

A (Lisp-Like) TOY Language [Version 1]

The language **TOY** is composed of terms (as opposed to instructions) built up from constants, variables and lesser terms by applying functions. The objects of computation (i.e., the data structures) are integers $\dots -2 -1 0 1 2 3 \dots$. $\underline{\mathbf{Z}}$ denotes the set of integers. $\underline{\mathbf{FUN}}$ is a set of non-numeric words naming functions. $\underline{\mathbf{MINUS}}$ and $\underline{\mathbf{IF}}$ (the constants of **FUN**) name primitive functions from $\mathbf{Z} \times \mathbf{Z}$ to \mathbf{Z} . Other names in **FUN** refer to functions defined by terms of the language **L**.

$\underline{\mathbf{L}}$ is the set of all **terms** as defined by the following.

- (t1) The variables $v_1 v_2 v_3 v_4 \dots$ (i.e., identifiers) are terms.
- (t2) The constants $\dots -3 -2 -1 0 1 2 3 \dots$ are terms.
- (t3) IF t_1 and t_2 are terms, then **(MINUS $t_1 t_2$)** and **(IF $t_1 t_2$)** are terms.

INTERPRETER. A higher-level expression of interpreting term is built on top of the terms of **TOY**. These interpreting terms use the function **VALUE** $\langle \rangle$. The interpreter itself consists of a set of equations (rewrite rules) in these terms used to direct computations in **TOY**.

The function **VALUE**: **TOY** \rightarrow \mathbf{Z} is defined as follows.

- (v1) **VALUE** $\langle u \rangle$ = undefined if u is a variable.
- (v2) **VALUE** $\langle n \rangle$ = n if n is an integer.
- (v3) **VALUE** $\langle (\mathbf{MINUS} t_1 t_2) \rangle$
= $\langle t_1 - t_2 \rangle$ if t_1 and t_2 are integers,
= **VALUE** $\langle (\mathbf{MINUS} \mathbf{VALUE}\langle t_1 \rangle \mathbf{VALUE}\langle t_2 \rangle) \rangle$ otherwise.
VALUE $\langle (\mathbf{IF} t_1 t_2) \rangle$
= **VALUE** $\langle t_2 \rangle$ if t_1 is positive integer and t_2 has a value,
= 0 if t_1 is 0 or a negative integer,
= **VALUE** $\langle (\mathbf{IF} \mathbf{VALUE}\langle t_1 \rangle t_2) \rangle$ otherwise.

* Tip: The **TOY** language Interpreter consists of two parts:

The first part generates "Intermediate Codes".

The second part executes the "Intermediate Codes" and produces the result.