RE510 Lab 4 Graph-Based SLAM

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Lab 4

- Learn about Graph based SLAM (Simultaneous Localization And Mapping)
- •In this lab, we use **odometry** and **LiDAR** data.
- Brief introduction for SLAM...
 - Odometry always have error (drift, wheel diameter changing, etc.)
 - Local odometry might be accurate, but after accumulation, it's not.
 - With SLAM, using external sensor(LiDAR, image, ...), can correct the robot position.





SLAM Approaches

- Filtering
 - Current robot pose
 - All landmark positions
 - Matrix inverse (EKF-SLAM)
 - Fixed-linearize point
 - Particle filter SLAM
 - Fast SLAM

EKF-SLAM (Dissanayake, IEEE TRO, 2001) Sparse Extended I nformation Filter (S. Thrun, IJRR, 200 4)

- Graph-based (Smoothing)
 - All robot pose
 - All landmark positions
 - *Least square* approach
 - Sparse matrix factorization
 - Re-linearize

SAM (F. Dellaert, M. Kae ss, IJRR, 2006) iSAM (M. Kaess, IEEE T.R O., 2008)





Least-Square Error

- Error function
 - Error e_i is typically the **difference** between the **predicted and actual** measurement

$$\mathbf{e}_i(\mathbf{x}) = \mathbf{z}_i - f_i(\mathbf{x})$$

- We assume that the error has zero mean and is normally distributed
- Gaussian error with information matrix Ω_i
- The squared error of a measurement depends only on the state and is a scalar

$$e_i(\mathbf{x}) = \mathbf{e}_i(\mathbf{x})^T \mathbf{\Omega}_i \mathbf{e}_i(\mathbf{x})$$

Inverse of covariance matrix of measurement





Least-Square Error

- Find minimum of error function
 - ullet Find the state \mathbf{x}^* which minimizes the error given all measurements

$$\mathbf{x}^* = \underset{\mathbf{x}}{\operatorname{argmin}} F(\mathbf{x}) \longleftarrow \underset{\mathbf{global \ error \ (scalar)}}{\operatorname{global \ error \ (scalar)}}$$

$$= \underset{\mathbf{x}}{\operatorname{argmin}} \sum_{i} e_i(\mathbf{x}) \longleftarrow \underset{\mathbf{x}}{\operatorname{squared \ error \ terms \ (scalar)}}$$

$$= \underset{\mathbf{x}}{\operatorname{argmin}} \sum_{i} e_i^T(\mathbf{x}) \Omega_i e_i(\mathbf{x})$$

$$\underset{\mathbf{error \ terms \ (vector)}}{\overset{\uparrow}{\operatorname{error \ terms \ (vector)}}}$$

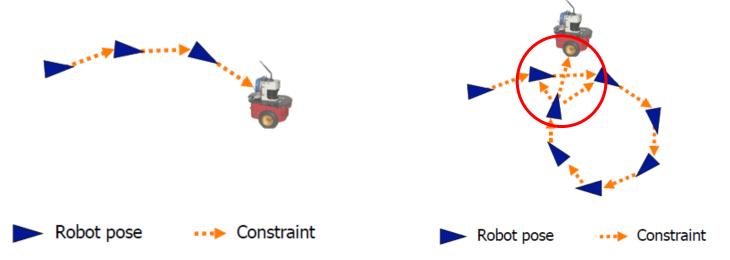
- When measurement's dimension is 'n',
- Omplex and no closed form (미지수의 해가 수식으로 정리되는 형태가 아님)
- So, numerical approaches is needed





Least-Square Approach to SLAM

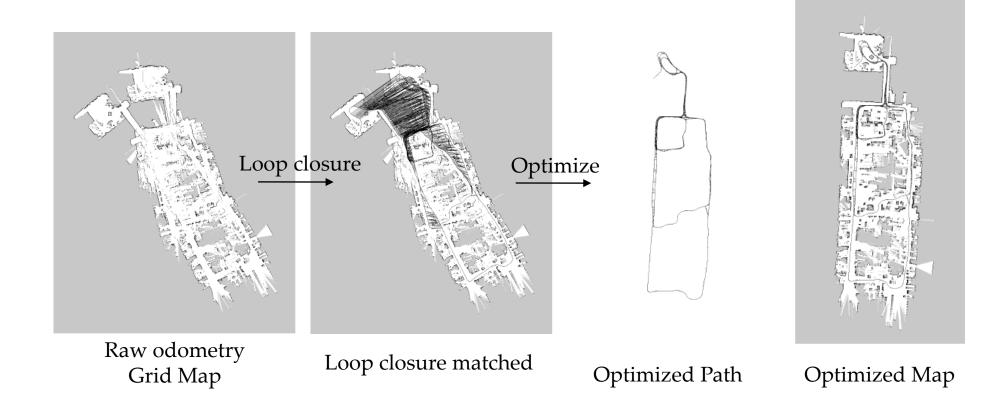
- Graph SLAM: use a graph to represent the problem
- Node(Vertex) : pose of robot
- Edge: constraint between nodes (odometry, LiDAR, vision..)
- <u>Build the graph and find a node configuration that minimize the error introduce</u> <u>d by the constraints</u>



