

# **Part X.**

# **Optimization and Code Generation**

## Basic Blocks

- A *basic block* is a sequence of statements executed sequentially from beginning to end
  - A *leader* is the first statement of a basic block
- 

**Determine the set of leaders as follows:**

- The first statement is a **leader**
- Any statement that is the label of a goto statement is a **leader**
- Any statement that follows a goto statement is a **leader**

# Basic Blocks: Example

```
sum := 0;
```

```
i := 0;
```

```
L1:
```

```
if i >= n goto L2;
```

```
sum := sum + a[i];
```

```
i := i + 1;
```

```
goto L1;
```

```
L2:
```

```
result := sum
```

# Basic Blocks: Example

```
sum := 0;  LEADER  
      (first statement)  
i := 0;
```

```
L1:
```

```
if i >= n goto L2;
```

```
sum := sum + a[i];
```

```
i := i + 1;
```

```
goto L1;
```

```
L2:
```

```
result := sum
```

# Basic Blocks: Example

`sum := 0;`  **LEADER**  
(first statement)  
`i := 0;`

`L1:`  **LEADER**  
(label)  
`if i >= n goto L2;`

`sum := sum + a[i];`

`i := i + 1;`

`goto L1;`

`L2:`

`result := sum`

# Basic Blocks: Example

`sum := 0;`  **LEADER**  
(first statement)  
`i := 0;`

`L1:`  **LEADER**  
(label)  
`if i >= n goto L2;`

`sum := sum + a[i];`  **LEADER**  
(follows a goto statement)  
`i := i + 1;`

`goto L1;`

`L2:`

`result := sum`

# Basic Blocks: Example

**sum := 0;** → LEADER  
(first statement)

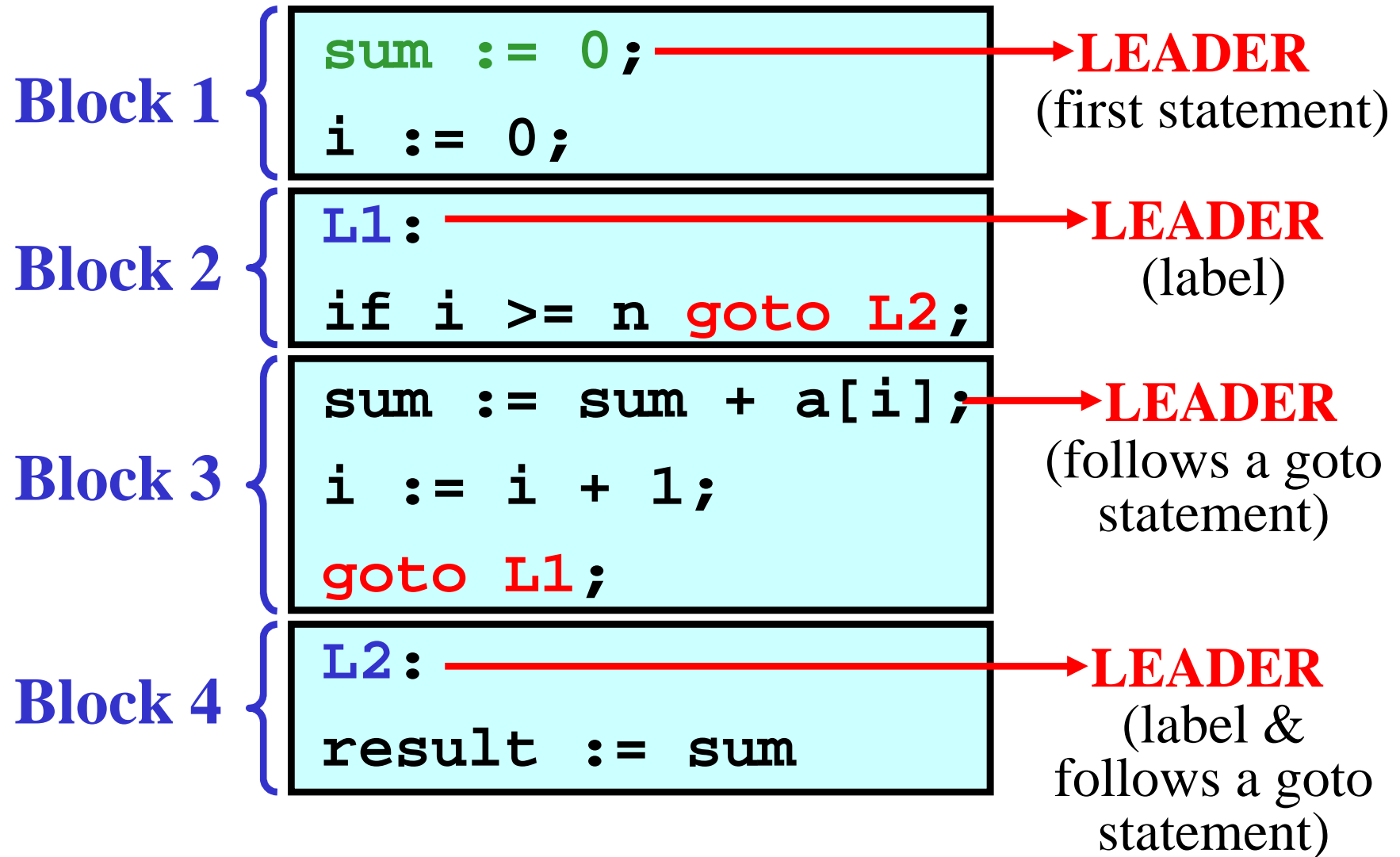
**L1 :**  **LEADER**  
(label)

```
sum := sum + a[i]; → LEADER  
i := i + 1; (follows a goto statement)
```

goto L1;

