0.73$.
- Calculate the updated pheromone amounts after applying the ACO evaporation step assuming $p=0.86$.
- Calculate the updated pheromone amounts after applying the ACO depositing step assuming $Q=25.08$.

Answer

a. The cost of the aforementioned route:181.00

b. At node 3 the ant has 2 choices:From C3 to C0 the heuristic value is 0.02 and its pheromone value is 6.94 hence $P=0.27$

From C3 to C1 the heuristic value is 0.03 and its pheromone value is 17.47 hence $P=0.73$

At node 0 the ant has 2 choices:From C0 to C1 the heuristic value is 0.04 and its pheromone value is 28.25 hence $P=0.98$

From C0 to C2 the heuristic value is 0.02 and its pheromone value is 0.11 hence $P=0.02$

At node 2 the ant has 1 choices:From C2 to C1 the heuristic value is 0.02 and its pheromone value is 47.56 hence $P=1.00$

c. The pheromone matrix will evaporate according to the rule:pheromone=(1-p)pheromone

	C0	C1	C2	C3
C0	0.00	3.96	0.02	0.97
C1	3.96	0.00	6.66	2.45
C2	0.02	6.66	0.00	0.00
C3	0.97	2.45	0.00	0.00

The route links pheromone will be enhanced by $\Delta=Q/L$ (where L is the path cost)

$\Delta=0.14$

The updated Pheromone matrix:

	C0	C1	C2	C3
C0	0.00	3.96	0.15	0.97
C1	3.96	0.00	6.66	2.58
C2	0.02	6.80	0.00	0.00
C3	1.11	2.45	0.00	0.00

Question 21

Having the following routing table at node 5

	N96	N2	N94	N3	N98
N29	0.10	0.05	0.35	0.09	0.26
N50	0.31	0.23	0.23	0.39	0.24
N81	0.09	0.39	0.10	0.38	0.21
N83	0.50	0.32	0.31	0.14	0.29

Having started at node 96 and reaching node 5 via node 81.Assuming it has been in the network for 9.757071 time units, what effect will it have on the routing table on node 5

assume a and b equals 0.010000 and 0.020000 in order for ABC model

$$\delta r=a/T+b$$

$$\delta r=0.021025$$

$$r_{3_1}=(r_{3_1}+\delta r)/(1+\delta r)$$

$$=0.108443$$

The remaining cells in the source column will be updated by $rks/(1+\delta r)$

The updated table will be:

	N96	N2	N94	N3	N98
N29	0.10	0.05	0.35	0.09	0.26
N50	0.31	0.23	0.23	0.39	0.24
N81	0.11	0.39	0.10	0.38	0.21
N83	0.49	0.32	0.31	0.14	0.29

Question 22

At a given point of time and given an ant, the ant found 5 possible routes at its journey. The pheromone amounts on each route are :

0.000000 1.000000 5.000000 8.000000 10.000000

If the length of each route which is inversely proportional to the route desirability is known to the ant and lengths are :

