How to use package spatcart

Package installation

spatcart may be installed with the following command

```
library(devtools)
devtools::install_github("Servane-Gey/spatcart")
```

or directly from the source file spatcart_1.0.0.tar.gz or the binary file spatcart_1.0.0.tgz.

Load the package, and let's start.

library(spatcart)

Package description

spatcart provides classification trees adapted to spatial bivariate marked point processes by using a splitting criterion associated with the intertype K-function interaction between marks proposed by Ripley. The package also provides heatmap colored partitions induced by tree leaves with respect to interaction between marks.

The full description of the SpatCART algorithm can be found in the article *Spatial Classification Trees*, by A. Bar-Hen, S. Gey and J.-M. Poggi, HAL 01837065 (2018).

Main features

The main features of **spatcart** are presented with respect to the lines followed in the article *Spatial Classification Trees*.

Spatial classification trees

- spatcart constructs the spatial classification trees using Ripley's intertype K-function as impurity function to partition spatial bivariate marked point process, with pruning. Also provides optional graphical results on the obtained partitions. The output values of the function spatcart() are listed in the following objects:
 - max.tree: maximal tree, of class 'tree'.
 - pruned.seq: sequence of subtrees pruned from the maximal one, list of corresponding number of leaves, pruning complexities, and deviance.
 - opt.tree.max: largest optimal tree, selected among the pruned sequence with respect to the modified largest gap slope heuristic (see article). Object of class 'tree'.
 - opt.tree.min: smallest optimal tree, selected among the pruned sequence with respect to the largest plateau slope heuristic (see article). Object of class 'tree'.
 - cp: numeric vector of inside node scale resolutions in maximal tree.
 - K: numeric vector of inside node impurities in maximal tree.

Load the ants data set from package spatstat:

```
library(spatstat)
ypp = ants
ypp
```

```
#> Marked planar point pattern: 97 points
#> Multitype, with levels = Cataglyphis, Messor
#> window: polygonal boundary
#> enclosing rectangle: [-25, 803] x [-49, 717] units (one unit = 0.5 feet)
```

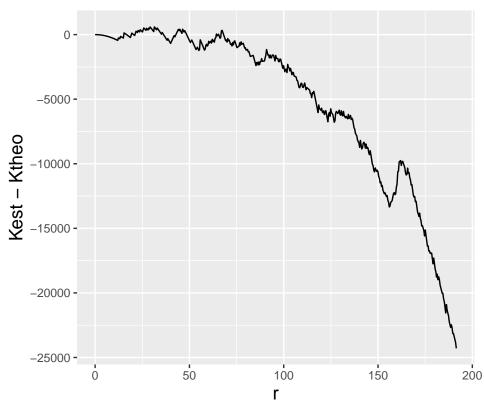
Look at the difference between estimated and theoretical uncorrected intertype K-functions to determine initial scale resolution to put into function spatcart():

```
library(dplyr)
library(ggplot2)
major = names(which.max(intensity(ypp)))
minor = names(which.min(intensity(ypp)))

K0 = Kcross(ypp, major, minor, correction="none")
K01 = tibble(
    scale = K0$r,
    difference = K0$un-K0$theo
)

ggplot(K01, aes(x=scale, y=difference))+geom_line()+xlab("r")+
    ylab("Kest - Ktheo")+
    ggtitle("Difference between estimated and theoretical K")+
    theme(axis.title.x = element_text(size=14))+
    theme(axis.title.y = element_text(size=14))+
    theme(plot.title = element_text(hjust = 0.5, size=14))
```

Difference between estimated and theoretical K

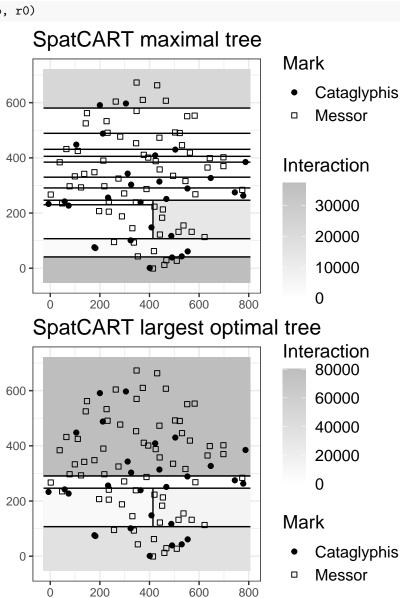


For example, select the value $r\theta$ for initial resolution scale as the local minimum between r=150 and r=170:

