

1T. 解: for $-\frac{17}{64}$ the binary is -0.010001

as the machine number is 8 bits long (1 bit for sign)

$$\text{so the } [-\frac{17}{64}]_{TF} = 1.0100010$$

$$[-\frac{17}{64}]_{1'} = 1.1011101$$

$$[-\frac{17}{64}]_{2'} = 1.1011110$$

for $\frac{93}{128}$ the binary is $+0.1011101$

$$\text{so the } [\frac{93}{128}]_{TF} = 0.1011101$$

$$[\frac{93}{128}]_{1'} = 0.0100010$$

$$[\frac{93}{128}]_{2'} = 0.0100011$$

for 100 the binary is $+1100100$

$$\text{so the } [100]_{TF} = 0.1100100$$

$$[100]_{1'} = 0.0011011$$

$$[100]_{2'} = 0.0011100$$

for -73 the binary is -1001001

$$\text{so the } [-73]_{TF} = 1.1001001$$

$$[-73]_{1'} = 1.0110110$$

$$[-73]_{2'} = 1.0110111$$

for $-\frac{4}{7}$ the binary is $\frac{4}{7} \times 2 = \frac{8}{7} \rightarrow 1$

$$(\frac{8}{7} - 1) \times 2 = \frac{2}{7} \rightarrow 0$$

$$\frac{2}{7} \times 2 = \frac{4}{7} \rightarrow 0$$

$$\frac{4}{7} \times 2 = \frac{8}{7} \rightarrow 1 \text{ (the same as the first step)}$$

so the binary is -0.1001001

$$\text{Thus the } [-\frac{4}{7}]_{TF} = 1.1001001$$

$$[-\frac{4}{7}]_{1'} = 1.0110110$$

$$[-\frac{4}{7}]_{2'} = 1.0110111$$

2T. 解: from $[x]_{TF}$ to $[x]_{2'}$, we first get the invert, by bit (except sign bit) and add 1 at the end position. Thus from $[x]_{2'}$ to $[x]_{TF}$, we first minus 1 at the end position and then invert by bit (except sign bit)

$$\text{So for } [x_1]_{2'} = 1.1100 \quad [x_1]_{TF} = 1.0100 \quad x_1 = -\frac{1}{4}$$

$$[x_2]_{2'} = 1.1001 \quad [x_2]_{TF} = 1.0111 \quad x_2 = -\frac{7}{16}$$

$$[x_3]_{2'} = 0.1110 \quad [x_3]_{TF} = 0.1110 \quad x_3 = \frac{7}{8}$$

$$[X_4]_S = 1.0000 \quad [X_4]_{TF} \text{ no exist.} \quad X_4 = -1 \quad (\text{no express -1 as a decimal})$$

$$[X_5]_S = 1.0101 \quad [X_5]_{TF} = 1.1011 \quad X_5 = -11$$

$$[X_6]_S = 1.1101 \quad [X_6]_{TF} = 1.0011 \quad X_6 = -3$$

$$[X_7]_S = 0.0111 \quad [X_7]_{TF} = 0.0111 \quad X_7 = 7$$

$$[X_8]_S = 1.0000 \quad [X_8]_{TF} = 1.10000 \quad X_8 = -16$$

(5 bits long if it only has 4 bits may produce loss, 1.0000)

3.7 解: (1) for it is represented by IEEE 754 short in computer

So there are 32 bits would be in FR1

(2) for $x = -8.5$ the binary is -1000.01

for 1000.01 the binary floating point representation is 1.00001×2^1

Thus the exponent is $00000011 + 01111111 = \underbrace{10000010}_8$

the Significand is $\underbrace{000010000000000000000000}_{23}$

So the finally code is

1 10000010 000010000000000000000000

$$4.7. \text{ 解: } (45100000H) = 0100\ 0101\ 0001\ 0000\ 0000\ 0000\ 0000\ 0000$$

So the sign is 0 the exponent is 10001010

the significand is 001000000000000000000000

for the exponent is added 01111111 when calculated

So the exponent should be $10001010 - 01111111 = 00001011$

for the significand omit 1 at the first

So the binary floating point representation is 1.001×2^{1011}

Thus the binary is $+100100000000$

Thus the True value of $45100000H$ is $+2304$

the greatest positive appear when the biased representation is 111111 and the mantissa is 0.0000001

the true form of the biased representation is +111111

the true form of the mantissa is +1111111

Thus the greatest positive is $0.1111111 \times 2^{111111} = (1-2^{-8}) \times 2^{12}$

the minimum positive appear when the biased representation is 0000001 and the mantissa is 0.1111111

the true form of the biased representation is -111111

the true form of the mantissa is 0.00000001

Thus the minimum positive is $0.00000001 \times 2^{-111111} = 2^{-8} \times 2^{-12}$

So the greatest negative is $-2^{-8} \times 2^{-12}$

for. $[a+b]_2 = [a]_2 + [b]_2$

(1) $[a]_{TF} = 1,011$ $[b]_{TF} = 1,100$

Thus $[a]_2 = 1,101$ $[b]_2 = 1,100$

$$\begin{array}{r} \text{So} \quad 1,101 \\ + 1,100 \\ \hline 11,001 \end{array} \leftarrow [a+b]_2 = 1,001$$

Thus there is no overflow

the result in true value is $1,111 = 7$

(2) $[a]_{TF} = 1,0101$ $[b]_{TF} = 0,1010$

Thus $[a]_2 = 1,1011$ $[b]_2 = 0,1010$

$$\begin{array}{r} \text{So} \quad 1,1011 \\ + 0,1010 \\ \hline 10,0101 \end{array} \leftarrow [a+b]_2 = 0,0101$$

Thus there is no overflow

the result in true value is $0,0101 = 5$

(3) $[a]_{TF} = 1,1000$ $[b]_{TF} = 1,1001$

So $[a]_2 = 1,1000$ $[b]_2 = 1,0111$

$$\begin{array}{r} \text{Thus} \quad 1,1000 \\ + 1,0111 \\ \hline 10,1111 \end{array} \leftarrow [a+b]_2 = 0,1111$$

Thus there is an overflow

(4) $[a]_{TF} = 11,01000$ $[b]_{TF} = 11,01001$

$[a]_2 = 11,11000$ $[b]_2 = 11,10111$

$$\begin{array}{r} \text{Thus} \quad 11,11000 \\ + 11,10111 \\ \hline 111,01111 \end{array} \leftarrow [a+b]_2$$

Thus there is no overflow

the result in true value is

$$1,10001 = -1$$