**L2:**  **LEADER**  
(label & follows a goto statement)

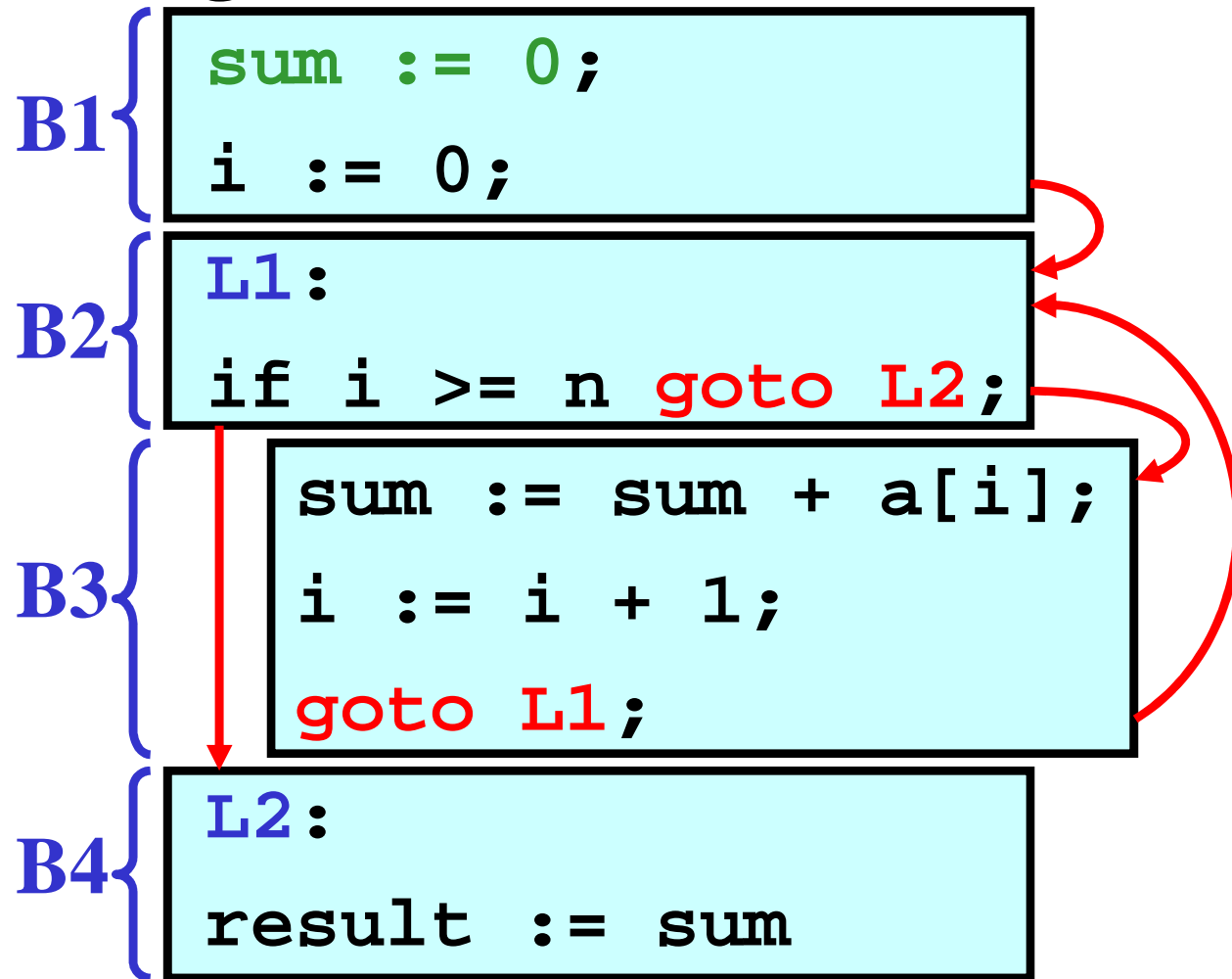
# Basic Blocks: Example



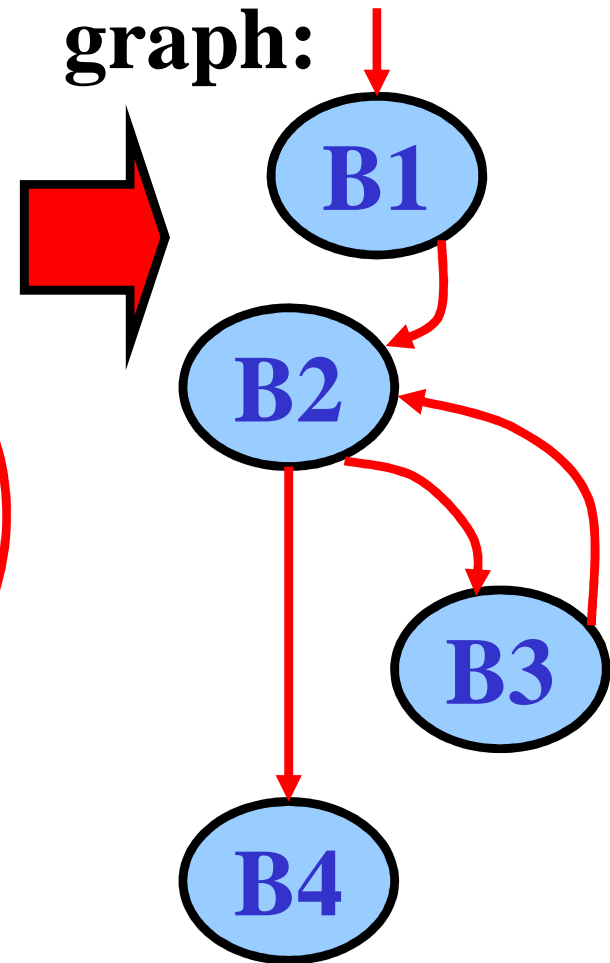


# Flow Graph over Blocks

Program with basic blocks:



