

解: (i) using true form one-bit multiply

$$[x]_{TF} = 0,010011 \quad [y]_{TF} = 0,110011$$

$$\begin{array}{r}
 0,000000 \\
 + 0,010011 \\
 \hline
 0,010011 \\
 0,001001 \\
 + 0,010011 \\
 \hline
 0,011000 \\
 0,001110 \\
 + 0,000000 \\
 \hline
 0,001110 \\
 0,000111 \\
 + 0,000000 \\
 \hline
 0,000111 \\
 0,000011 \\
 + 0,010011 \\
 \hline
 0,010110 \\
 0,001011 \\
 + 0,010011 \\
 \hline
 0,011110 \\
 0,001110 \quad 01001 \\
 \hline
 0,001110 \quad 01001
 \end{array}$$

for  $0 \oplus 0 = 0$

Thus the result is  $0,001111001001$

using form two-bit multiply

$$2x^* = 0,100110 \quad [-x^*]_{TF} = 1,101101$$

$$\begin{array}{r}
 000,000000 \\
 + 111,101101 \\
 \hline
 111,101101 \\
 111,111011 \\
 + 000,010011 \\
 \hline
 ①000,001110 \\
 000,000011 \\
 + 111,101101 \\
 \hline
 111,110000 \\
 111,111100 \\
 + 000,010011 \\
 \hline
 ①000,001111 \quad 001001
 \end{array}$$

for  $0 \oplus 0 = 0$

Thus the result is  $0,001111001001$

using booth's algorithm

$$[x]_2 = 0,010011 \quad [y]_2 = 0,110011 \quad [-x]_2 = 1,101101$$

$$\begin{array}{r}
 00,000000 \\
 + 11,101101 \\
 \hline
 11,101101 \\
 11,110110 \\
 + 00,010011 \\
 \hline
 ①00,001110 \\
 00,000111 \\
 + 11,101101 \\
 \hline
 11,110000 \\
 11,111000 \\
 + 00,010011 \\
 \hline
 ①00,001111 \quad 001001
 \end{array}$$

Thus  $[x \cdot y]_2 = 0,001111001001$

So  $[x \cdot y]_{TF} = 0,001111001001$



1) using true form one-bit multiply

$$[x]_{TF} = 1.010111 \quad [y]_{TF} = 1.011011$$

$$\begin{array}{r}
 0.000000 \quad 011011 \\
 + 0.010111 \quad + [x]_{TF} \\
 \hline
 0.010111 \\
 0.001011 \quad \underline{01101} \\
 + 0.010111 \quad \rightarrow 1, + [x]_{TF} \\
 \hline
 0.100010 \\
 0.010001 \quad \underline{01} 0110 \\
 + 0.000000 \quad \rightarrow 1, + 0 \\
 \hline
 0.010001 \\
 0.001000 \quad \underline{101} 011 \rightarrow 1, + [x]_{TF} \\
 + 0.010111 \\
 \hline
 0.011111 \\
 0.001111 \quad \underline{1101} 01 \rightarrow 1, + [x]_{TF} \\
 + 0.010111 \\
 \hline
 0.100110 \\
 0.010011 \quad \underline{01101} 0 \rightarrow 1, + 0 \\
 + 0.000000 \\
 \hline
 0.010011 \\
 0.001001 \quad 101101 \rightarrow 1
 \end{array}$$

for  $1 \oplus 1 = 0$

$$\text{Thus } [x \cdot y]_{TF} = 0.001001101101$$

using true form two-bit multiply

$$[x^*]_{TF} = 0.010111 \quad [2x^*]_{TF} = 0.101110 \quad [-x^*]_2 = 1.101001$$

$$\begin{array}{r}
 000.000000 \quad 00011011 \quad 0 \\
 + 111.101001 \quad + [-x^*]_2 \\
 \hline
 111.101001 \\
 111.111010 \quad \underline{01} 000110 \quad 1 \rightarrow 2 + [x^*]_2 \\
 + 111.101001 \\
 \hline
 ① 111.100011 \\
 111.111000 \quad \underline{1101} 0001 \quad 1 \rightarrow 2, + 2x^* \\
 + 000.101110 \\
 \hline
 ① 000.100110 \\
 000.001001 \quad \underline{101101} 00 \quad 0 \rightarrow 2 + 0 \\
 + 000.000000 \\
 \hline
 000.001001 \quad 101101
 \end{array}$$