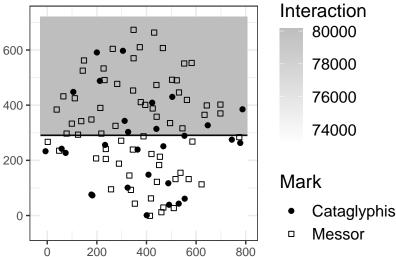
```
zone = which(K0$r>=150 & K0$r<=170)
r1 = K0$r[zone]
r0 = r1[which.min((K0$un-K0$theo)[zone])]
r0
#> [1] 155.9678
```

Apply function spatcart() on the ants data set, with initial resolution $r\theta$:

t = spatcart(ypp, r0)







Here optional parameters are set as default: ties = TRUE, method = "deviance", minsplit = 10, minleaf = 5 and graph = TRUE.

This produces a maximal tree having at least minleaf = 5 points in each leaf, and stopping splitting process if a node contains less than minsplit = 10 points. Let us note that minsplit must be at least equal to 2xminleaf.

ties = TRUE does not optimize on tie splits, and take the lowest value for the corresponding split. To optimize on tie splits using scale adaptation, set as ties = FALSE.

method = "deviance" produces class probability trees using Gini's criterion to prune the maximal tree. To obtain classification trees using misclassification criterion, set method = "misclass".

graph = TRUE produces heatmap colored partitions induced by respectively the maximal, largest optimal and smallest optimal trees' leaves with respect to the interaction between marks.

- spattree constructs the maximal spatial classification tree using Ripley's intertype K-function as impurity function to partition spatial bivariate marked point process. The output values of the function spattree() are listed in the following objects:
 - max.tree: maximal tree, of class 'tree'.
 - cp: numeric vector of inside node scale resolutions in maximal tree.
 - K: numeric vector of inside node impurities in maximal tree.

Construct the maximal spatial classification tree at initial scale resolution $r\theta$ on the ants data set:

```
tmax = spattree(ypp, r0)
```

Here optional parameters are set as default: ties = TRUE, minsplit = 10 and minleaf = 5.

This produces a maximal tree having at least minleaf = 5 points in each leaf, and stopping splitting process if a node contains less than minsplit = 10 points. Let us note that minsplit must be at least equal to 2xminleaf.

ties = TRUE does not optimize on tie splits, and take the lowest value for the corresponding split. To optimize on tie splits using scale adaptation, set as ties = FALSE.

- **spatprune** prunes a tree. The output values of the function spatprune() are listed in the following objects:
 - pruned.seq: sequence of subtrees pruned from the maximal one, list of corresponding number of leaves, pruning complexities, and deviance.
 - opt.tree.max: largest optimal tree, selected among the pruned sequence with respect to the modified largest gap slope heuristic (see article). Object of class 'tree'.

- opt.tree.min: smallest optimal tree, selected among the pruned sequence with respect to the largest plateau slope heuristic (see article). Object of class 'tree'.

Prune the maximal tree to obtain the pruned subtrees sequence, and the largest and smallest optimal trees:

```
seq = spatprune(tmax)
```

Here optional parameters are set as default: method = "deviance" and qraph = TRUE.

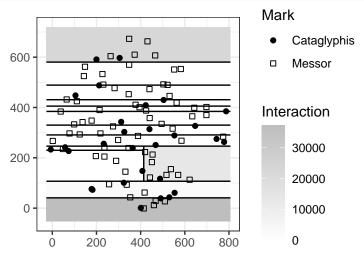
method = "deviance" produces class probability trees using Gini's criterion to prune the maximal tree. To obtain classification trees using misclassification criterion, set method = "misclass".

graph = TRUE produces the graphics of the number of leaves of the pruned subtrees sequence with respect to the complexity parameter used in the pruning algorithm. The triangle symbol represents the tree selected via the modified largest jump method, while the diamond symbol represents the tree selected via the largest plateau method.

