

Define  $v[n] = x[n] + 0.5x[n-1]$

$$y[n] = v[n] + 0.5y[n-1]$$

$$y[n] = \sum_{k=0}^{\infty} (0.5)^k v[n-k] \quad (\text{eq 1.115/1.116})$$

$$y[n] = \sum_{k=0}^{\infty} (0.5)^k (x[n-k] + 0.5x[n-k-1])$$

$$y[n] = \sum_{k=0}^{\infty} (0.5)^k x[n-k] + \underbrace{\sum_{k=0}^{\infty} [0.5)^k + 0.5x[n-k-1]]}_{\substack{\rightarrow \sum_{k=0}^{\infty} [0.5^{(k+1)} x[n-(k+1)]] \\ m=k+1 \\ \sum_{m=1}^{\infty} [0.5^m x[n-m]] \\ \rightarrow \sum_{k=1}^{\infty} [0.5^k x[n-k]]}}$$

$$y[n] = \sum_{k=0}^{\infty} (0.5)^k x[n-k] +$$

$$y[n] = (0.5)^{k=0} x[n-k=0] + 2 \sum_{k=1}^{\infty} 0.5^k x[n-k]$$

$$y[n] = x[n] + 2 \sum_{k=1}^{\infty} 0.5^k x[n-k]$$