0.000000 38.000000 60.000000 64.000000 59.000000

Calculate the probability of selecting each route by that given ant

Assume Alpha=0.9 and beta= 0.7

Answer

eta=1/d

eta1=Inf

eta2=0.026316

eta3=0.016667

eta4=0.015625

eta5=0.016949

P-1=NaN

P-2=NaN

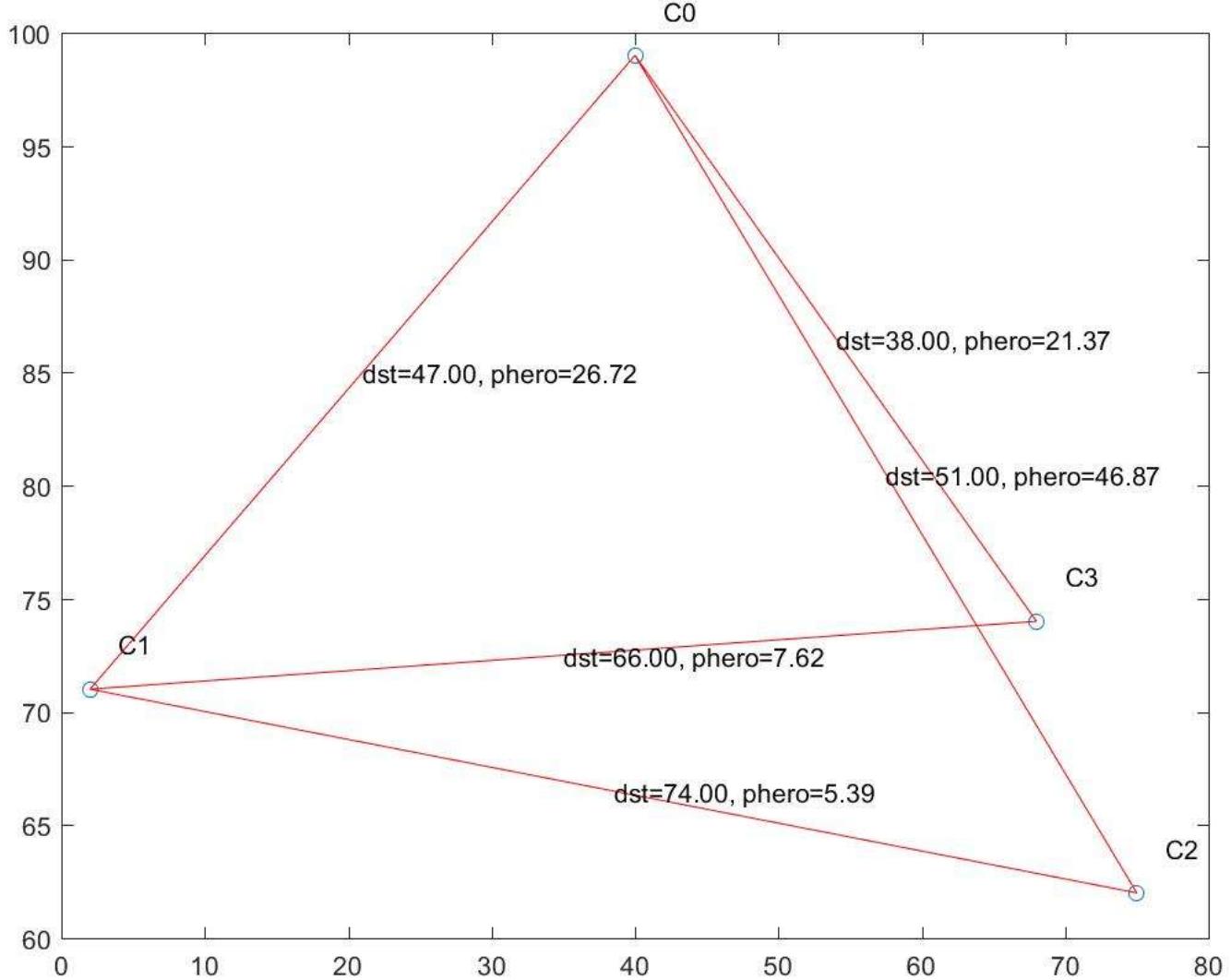
P-3=NaN

P-4=NaN

P-5=NaN

Question 23

In a TSP problem with 4 cities, cities are connected as shown in the figure:



the following table shows the distances between different cities

	C0	C1	C2	C3
C0	0.00	47.00	51.00	38.00
C1	47.00	0.00	74.00	66.00
C2	51.00	74.00	0.00	38.00
C3	38.00	66.00	38.00	0.00

C2	51.00	74.00	0.00	14.00
C3	38.00	66.00	14.00	0.00

[Distance of 0 means distance is not applicable.

]The following table shows the pheromone in units between different cities

	C0	C1	C2	C3
C0	0.00	26.72	46.87	21.37
C1	26.72	0.00	5.39	7.62
C2	46.87	5.39	0.00	0.00
C3	21.37	7.62	0.00	0.00

- Assume that an ant has followed the following route:[2,0,3,1,] and back to source
 - Calculate the total cost of the above route.
 - Calculate the ant's switching probabilities for the first 2 steps in the above route assuming pheromone exponent parameter $\alpha=0.88$ and heuristic exponent parameter $\beta=0.73$.
 - Calculate the updated pheromone amounts after applying the ACO evaporation step assuming $\rho=0.41$.
 - Calculate the updated pheromone amounts after applying the ACO depositing step assuming $Q=24.17$.