• partition.spattree plots the heatmap colored partitions induced by a tree's leaves with respect to the interaction between marks of a spatial bivariate marked point process. The output value of the function partition.spattree() is the corresponding 'ggplot' object. Needs also the input values of impurities inside tree leaves.

Plot the partition induced by the maximal spatial classification tree constructed on the ants data set:

K = tmax\$K[rownames(tmax\$tree\$frame)][tmax\$tree\$frame\$var=="<leaf>"]
partition.spattree(tmax\$tree, ypp, K)



Here the optional parameter d is set as default d = 100. d sets the resolution of the grid used to construct the heatmap at d^2 .

Simulations

The features for simulations of package **spatcart** are presented to cope with the simulation study proposed in R script *Simulation.study.R*, which can be found on the github repository https://github.com/Servane-Gey/Spatial-classification-trees. For more details about simulations, please see the article *Spatial Classification Trees*, by A. Bar-Hen, S. Gey and J.-M. Poggi, HAL 01837065 (2018).

• damier, repulsion respectively simulates the *chess* and *locally repulsive* data sets presented in the article. The optional parameter *model* of the function *damier()* allows to simulate points as uniformly distributed on the unit square if *model* = "unif" (default), or as a Poisson point process on the unit square if *model* = "Poisson".

For both functions damier() and repulsion(),

- the optional margin parameter h = 0.4 (default) defines the mixing proportion of marks inside windows,
- the optional parameter graph = TRUE (default) produces the scatter plot of the resulting simulated points.

Simulate 1000 points from functions damier() and repulsion(), with repulsive scale equal to 0.05 for repulsion():

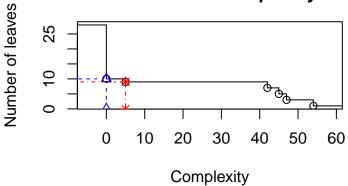
set.seed(12) chess = damier(1000)0.8 9.0 0.4 0.2 0.0 0.0 0.2 0.4 0.6 8.0 1.0 chess = damier(1000, h=0.45,model = "Poisson") 0.8 9.0 0.4 0.2 0.0 0.2 8.0 0.4 0.6 1.0 repuls = repulsion(1000, 0.05) 0.8 9.0 0.4 0.2 0.0 0.2 0.4 0.6 8.0 1.0

• gg.partition.tree plots the partition of a tree involving one or two variables.

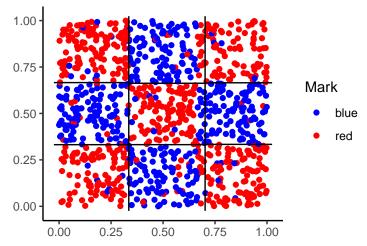
Plot the partition induced by a classical CART classification tree on the chess data set:

```
nuage = data.frame(
    x = chess$data$x1,
    y = chess$data$x2,
    Mark = chess$data$label
    )
library(tree)
tmax = tree(Mark~.,data=nuage,split="gini",model=T, minsize=50,mincut=25)
seq = spatprune(tmax, method = "misclass")
```

Classification trees Nb leaves vs complexity



```
t = seq$opt.tree.min # selects smallest optimal subtree
nuage %>% ggplot(aes(x,y, color = Mark))+geom_point()+
    scale_color_manual(values = c("blue", "red"))+
    gg.partition.tree(t)+
    labs(x = "", y = "")+
    theme_classic()
```



See function partition.tree() of package tree for optional arguments.

Note gg.partition.tree() does not assign tree labels on the partition.

