

## INEQUALITIES

### Basic Model

These statements are followed by two conclusions:

- (a) If only conclusion I follows.
- (b) If only conclusion II follows.
- (c) If either conclusion I or II follows.
- (d) If neither conclusion I nor II follows.
- (e) If both conclusion I and II follow.

**1. Statement:  $M \leq N > O \geq P = Q$**

**Conclusions: I.  $M \geq Q$  II.  $Q < M$**

$M \geq Q$ ,  $Q < M$  opposite symbols, so both are false.

**2. Statement:  $U \leq V < W = X < Y$**

**Conclusions: I.  $Y > V$  II.  $W > U$**

Both conclusions are true

**3. Statements :  $C > A \geq T$  ,  $S < E = T$**

**Conclusions :  $A > E$  ,  $C > S$**

After combining both the statements, we get:

$$C > A \geq T = E > S$$

Thus  $A > E$  is false as the true relationship is  $A \geq E$ .

$C > S$  is true.

Hence only conclusion II follows.

**4. Statements :  $F < U \leq N$  ,  $D > H < U = B$**

**Conclusions :  $H < N$  ,  $H = N$**

From statements I and II , we get:

$$H < U \leq N$$

Thus  $H < U$  is true whereas  $H = N$  is false.

Hence only conclusion I follows.

**5. Statement :  $G \leq L \geq O \geq W \geq I < N$**

**Conclusions : I.  $I < L$  II.  $L = I$**

Given statement:  $G \leq L \geq O \geq W \geq I < N$

Thus,  $L \geq I$  or  $I \leq L$  is true.

It means either  $I < L$  or  $L = I$  is true.

Thus, Conclusion I and II make a complementary pair.

Hence, either conclusion I or II is true.

**6. Statement :  $G \leq L \geq O \geq W \geq I < N$**

**Conclusions : I.  $O > G$  II.  $W < N$**

Given statement:  $G \leq L \geq O \geq W \geq I < N$

Thus, we can't compare  $G$  and  $O$  or  $W$  and  $N$ ,

Hence neither conclusion I ( $O > G$ ) nor II ( $W < N$ ) is true.

**7. Statement :  $R > M \geq T \leq Q = S$**

**Conclusions : I.  $R > Q$ , II.  $Q \geq M$**

Given statement:

$$R > M \geq T \leq Q = S$$

Thus, we can't compare  $R$  and  $Q$  or  $Q$  and  $M$ .

Hence neither I ( $R > Q$ ) nor II ( $Q \geq M$ ) is true.

**8. Statements :  $P \leq Q \leq R = S$ ,  $U \geq V \geq S$**

**Conclusions :  $P < U$ ,  $P = U$**

Combining statements I and II, we get:

$$P \leq Q \leq R = S \leq V \leq U$$

Here, the common sign between  $P$  and  $U$  is ' $\leq$ ' and the given conclusions are  $P < U$  and  $P = U$ . Hence, either  $P < U$  or  $P = U$  follows.

Hence, the correct answer would be Either conclusion I or conclusion II follows.

**9. Statement :  $P = R$ ,  $R < F$ ,  $F < T$**

**Conclusions :  $T < R$ ,  $F < P$**

Combining statements II and III, we get:  
 $R < F < T$

Here, the common sign between R and T is ' $<$ ' and the given conclusion is  $T < R$ . Hence, conclusion I does not follow.

For conclusion II:  $F < P$

Combining statement I and II, we get:

$P = R < F$

Here the common sign between P and F is ' $<$ ' and the given code is  $F < P$ . Hence, conclusion II does not follow too.

Hence, the correct answer would be 'Neither conclusion I nor conclusion II follows'.

**10. Statements :  $P \geq Q$ ,  $R < S$ ,  $Q = S$ ,  $T > P$**

**Conclusions :  $R < T$ ,  $T > S$**

Checking C1:

$R < S = Q \leq P < T$

Thus C1 follows.

Checking C2:

$S = Q \leq P < T$

Thus C2 also follow.

Both C1 and C2 follow

**11. Statements:  $D \geq S$ ,  $X < W$ ,  $S = J$ ,  $W > Y$ ,  $X > D$ ,  $Y \leq O$ ,  $J \geq E$**

**Conclusions: (i)  $D > E$  (ii)  $D = E$  (iii)  $O > S$**

By combining all the statements, we get the following equation:

$O \geq Y < W > X > D \geq S = J \geq E$

For conclusion (i):  $D > E$

Here, the common sign between D and E is ' $\geq$ '. Thus  $D \geq E$ .

Hence conclusion (i) does not follow individually.

For conclusion (ii):  $D = E$

Here, the common sign between D and E is ' $\geq$ '. Thus  $D \geq E$ .

Thus conclusion (ii) does not follow individually.

On combining conclusions I and II we get " $D \geq E$ ".

Therefore either conclusion (i) or (ii) follows.

For conclusion (iii):  $O > S$

Here we can see the opposite signs between O and S, thus no relationship can be established between them.

Therefore conclusion (iii) does not follow.