for  $1 \oplus 1 = 0$

$$\text{Thus } [x \cdot y]_{TF} = 0.001001101101$$

using booth's algorithm

$$[x]_2 = 1.101001 \quad [y]_2 = 1.100101 \quad [-x]_2 = 0.010111$$

$$\begin{array}{r}
 00.000000 \quad 11001010 \\
 + 00.010111 \quad + [-x]_2 \\
 \hline
 00.010111 \\
 00.001011 \quad \underline{11} 00101 \rightarrow 1, + [x]_2 \\
 + 11.101001 \\
 \hline
 11.110100 \\
 11.111010 \quad \underline{01} 110010 \rightarrow 1, + [-x]_2 \\
 + 00.010111 \\
 \hline
 ① 00.010001 \\
 00.001000 \quad \underline{101} 11001 \rightarrow 1, + [x]_2 \\
 + 11.101001 \\
 \hline
 11.110001 \\
 11.111000 \quad \underline{1101} 1100 \rightarrow 1, \rightarrow 1 \\
 11.111100 \quad \underline{01101} 110 \quad + [-x]_2 \\
 + 00.010111 \\
 \hline
 ① 00.010011 \\
 00.001001 \quad \underline{101101} 11 \rightarrow 1, + 0 \\
 + 00.000000 \\
 \hline
 00.001001 \quad 101101
 \end{array}$$

for  $1 \oplus 1 = 0$

$$\text{Thus } [x \cdot y]_2 = 0.001001101101$$

$$\text{So } [x \cdot y]_{TF} = 0.001001101101$$



(3) using true form one-bit multiply

$$[x]_{TF} = 0.11011 \quad [y]_{TF} = 1.11101$$

$$\begin{array}{r}
 0.00000 \quad 11101 \\
 + 0.11011 \quad + [x]_{TF} \\
 \hline
 0.11011 \\
 0.01101 \quad \underline{1110} \rightarrow 1, + 0 \\
 + 0.00000 \\
 \hline
 0.01101 \\
 0.00110 \quad \underline{111} \rightarrow 1, + [x]_{TF} \\
 + 0.11011 \\
 \hline
 1.00001 \\
 0.10000 \quad \underline{1111} \rightarrow 1, + [x]_{TF} \\
 + 0.11011 \\
 \hline
 1.01011 \\
 0.10101 \quad \underline{1111} \rightarrow 1, + [x]_{TF} \\
 + 0.11011 \\
 \hline
 1.10000 \\
 0.11000 \quad 01111 \rightarrow 1
 \end{array}$$

for  $0 \oplus 1 = 1$

$$\text{Thus } [x \cdot y]_{TF} = 1.1100001111$$

using true form two-bits multiply

$$x^* = 0.11011 \quad 2x^* = 1.10110 \quad [-x^*]_2 = 1.00101$$

$$\begin{array}{r}
 000.00000 \quad 011101 \quad 0 \\
 + 000.11011 \quad + x^* \\
 \hline
 000.11011 \\
 000.00110 \quad \underline{11} 0111 \quad 0 \rightarrow 2, + [-x^*]_2 \\
 + 111.00101 \\
 \hline
 111.01011 \\
 111.11010 \quad \underline{1111} 01 \quad 1 \rightarrow 2, + 2x^* \\
 + 001:10110 \\
 \hline
 100.110000 \\
 000.1100001111 \rightarrow 1
 \end{array}$$

for  $0 \oplus 1 = 1$

$$\text{Thus } [x \cdot y]_{TF} = 1.1100001111$$

using booth's algorithm

$$[x]_2 = 0.11011 \quad [y]_2 = 1.00011 \quad [-x]_2 = 1.00101$$

$$\begin{array}{r}
 00.00000 \quad 1000110 \\
 + 11.00101 \quad + [-x]_2 \\
 \hline
 11.00101 \\
 11.10010 \quad \underline{100011} \rightarrow 1, \rightarrow 1 \\
 11.11001 \quad \underline{01} 10001 \quad + [x]_2 \\
 + 00.11011 \\
 \hline
 100.10100 \\
 00.01010 \quad \underline{001} 1000 \rightarrow 1, \rightarrow 1 \\
 00.00101 \quad \underline{0001} 100 \rightarrow 1 \\
 00.00010 \quad \underline{10001} 10 \quad + [-x]_2 \\
 + 11.00101 \\
 \hline
 11.00111 \quad 10001
 \end{array}$$

$$\text{Thus } [x \cdot y]_2 = 1.0011110001$$

$$\text{So } [x \cdot y]_{TF} = 1.1100001111$$