Paracou data set

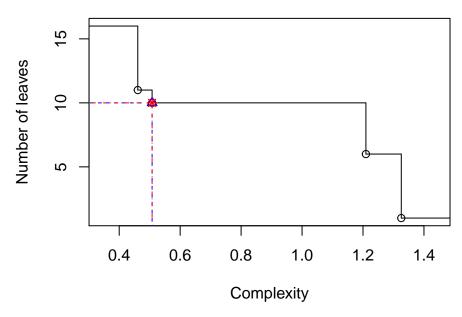
The features for the Paracou data set proposed in package **spatcart** are presented to cope with the experiments done in the article *Spatial Classification Trees*, by A. Bar-Hen, S. Gey and J.-M. Poggi, HAL 01837065 (2018). The original data set can be freely downloaded from https://paracou.cirad.fr/.

- **Paracou** produces graphical results of CART and SpatCART algorithms at fixed initial resolution for the Paracou data set. The output value of the function Paracou() is the following list of 'ggplot' objects:
 - DiffK: graphic of difference between estimated and theoretical intertype K-functions with respect to scale resolution, with a dashed line at the value of initial resolution.
 - SC.maxtree: graphic of the heatmap colored partition induced by the maximal SpatCART classification tree's leaves with respect to the interaction between marks.
 - SC. Classprobtree: graphic of the heatmap colored partition induced by the optimal SpatCART class probability tree's leaves with respect to the interaction between marks.
 - SC. Classtree: graphic of the heatmap colored partition induced by the optimal SpatCART classification tree's leaves with respect to the interaction between marks.
 - C.maxtree: graphic of the partition induced by the maximal CART classification tree's leaves.
 - C.Classprobtree: graphic of the partition induced by the optimal CART class probability tree's leaves.
 - C. Classtree: graphic of the partition induced by the optimal CART classification tree's leaves.

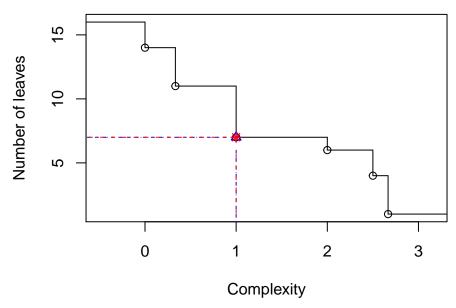
Produce graphics for initial scale resolution $r\theta = 15$:

Paracou(15)

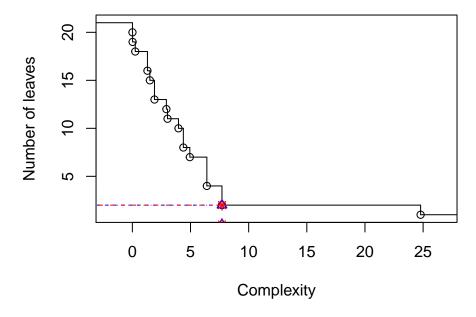
Class probability trees Nb leaves vs complexity



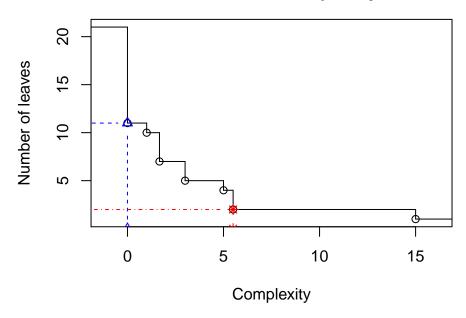
Classification trees Nb leaves vs complexity



CART class probability trees Nb leaves vs complexity

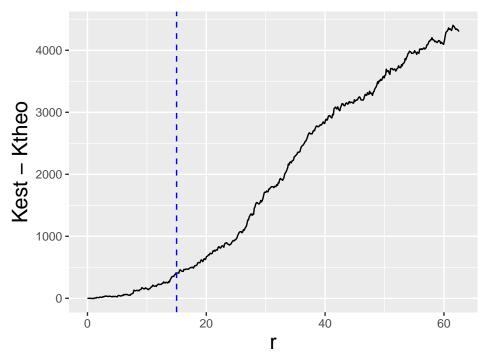


CART classification trees Nb leaves vs complexity



#> \$DiffK

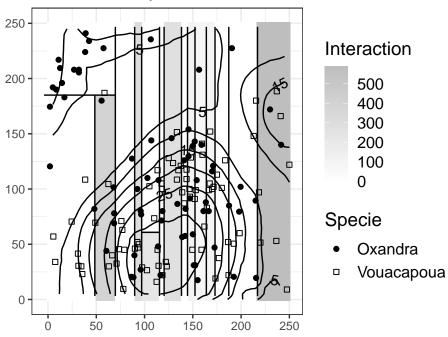
Difference between estimated and theoretical