Flow control graph:



**Note:** Isolated blocks in a flow graph = **dead code**

# Optimization: Introduction

**Gist:** *Optimizer* makes a more efficient version of the intermediate or target code

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## Variants of optimizations:

### 1) **Local optimization** × **Global optimization**

- **Local optimization** – within a basic block
- **Global optimization** – span several basic blocks

### 2) **Optimization for speed** × **Optimization for size**

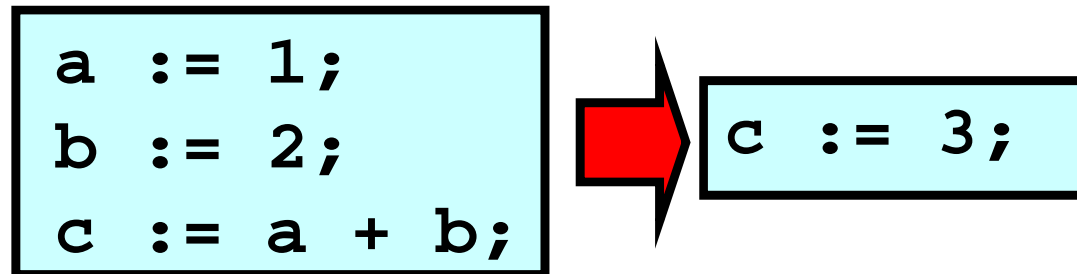
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## Optimization methods:

- |                         |                               |
|-------------------------|-------------------------------|
| 1) Constant folding     | 4) Loop invariant expressions |
| 2) Constant propagation | 5) Loop unrolling             |
| 3) Copy propagation     | 6) Dead code elimination      |

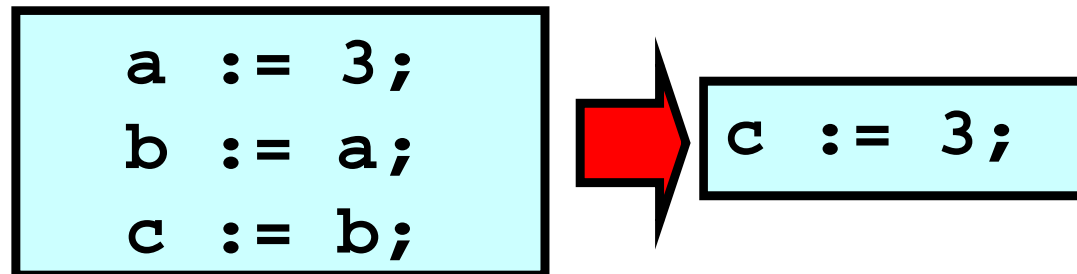
# Optimization Methods 1/3

## 1) Constant folding



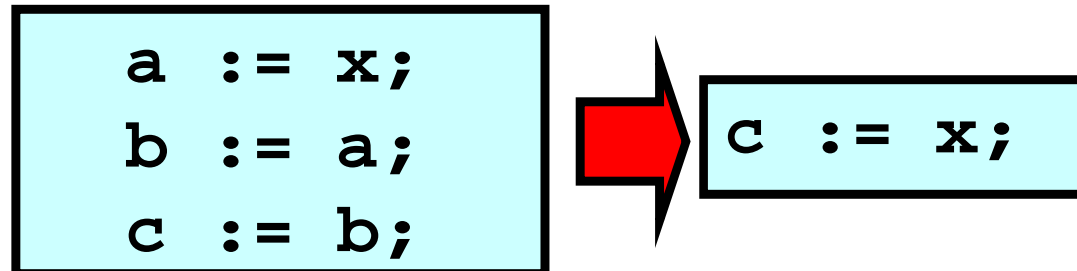
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## 2) Constant propagation



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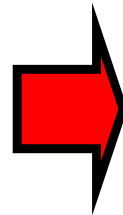
## 3) Copy propagation



## Optimization Methods 2/3

### 4) Loop invariant expressions

```
for i := 1 to 100 do  
  a[i] := p*q/r + i
```

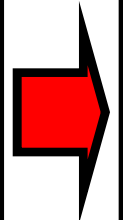


```
x := p*q/r  
for i := 1 to 100 do  
  a[i] := x + i
```

---

### 5) Loop unrolling

```
for i := 1 to 100 do  
begin  
  for j := 1 to 2 do  
    write(x[i, j]);  
end;
```



```
for i := 1 to 100 do  
begin  
  write(x[i, 1]);  
  write(x[i, 2]);  
end;
```

---

# Optimization Methods 3/3

## 6) Dead code elimination

- **Dead code:** a) Never executed  
b) Does nothing useful

ad a)

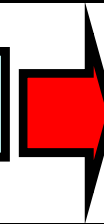
```
trace := false;  
if trace then begin  
    writeln(...);  
    ...  
end;
```



**nothing**

ad b)

```
x := x;
```



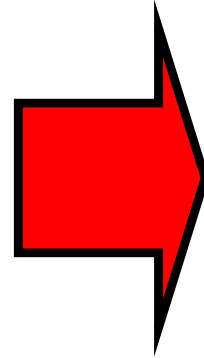
**nothing**

# Optimization For Size

- This optimization only makes a shorter program

## Example:

```
case p of
  1: u := a*b * c;
  2: v := a*b + c;
  3: x := d - a*b;
  4: y := a*b / d;
  5: z := 2 * a*b;
end;
```



```
T := a*b;
case p of
  1: u := T * c;
  2: v := T + c;
  3: x := d - T;
  4: y := T / d;
  5: z := 2 * T;
end;
```

- Note: (a\*b) is very busy.