• When revisiting a previously visited place, optimizes the graph by recognizing that it is the same location us ing information about the surrounding environment (sensor data) and adding constraints between non-succ essive nodes.



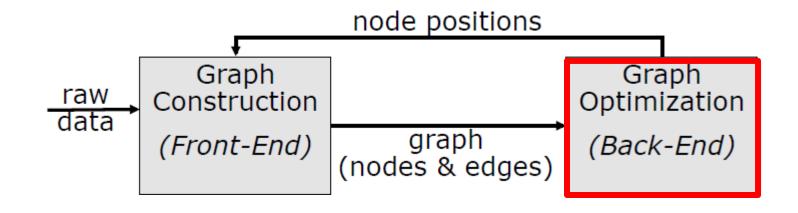
Example







Overall Graph SLAM system



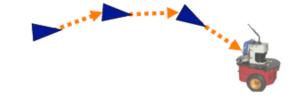
- Front-End: generates constraints between nodes
- Back-End: optimizing nodes(pose) using constraints and information (ex. iSAM, g2o, ceres)

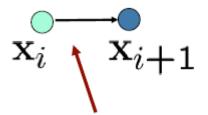




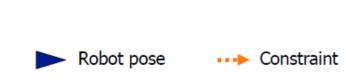
The Graph

- It consists of n nodes $x = x_{1:n}$
- Each x_i is a 2D or 3D transformation (the pose of the robot at time t_i)
- ullet A constraint/edge exists between the nodes \mathbf{x}_i and \mathbf{x}_j if...
- Create an Edge if.. (1)
- ...the robot moves from \mathbf{x}_i to \mathbf{x}_{i+1}
- Edge corresponds to odometry





The edge represents the **odometry** measurement

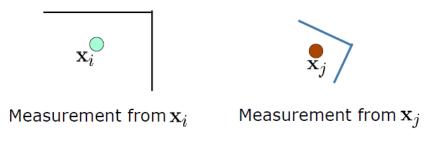




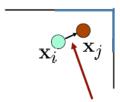


The Graph

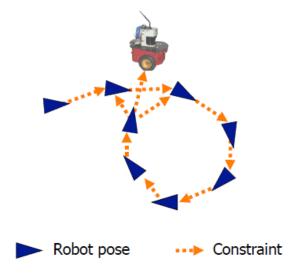
- Create an Edge if.. (2)
 - ...the robot observes the same part of the environment from \mathbf{x}_i and from \mathbf{x}_j



• Construct a **virtual measurement** about the position of \mathbf{x}_j seen from \mathbf{x}_i



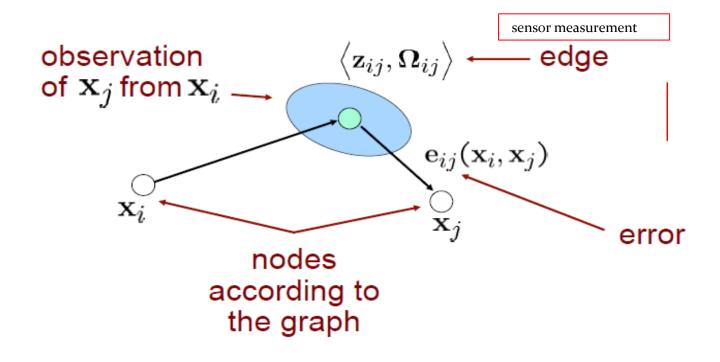
Edge represents the position of \mathbf{x}_j seen from \mathbf{x}_i based on the **observation**







The Graph



• Goal:
$$\mathbf{x}^* = \operatorname*{argmin} \sum_{ij} \mathbf{e}_{ij}^T \Omega_{ij} \mathbf{e}_{ij}$$

- Information matrix is inverse of covariance
- The "bigger", the more the edge "matters" in the optimization.