Either conclusion (i) or (ii) follows

**12. Statements:  $S < V$ ,  $P = M$ ,  $T > V$ ,  $M < I$ ,  $R = I$ ,  $P < T$**

**Conclusions: (i)  $I > P$  (ii)  $S > M$  (iii)  $I < T$**

By combining all the statements, we get the following equation:

$$R = I > M = P < T > V > S$$

For conclusion (i):  $I > P$

Here we can see the common sign between I and P is '>', thus  $I > P$ .

Hence conclusion (i) follows.

For conclusion (ii):  $S > M$

Here we can see opposite sign between S and M, thus no relationship can be established between them.

Thus conclusion (ii) does not follow.

For conclusion (iii):  $I < T$

Here we can see opposite sign between I and T, thus no relationship can be established between them.

Therefore conclusion (iii) does not follow.

**Only conclusion (i) follows**

### True / False

13. Which of the following expressions will be true if the expression ' $K \geq L > M \geq N$ ' is definitely true?

- (a)  $N \leq K$       (b)  $K = M$       (c)  $K < N$       (d)  $L \geq N$       (e) **None is true**

14. Which of the following expressions will be true if the expression ' $M \geq K < T = Q$ ' is definitely true?

- (a)  $Q < K$       (b)  $M \geq T$       (c)  **$K < Q$**       (d)  $T = M$       (e) None is true

### Using symbols

In the following questions, the symbols \$, @, %, & and # are used with the following meanings as illustrated below:

**'A \$ B' means A is neither greater nor smaller than B**

**'A @ B' means A is neither greater than nor equal to B**

**'A % B' means A is neither smaller than nor equal to B**

**'A & B' means A is not smaller than B**

**'A # B' means A is not greater than B**

In each of the following questions, assuming the given statements to be true, find out which of the two conclusions I and II given below them is/are definitely true. Give answer

- a) if only conclusion I is true.
- b) if only conclusion II is true.
- c) if either conclusion I or II is true.
- d) if neither conclusion I nor II is true.
- e) if both conclusions I and II are true.

**15. Statements:  $V \& D$ ,  $D \% T$ ,  $K \$ T$ ,  $K \# F$**

**Conclusions: I.  $V \% F$  II.  $V \% K$**

Conclusion 1 :  $V > F$

Comparing with statement it is false.

Conclusion 2 :  $V > K$

Comparing with statements it is true

Hence option b (only conclusion 2 Follows)

**16. Statements:  $S \leq Q$ ,  $Q @ B$ ,  $B \& K$ ,  $K \# W$**

**Conclusions: I.  $W \% K$  II.  $S @ B$**

Conclusion 1 ;  $W > K$

Comparing with statements it is false

Conclusion 2 :  $S < B$

Comparing with statements it is true.

Hence Option B (only conclusion 2 follows)

**$A @ B$  means A is not greater than B.**

**$A ! B$  means A is greater than B.**

**$A * B$  means A is not less than B.**

**$A \% B$  means A is less than B.**

**$A \# B$  means A is neither greater nor less than B.**

**17. Statements :  $M ! H$ ,  $K \% M$ ,  $G \# H$**

**Conclusions :  $H \# K$ ,  $M * G$**

From statements I and II, we get:

$$K < M > H$$

Here, we get the opposite signs between H and K, thus no relationship can be established between them.

Hence conclusion I does not follow.

From statements I and III, we get:

$$M > H = G$$

Thus  $M \geq G$  is not a true relationship from the above equation.

Hence conclusion II does not follow.

**neither conclusion I nor II follows.**

18. Statements :  $E@F$  ,  $D\%E$  ,  $T*F$

Conclusions :  $D\%F$  ,  $T*E$

From statements I and II, we get:

$$D < E \leq F$$

Thus  $D < F$  is the true relationship.

Hence conclusion I follows.

From statements I and III, we get:

$$T \geq F \geq E$$

Thus  $T \geq E$  is the true relationship.

Hence conclusion II follows.

**both conclusion I and II follow.**

19. Statements:  $T\#Y$  ,  $Y\%L$  ,  $G*L$

Conclusions:  $L!T$  ,  $G*T$

From statements I and II, we get:

$$T = Y < L$$

Thus  $L > T$  is the true relationship.

Hence conclusion I follows.

From statements I, II and III, we get:

$$G \geq L > Y = T$$

Thus  $G \geq T$  is not a true relationship.

Hence conclusion II does not follow.

**Only conclusion I follows**

20. Statements :  $G!U$  ,  $L@U$  ,  $M*G$

**Conclusions :  $M \# U$  ,  $M ! U$**

$M \geq G > U \geq L$

Thus  $M > U$  is the true relationship.

Hence conclusion I does not follow.

But conclusion II definitely follows.

Only conclusion II follows

**21. Statements :  $Z ! U$  ,  $P * W$  ,  $W @ U$**

**Conclusions :  $Z ! W$  ,  $P \% U$**

From statements I and III, we get:

$Z > U \geq W$

$Z > W$  is the true relationship.

Hence the conclusion I follows.

From statements II and III, we get:

$P \geq W \leq U$

Thus due to opposite sign between P and U no relationship can be established between them.

Hence conclusion II does not follow.

Only conclusion I follows