# Code Generation: Introduction

## Variants of code generations:

- **Blind generation vs. Context-sensitive generation**

### 1) **Blind generation**

- For every 3AC instruction, there is a procedure that generates the corresponding target code

### Main disadvantage:

- As each 3AC instruction is out of the basic block context, a lot of redundant loading and storing occur

### 2) **Context-sensitive generation**

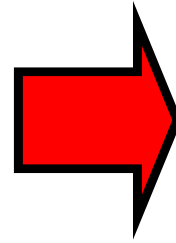
- Reduction of loading and storing between registers and memory.

# Blind Generation: Example

3AC:

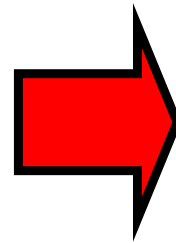
Generated code:

(+ , a , b , r)



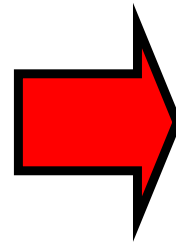
load  $r_i$ , a  
add  $r_i$ , b  
store  $r_i$ , r

(\* , a , b , r)



load  $r_i$ , a  
mul  $r_i$ , b  
store  $r_i$ , r

(:= , a , , r)



load  $r_i$ , a  
store  $r_i$ , r



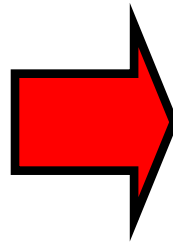
# Blind Generation

**Example:**

3AC:

Generated target code:

( + , a , b , c )  
( \* , c , d , e )



```
load  r1, a
add   r1, b
store r1, c
load  r1, c
mul   r1, d
store r1, e
```

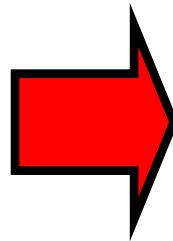
# Blind Generation

**Example:**

3AC:

Generated target code:

( + , a , b , c )  
( \* , c , d , e )



```
load  r1, a
add   r1, b
store r1, c
load  r1, c
mul   r1, d
store r1, e
```

**A redundant instruction**

# Context-Sensitive Generation (CSG)

- Minimization of loading and storing between registers and memory:
  - **General rule:** If a value is in a register and will be used “*soon*”, keep it in the register
- 

## Information needed :

- 1) **Question:** Which variables are needed later in the block and where?

**Answer** is in the *Basic block table* (**BBT**)

- 2) **Q:** Which registers are in use and what they hold?

**A** is in the *Register association table* (**RAT**)

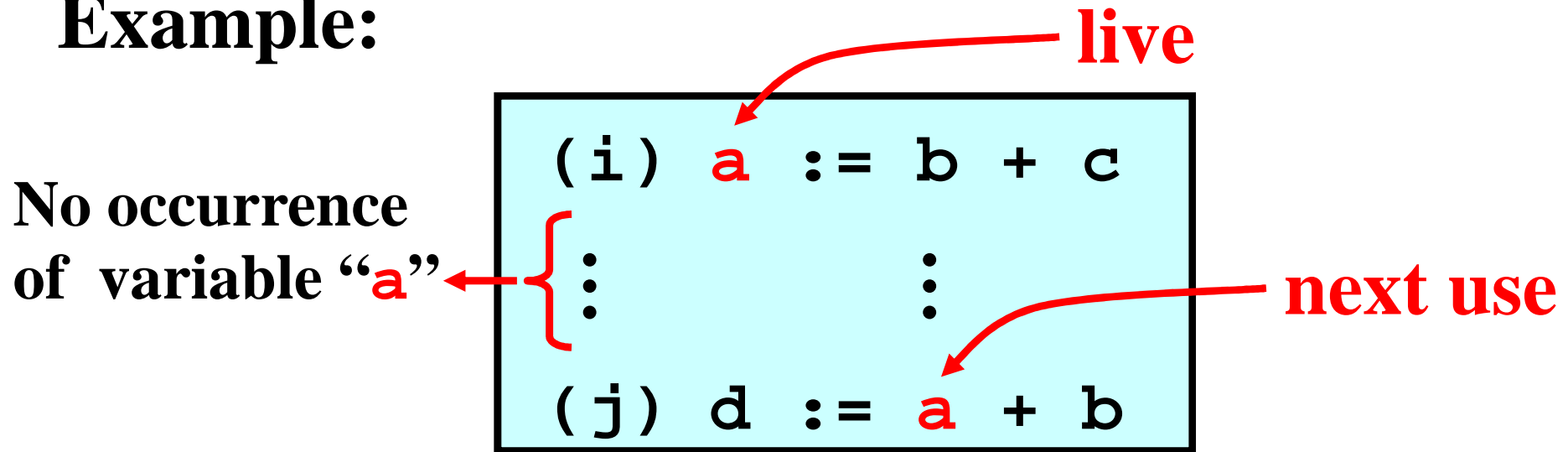
- 3) **Q:** Where the current value of a variable is to be found?