Optimize algorithm

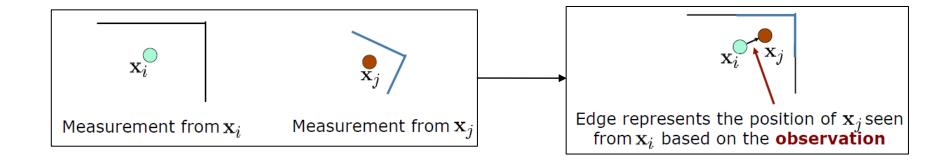
- In this experiment, we use G2O ported to python.
- If you're interested in optimization equations and algorithm, read the paper:
 - Kümmerle, Rainer & Grisetti, Giorgio & Strasdat, Hauke & Konolige, Kurt & Burgard, Wolfram. (2011). G2o: A general framework for graph optimization. Proc. of the IEEE Int. Conf. on Robotics and Automation (ICRA). 3607 3613. 10.1109/ICRA.2011.5979949.





ICP

- In page 8, there is situation of creating observation edge.
- How can we get those type of edge?
- For matching two LiDAR point clouds, we use Iterative-Closest-Point algorithm.







ICP

Given two corresponding point sets:

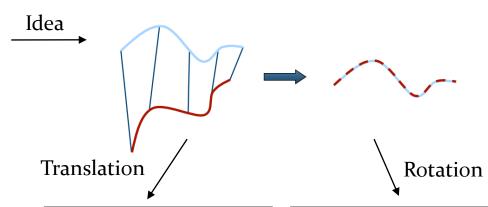
$$X = \{x_1, ..., x_{N_x}\}$$
$$P = \{p_1, ..., p_{N_p}\}$$

Wanted: Translation t and rotation R that minimize the sum of the squared error:

$$E(R,t) = \frac{1}{N_p} \sum_{i=1}^{N_p} ||x_i - Rp_i - t||^2$$

Where x_i and p_i are corresponding points

 If the correct correspondences are known, the correct relative rotation/translation can be calculated in closed form



Center of Mass

$$\mu_x = \frac{1}{N_x} \sum_{i=1}^{N_x} x_i \quad \text{and} \quad \mu_p = \frac{1}{N_p} \sum_{i=1}^{N_p} p_i$$

are the centers of mass of the two point sets $% \left\{ 1\right\} =\left\{ 1$

Idea:

- Subtract the corresponding center of mass from every point in the two point sets before calculating the transformation
- The resulting point sets are:

$$X' = \{x_i - \mu_x\} = \{x_i'\}$$

 $P' = \{p_i - \mu_p\} = \{p_i'\}$

Singular Value Decomposition

Let
$$W = \sum_{i=1}^{N_p} x_i' p_i'^T$$

denote the singular value decomposition (SVD) of W by:

$$W = U \begin{bmatrix} \sigma_1 & 0 & 0 \\ 0 & \sigma_2 & 0 \\ 0 & 0 & \sigma_3 \end{bmatrix} V^T$$

where $~U,V\in\mathbb{R}^{3 imes3}~$ are unitary, and $\sigma_1\geq\sigma_2\geq\sigma_3~$ are the singular values of W





Basic ICP Algorithm

- Determine corresponding points Find nearest neighbor of each points
- Compute rotation R, translation t via SVD
 T by centroid, R by SVD
- Apply R and t to the points of the set to be registered
- Compute the error E(R,t) Mean distance between all corresponding points
- If error decreased and error > threshold
 - Repeat these steps
 - Stop and output final alignment, otherwise





- Environment
 - Ubuntu (18.04, 20.04 tested)
 - Python (2.7 prefered)
 - · numpy
 - sklearn
 - · scipy
 - · matplotlib
 - G2opy (Ported g2o)
 - Included on prereq/g2opy
 - Have to build.. (instruction : prereq/Readme.txt)





Anaconda environment

- If you use ubuntu 20.04 / 22.04, it would be better to use anaconda for Python2.7
 - https://www.anaconda.com/

```
conda create --name re510_pyslam python=2.7
conda activate re510_pyslam

(build g2opy)

pip install numpy scikit-learn matplotlib
pip install scipy == 1.2.0

(execute slam.py)
```