Answer

- The cost of the aforementioned route:229.00
- At node 2 the ant has 2 choices:From C2 to C0 the heuristic value is 0.02 and its pheromone value is 46.87 hence P=0.90
From C2 to C1 the heuristic value is 0.01 and its pheromone value is 5.39 hence P=0.10
- At node 0 the ant has 2 choices:From C0 to C1 the heuristic value is 0.02 and its pheromone value is 26.72 hence P=0.51
From C0 to C3 the heuristic value is 0.03 and its pheromone value is 21.37 hence P=0.49
- The pheromone matrix will evaporate according to the rule:pheromone=(1-p)pheromone

	C0	C1	C2	C3
C0	0.00	15.76	27.65	12.61
C1	15.76	0.00	3.18	4.50
C2	27.65	3.18	0.00	0.00
C3	12.61	4.50	0.00	0.00

The route links pheromone will be enhanced by $\Delta=Q/L$ (where L is the path cost)

$\Delta=0.11$

The updated Pheromone matrix:

	C0	C1	C2	C3
C0	0.00	15.76	27.65	12.71
C1	15.76	0.00	3.29	4.50
C2	27.65	3.18	0.00	0.00
C3	12.61	4.60	0.00	0.00

Question 24

Having the following routing table at node 5

	N85	N91	N2	N51	N63
N37	0.41	0.29	0.38	0.31	0.05
N62	0.08	0.48	0.37	0.20	0.44
N71	0.31	0.22	0.14	0.22	0.47
N53	0.20	0.02	0.11	0.27	0.05

Having started at node 51 and reaching node 5 via node 62.Assuming it has been in the network for 4.268350 time units, what effect will it have on the routing table on node 5

assume a and b equals 0.060000 and 0.080000 in order for ABC model

$$\delta r = a/T + b$$

$$\delta r = 0.094057$$

$$r_{2_4} = (r_{2_4} + \delta r) / (1 + \delta r)$$

$$= 0.269649$$

The remaining cells in the source column will be updated by $rks/(1+\delta r)$

The updated table will be:

	N85	N91	N2	N51	N63
N37	0.41	0.29	0.38	0.28	0.05
N62	0.08	0.48	0.37	0.27	0.44
N71	0.31	0.22	0.14	0.20	0.47
N53	0.20	0.02	0.11	0.25	0.05

Question 25

At a given point of time and given an ant, the ant found 4 possible routes at its journey. The pheromone amounts on each route are :

4.000000 6.000000 4.000000 1.000000

If the length of each route which is inversely proportional to the route desirability is known to the ant and lengths are :