**A** is in the *Address table* (**AT**)

# CSG: Analysis within a Basic Block

- A variable is *live* if it is used later in the block

## Example:



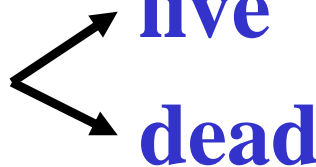
**Question:** How to detect live variables effectively?

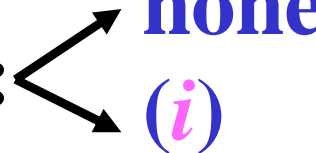
**Answer:** Apply *backward finding*—that is, read the instructions from the block end towards its begin

# Symbol Table (ST)

## Extention of a ST:

<i>variable</i>	<i>status</i>	<i>next use</i>
a	live	(10)
b	live	(20)
pos	dead	none
⋮	⋮	⋮

*Status:*  **live**  
**dead**

*Next use:*  **none**  
**(i)**

• *i* = number of a line


## Initial assumption:

- All programmer variables: *Status:* **live**
- All temporary variables: *Status:* **dead**
- All variables: *Next use:* **none**

# Basic Block Table (BBT)

## Structure of a BBT:

<i>line</i>	<i>instruction</i>	<i>status</i>	<i>next use</i>
⋮	⋮		
( <i>i</i> )	<i>a</i> := <i>b</i> + <i>c</i>		
⋮	⋮		



### • Method:

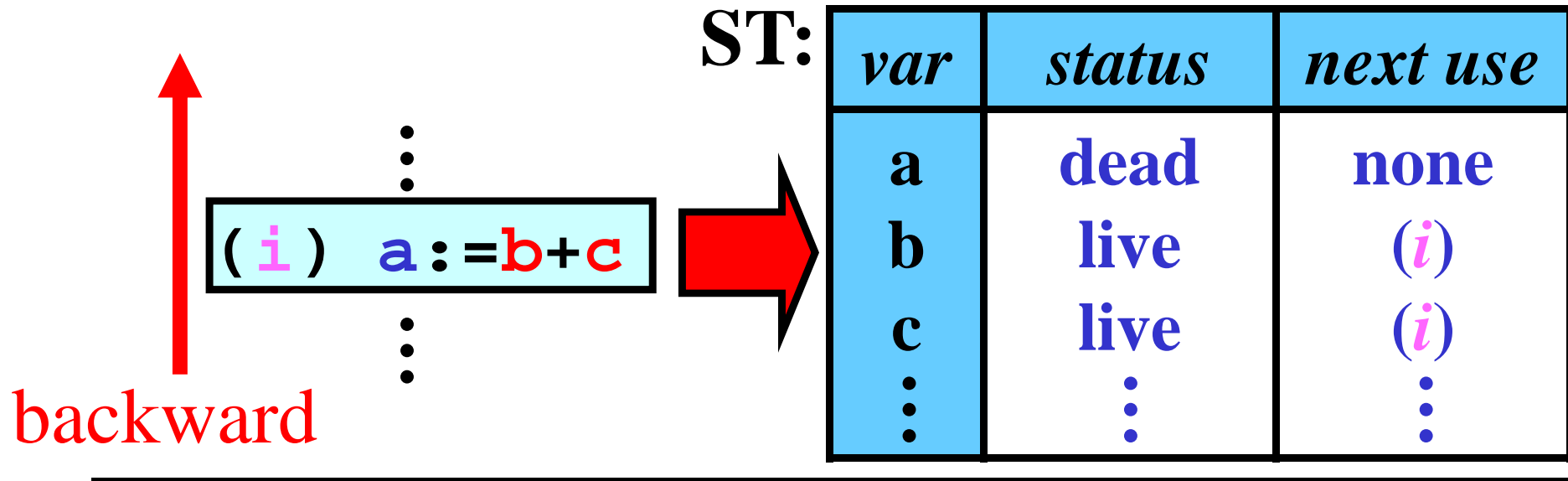
Suppose that (*i*) is the current instruction:

- 1) Move *status* and *next use* of *a*, *b*, *c* from ST to BBT
- 2) In ST make these changes:

For variable *a*:      *Status*: **dead**      *Next use*: **none**

For variables *b*, *c*:      *Status*: **live**      *Next use*: (*i*)

# Changes in a ST: Illustration



*a* is dead because  **$a := b + c$**  kills any **previous** definition of *a*

*b*, *c* are alive and used in (*i*); this information reflects the situation **earlier** in the block

# Filling BBT: Example 1/8

$$d := \underbrace{(a-b)}_u + \underbrace{(c-a)}_v - \underbrace{(d+b)}_x * \underbrace{(c+1)}_y$$

$\underbrace{\hspace{100px}}_w$ 
 $\underbrace{\hspace{100px}}_z$

**BBT:**

<i>line</i>	<i>instruction</i>	<i>status</i>	<i>next use</i>
(1)	<b>u := a - b</b>		
(2)	<b>v := c - a</b>		
(3)	<b>w := u + v</b>		
(4)	<b>x := d + b</b>		
(5)	<b>y := c + 1</b>		
(6)	<b>z := x * y</b>		
(7)	<b>d := w - z</b>		



# Filling BBT: Example 2/8

ST - line (7):

program  
variables

temporary  
variables

<i>var</i>	<i>status</i>	<i>next use</i>
a	L	N
b	L	N
c	L	N
d	L [1]	N [3]
u	D	N
v	D	N
w	D [2]	N [3]
x	D	N
y	D	N
z	D [2]	N [3]