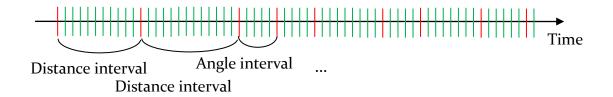


- Assignment
 - Fill the skeleton code in slam.py
 - Run the code, save the result of matplotlib
 - Write the report..
 - Explain slam.py code (with theory of graph SLAM)
 - Explain icp.py code (with theory of ICP)
- Score Criteria
 - Make runnable code. (35%)
 - Write report. (50%)
 - Upgrade loop closing (10%)
 - Define new information matrix (5%)

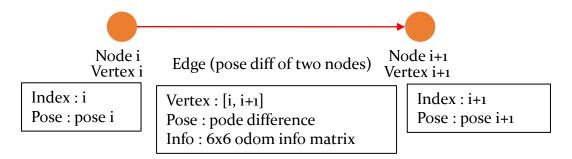




- Assignments
 - Assignment 1 : Node generation
 - Calculate pose difference using odometry.
 - In certain interval, generate node (odometry+LiDAR)



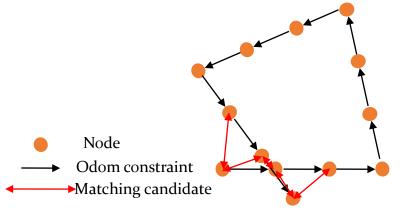
- Assignment 2 : Add odometry vertex & edge
 - Add vertex and edge of odometry information







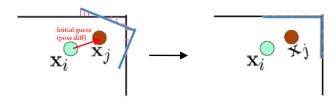
- Assignments
 - Assignment 3 : Find loop closure
 - Find loop closure (matching pair)
 - Pair can be near nodes. (in certain distance threshold)
 - Or just simply, try to match all pairs ([1,2], [1,3], [1,4], [1,5], [2,3], [2,4], ...)



- Assignment 4 : ICP matching, Add edge and Optimize
 - With no initial guess

 $\mathbf{x}_{\mathbf{x}_{j}}^{\bullet}$ \longrightarrow \mathbf{x}_{i}°

Hard to find correspondences between points Hard to match, or even cannot match



Can find correct correspondences Easy to match within few steps

With initial guess

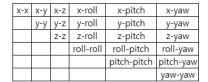
- Add edge using ICP constraint
 - If ICP matching is correct (can determine using distances between corresponding points.)
 - Add edge to graph structure for optimization.
 - How can you put constraint pose? (calculate using initial guess and ICP result)





- Additional notes
 - Actually, assignment 3 and assignment 4 have to done simultaneously
 (find loop closure -> try matching -> optimize -> find another using optimized pose)
 But for simplicity, I split assignment 3 and assignment 4.
 If you want to do strictly, you can merge them.
 - Loop closure score
 - Brute force(all pair): 5 / 10
 - Find near node in odom: 8 / 10
 - Merge assign 3,4 : 10 / 10
 - Information matrix score
 - Identity matrix * constant : 3/5
 - Related to odometry difference : 5/5

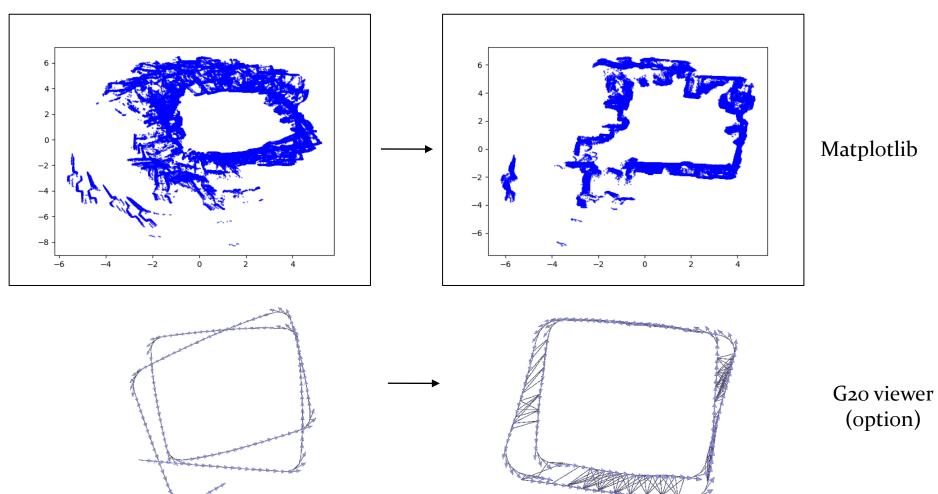
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Example result







Thanks for your kind attention

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