52.000000 2.000000 30.000000 3.000000

Calculate the probability of selecting each route by that given ant

Assume Alpha=1.0 and beta= 0.5

Answer

eta=1/d

eta1=0.019231

eta2=0.500000

eta3=0.033333

eta4=0.333333

P-1=0.090860

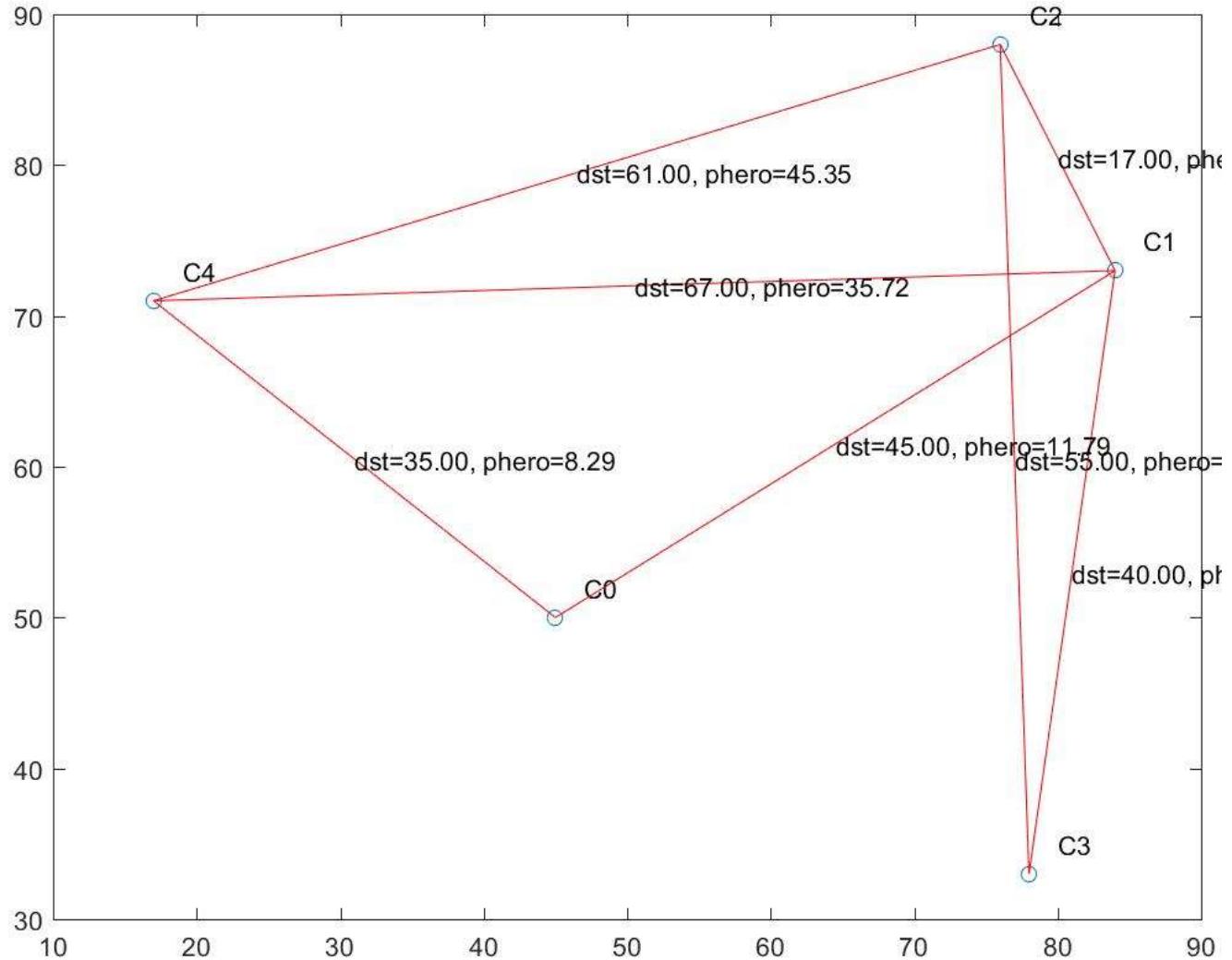
P-2=0.694947

P-3=0.119623

P-4=0.094570

Question 26

In a TSP problem with 5 cities, cities are connected as shown in the figure:



the following table shows the distances between different cities

	C0	C1	C2	C3	C4
C0	0.00	45.00	49.00	37.00	35.00
C1	45.00	0.00	17.00	40.00	67.00

C2	49.00	17.00	0.00	55.00	61.00
C3	37.00	40.00	55.00	0.00	72.00
C4	35.00	67.00	61.00	72.00	0.00

[Distance of 0 means distance is not applicable.

The following table shows the pheromone in units between different cities

	C0	C1	C2	C3	C4
C0	0.00	11.79	0.00	0.00	8.29
C1	11.79	0.00	16.37	8.70	35.72
C2	0.00	16.37	0.00	31.37	45.35
C3	0.00	8.70	31.37	0.00	0.00
C4	8.29	35.72	45.35	0.00	0.00

- Assume that an ant has followed the following route:[1,0,4,2,3,] and back to source

- Calculate the total cost of the above route.
- Calculate the ant's switching probabilities for the first 5 steps in the above route assuming pheromone exponent parameter $\alpha=0.86$ and heuristic exponent parameter $\beta=0.52$.
- Calculate the updated pheromone amounts after applying the ACO evaporation step assuming $\rho=0.48$.
- Calculate the updated pheromone amounts after applying the ACO depositing step assuming $Q=35.60$.