**L – live**

**D – dead**

**N – none**

# Filling BBT: Example 3/8

**BBT:**

<i>line</i>	<i>instruction</i>	<i>status</i>	<i>next use</i>
(1)	$u := a - b$		
(2)	$v := c - a$		
(3)	$w := u + v$		
(4)	$x := d + b$		
(5)	$y := c + 1$		
(6)	$z := x * y$		
(7)	$d := w - z$	$d:L^{[1]}; w,z:D^{[2]}$	$d,w,z:N^{[3]}$

# Filling BBT: Example 4/8

ST - line (6):

<i>var</i>	<i>status</i>	<i>next use</i>
<b>a</b>	<b>L</b>	<b>N</b>
<b>b</b>	<b>L</b>	<b>N</b>
<b>c</b>	<b>L</b>	<b>N</b>
<b>d</b>	<b>D</b>	<b>N</b>
<b>u</b>	<b>D</b>	<b>N</b>
<b>v</b>	<b>D</b>	<b>N</b>
<b>w</b>	<b>L</b>	<b>(7)</b>
<b>x</b>	<b>D</b> [1]	<b>N</b> [3]
<b>y</b>	<b>D</b> [1]	<b>N</b> [3]
<b>z</b>	<b>L</b> [2]	<b>(7)</b> [4]

# Filling BBT: Example 5/8

**BBT:**

<i>line</i>	<i>instruction</i>	<i>status</i>	<i>next use</i>
(1)	$u := a - b$		
(2)	$v := c - a$		
(3)	$w := u + v$		
(4)	$x := d + b$		
(5)	$y := c + 1$		
(6)	$z := x * y$	$z:L^{[2]}; x,y:D^{[1]}$	$z:7^{[4]}; x,y:N^{[3]}$
(7)	$d := w - z$	$d:L; w,z:D$	$d,w,z:N$

# Filling BBT: Example 6/8

ST - line (5):

<i>var</i>	<i>status</i>	<i>next use</i>
<b>a</b>	<b>L</b>	<b>N</b>
<b>b</b>	<b>L</b>	<b>N</b>
<b>c</b>	<b>L</b> <sup>[1]</sup>	<b>N</b> <sup>[2]</sup>
<b>d</b>	<b>D</b>	<b>N</b>
<b>u</b>	<b>D</b>	<b>N</b>
<b>v</b>	<b>D</b>	<b>N</b>
<b>w</b>	<b>L</b>	<b>(7)</b>
<b>x</b>	<b>L</b>	<b>(6)</b>
<b>y</b>	<b>L</b> <sup>[1]</sup>	<b>(6)</b> <sup>[3]</sup>
<b>z</b>	<b>D</b>	<b>N</b>

# Filling BBT: Example 7/8

**BBT:**

<i>line</i>	<i>instruction</i>	<i>status</i>	<i>next use</i>
(1)	$u := a - b$		
(2)	$v := c - a$		
(3)	$w := u + v$		
(4)	$x := d + b$		
(5)	$y := c + 1$	$y, c: L^{[1]}$	$y: 6^{[3]}; c: N^{[2]}$
(6)	$z := x * y$	$z: L; x, y: D$	$z: 7; x, y: N$
(7)	$d := w - z$	$d: L; w, z: D$	$d, w, z: N$

- Fill the rest analogically.

# Filling BBT: Example 8/8

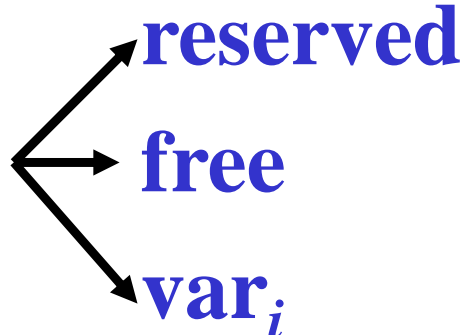
## Final BBT:

<i>line</i>	<i>instruction</i>	<i>status</i>	<i>next use</i>
(1)	<b>u := a - b</b>	u,a,b:L	u:3; a:2; b:4
(2)	<b>v := c - a</b>	v,c,a:L	v:3; c:5; a:N
(3)	<b>w := u + v</b>	w:L; u,v:D	w:7; u,v:N
(4)	<b>x := d + b</b>	x,b:L; d:D	x:6; d,b:N
(5)	<b>y := c + 1</b>	y,c:L	y:6; c:N
(6)	<b>z := x * y</b>	z:L; x,y:D	z:7; x,y:N
(7)	<b>d := w - z</b>	d:L; w,z:D	d,w,z:N

# Register Association Table

## Structure of a RAT:

<i>reg.</i>	<i>contents</i>
0	reserved
1	reserved
2	free
3	a
4	free
5	b
⋮	⋮

*Contents:* 

- **reserved** for some operation system purposes
- **var<sub>i</sub>** = name of variable


- Every use of a register updates RAT.
- RAT indicates the current contents of each register



# Address Table (AT)

## Structure of an AT:

<i>variable</i>	<i>address</i>
a	in memory
b	reg. 5
c	nowhere
⋮	⋮

*Address:* 

- *i* = number of register

- 
- Address table shows where the current value of every variable can be found.