#>

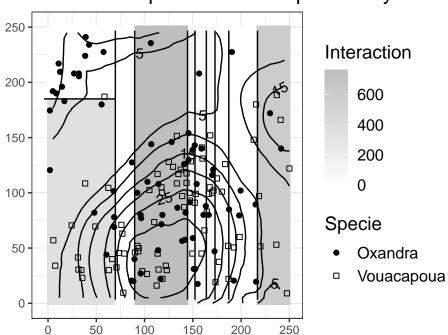
#> \$SC.maxtree

Paracou - SpatCART maximal tree



#>
#> \$SC.Classprobtree

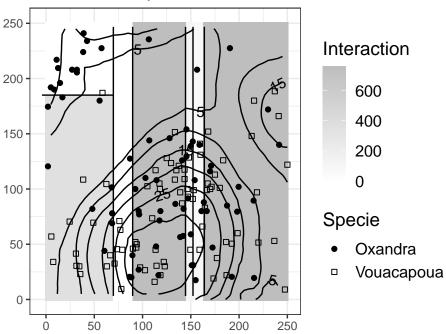
Paracou - SpatCART class probability tree



#>

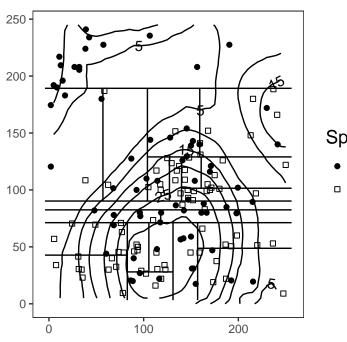
#> \$SC.Classtree

Paracou - SpatCART classification tree



#>
#> \$C.maxtree

Paracou - CART maximal tree



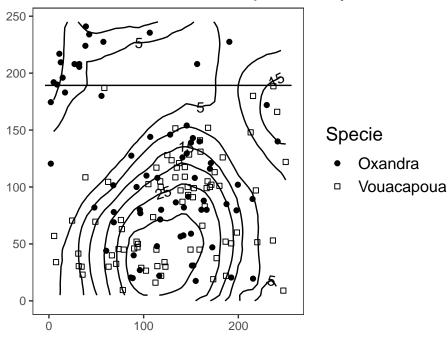
Specie

- Oxandra
- □ Vouacapoua

#>

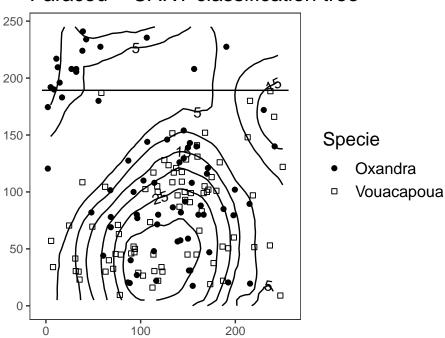
#> \$C.Classprobtree

Paracou - CART class probability tree



#> \$C.Classtree

Paracou - CART classification tree



• Paracoudata, Paracou.plot respectively loads the Paracou data set as a spatial bivariate point process of class 'ppp', and plots the heatmap colored partition induced by a SpatCART classification tree's leaves with respect to the interaction between marks of the Paracou data set. The output value of the function Paracou.plot() is the corresponding 'ggplot' object. Needs also the input values of impurities inside tree leaves.

Plot the graphic of heatmap colored partition induced by the SpatCART class probability tree's leaves:

```
ypp = Paracoudata()

# SpatCART trees
t = spatcart(ypp, 15, graph = FALSE)

a = t$opt.tree.min
K = t$K[rownames(a$frame)][a$frame$var=="<leaf>"]

Paracou.plot(a,ypp,K)
```