Answer

a. The cost of the aforementioned route:236.00

b. At node 1 the ant has 4 choices:From C1 to C2 the heuristic value is 0.06 and its pheromone value is 16.37 hence $P=0.36$

From C1 to C3 the heuristic value is 0.03 and its pheromone value is 8.70 hence $P=0.13$

From C1 to C0 the heuristic value is 0.02 and its pheromone value is 11.79 hence $P=0.16$

At node 0 the ant has 1 choices:From C0 to C4 the heuristic value is 0.03 and its pheromone value is 8.29 hence $P=1.00$

At node 4 the ant has 2 choices:From C4 to C1 the heuristic value is 0.01 and its pheromone value is 35.72 hence $P=0.44$

From C4 to C2 the heuristic value is 0.02 and its pheromone value is 45.35 hence $P=0.56$

At node 2 the ant has 2 choices:From C2 to C3 the heuristic value is 0.02 and its pheromone value is 31.37 hence $P=0.49$

From C2 to C1 the heuristic value is 0.06 and its pheromone value is 16.37 hence $P=0.51$

At node 3 the ant has 1 choices:From C3 to C1 the heuristic value is 0.03 and its pheromone value is 8.70 hence $P=1.00$

c. The pheromone matrix will evaporate according to the rule:pheromone=(1-p)pheromone

	C0	C1	C2	C3	C4
C0	0.00	6.13	0.00	0.00	4.31
C1	6.13	0.00	8.51	4.52	18.57
C2	0.00	8.51	0.00	16.31	23.58
C3	0.00	4.52	16.31	0.00	0.00
C4	4.31	18.57	23.58	0.00	0.00

The route links pheromone will be enhanced by $\Delta=Q/L$ (where L is the path cost)

$\Delta=0.15$

The updated Pheromone matrix:

	C0	C1	C2	C3	C4
C0	0.00	6.13	0.00	0.00	4.46
C1	6.28	0.00	8.51	4.52	18.57
C2	0.00	8.51	0.00	16.46	23.58
C3	0.00	4.67	16.31	0.00	0.00
C4	4.31	18.57	23.73	0.00	0.00

Question 27

Having the following routing table at node 5

	N14	N71	N46	N11	N68
N18	0.03	0.20	0.36	0.08	0.46
N76	0.26	0.02	0.14	0.22	0.27
N48	0.32	0.12	0.37	0.33	0.14
N51	0.38	0.66	0.12	0.37	0.13

Having started at node 71 and reaching node 5 via node 51.Assuming it has been in the network for 5.710234 time units, what effect will it have on the routing table on node 5

assume a and b equals 0.040000 and 0.070000 in order for ABC model

$$\delta r = a/T + b$$

$$\delta r = 0.077005$$

$$r_{4_2} = (r_{4_2} + \delta r) / (1 + \delta r)$$

=0.687244The remaining cells in the source column will be updated by $rks/(1+\delta r)$

The updated table will be:

	N14	N71	N46	N11	N68
N18	0.03	0.18	0.36	0.08	0.46
N76	0.26	0.02	0.14	0.22	0.27
N48	0.32	0.11	0.37	0.33	0.14
N51	0.38	0.69	0.12	0.37	0.13

Question 28

At a given point of time and given an ant, the ant found 3 possible routes at its journey. The pheromone amounts on each route are :

6.000000 9.000000 4.000000

If the length of each route which is inversely proportional to the route desirability is known to the ant and lengths are :