## *GetReg*

- *GetReg* returns an optimal register for **b** in  $a := b + c$
- 

*GetReg*:

begin

if **b** is in register **R** and **b** is dead and  
**b** has no next use then return **R**

else

if there is any free register **R** then return **R**

else begin

- select an occupied register **R**
- save **R**'s current contents
- update RAT & AT
- return **R**

end;

end;

## GenCode

- **GenCode** generate an optimal code for command **a := b + c**
- 

**GenCode:**

**begin**

- Ask **GetReg** for a register **R** for **b**
- **if** **b** is not in **R** **then** generate **load R, b**
- **if** **c** is in reg. **S** **then** generate **add R, S**  
   **else** generate **add R, c**  
   {= c is in memory }
- Update RAT & AT to indicate that current value of **a** is in **R**
- **if** **c** is in **S** **and** **c** is dead **and** has no next use **then** mark **S** as free in RAT

**end;**

# *GetReg* and *GenCode*: Example 1/10

**BBT:**

<i>line</i>	<i>instruction</i>	<i>status</i>	<i>next use</i>
(1)	<b>u := a - b</b>	u,a,b:L	u:3; a:2; b:4
(2)	<b>v := c - a</b>	v,c,a:L	v:3; c:5; a:N
(3)	<b>w := u + v</b>	w:L; u,v:D	w:7; u,v:N
(4)	<b>x := d + b</b>	x,b:L; d:D	x:6; d,b:N
(5)	<b>y := c + 1</b>	y,c:L	y:6; c:N
(6)	<b>z := x * y</b>	z:L; x,y:D	z:7; x,y:N
(7)	<b>d := w - z</b>	d:L; w,z:D	d,w,z:N

**RAT:**

<i>reg.</i>	<i>contents</i>
0,1	reserved
2-11	free
12-15	reserved

**AT:**

<i>var.</i>	<i>address</i>
a-d	in memory
u-z	nowhere

# *GetReg* and *GenCode*: Example 2/10

**Instruction:**        (1)  $u := a - b$

**Properties:**         $u, a, b$ : live

---

*GetReg:*                **R2**

*GenCode:*            **load R2, a**  
                              **sub    R2, b**

---

**RAT:**

<i>reg.</i>	<i>contents</i>
0,1	reserved
2-11	free
12-15	reserved

**AT:**

<i>var.</i>	<i>address</i>
a-d	in memory
u-z	nowhere

# *GetReg* and *GenCode*: Example 3/10

**Instruction:**        ( 2 )  $v := c - a$

**Properties:**         $v, c, a$ : live

*GetReg:*                R3

*GenCode:*            load R3, c  
                              sub R3, a

**RAT:**

<i>reg.</i>	<i>contents</i>
0,1	reserved
2	u
3-11	free
12-15	reserved

**AT:**

<i>var.</i>	<i>address</i>
a-d	in memory
u	2
v-z	nowhere

# *GetReg* and *GenCode*: Example 4/10

**Instruction:**            ( 3 )  $w := u + v$

**Properties:**             $w$ : live;  $u, v$ : dead

---

*GetReg:*                    **R2**

*GenCode:*                **add R2, R3**

---

**RAT:**

<i>reg.</i>	<i>contents</i>
0,1	reserved
2	$u$
3	$v$
4-11	free
12-15	reserved

**AT:**

<i>var.</i>	<i>address</i>
a-d	in memory
$u$	2
$v$	3
w-z	nowhere

# *GetReg* and *GenCode*: Example 5/10

**Instruction:**        ( 4 )  **$x := d + b$**   
**Properties:**         **$x, b$ : live;  $d$ : dead**

---

***GetReg:***                **R3**  
***GenCode:***            **load R3, d**  
                               **add R3, b**

---

**RAT:**

<i>reg.</i>	<i>contents</i>
0,1	reserved
2	w
3-11	free
12-15	reserved

**AT:**

<i>var.</i>	<i>address</i>
a-d	in memory
u, v	nowhere
w	2
x-z	nowhere



# *GetReg* and *GenCode*: Example 6/10

**Instruction:** ( 5 )  $y := c + 1$

**Properties:**  $y, c$ : live

***GetReg:*** R4

***GenCode:*** load R4, c  
add R4, #1

**RAT:**

<i>reg.</i>	<i>contents</i>
0,1	reserved
2	w
3	x
4-11	free
12-15	reserved

**AT:**

<i>var.</i>	<i>address</i>
a-d	in memory
u, v	nowhere
w	2
x	3
y, z	nowhere

# *GetReg* and *GenCode*: Example 7/10

**Instruction:**        ( 6 )    $z := x * y$   
**Properties:**         $z$ : live;  $x, y$ : dead

---

*GetReg:*                **R3**

*GenCode:*            **mul R3, R4**

---

**RAT:**

<i>reg.</i>	<i>contents</i>
0,1	reserved
2	w
3	x
4	y
5-11	free
12-15	reserved

**AT:**

<i>var.</i>	<i>address</i>
a-d	in memory
u, v	nowhere
w	2
x	3
y	4
z	nowhere

# *GetReg* and *GenCode*: Example 8/10

**Instruction:**      ( 7 )    $d := w - z$

**Properties:**         $d$ : live;  $w, z$ : dead

---

*GetReg:*              **R2**

*GenCode:*          **sub R2, R3**

---

**RAT:**

<i>reg.</i>	<i>contents</i>
0,1	reserved
2	w
3	z
4-11	free
12-15	reserved

**AT:**

<i>var.</i>	<i>address</i>
a-d	in memory
u, v	nowhere
w	2
x, y	nowhere
z	3

# *GetReg* and *GenCode*: Example 9/10

**Instruction:** *end of block*

**Properties:** **d: live;**

---

***GetReg:***

-

***GenCode:***

**store R2,d**

**(save all live variables!)**

---

**RAT:**

<i>reg.</i>	<i>contents</i>
0,1	reserved
2	d
3-11	free
12-15	reserved

**AT:**

<i>var.</i>	<i>address</i>
a-c	in memory
d	2
u-z	nowhere

# *GetReg* and *GenCode*: Example 10/10

- **Resulting Code: 12 instructions instead of 21**

<i>Line</i>	<i>3AC</i>	<i>generated code</i>
(1)	$u := a - b$	load R2, a sub R2, b
(2)	$v := c - a$	load R3, c sub R3, a
(3)	$w := u + v$	add R2, R3
(4)	$x := d + b$	load R3, d add R3, b
(5)	$y := c + 1$	load R4, c add R4, #1
(6)	$z := x * y$	mul R3, R4
(7)	$d := w - z$	sub R2, R3 store R2, d