46.000000 21.000000 43.000000

Calculate the probability of selecting each route by that given ant

Assume Alpha=0.3 and beta= 0.8

Answer

eta=1/d

eta1=0.021739

eta2=0.047619

eta3=0.023256

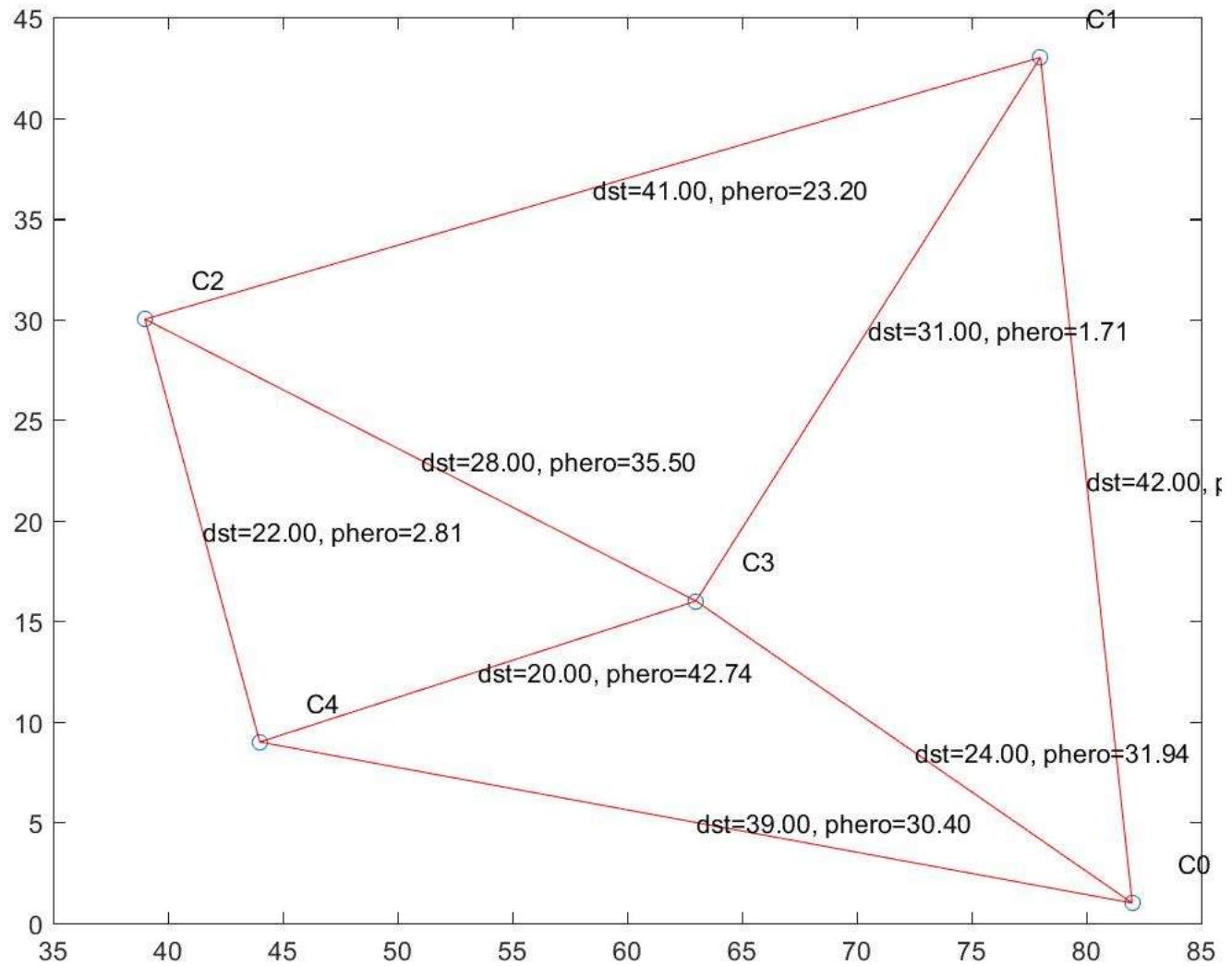
P-1=0.246956

P-2=0.522250

P-3=0.230794

Question 29

In a TSP problem with 5 cities, cities are connected as shown in the figure:



the following table shows the distances between different cities

	C0	C1	C2	C3	C4
C0	0.00	42.00	52.00	24.00	39.00
C1	42.00	0.00	41.00	31.00	48.00
C2	52.00	41.00	0.00	28.00	22.00
C3	24.00	31.00	28.00	0.00	20.00
C4	39.00	48.00	22.00	20.00	0.00

[Distance of 0 means distance is not applicable.

The following table shows the pheromone in units between different cities

	C0	C1	C2	C3	C4
C0	0.00	42.17	0.00	31.94	30.40
C1	42.17	0.00	23.20	1.71	0.00
C2	0.00	23.20	0.00	35.50	2.81
C3	31.94	1.71	35.50	0.00	42.74
C4	30.40	0.00	2.81	42.74	0.00

- Assume that an ant has followed the following route:[1,3,2,4,0,] and back to source

- Calculate the total cost of the above route.
- Calculate the ant's switching probabilities for the first 2 steps in the above route assuming pheromone exponent parameter $\alpha=0.56$ and heuristic exponent parameter $\beta=0.30$.
- Calculate the updated pheromone amounts after applying the ACO evaporation step assuming $\rho=0.37$.
- Calculate the updated pheromone amounts after applying the ACO depositing step assuming $Q=13.96$.

Answer

- a. The cost of the aforementioned route:162.00
 b. At node 1 the ant has 3 choices:From C1 to C2 the heuristic value is 0.02 and its pheromone value is 23.20 hence P=0.38
 From C1 to C3 the heuristic value is 0.03 and its pheromone value is 1.71 hence P=0.10
 From C1 to C0 the heuristic value is 0.02 and its pheromone value is 42.17 hence P=0.53
 At node 3 the ant has 3 choices:From C3 to C4 the heuristic value is 0.05 and its pheromone value is 42.74 hence P=0.38
 From C3 to C0 the heuristic value is 0.04 and its pheromone value is 31.94 hence P=0.31
 From C3 to C2 the heuristic value is 0.04 and its pheromone value is 35.50 hence P=0.31
 c. The pheromone matrix will evaporate according to the rule:pheromone=(1-p)pheromone

	C0	C1	C2	C3	C4
C0	0.00	26.57	0.00	20.12	19.15
C1	26.57	0.00	14.62	1.08	0.00
C2	0.00	14.62	0.00	22.36	1.77
C3	20.12	1.08	22.36	0.00	26.93
C4	19.15	0.00	1.77	26.93	0.00

The route links pheromone will be enhanced by $\Delta=Q/L$ (where L is the path cost)

$\Delta=0.09$

The updated Pheromone matrix:

	C0	C1	C2	C3	C4
C0	0.00	26.65	0.00	20.12	19.15
C1	26.57	0.00	14.62	1.16	0.00
C2	0.00	14.62	0.00	22.36	1.86
C3	20.12	1.08	22.45	0.00	26.93
C4	19.24	0.00	1.77	26.93	0.00

Question 30

Having the following rouing table at node 5

	N34	N43	N71	N89	N86
N13	0.20	0.20	0.30	0.20	0.36
N12	0.21	0.11	0.51	0.27	0.16
N84	0.31	0.52	0.05	0.42	0.29
N61	0.29	0.16	0.14	0.10	0.19

Having started at node 34 and reaching node 5 via node 84.Assuming it has been in the network for 3.857285 time units, what effect will it have on the routing table on node 5

assume a and b equals 0.030000 and 0.030000 in order for ABC model

$$\delta r = a/T + b$$

$$\delta r = 0.037777$$

$$r_{3_1} = (r_{3_1} + \delta r) / (1 + \delta r)$$

$$= 0.332269$$

The remaining cells in the source column will be updated by $rks/(1+\delta r)$

The updated table will be:

	N34	N43	N71	N89	N86
N13	0.19	0.20	0.30	0.20	0.36
N12	0.20	0.11	0.51	0.27	0.16
N84	0.33	0.52	0.05	0.42	0.29
N61	0.28	0.16	0.14	0.10	0.19