# Parallel Compilers: Introduction

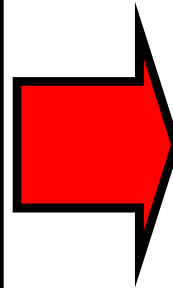
- *Lexical analyzer* translates a **complete** source program into tokens
- 
- **Preparation of the syntax analysis in parallel:**
    - A separation of some substrings of tokens. These substrings and the rest, called the program *skeleton*, are parsed in parallel.
    - In the skeleton, the removed substrings are replaced with *pseudotokens*.

# Parallel Compilers: Separation of Conditions

```

:
:
if cond1 then ...
:
:
while cond2 do ...
:
:
repeat ... until cond3
:
:

```



```

:
:
if [cond, 1] then ...
:
:
while [cond, 2] do ...
:
:
repeat ... until [cond, 3]
:
:

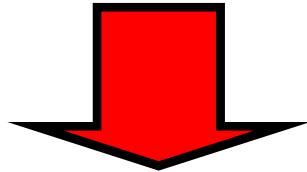
```

• Table of condition:

1	<i>cond</i> <sub>1</sub>
2	<i>cond</i> <sub>2</sub>
3	<i>cond</i> <sub>3</sub>

# Parallel Compilers: Multi-Level Separation

⋮  
 if  $a + b > c * d$  and  $a - b = c + d$  then ...  
 ⋮



⋮  
 if [*cond*, 1] then ...  
 ⋮

- Table of condition:

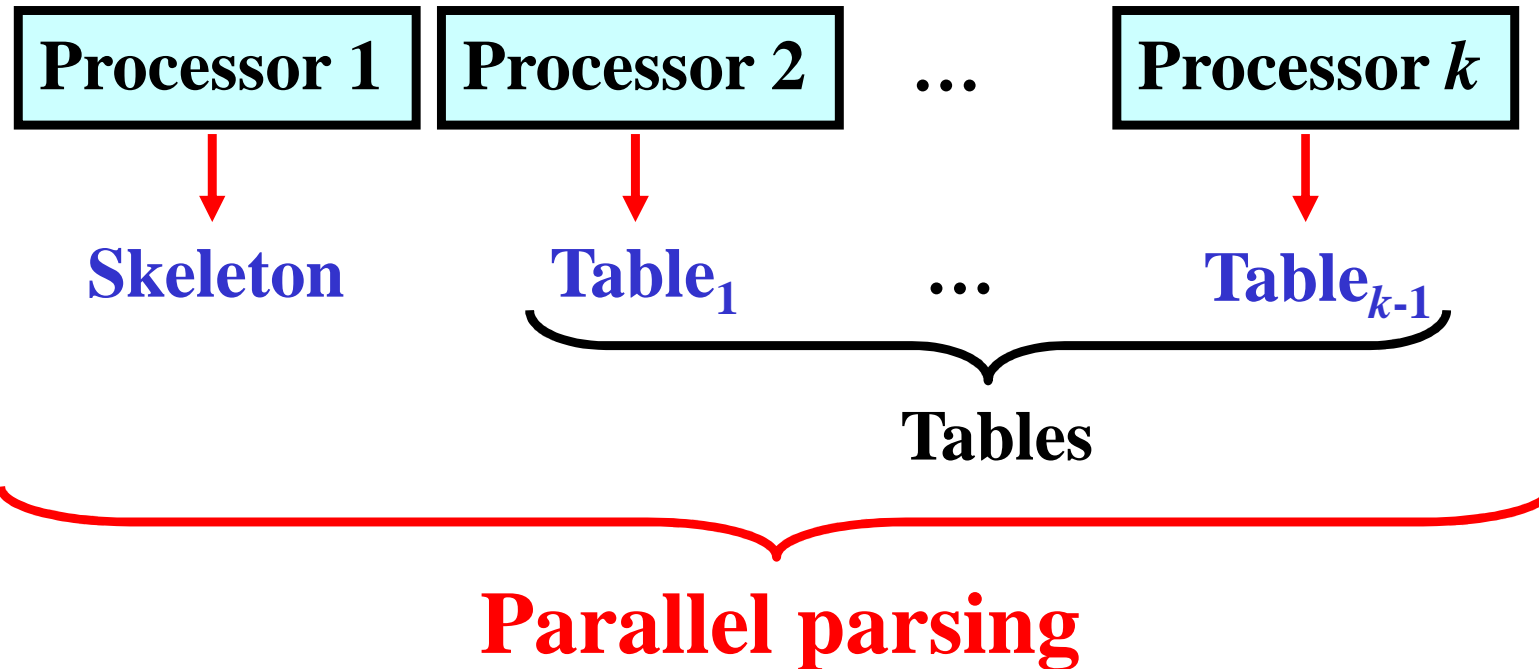
1	$[expr, 1] > [expr, 2]$ and $[expr, 3] = [expr, 4]$
2	...

- Table of expressions:

1	$a + b$
2	$c * d$
3	$a - b$
4	$c + d$



# Parallel Compilers: Parsing



- 
- different methods  $1 - k$
  - different intermediate codes